



# Evolution of Circumstellar Disks and Planet Formation



**Wladimir Lyra**  
New Mexico State University

**Current Funding**



AAG – 2020, 2021



XRP - 2023

EW – 2021, 2022, 2023

TCAN – 2020

**Computational Facilities**



## **Outline**

- Planet Formation
- Hydrodynamical Instabilities
- Disk observations

# TCAN-2020 (Theoretical and Computational Astrophysics Network) Planet Formation Collaboration



## PI

Wladimir Lyra – *New Mexico State University*

## Co-Is

Andrew Youdin – *University of Arizona*  
Jake Simon – *Iowa State University*  
Chao-Chin Yang – *University of Nevada, Las Vegas  
(now University of Alabama)*  
Orkan Umurhan – *NASA Ames*

## Postdocs

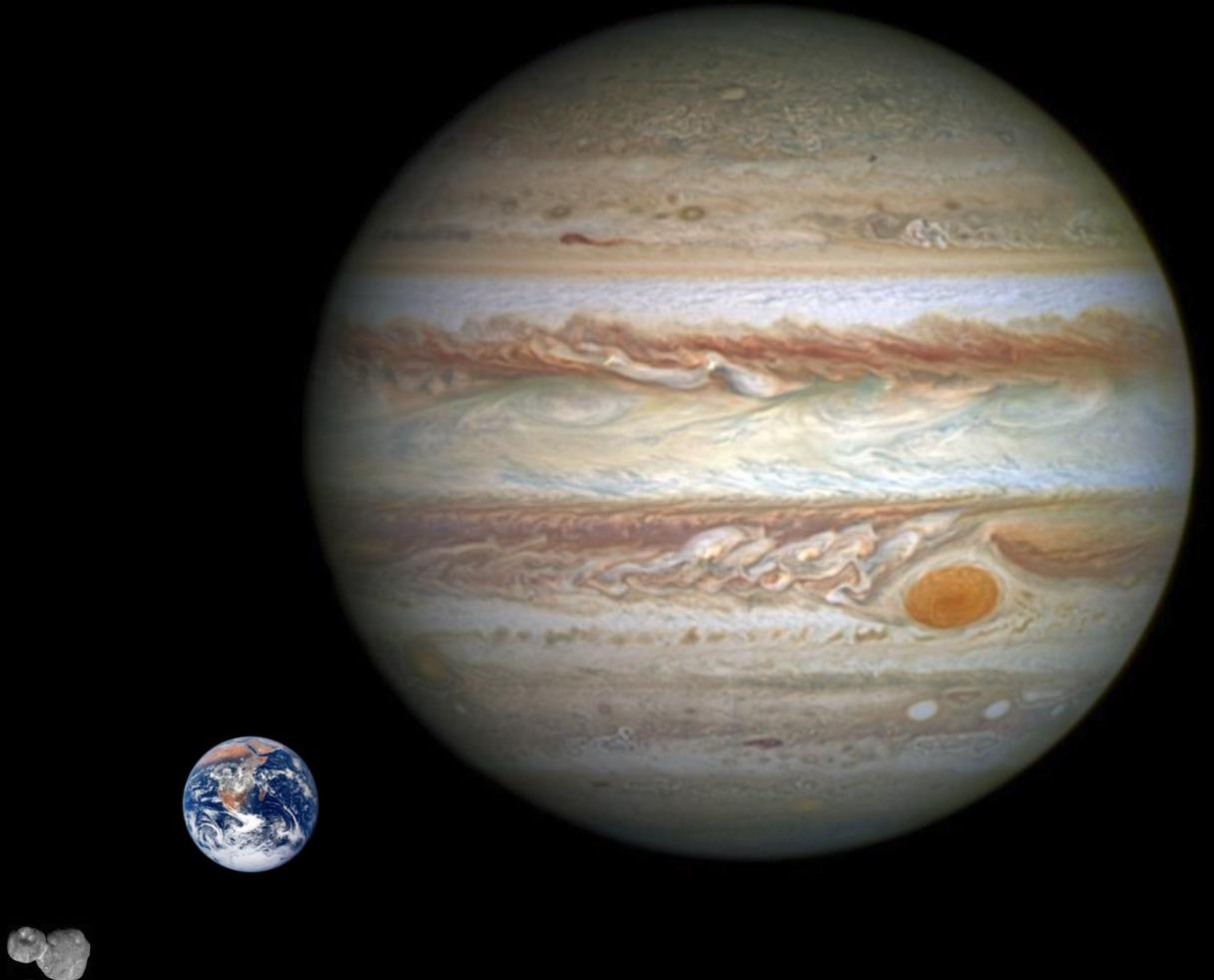
Debanjan Sengupta (NMSU)  
Leonardo Krapp (UA)  
Daniel Carrera (ISU)

## Graduate Students

NMSU - Daniel Godines, Victoria de Cun, Manuel Cañas.  
ISU – Jeonghoon Lim, David Rea, Olivia Brouillette  
UNLV – Alex Mohov, Stanley Baronett  
UA – Eonho Chang

# Planet Formation

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# Circumstellar/Protoplanetary Disks



## PP disk fact sheet

Density:  $10^{13} - 10^{15} \text{ cm}^{-3}$   
(Air:  $10^{21} \text{ cm}^{-3}$ )

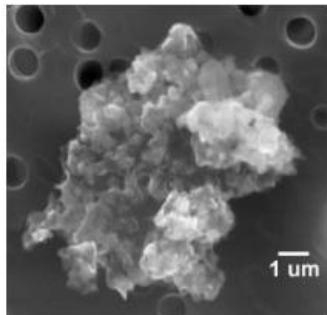
Temperature: 10-1000 K

Scale: 0.1-100AU

Mass:  $10^{-3} - 10^{-1} M_{\text{sun}}$

# Planet Formation

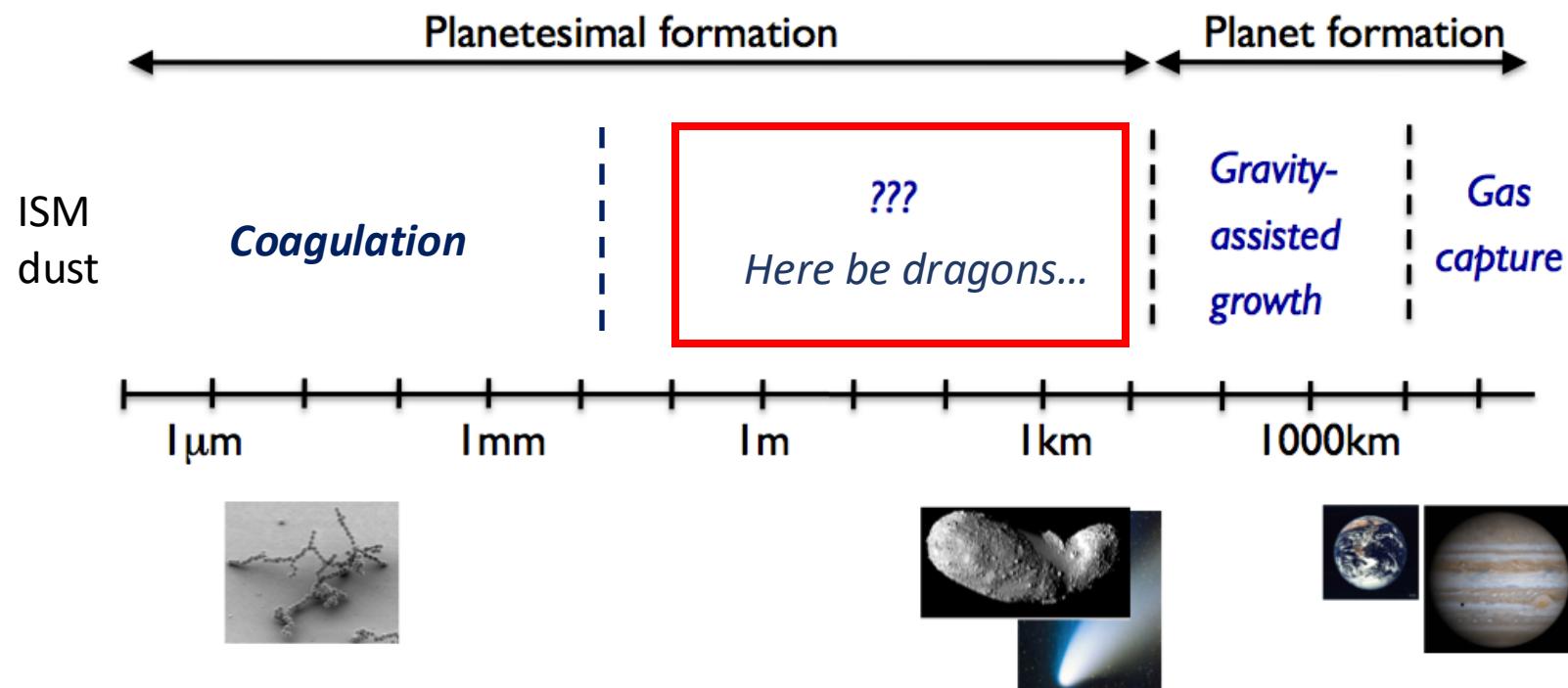
“Planets form in disks of gas and dust”



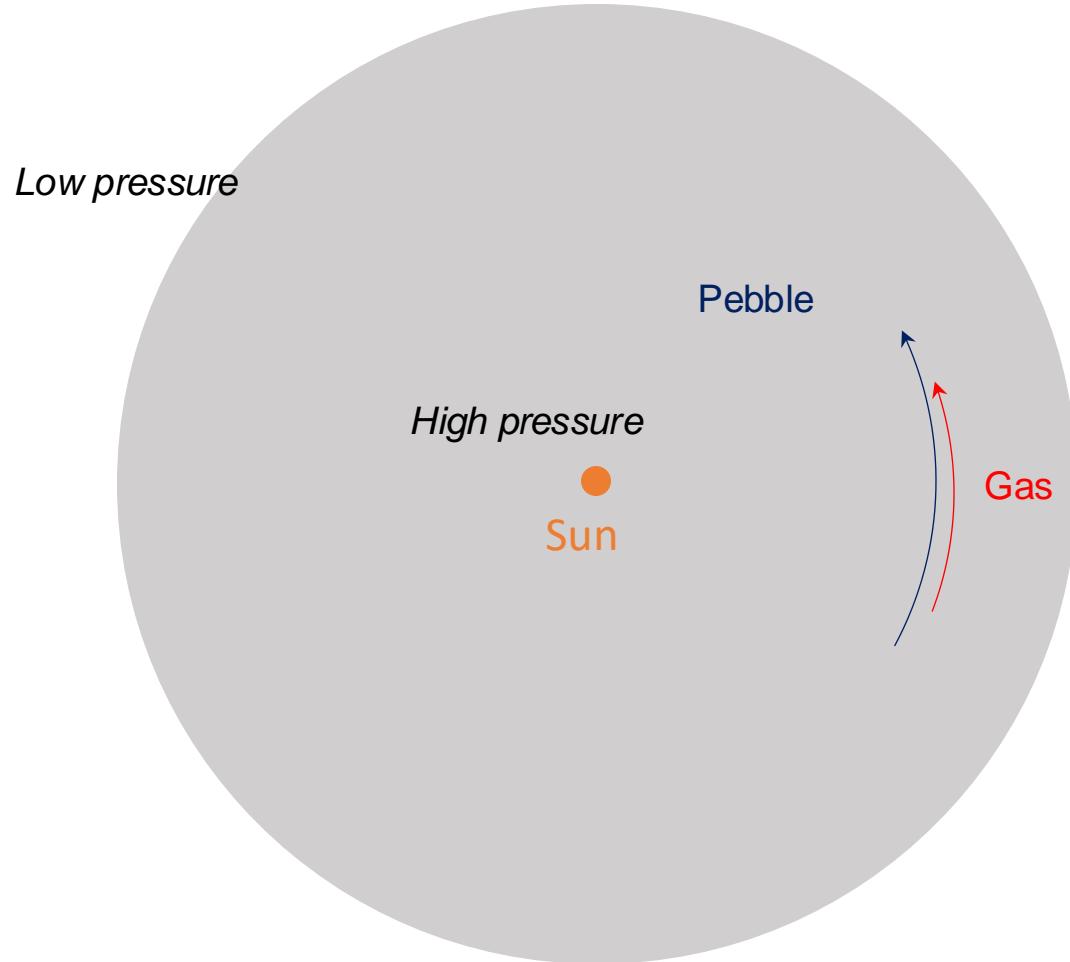
*A miracle happens* →



# Dust evolution



# Headwind and Dust Drift



The **gas** has some pressure support (sub-Keplerian).

The **pebbles** do not feel gas pressure (Keplerian).

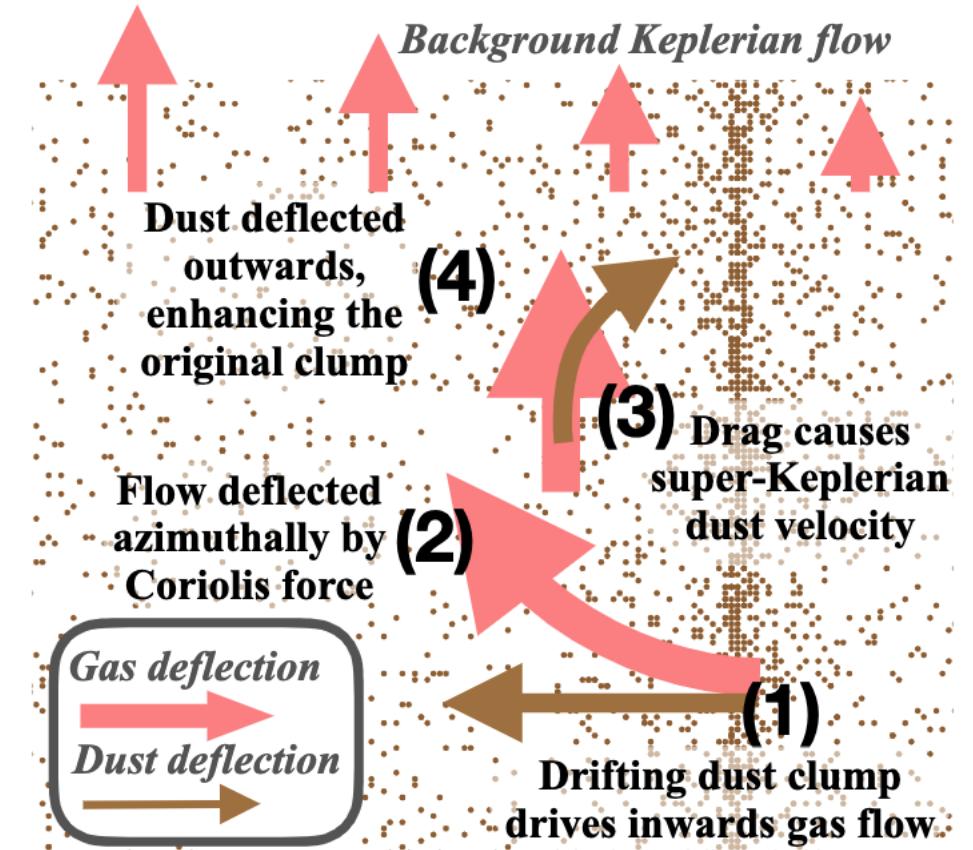
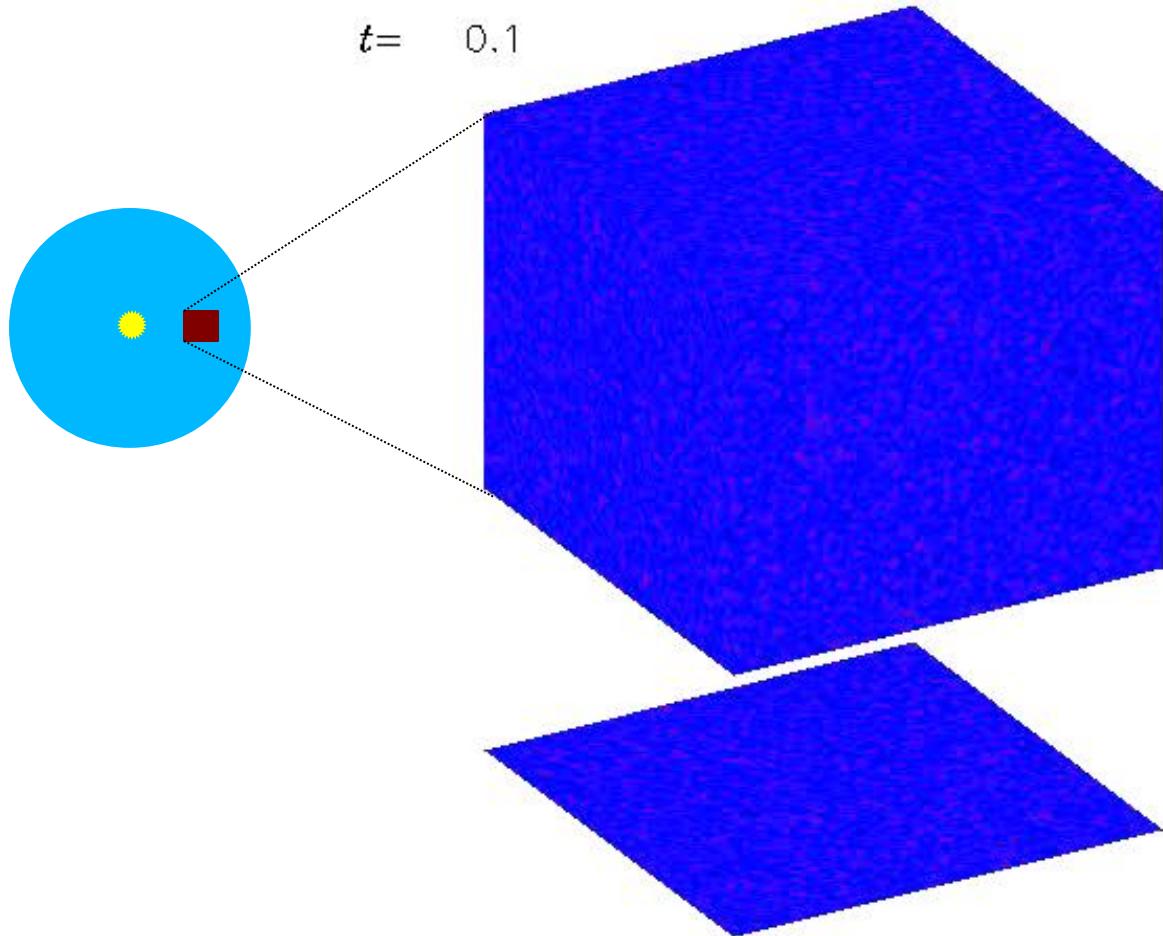
# Dust coagulation and drift

Dust particle  
coagulation  
and radial drift

F. Brauer, C.P. Dullemond  
Th. Henning

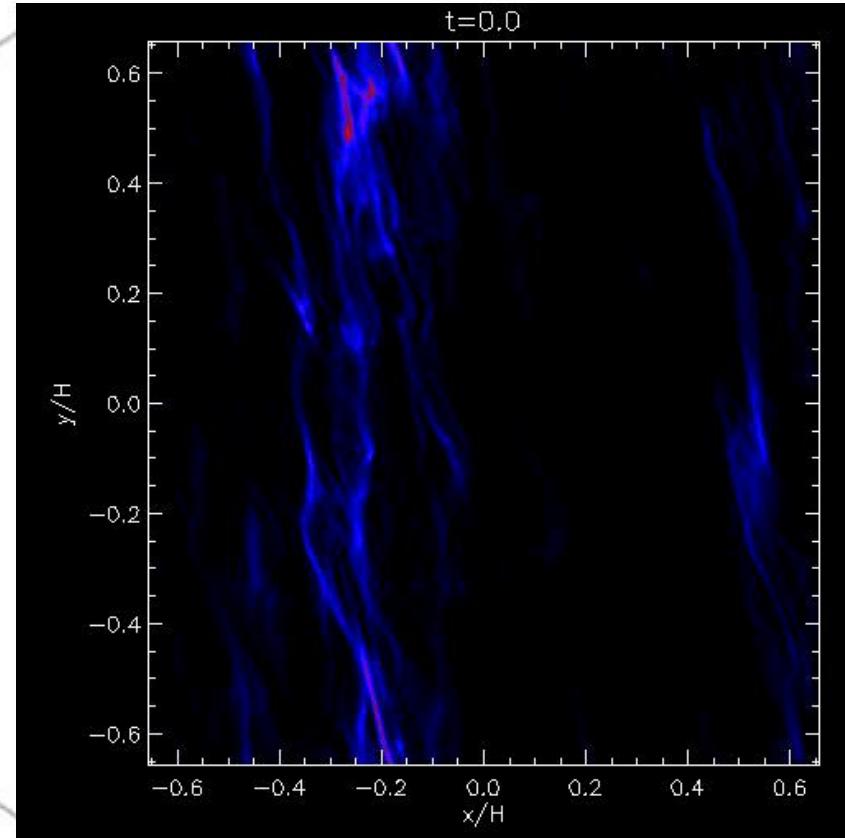
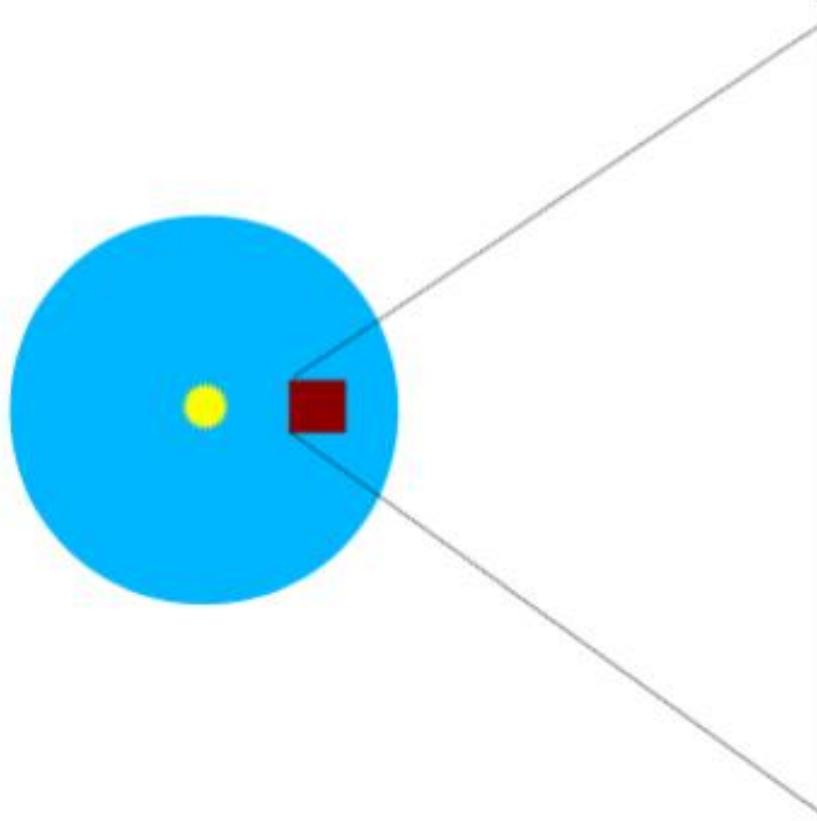
# Streaming Instability

The dust drift is hydrodynamically unstable



Lesur et al. (2022)

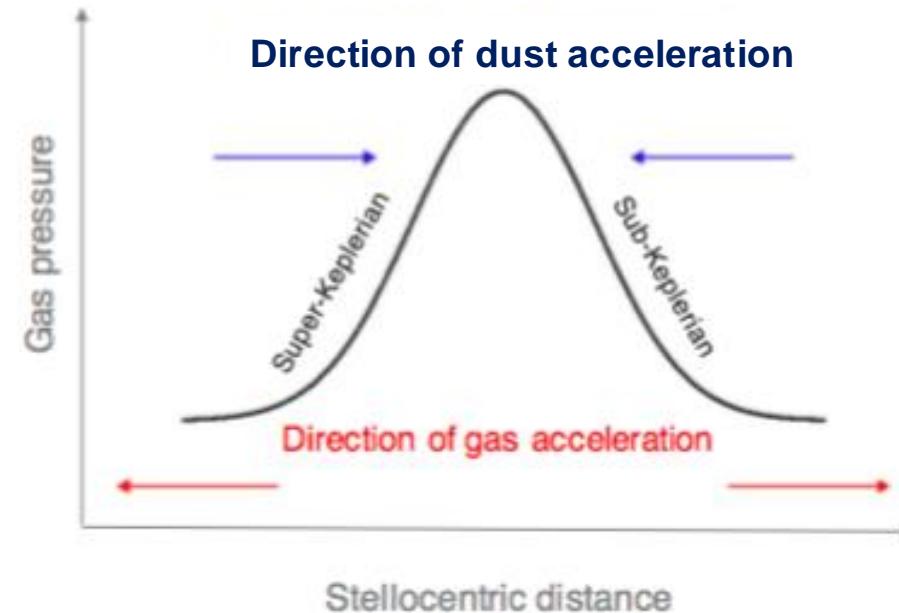
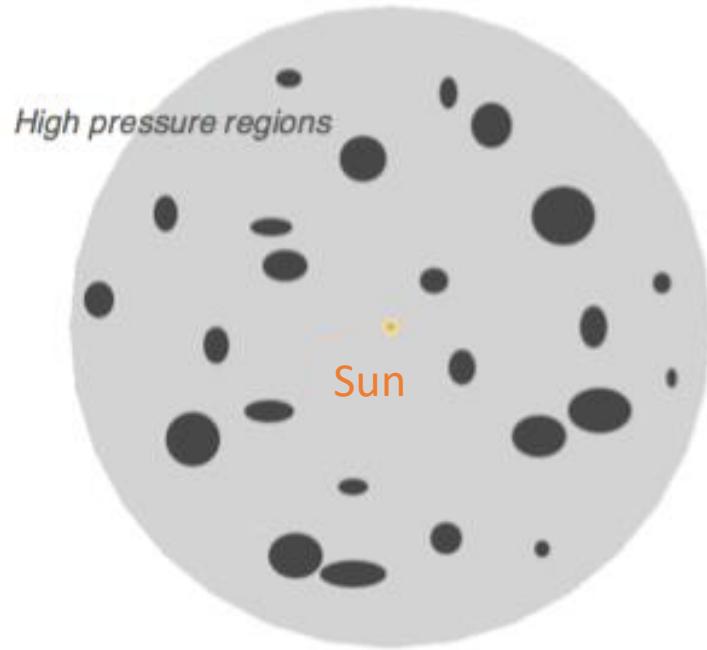
## Gravitational collapse into planetesimals



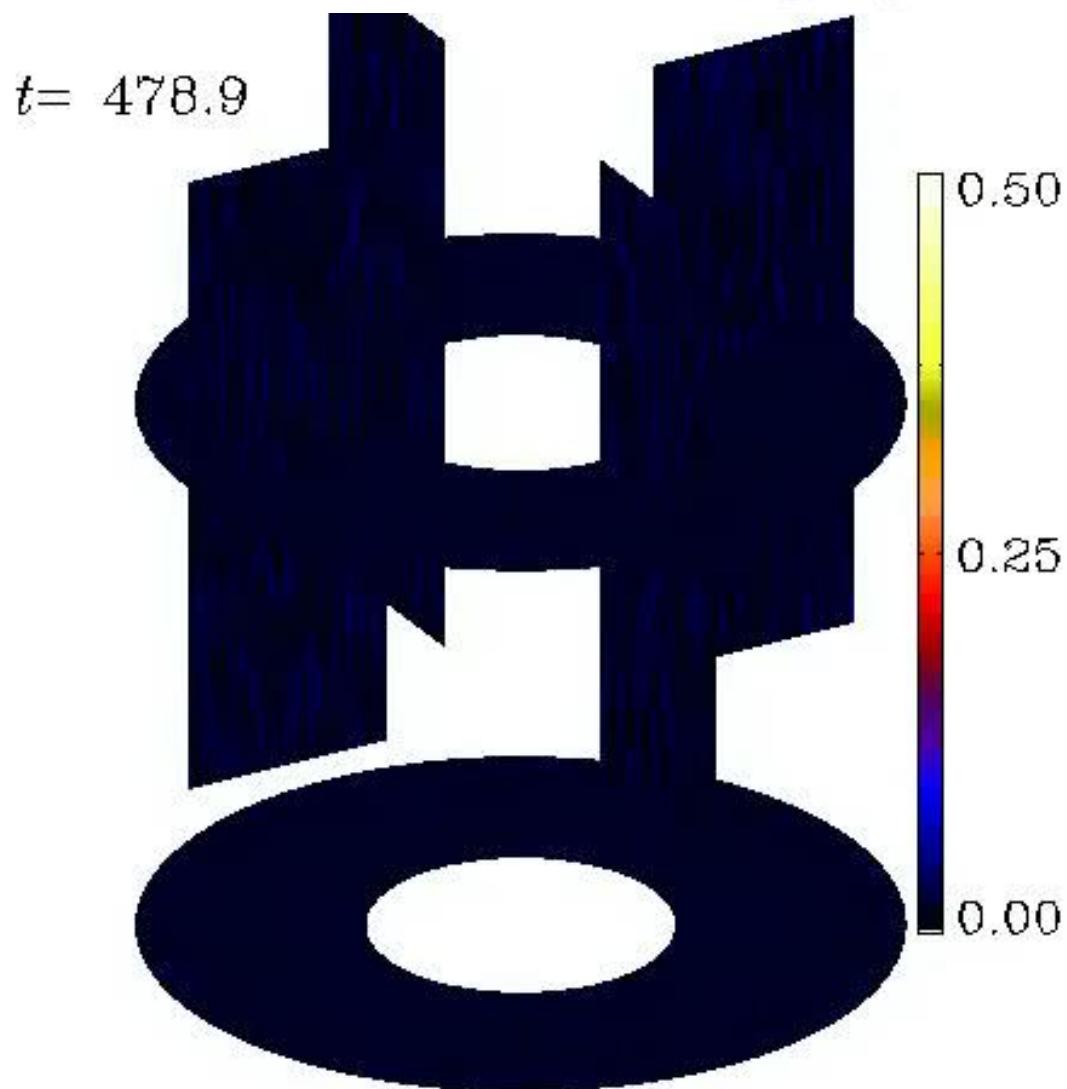
Johansen et al. (2007)

**Turbulence and Accretion in 3D Global  
MHD Simulations of Stratified Protoplanetary Disk**

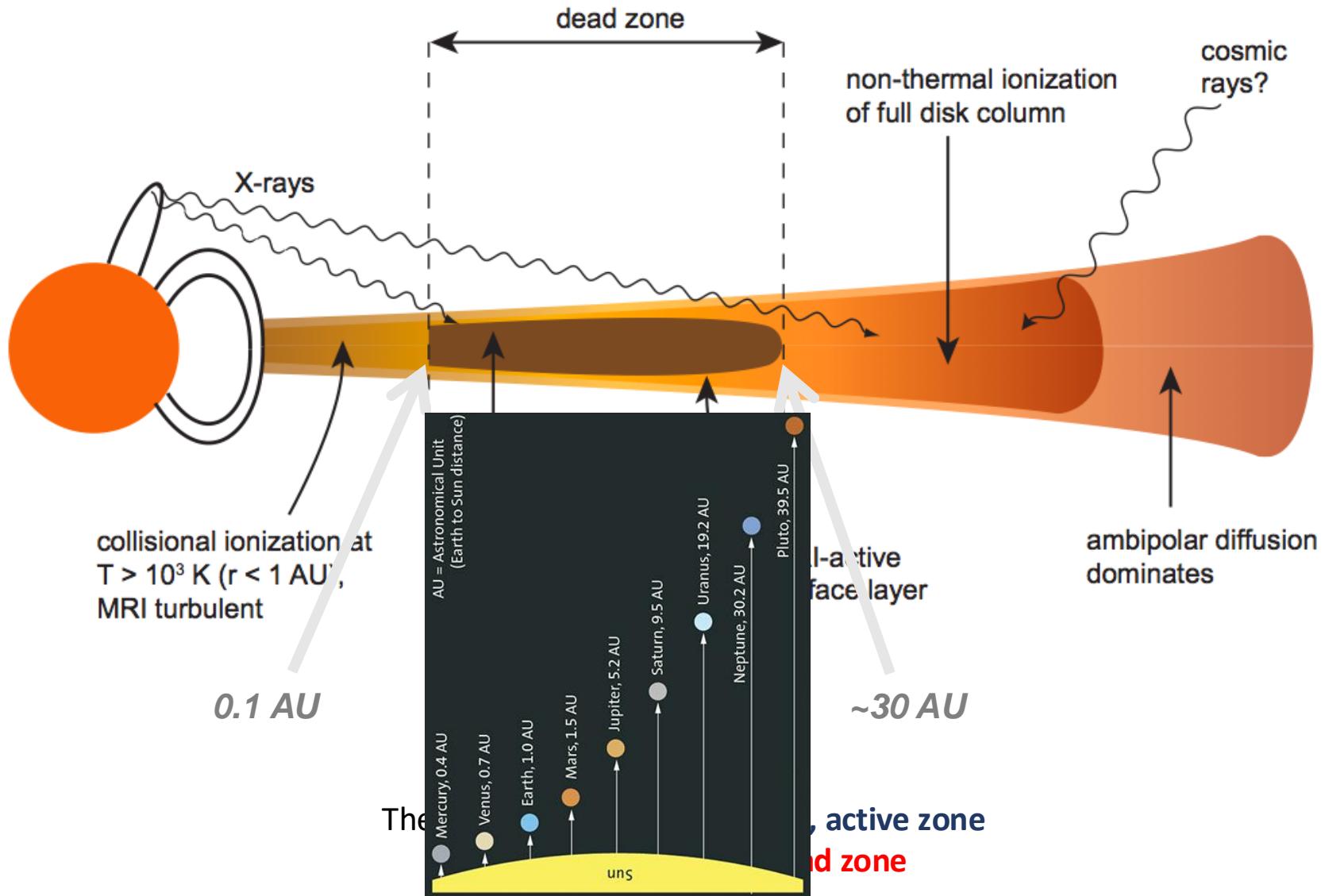
## Turbulence



**Turbulence concentrates solids mechanically in pressure maxima**

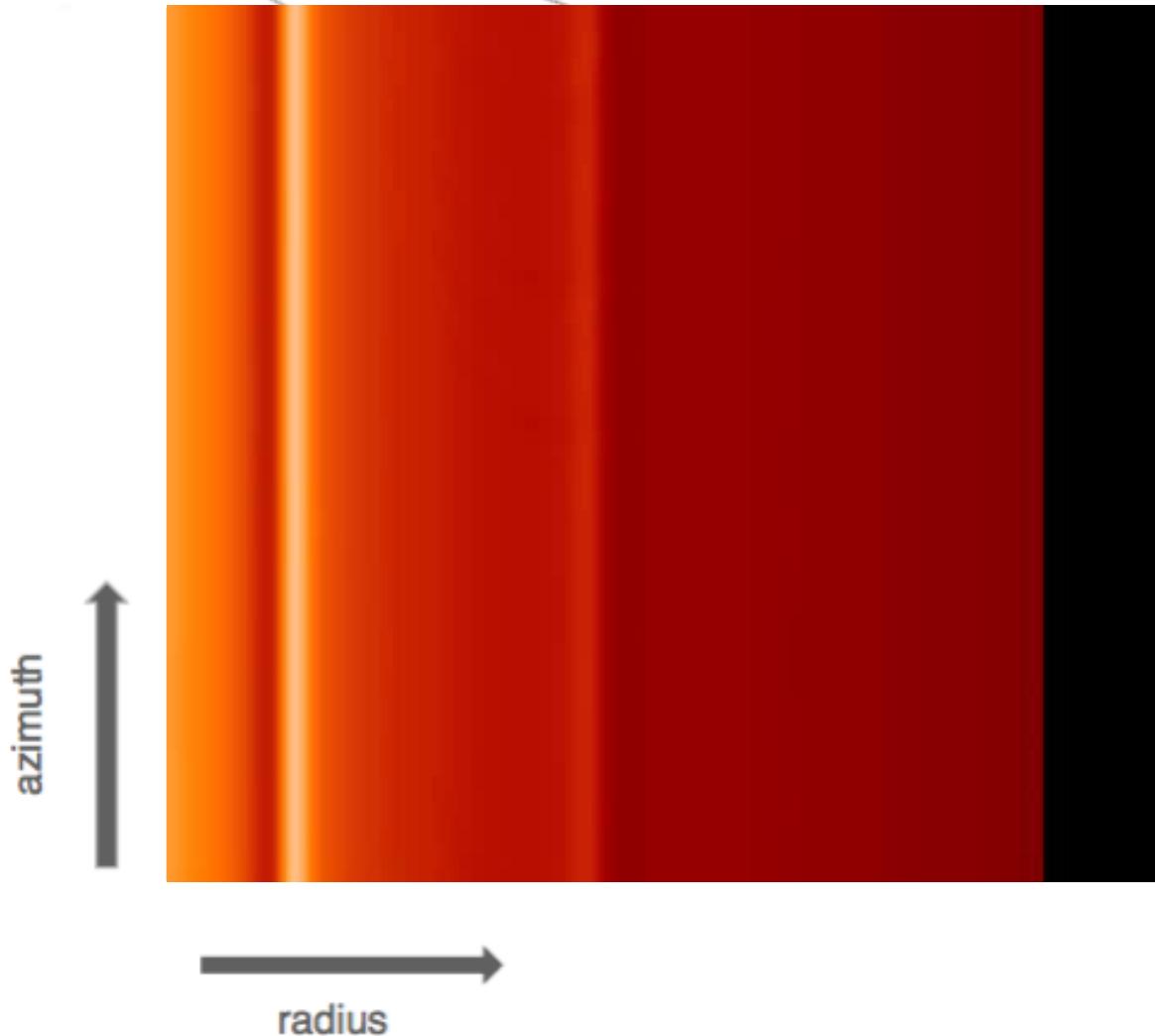


# Dead zones





## A simple dead zone model

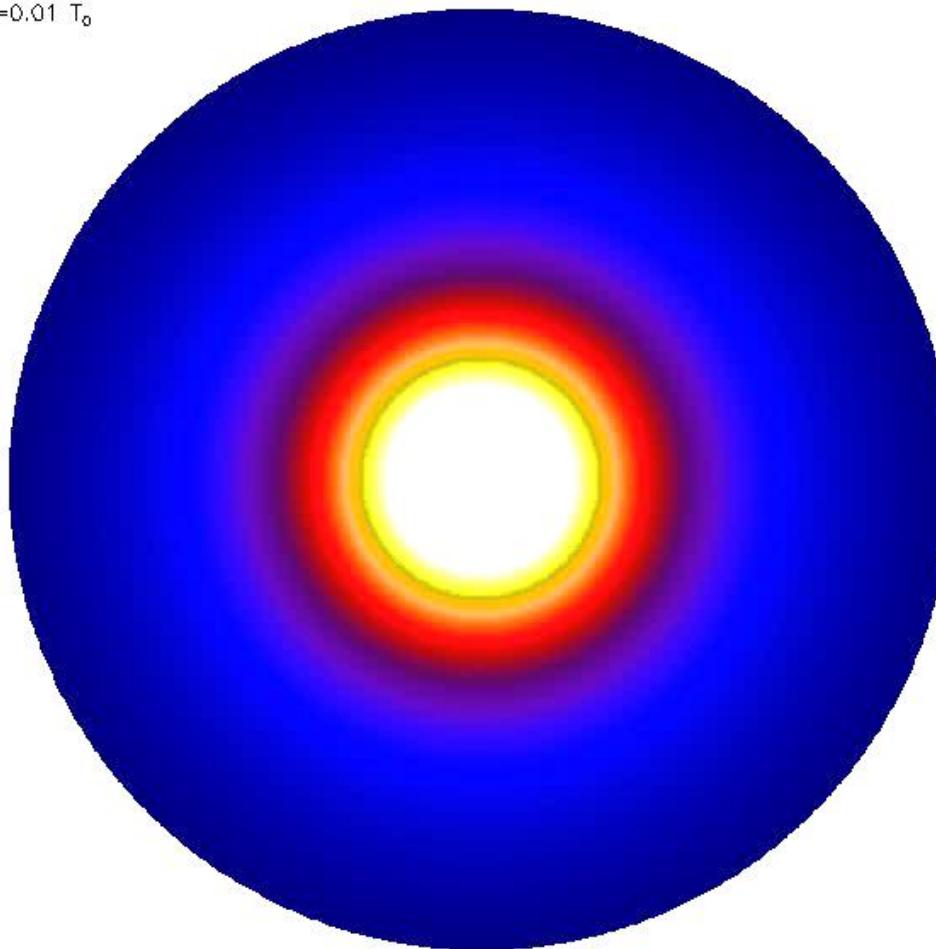


Lyra et al. (2008b, 2009a);  
After Lovelace & Hohlfeld 1978, Toomre 1981, Papaloizou & Pringle (1984), Hawley (1987), Lovelace et al (1999), Li et al. (2000), Varniere & Tagger (2005).



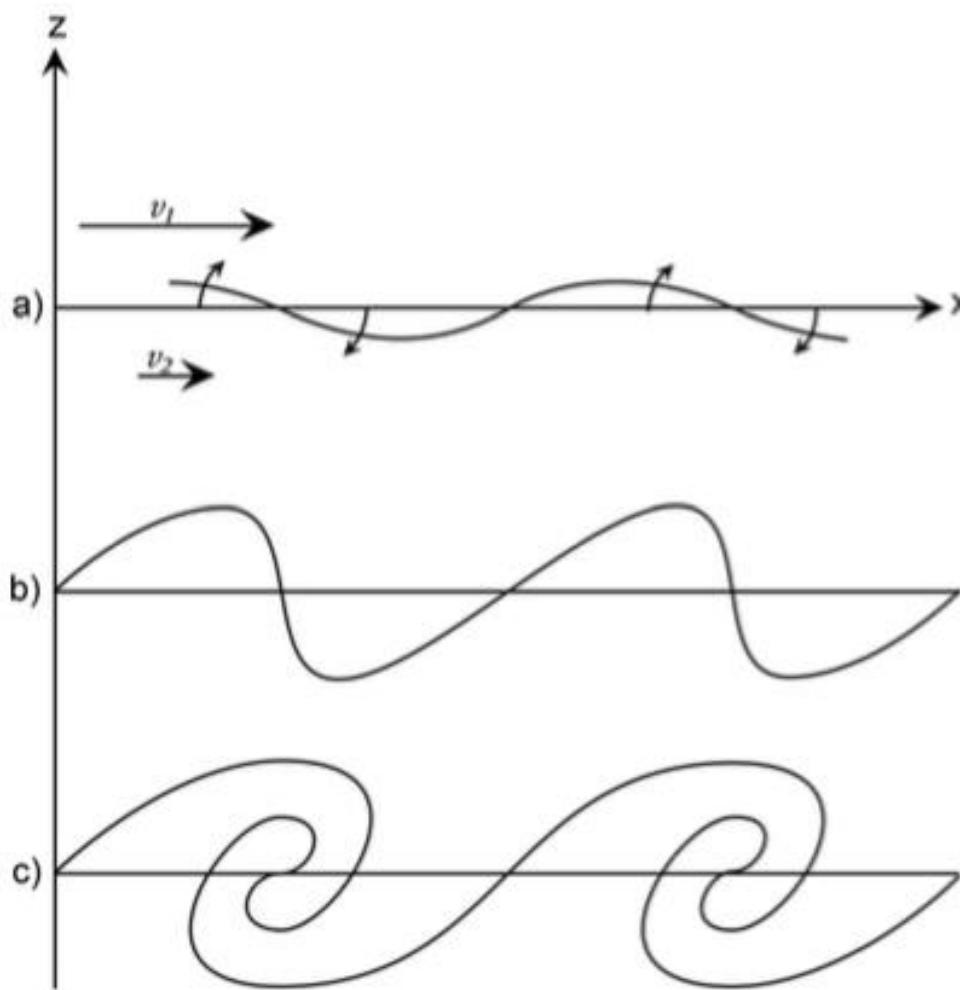
## Inner (0.1 AU) active/dead zone boundary

$t=0.01 T_0$



Magnetized inner disk + resistive outer disk  
Lyra & Mac Low (2012)

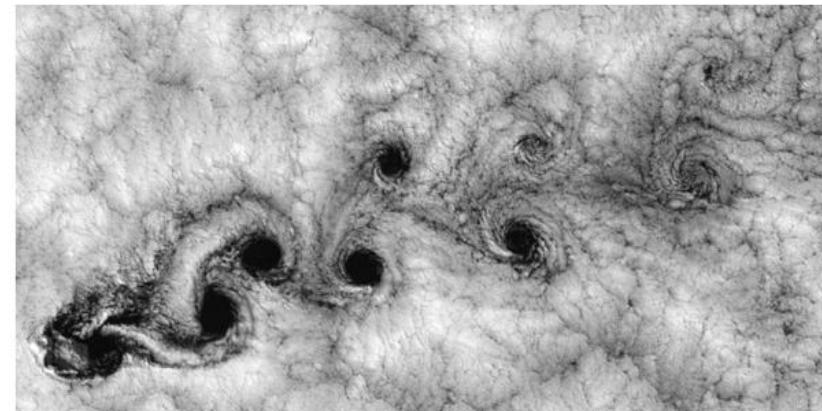
## Rossby wave instability (Kelvin-Helmholtz Instability in rotating disks)



## Vortices – an ubiquitous fluid mechanics phenomenon

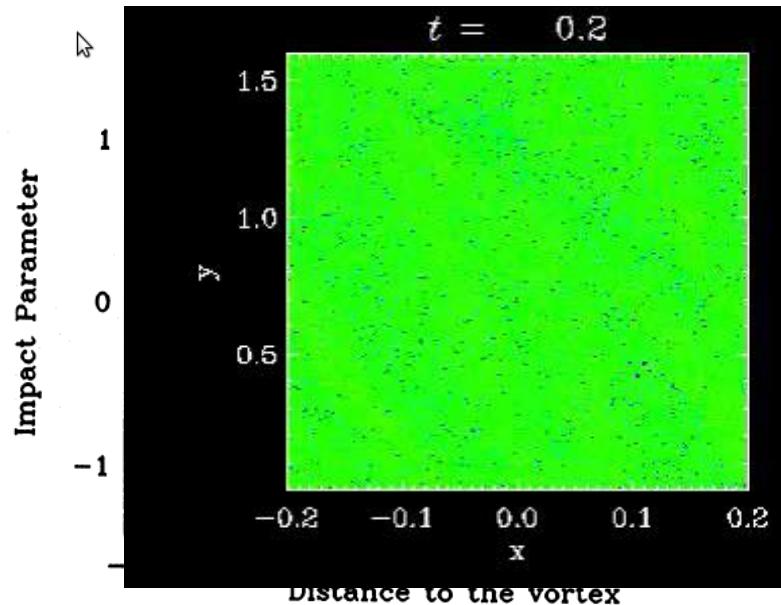
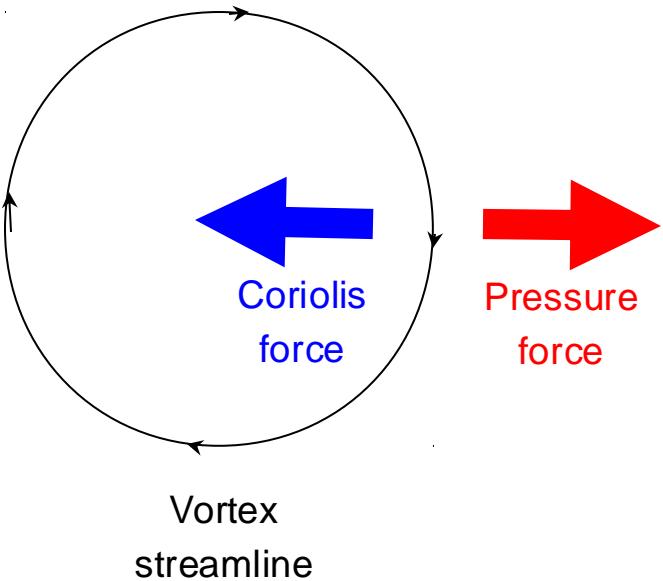


Von Kármán vortex street



# Vortex Trapping

Geostrophic balance:



Barge & Sommeria (1995)

Grains do not feel the pressure gradient.  
They sink towards the center, where they accumulate.

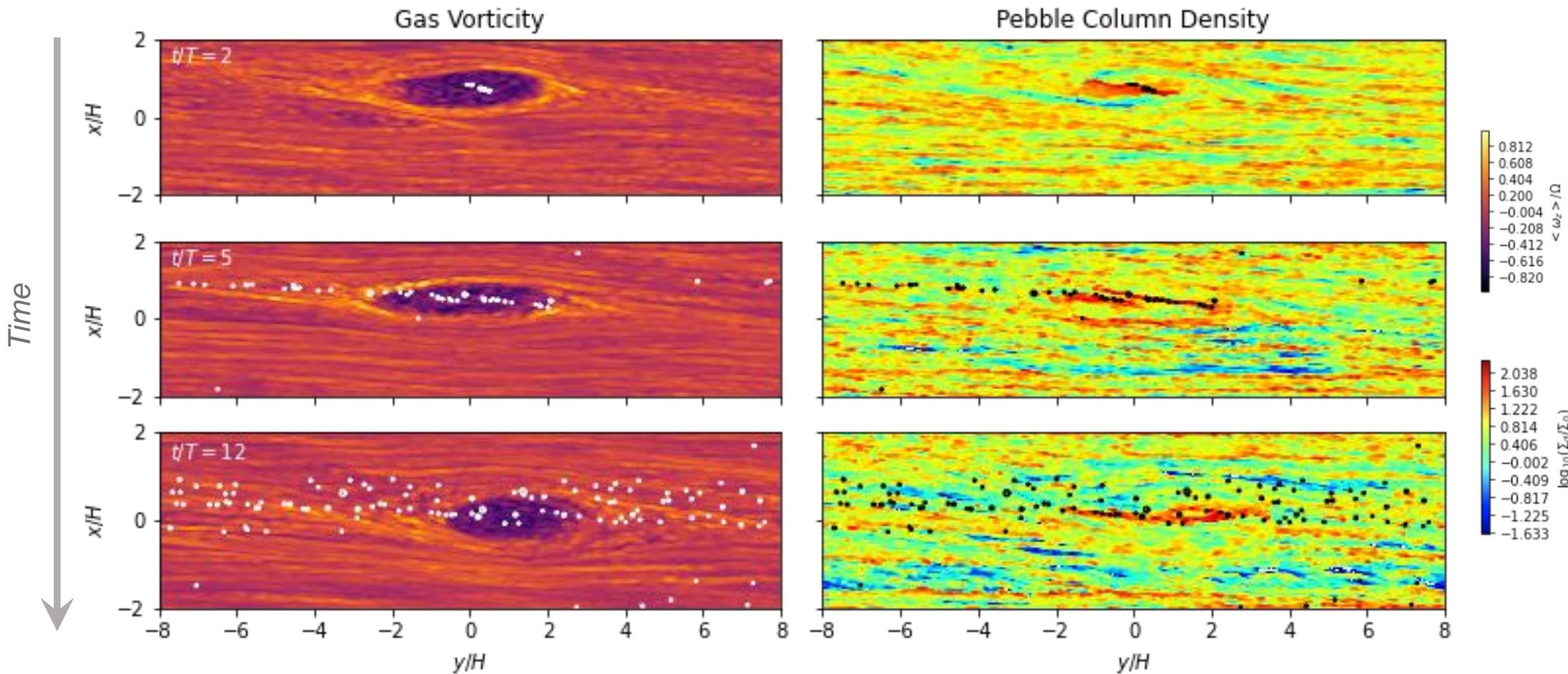
Aid to planet formation

(Barge & Sommeria 1995, Tanga et al. 1996, Adams et al. 1996)

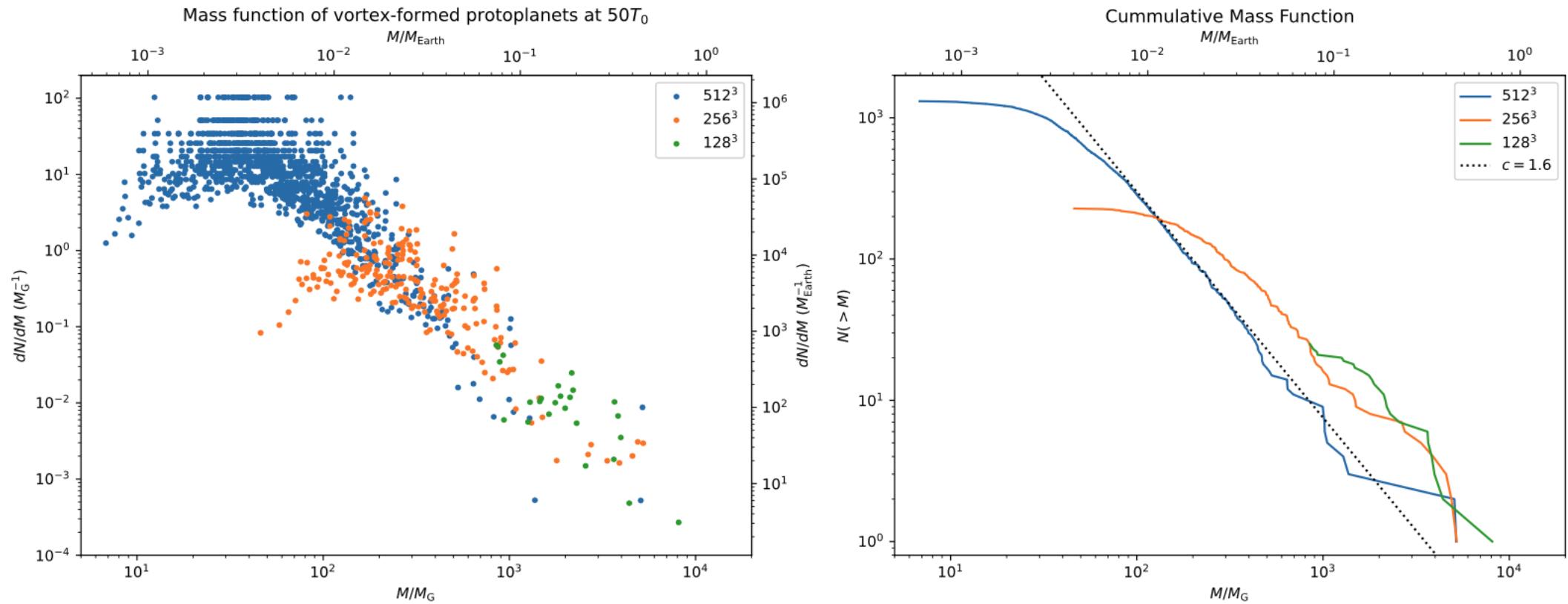
Speeds up planet formation enormously

(Lyra et al. 2008b, 2009ab, Raettig et al. 2012, 2021)

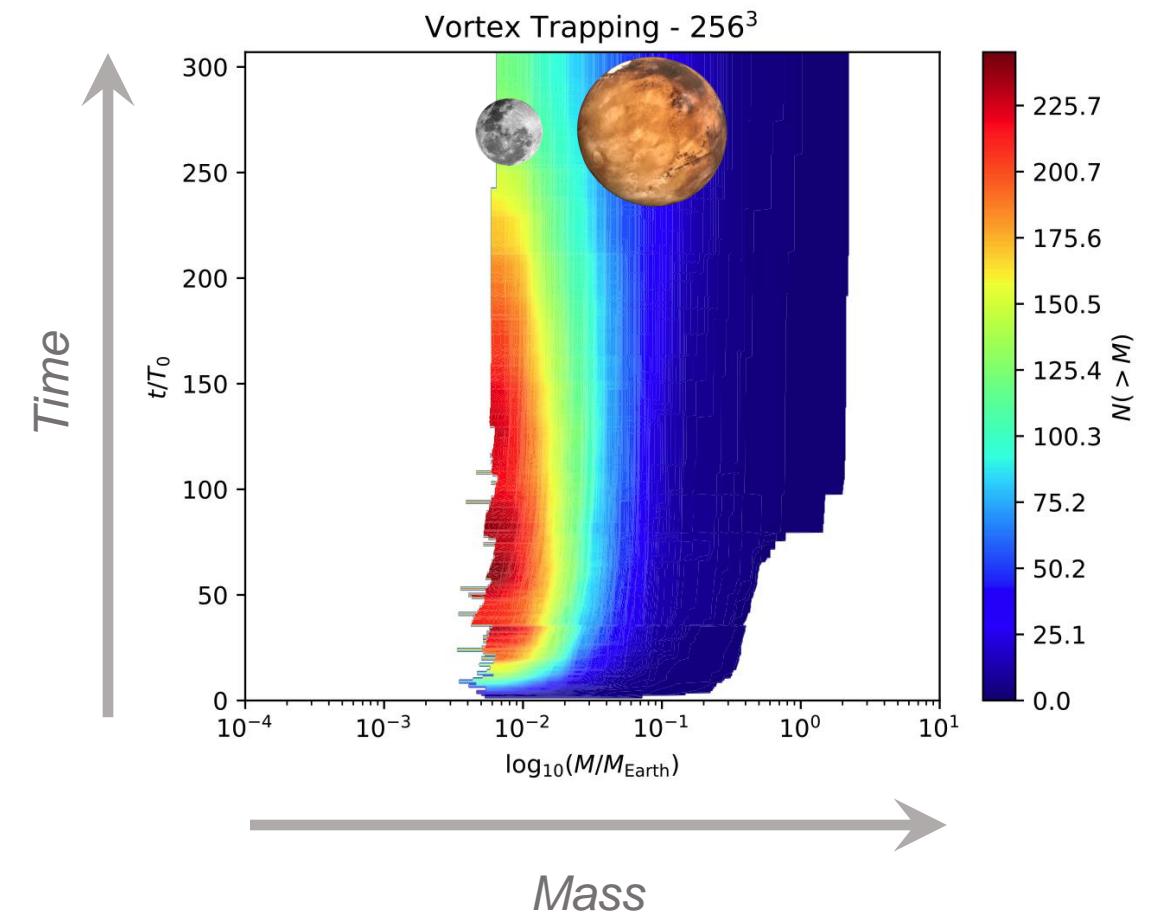
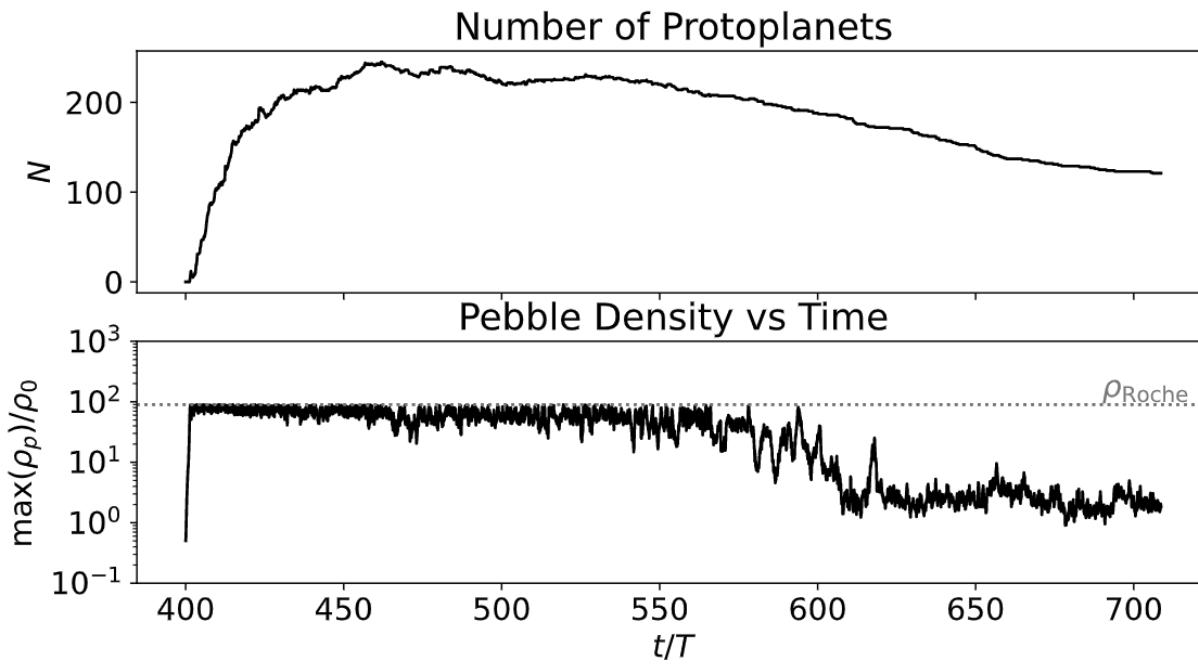
# Vortex Trapping



# Vortex Trapping – Initial Mass Function



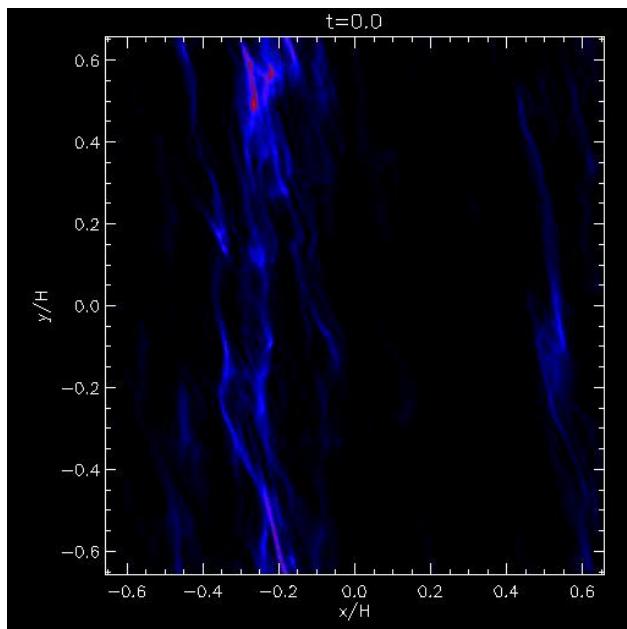
# Initial Mass Function - Convergence



# Take home message

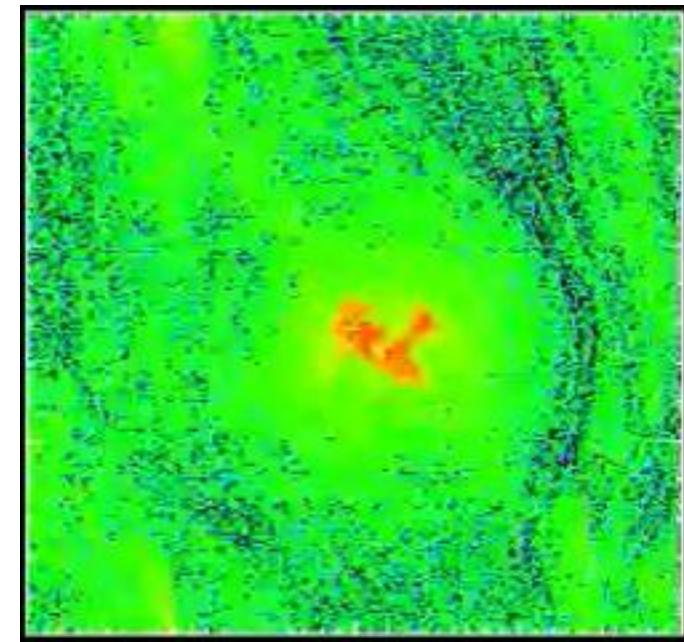
- Two routes for planet formation

Streaming Instability



Johansen+ 07

Vortex Trapping

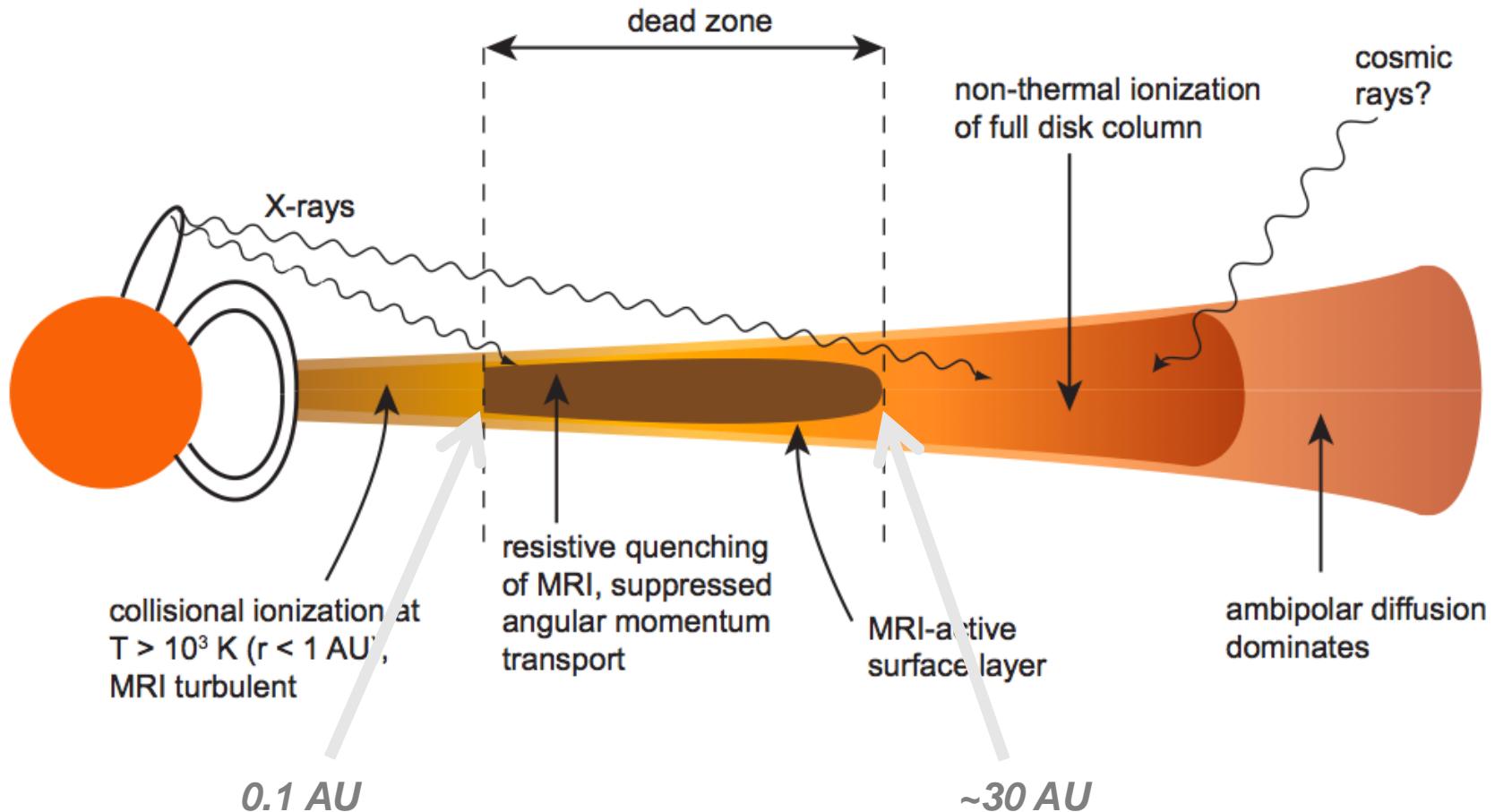


Lyra+08,18 Raettig+Lyra 12,15,21

- Planet formation and turbulence.
  - Does turbulence help (concentration at large scales) or hinder (diffusion at small scales)?

# Disk Instabilities

# Dead zones

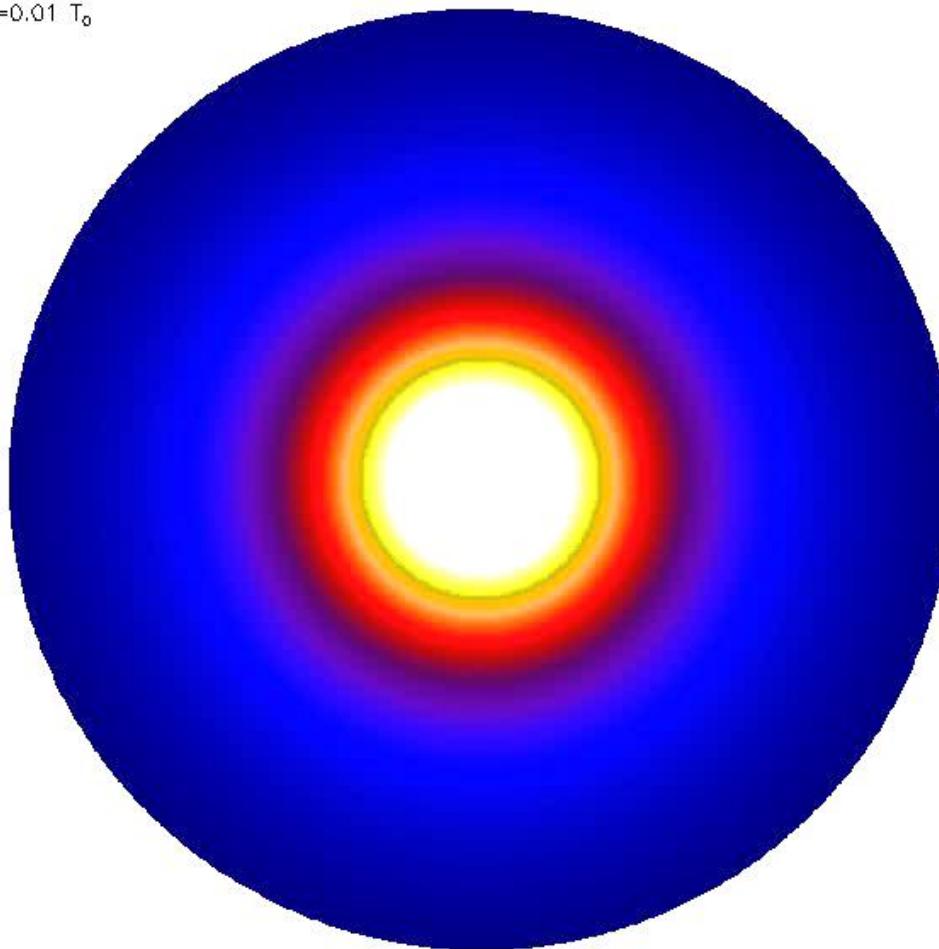


There should be a **magnetized, active zone**  
and a **non-magnetic, dead zone**



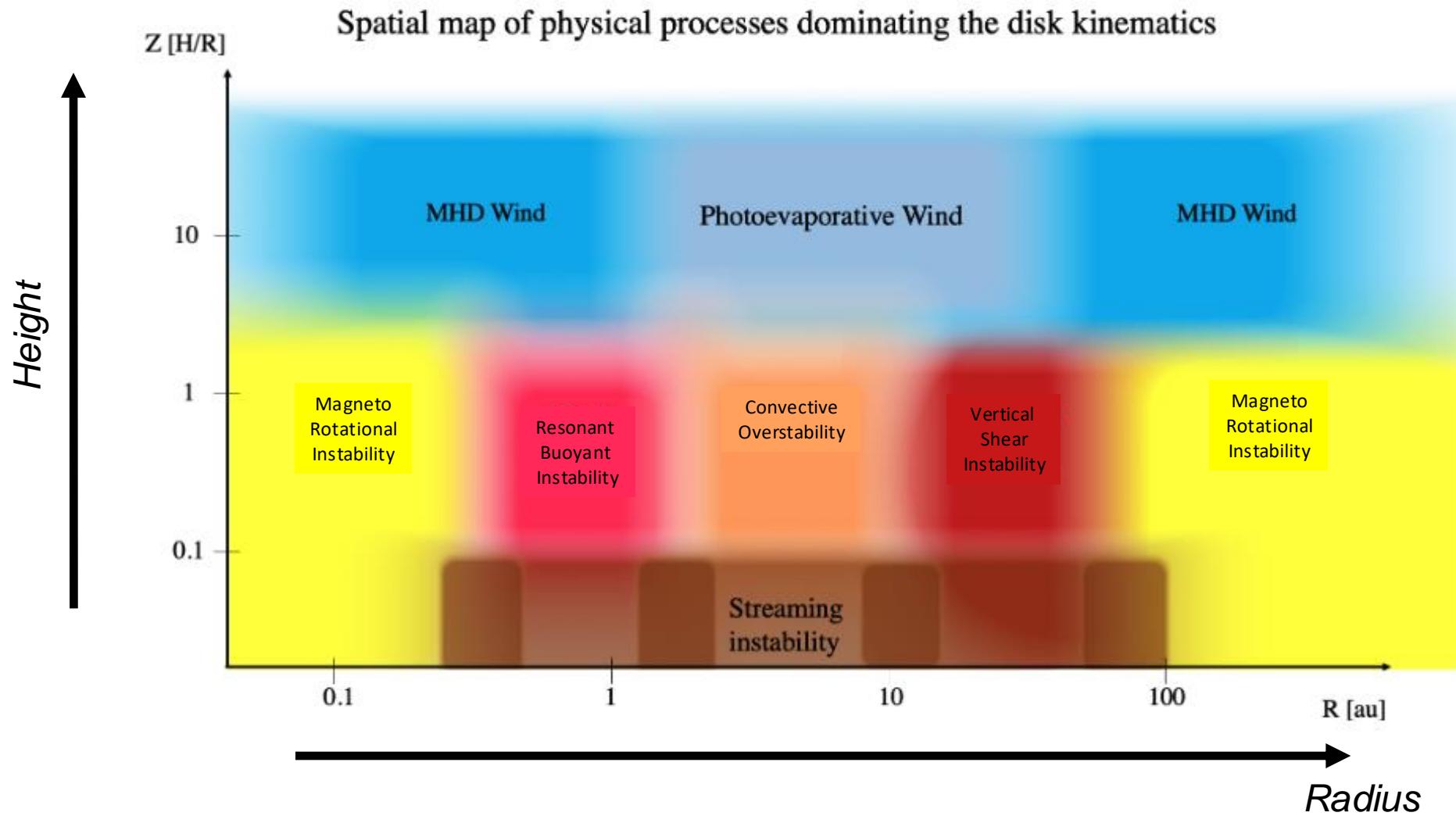
## Inner (0.1 AU) active/dead zone boundary

$t=0.01 T_0$



Magnetized inner disk + resistive outer disk  
Lyra & Mac Low (2012)

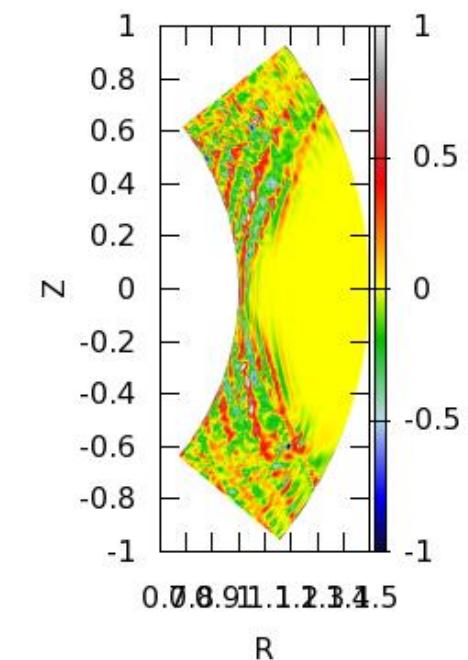
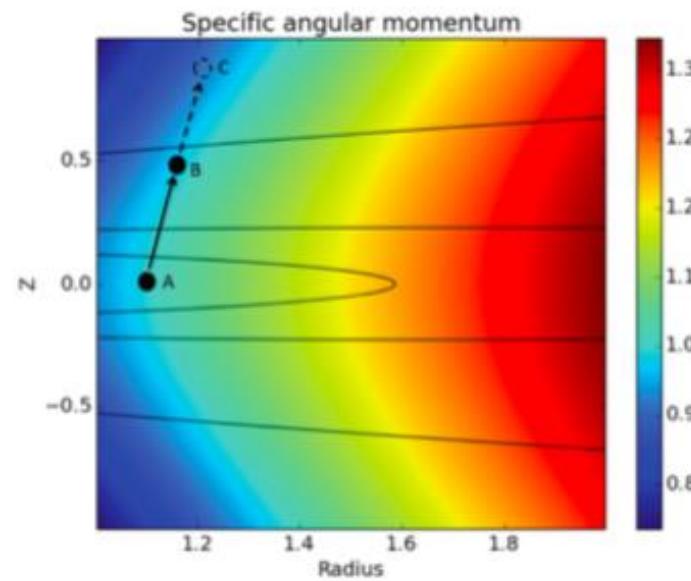
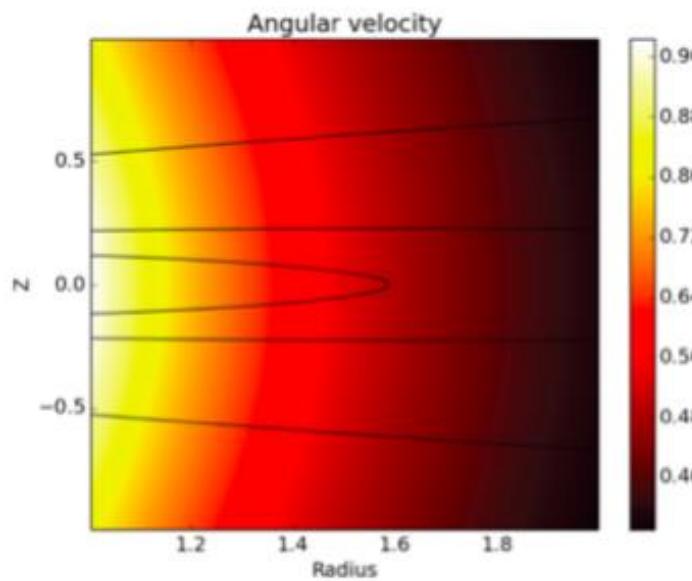
# Instability Map



## Vertical shear instability

Angular velocity not constant in cylinders: unstable

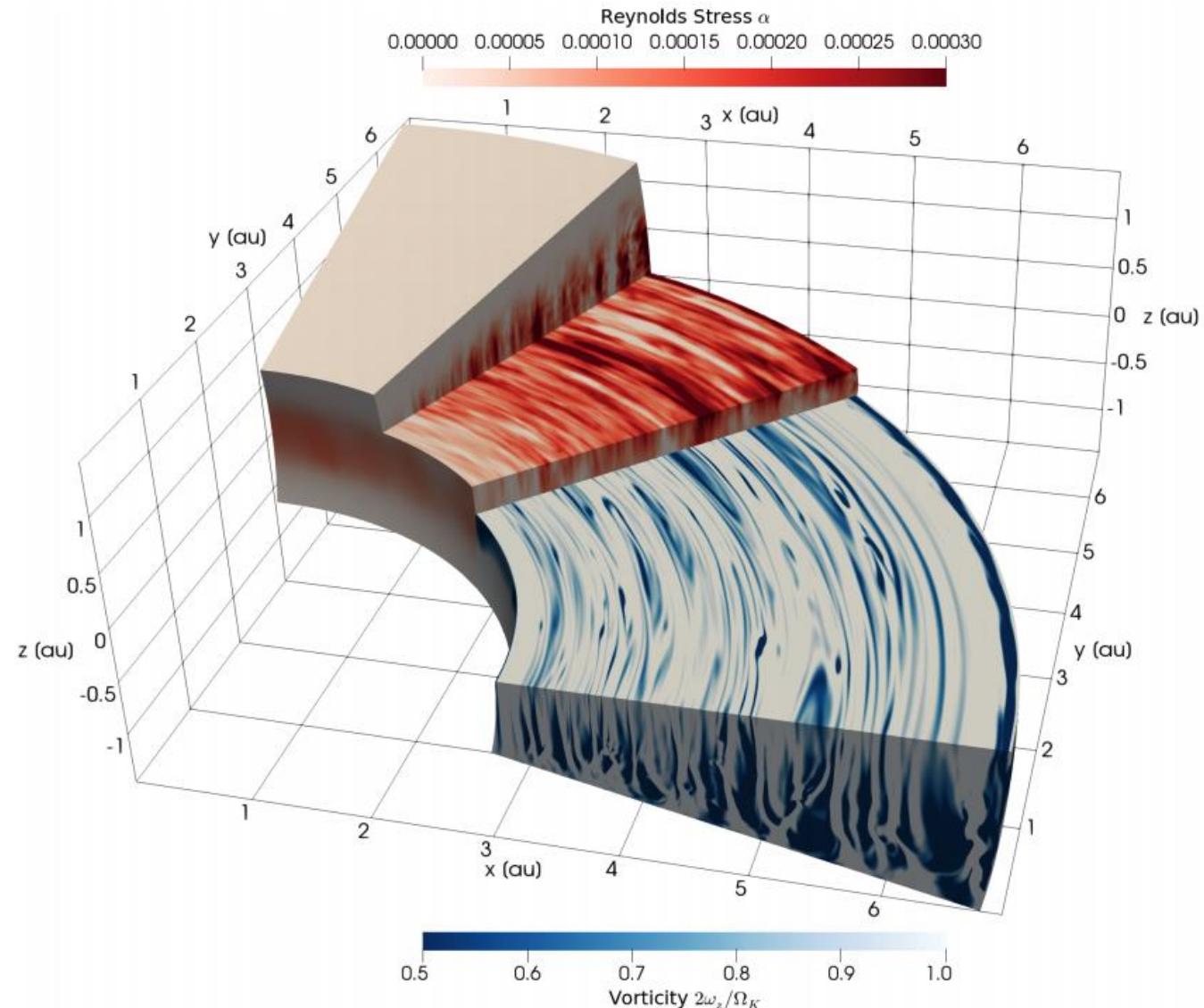
Buoyancy stabilizes. The most unstable mode is isothermal.



Fromang & Lesur (2017)

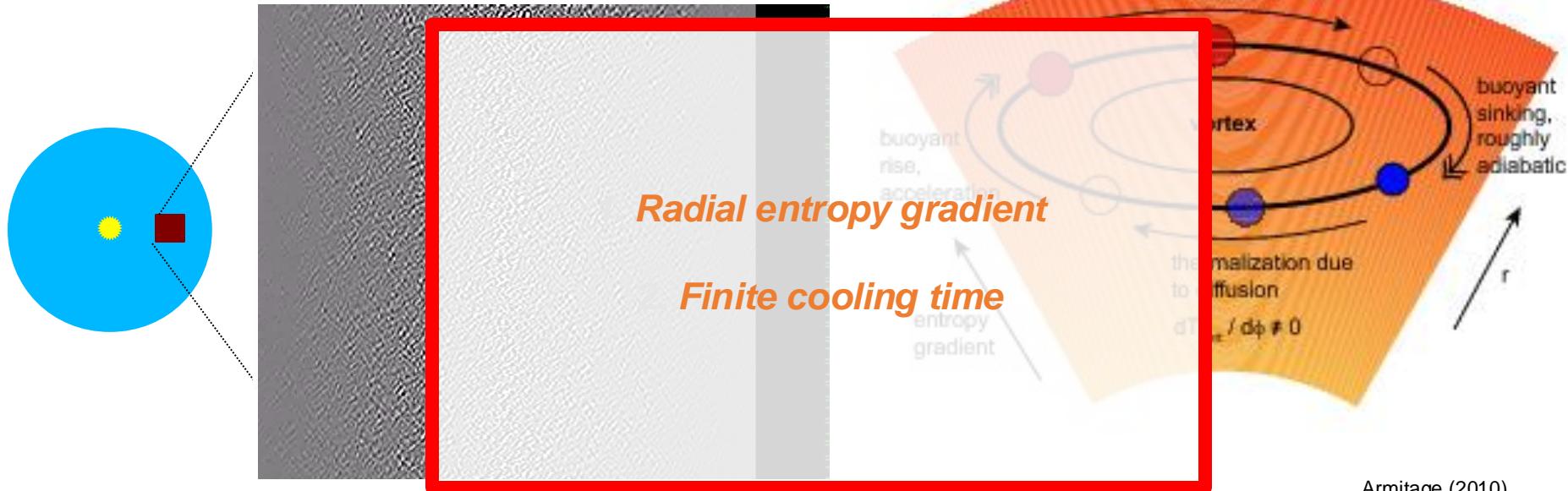
Nelson et al. (2013)

## Vertical shear instability



# Convective Overstability

Sketch of the  
Convective Overstability



Lesur & Papaloizou (2010)

Lyra & Klahr (2011)

Klahr & Hubbard (2014)

Lyra (2014)

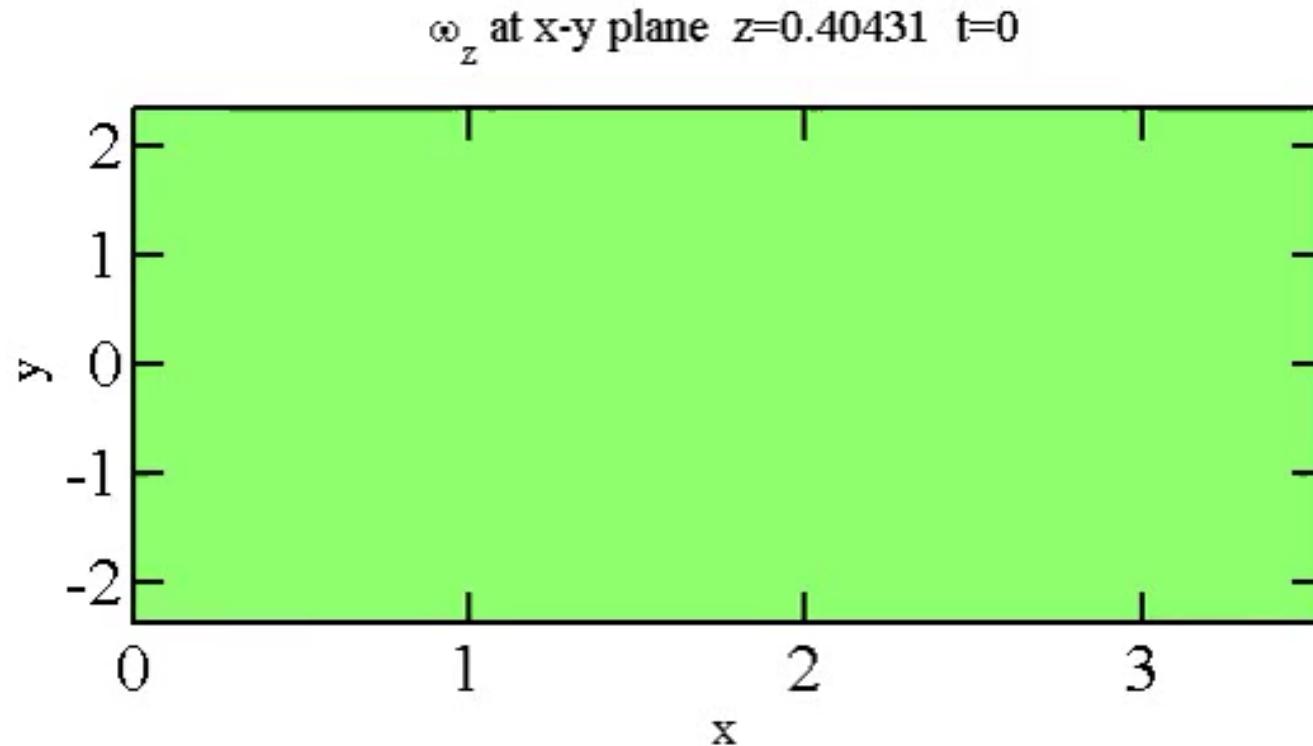
Latter (2016)

Volponi (2016)

Reed & Latter (2021)

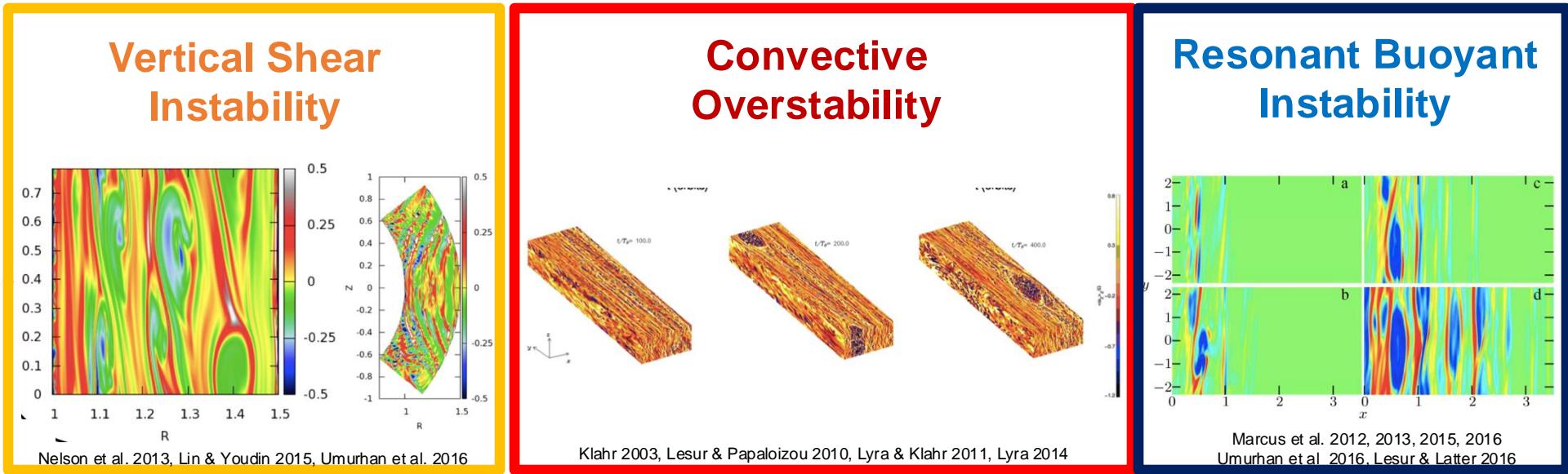
Raettig et al. (2021)

## Resonant Buoyant Instability (née Zombie Vortex Instability)



Cascade of baroclinic critical layers

# Hydrodynamical Instabilities



$\Omega\tau \ll 1$   
( $\kappa < 1 \text{ cm}^2/\text{g}$ )

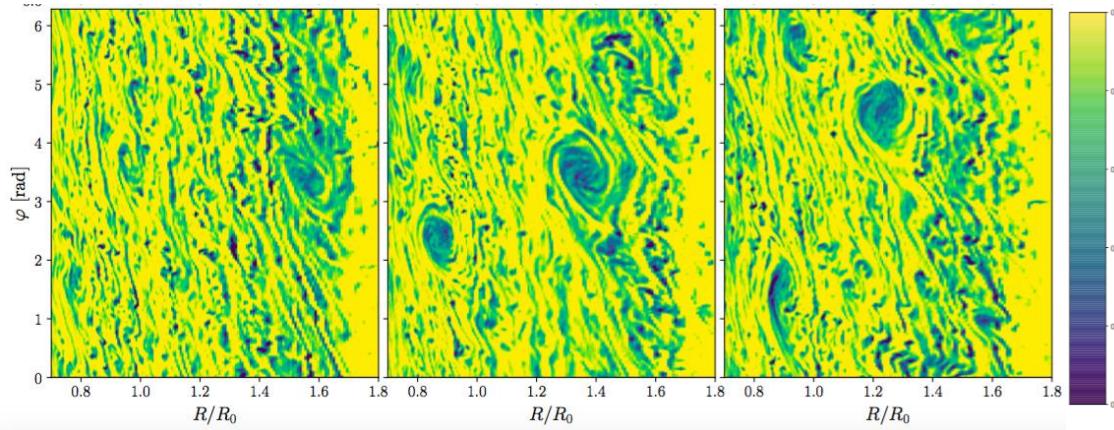
$\Omega\tau \sim 1$   
( $\kappa \sim 1\text{--}50 \text{ cm}^2/\text{g}$ )

$\Omega\tau \gg 1$   
( $\kappa > 50 \text{ cm}^2/\text{g}$ )

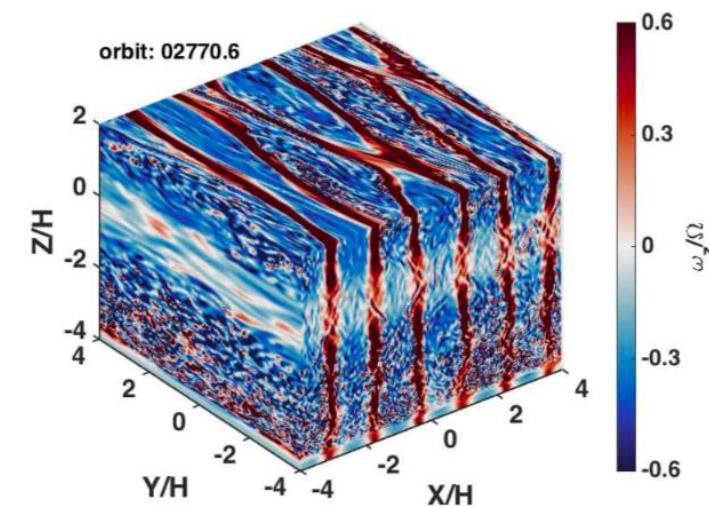


*Opacity*

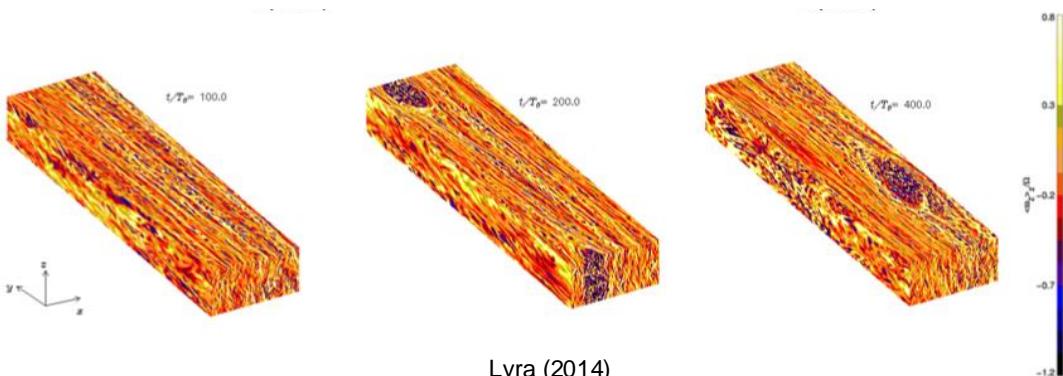
## Take-home message



**Vertical Shear Instability**  
saturates into  
**vortices**

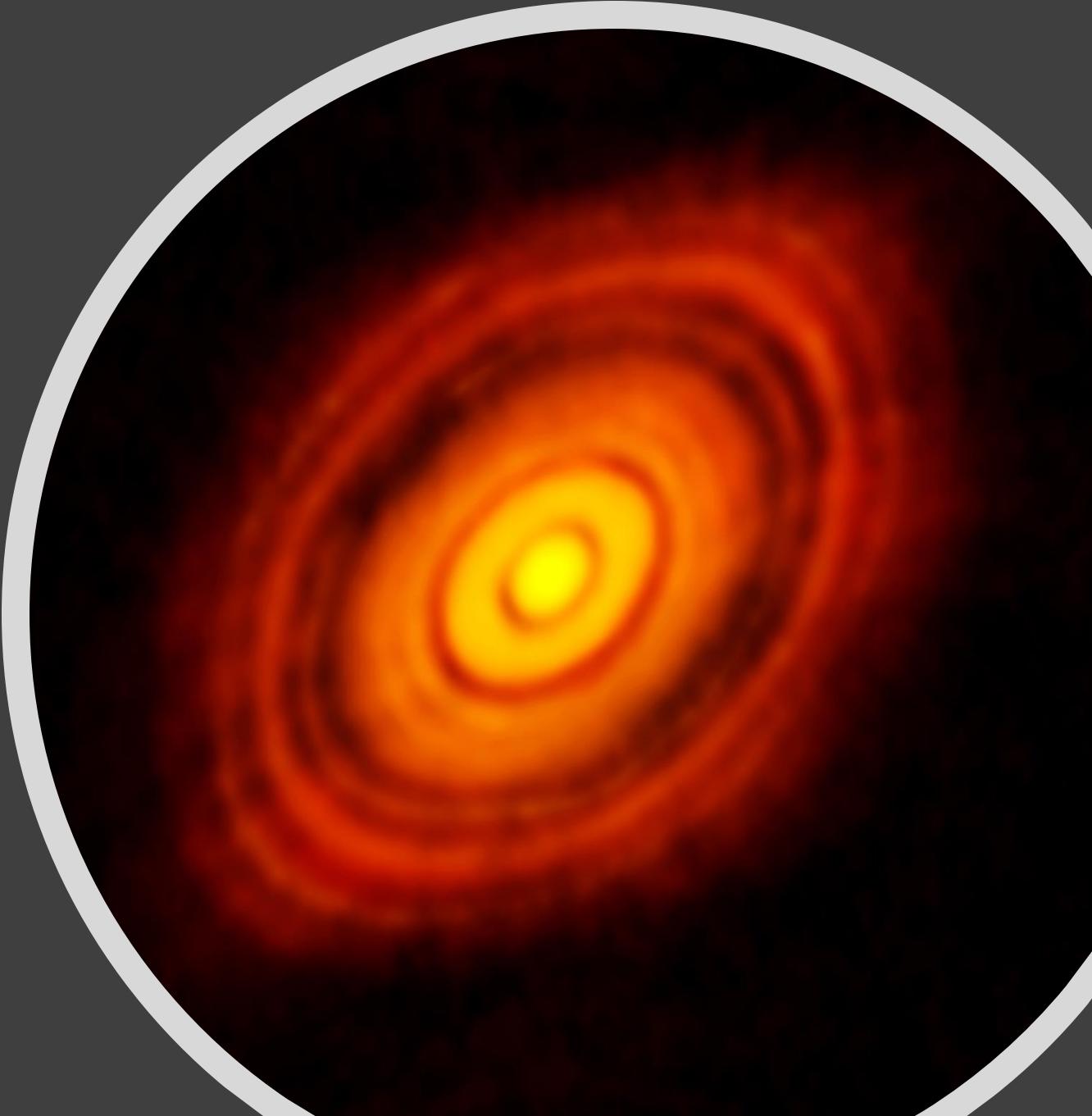


Barranco et al. (2018)

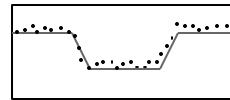


**Convective Overinstability**  
saturates into  
**vortices**

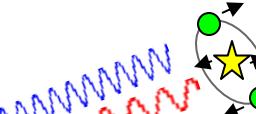
# Disk Observations



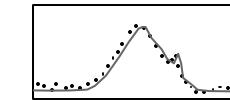
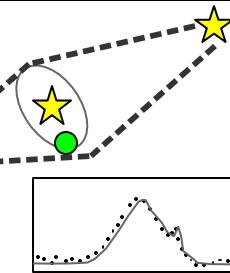
## Transits



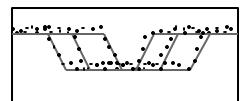
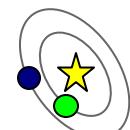
## Radial velocities



## Microlensing



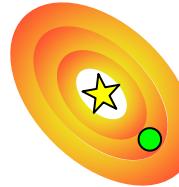
## Timing variations



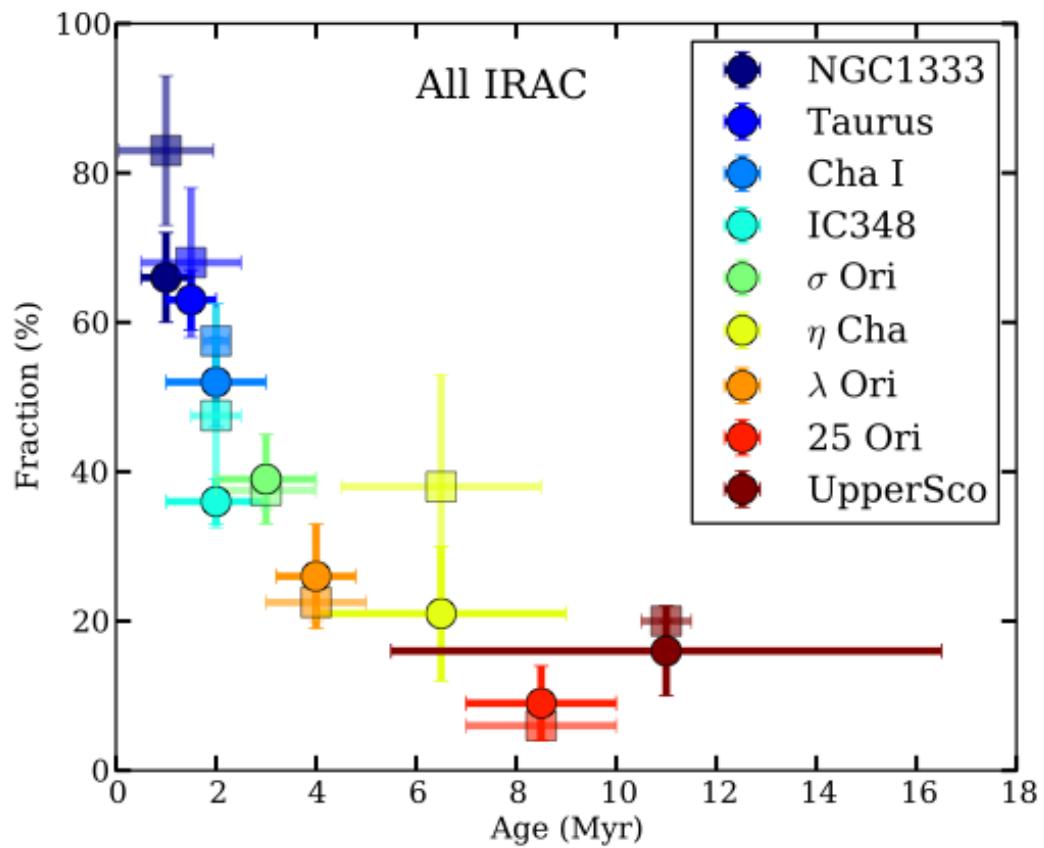
## Direct imaging



## Disk interactions



# Disk lifetime

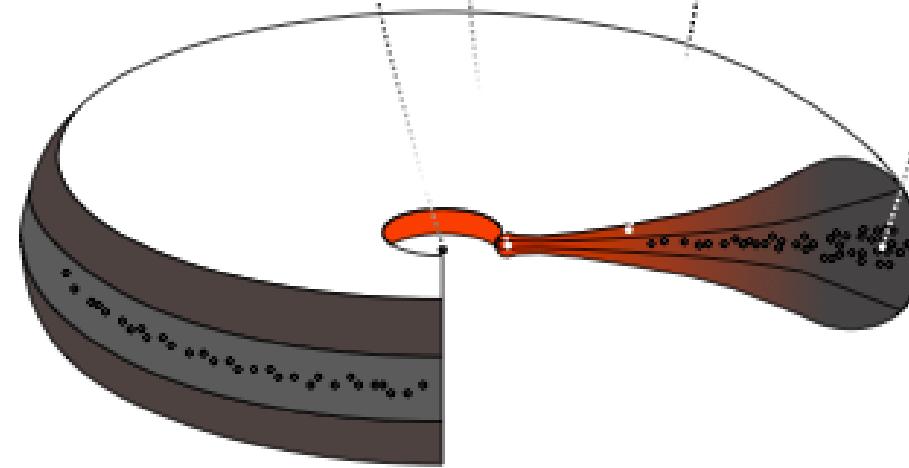
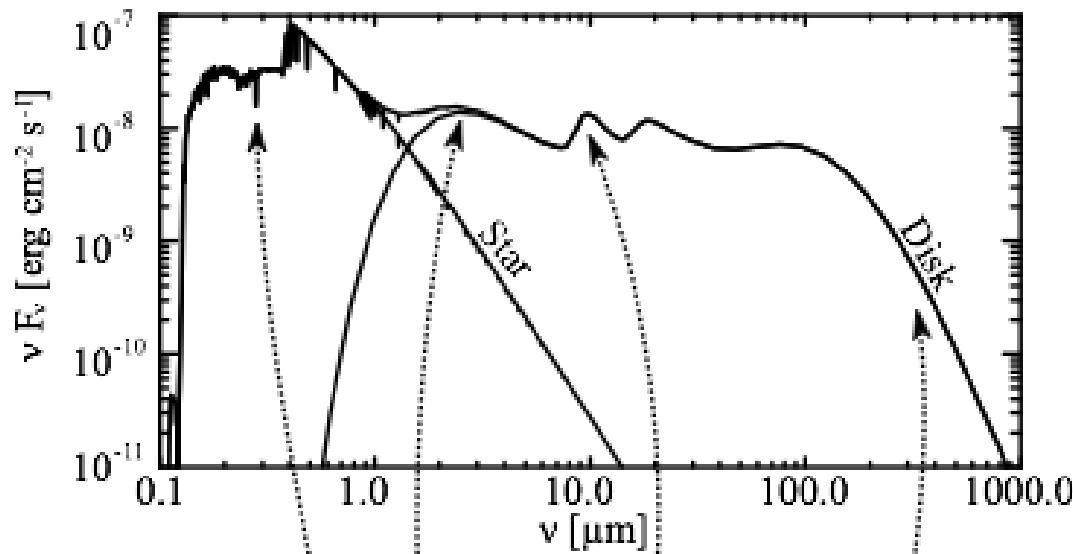


(Ribas et al. 2014)

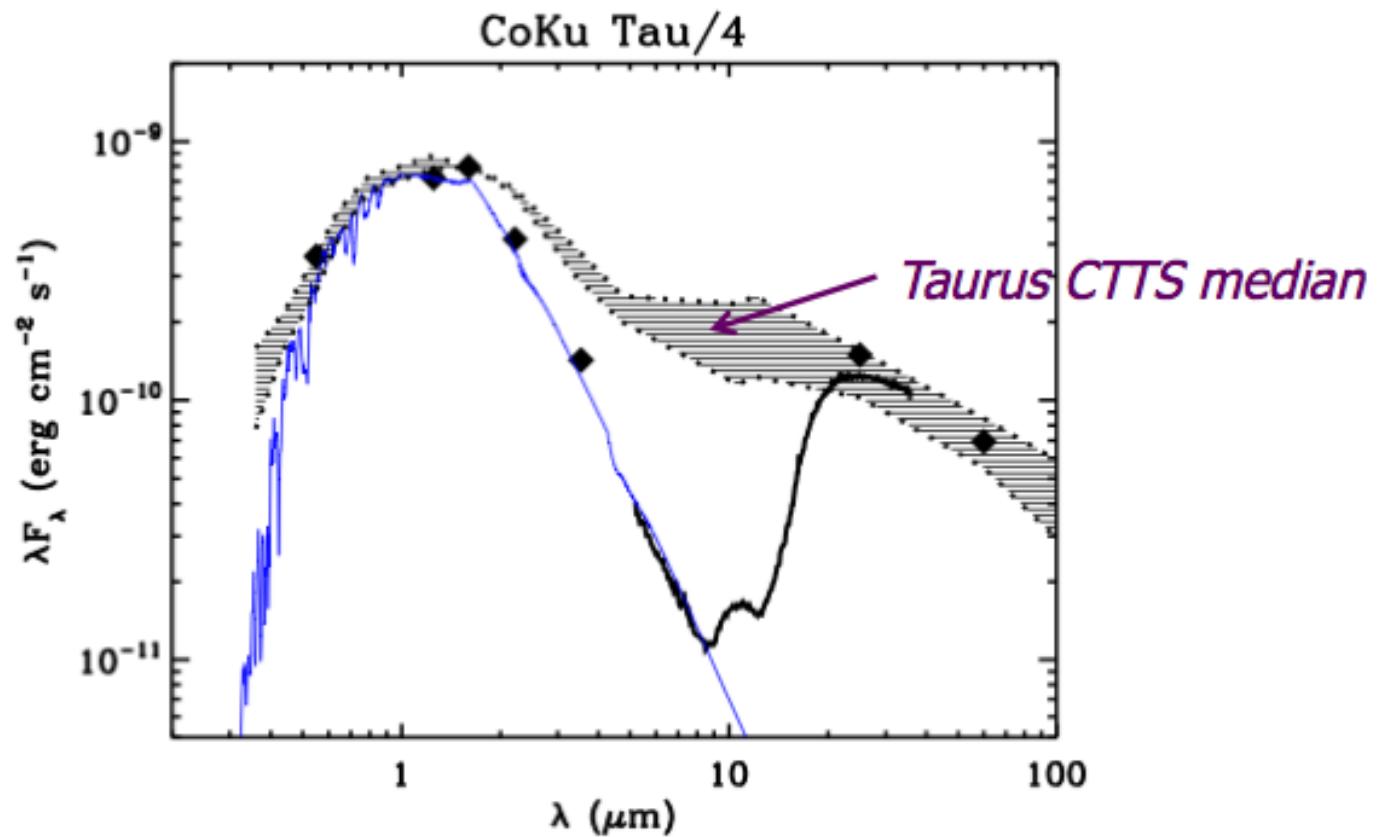


Disks dissipate within  $\sim$ 10 Myr  
Mass accretion rates  $\sim 10^{-8} M_{\odot} \text{ yr}^{-1}$

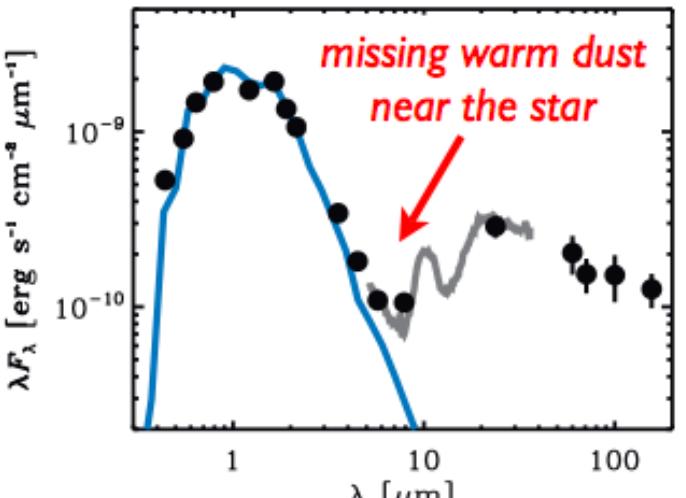
# Disk spectra



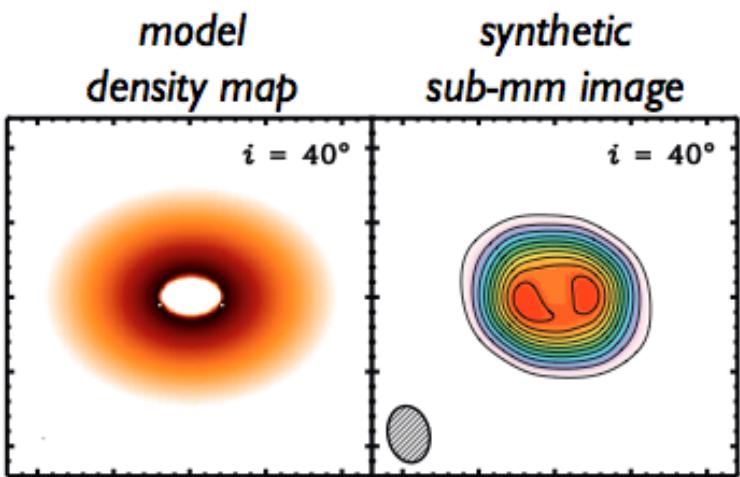
# A class of disks with missing hot dust.



# Disks with missing hot dust.



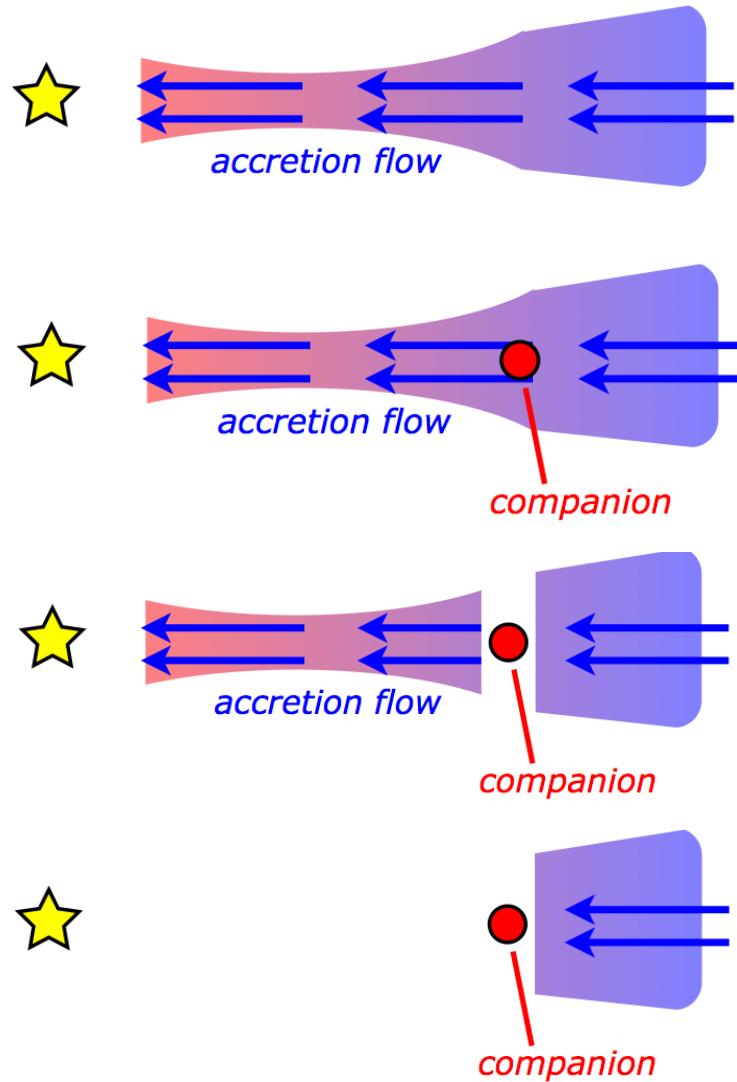
[e.g., Furlan et al. 2009]



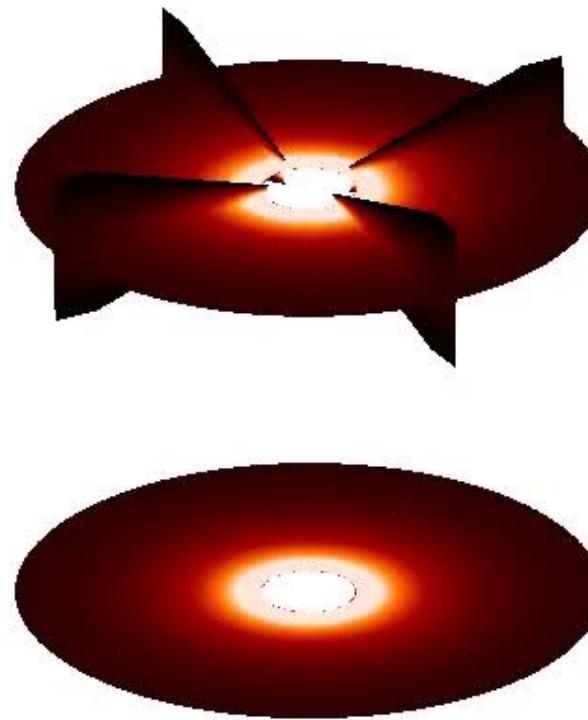
a disk with a large reduction  
in optical depth near the star  
(i.e., a “cavity” or “hole”)



# Planetary companion

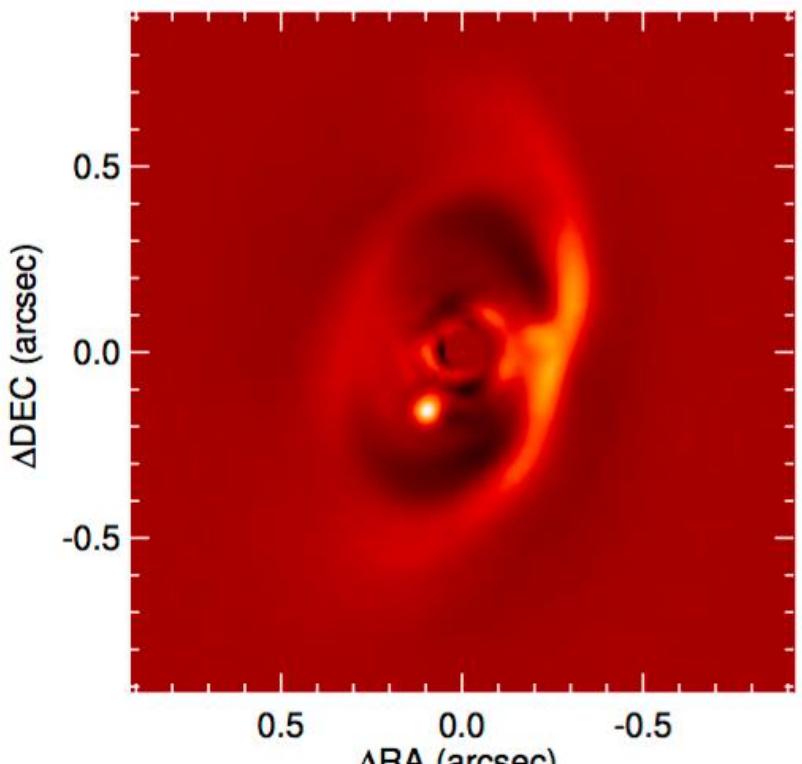


$t = 0.1$

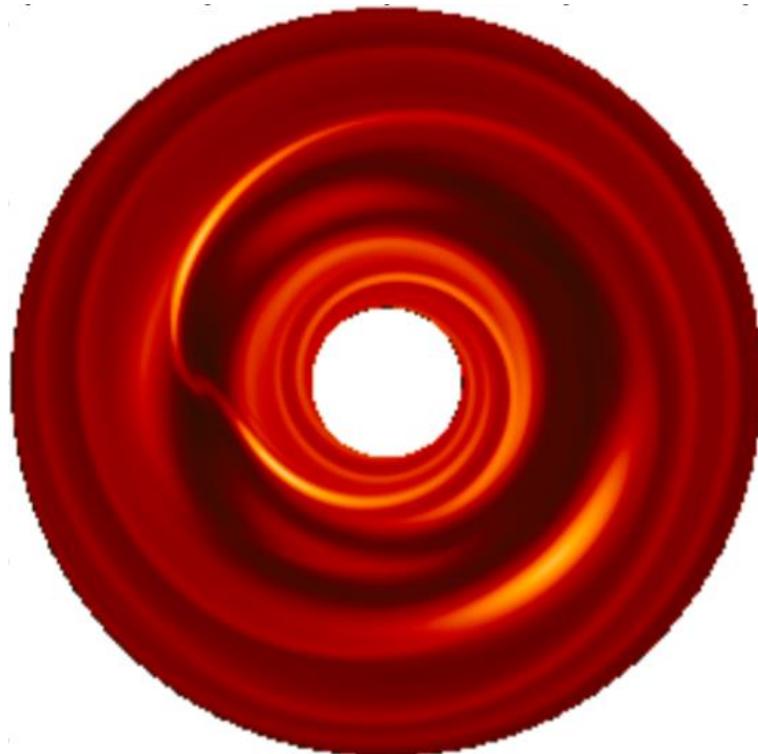


**These cavities may be the telltale signature of forming planets**

PDS 70 and PDS 70b



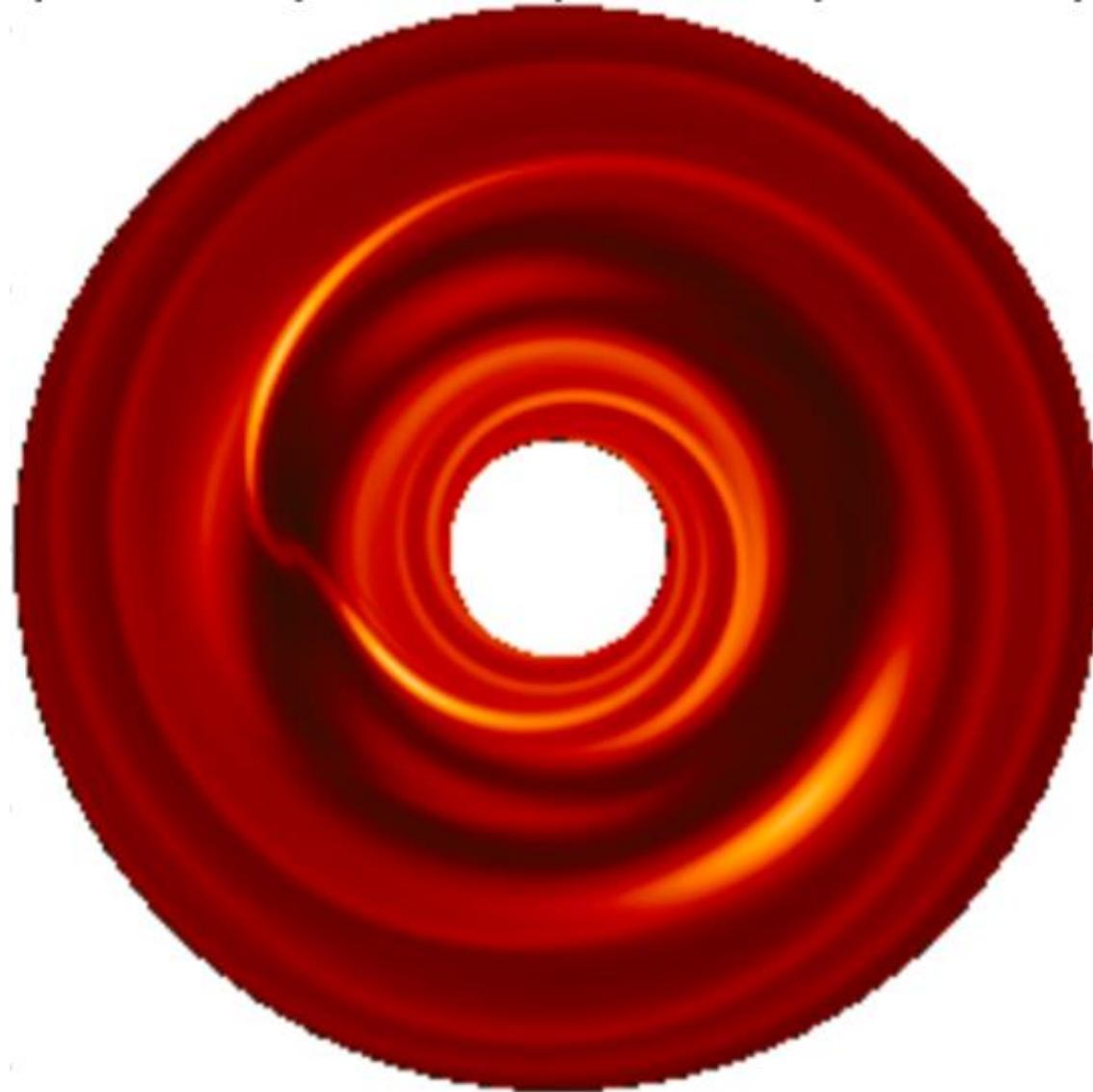
(Muller et al. 2018)



(Lyra et al. 2009b)

A way to directly study planet-disk interaction

## Planet-disk interaction: gaps, spirals, and vortices.

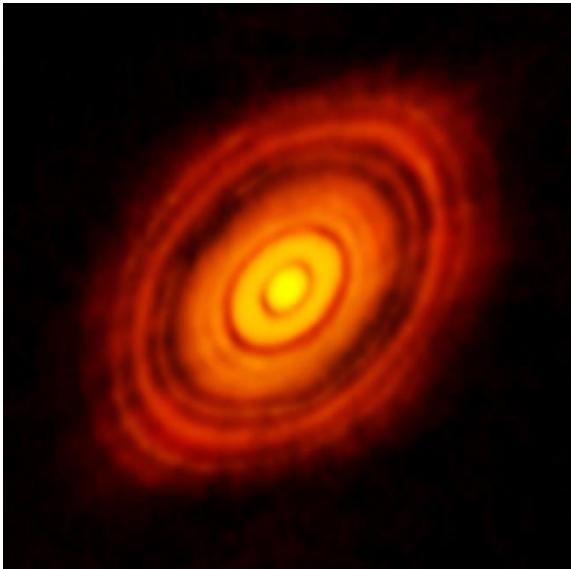


(Lyra et al. 2009b)

43

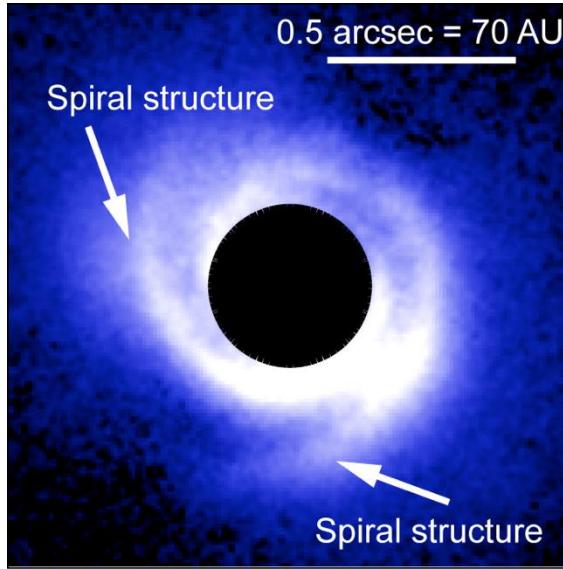
# Observational evidence: gaps, spirals, and vortices

HL Tau



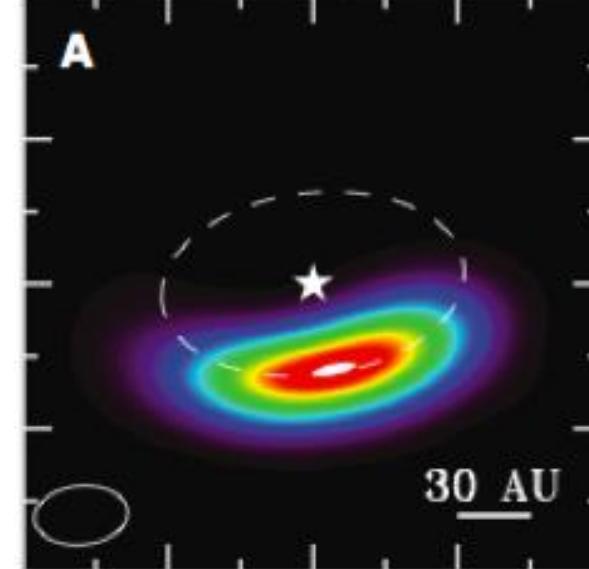
The ALMA Partnership et al. (2015)

SAO 206462



Muto et al. (2012)

Oph IRS 48



van der Marel et al. (2013)

**ALMA**

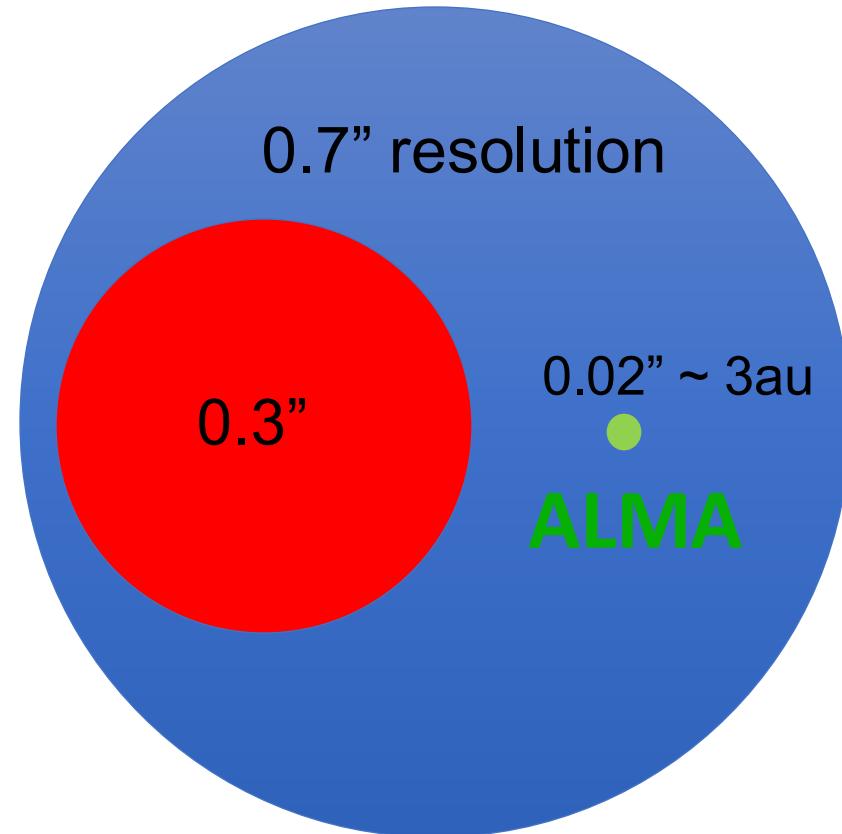
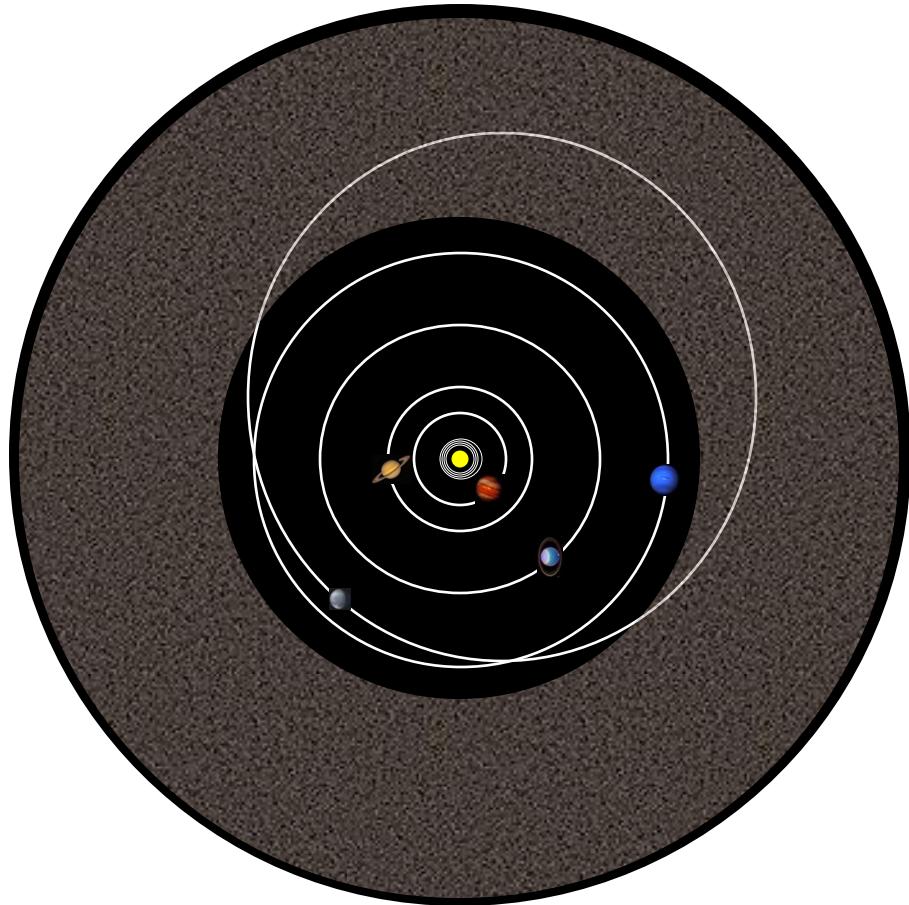


**VLA**

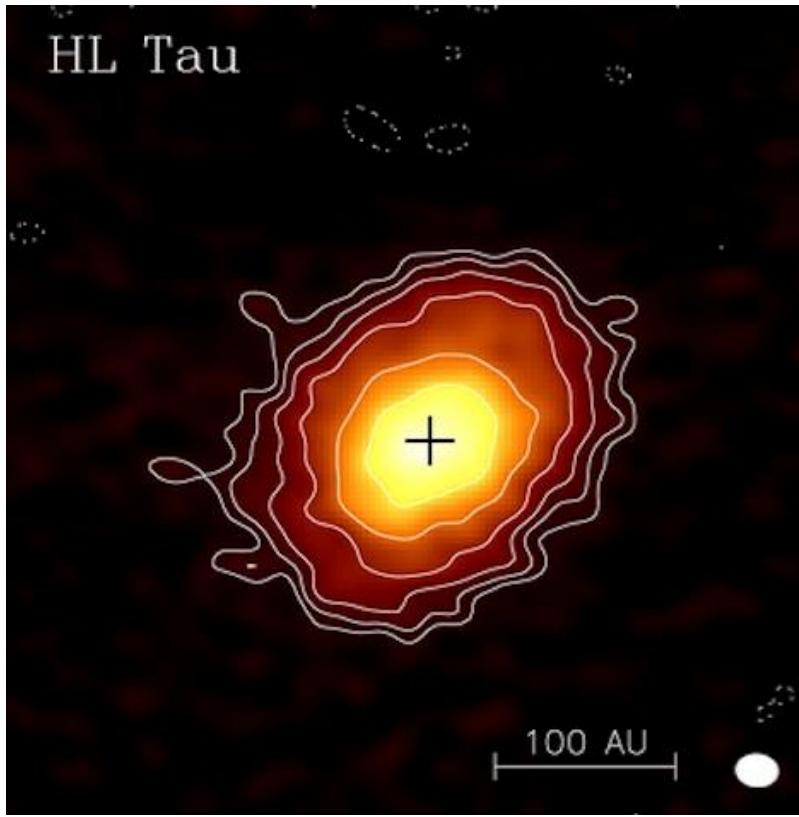


# The ALMA Revolution

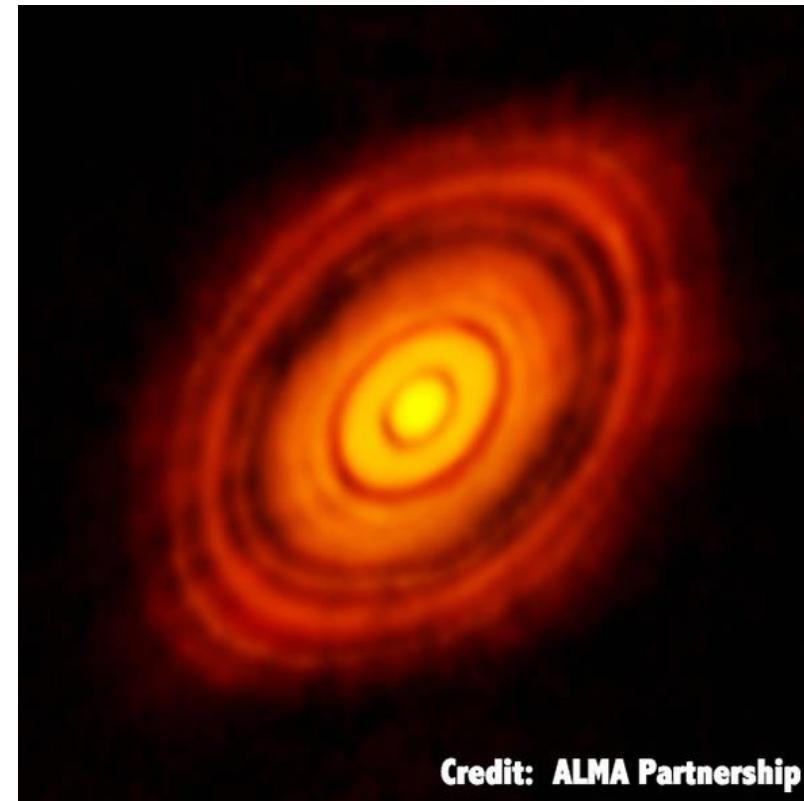
At 140 pc



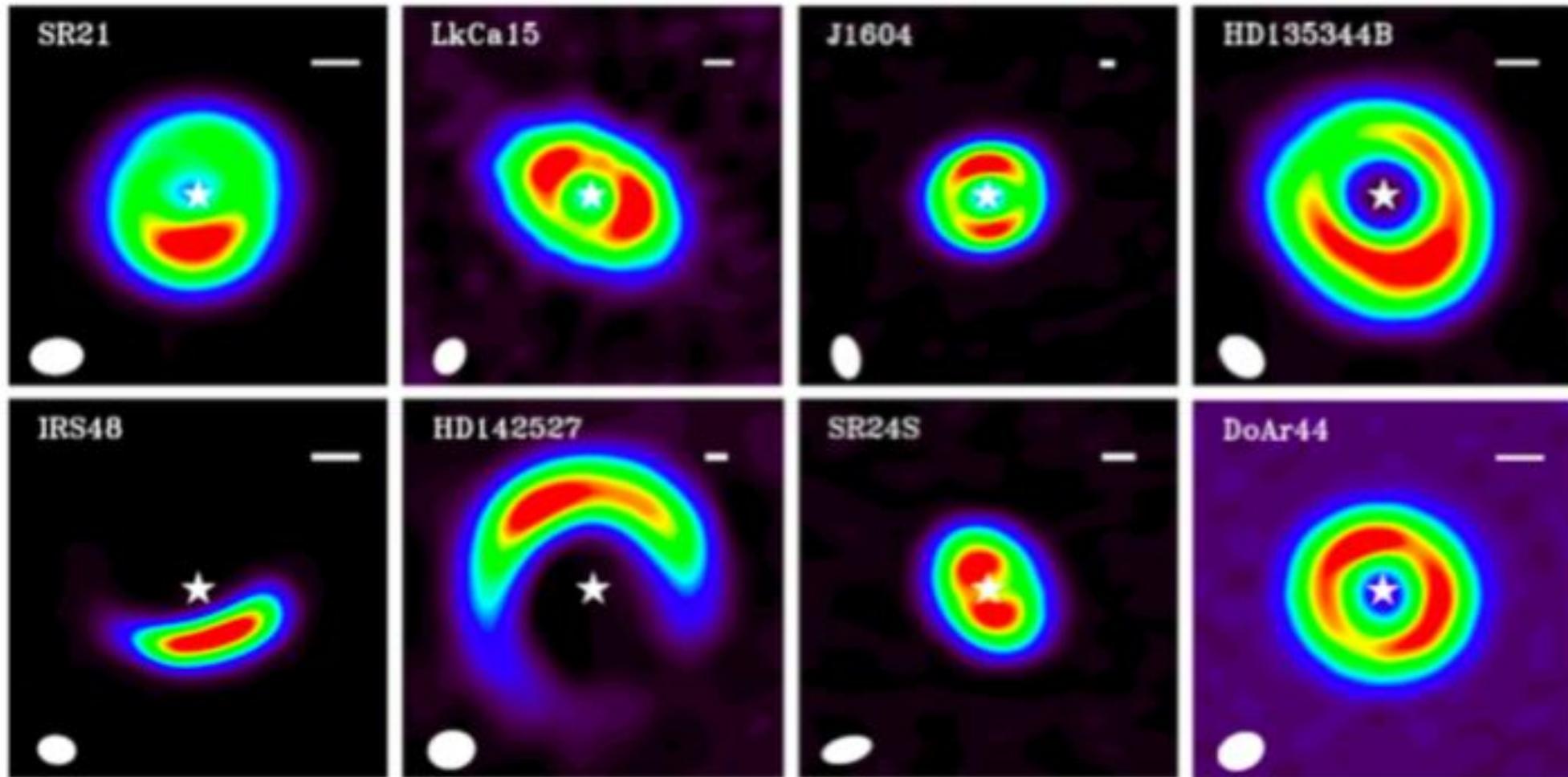
**Before ALMA**

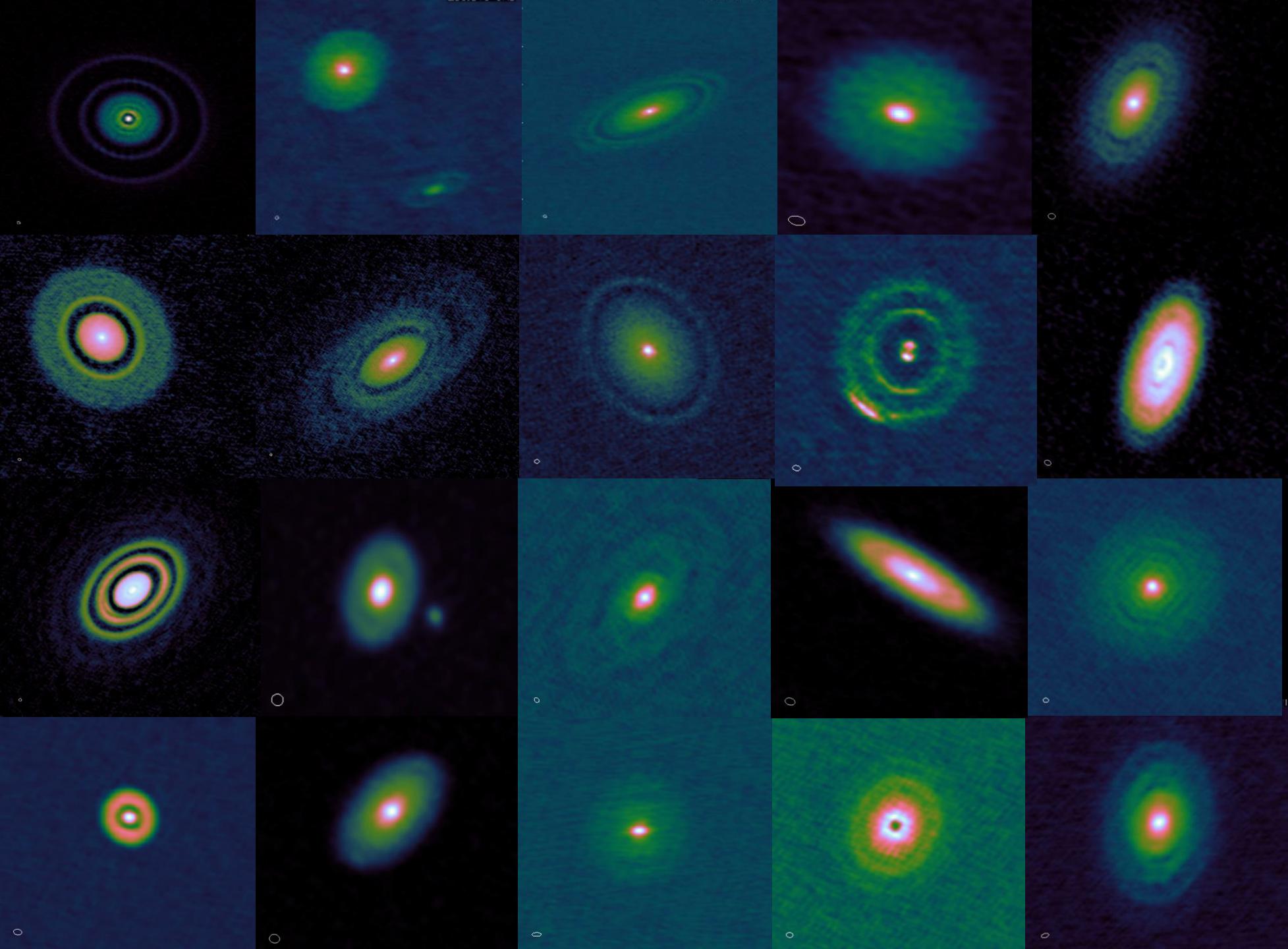


**ALMA**



## Dust traps in disks: ALMA Cycle 0 (2012)





# Oph IRS 48



Down

## A Major Asymmetric Dust Trap in a Transition Disk

Nienke van der Marel,<sup>1\*</sup> Ewine F. van Dishoeck,<sup>1,2</sup> Simon Bruderer,<sup>2</sup> Til Birnstiel,<sup>3</sup> Paola Pinilla,<sup>4</sup> Cornelis P. Dullemond,<sup>4</sup> Tim A. van Kempen,<sup>1,5</sup> Markus Schmalzl,<sup>1</sup> Joanna M. Brown,<sup>3</sup> Gregory J. Herczeg,<sup>6</sup> Geoffrey S. Mathews,<sup>3</sup> Vincent Geers<sup>7</sup>

The statistics of discovered exoplanets suggest that planets form efficiently. However, there are fundamental unsolved problems, such as excessive inward drift of particles in protoplanetary disks during planet formation. Recent theories invoke dust traps to overcome this problem. We report the detection of a dust trap in the disk around the star Oph IRS 48 using observations from the Atacama Large Millimeter/submillimeter Array (ALMA). The 0.44-millimeter-wavelength continuum map shows high-contrast crescent-shaped emission on one side of the star, originating from millimeter-sized grains, whereas both the mid-infrared image (micrometer-sized dust) and the gas traced by the carbon monoxide 6-5 rotational line suggest rings centered on the star. The difference in distribution of big grains versus small grains/gas can be modeled with a vortex-shaped dust trap triggered by a companion.

Although the ubiquity of planets is confirmed almost daily by detections of new exoplanets (*1*), the exact formation mechanism of planetary systems in disks of gas and dust around young stars remains a long-standing problem in astrophysics (*2*). In

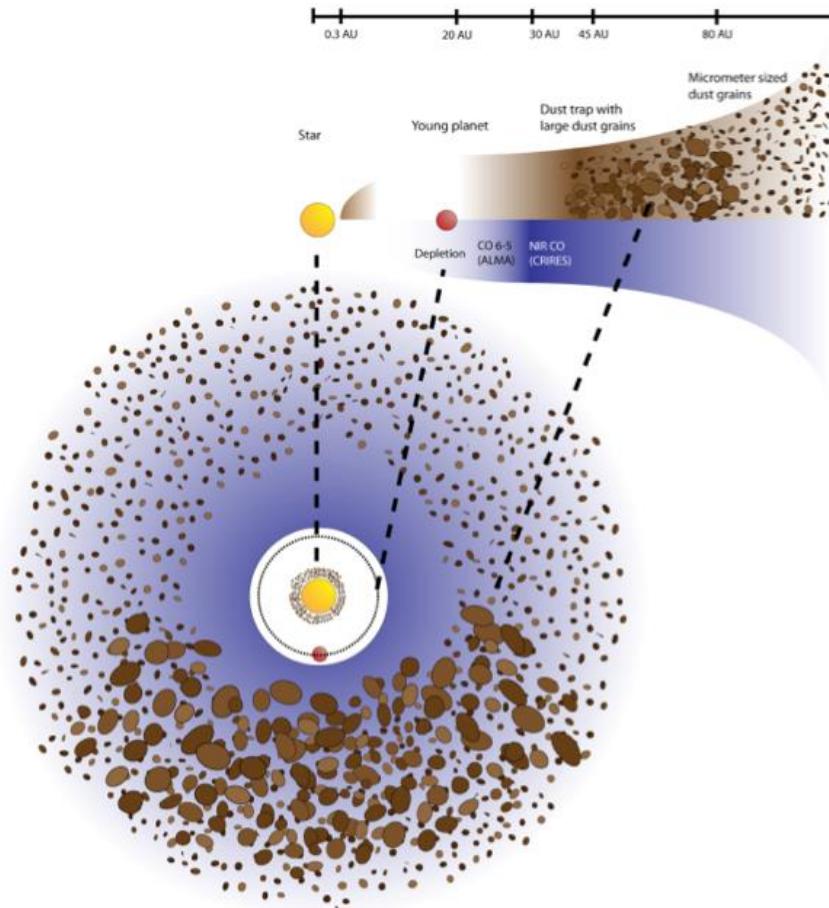
iencemag.org SCIENCE VOL 340 7 JUNE 2013

1199

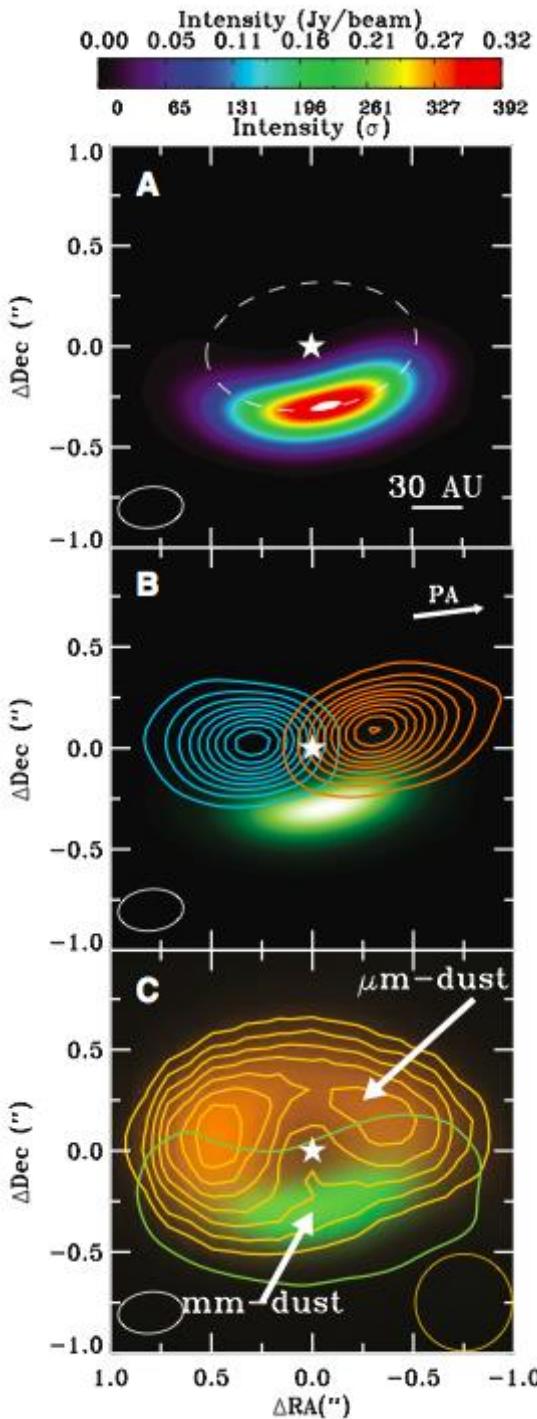
van der Marel+ '13

A huge vortex observed with ALMA

## The Oph IRS 48 “comet formation factory”



van der Marel+ '13

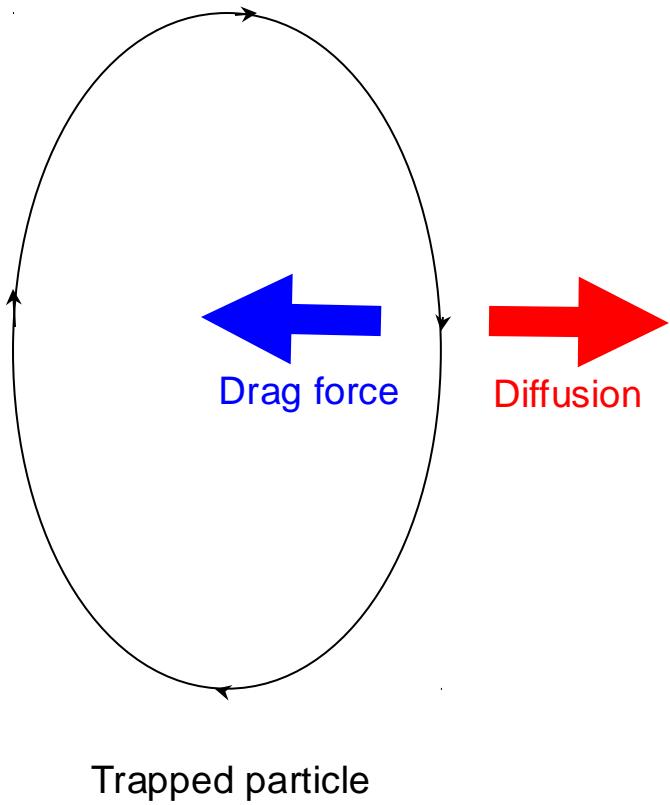


asymmetric  
mm dust  
at 63 AU

Gas detection:  
Keplerian rotation

Micron-sized  
dust follows gas

# Drag-Diffusion Equilibrium



Dust continuity equation

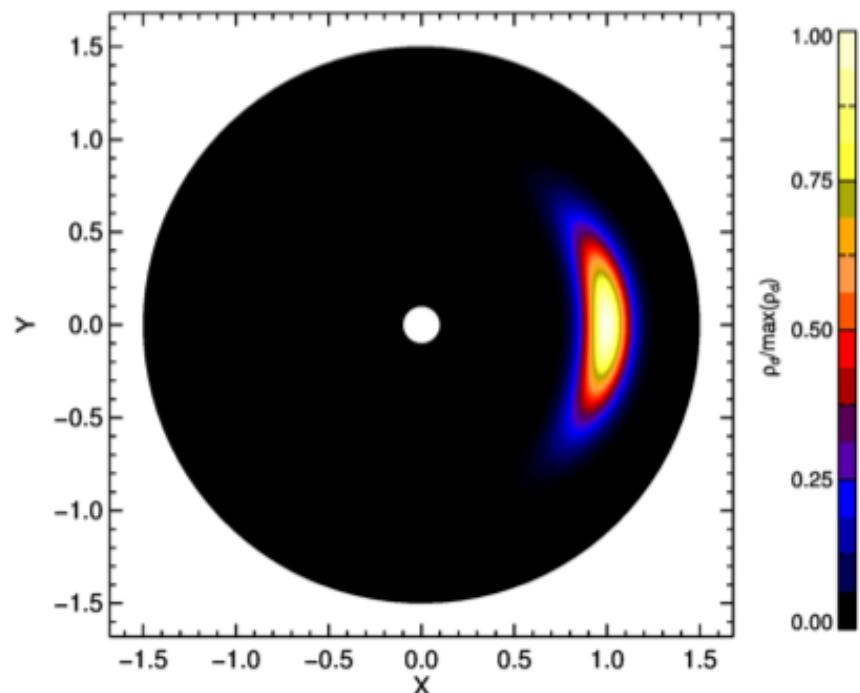
$$\frac{\partial \rho_d}{\partial t} = -(\mathbf{v} \cdot \nabla) \rho_d - \rho_d \nabla \cdot \mathbf{v} + D \nabla^2 \rho_d,$$

advection

compression

diffusion

# Analytical Solution for dust in Drag-Diffusion Equilibrium



Solution for

$$H/r=0.1 \quad \chi=4 \quad S=1$$

Steady-state solution

$$\rho_d(a, z) = \epsilon \rho_0 (S + 1)^{3/2} \exp \left\{ - \frac{[a^2 f^2(\chi) + z^2]}{2H^2} (S + 1) \right\}$$

Lyra & Lin '13

$$S = \frac{St}{d}$$

$$\delta = v_{\text{rms}}^2 / c_s^2,$$

$a$  = vortex semi-minor axis

$H$  = disk scale height (temperature)

$\chi$  = vortex aspect ratio

$\delta$  = diffusion parameter

$St$  = Stokes number (particle size)

$f(\chi)$  = model-dependent scale function

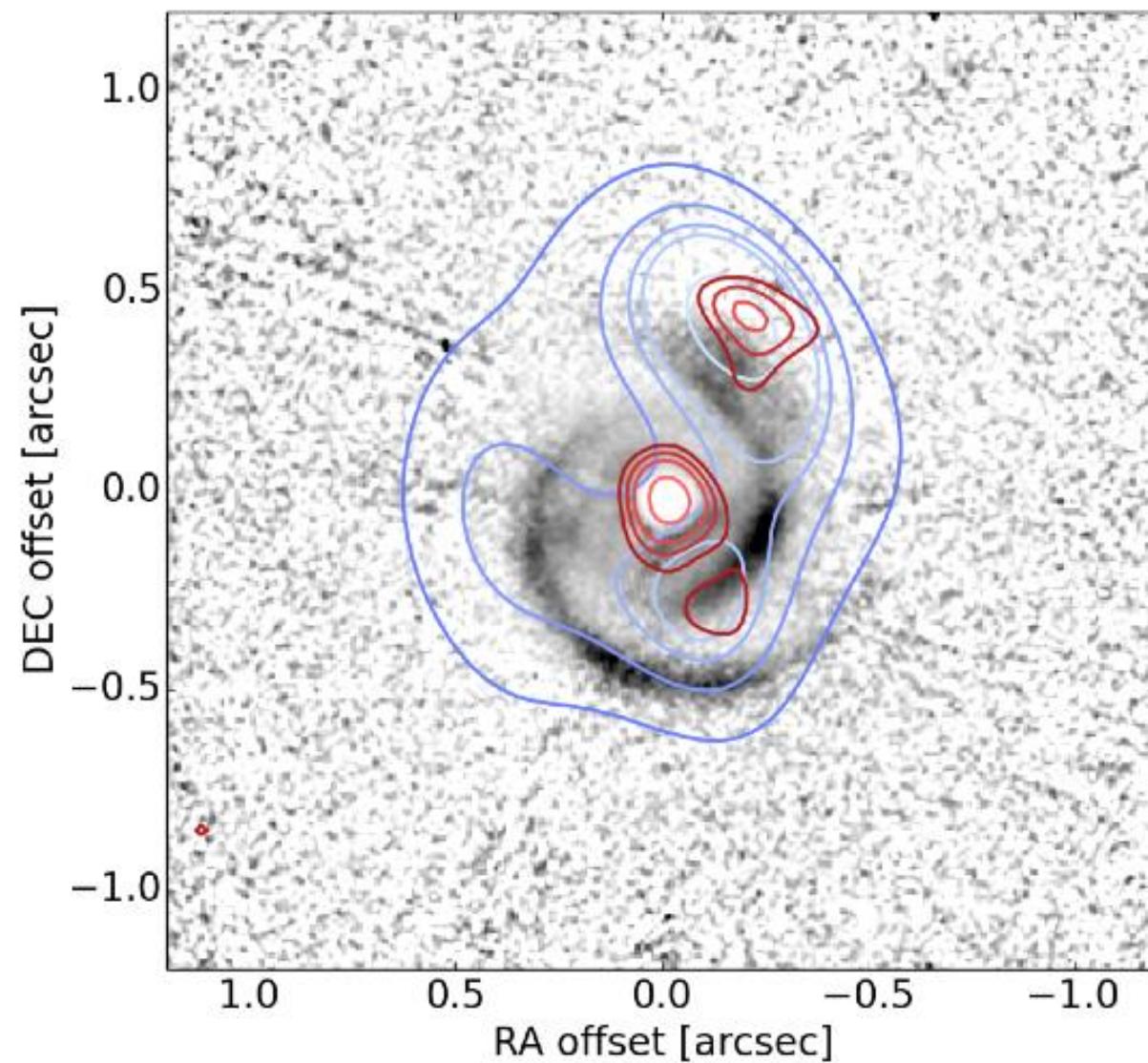
# Disk Tomography

## SPHERE-ALMA-VLA overlay of MWC 758

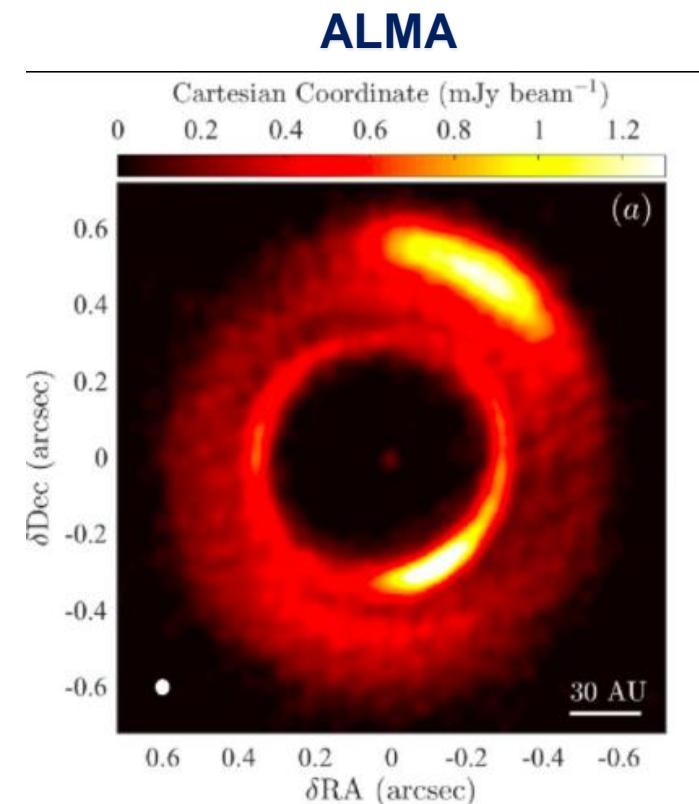
SPHERE ( $\mu\text{m}$ )

ALMA (~ mm)

VLA (cm-m)

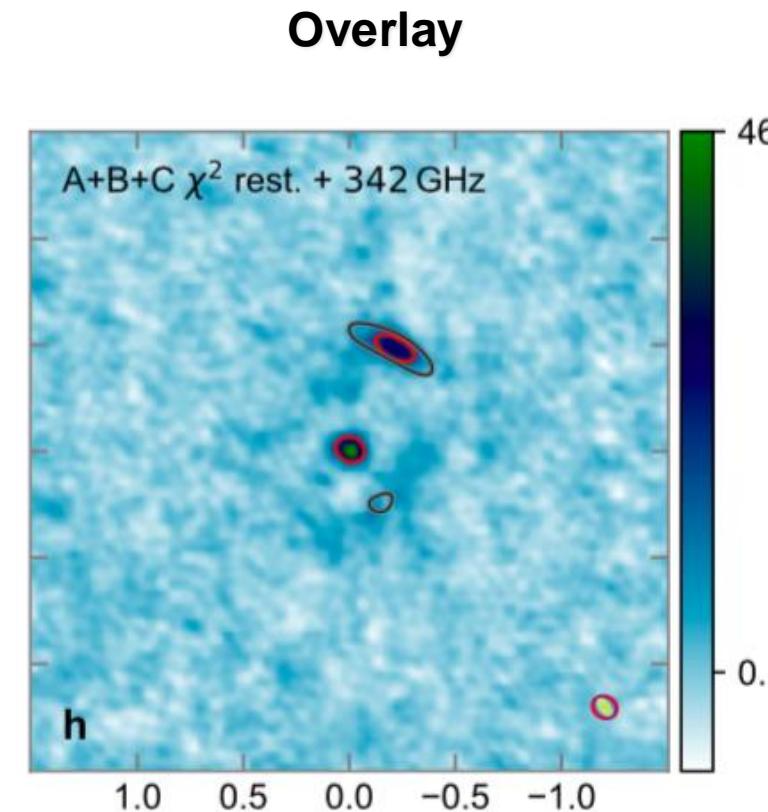
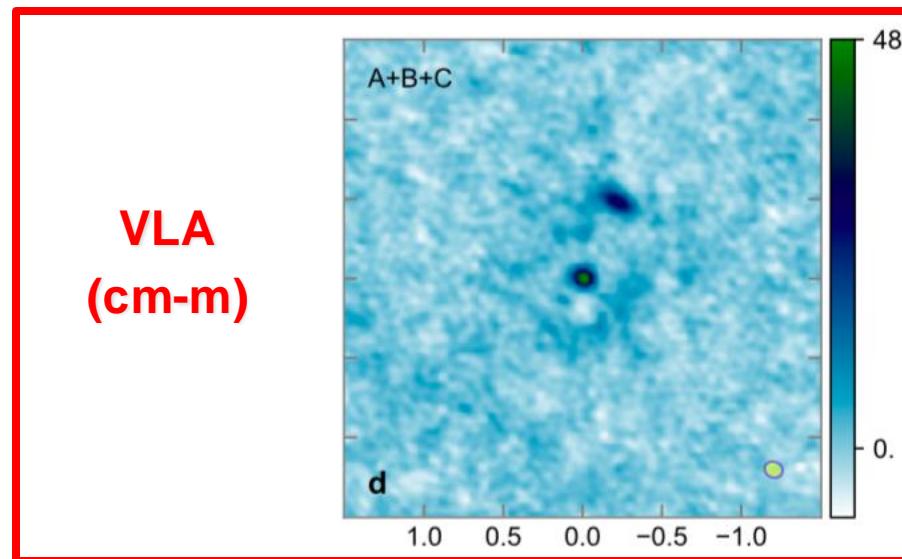
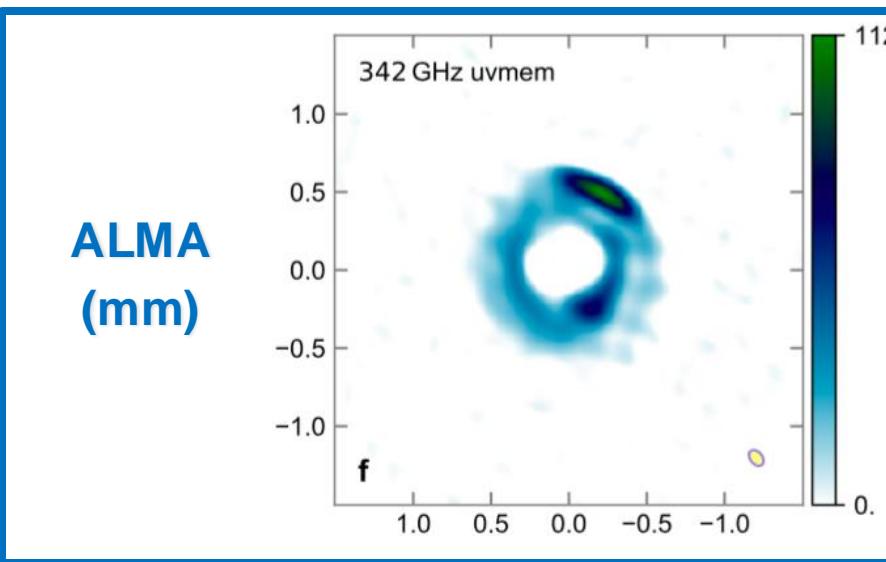


Marino+Lyra '15

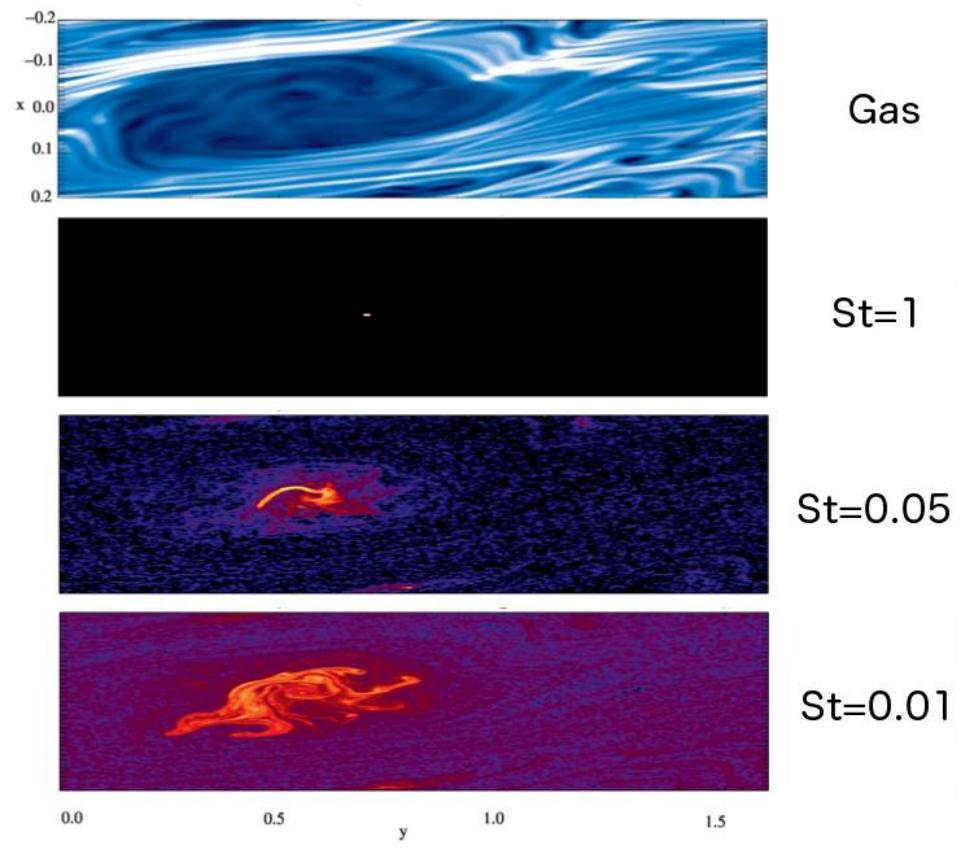
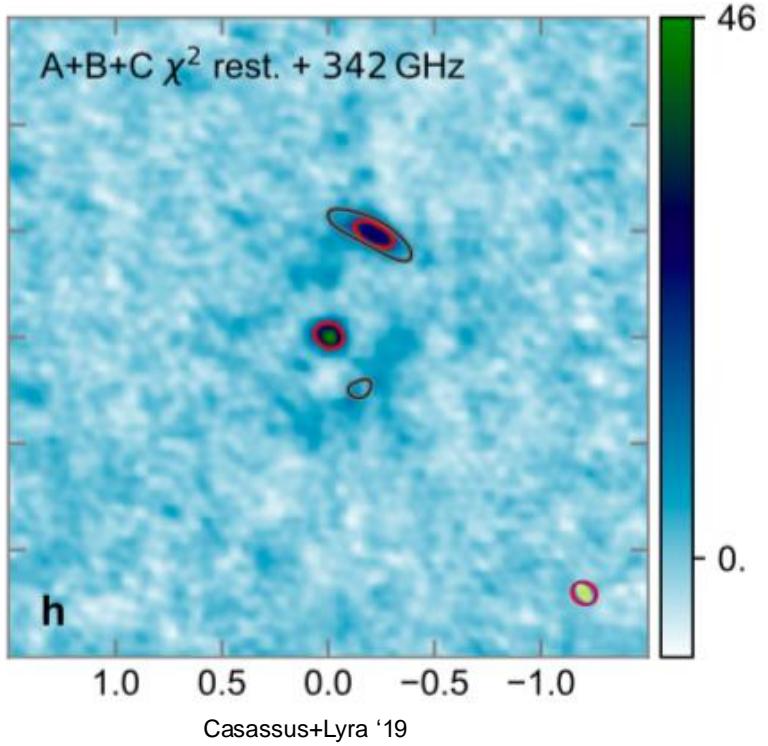


Dong+ '18

## Pebble trapping



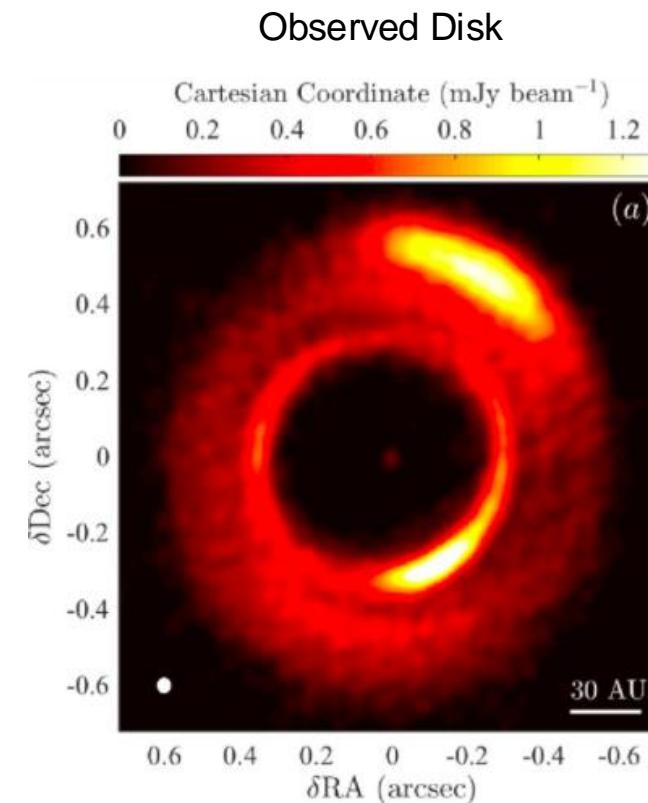
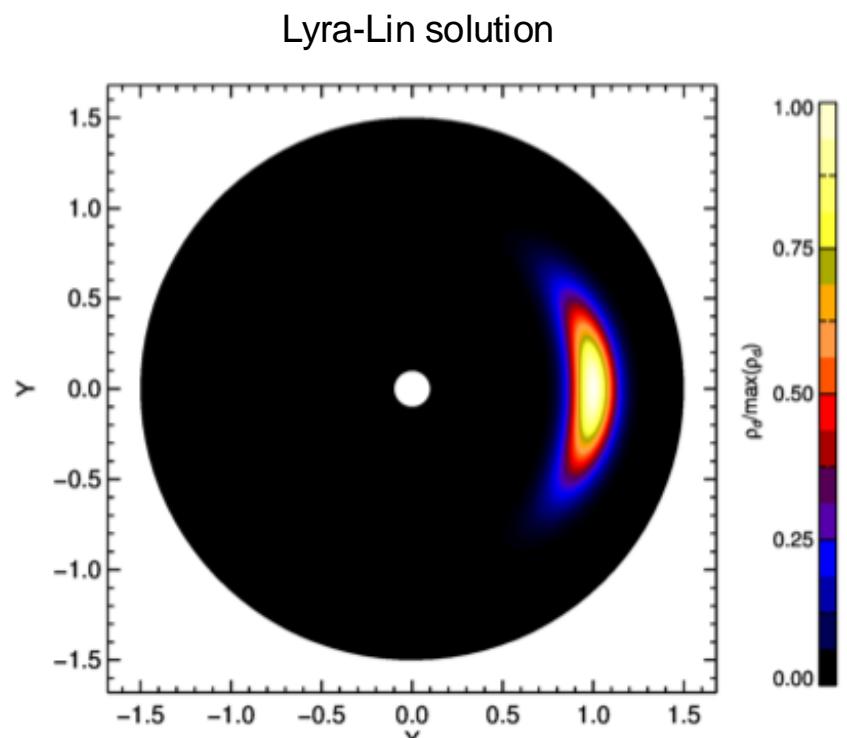
# Model vs Observation



# Take home message

- Vortex-trapped dust in drag-diffusion equilibrium explains the observations

$$\rho_d(a, z) = \epsilon \rho_0 (S + 1)^{3/2} \exp \left\{ - \frac{[a^2 f^2(\chi) + z^2]}{2H^2} (S + 1) \right\}$$



# The future

After 10 years of ALMA...

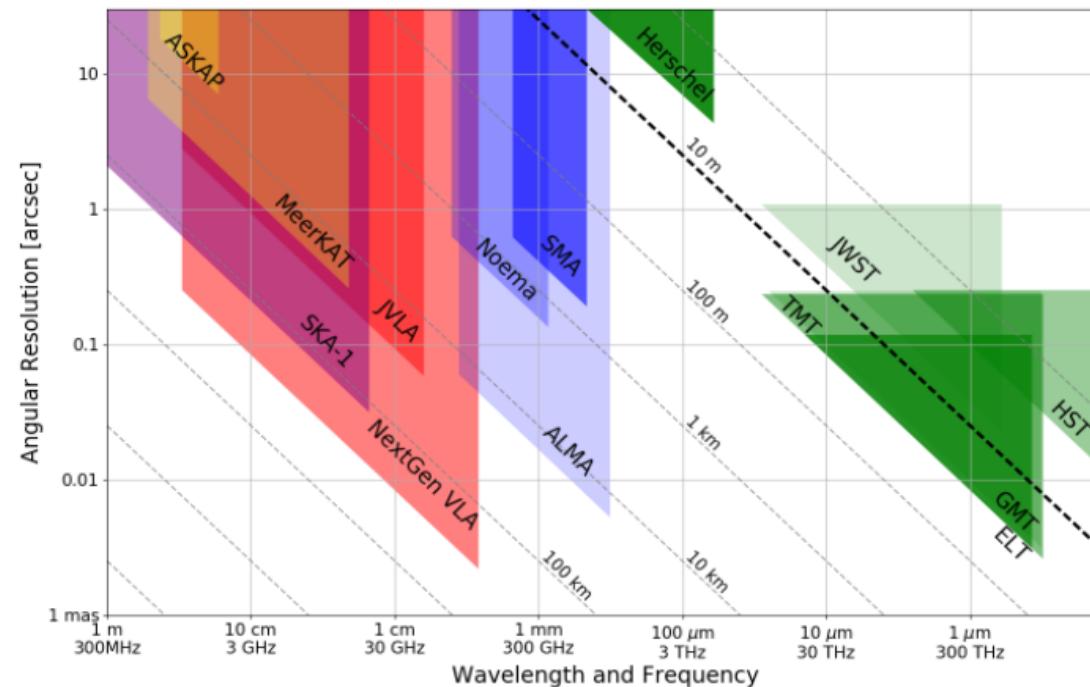
Nearly all nearby disks observed at  $<0.1''$  ( $< 20\text{-}30\text{AU}$ ) show substructures.

3 main types of substructures

- Crescent-shaped
- Spiral arms
- Rings/Gaps



# ngVLA rocks!

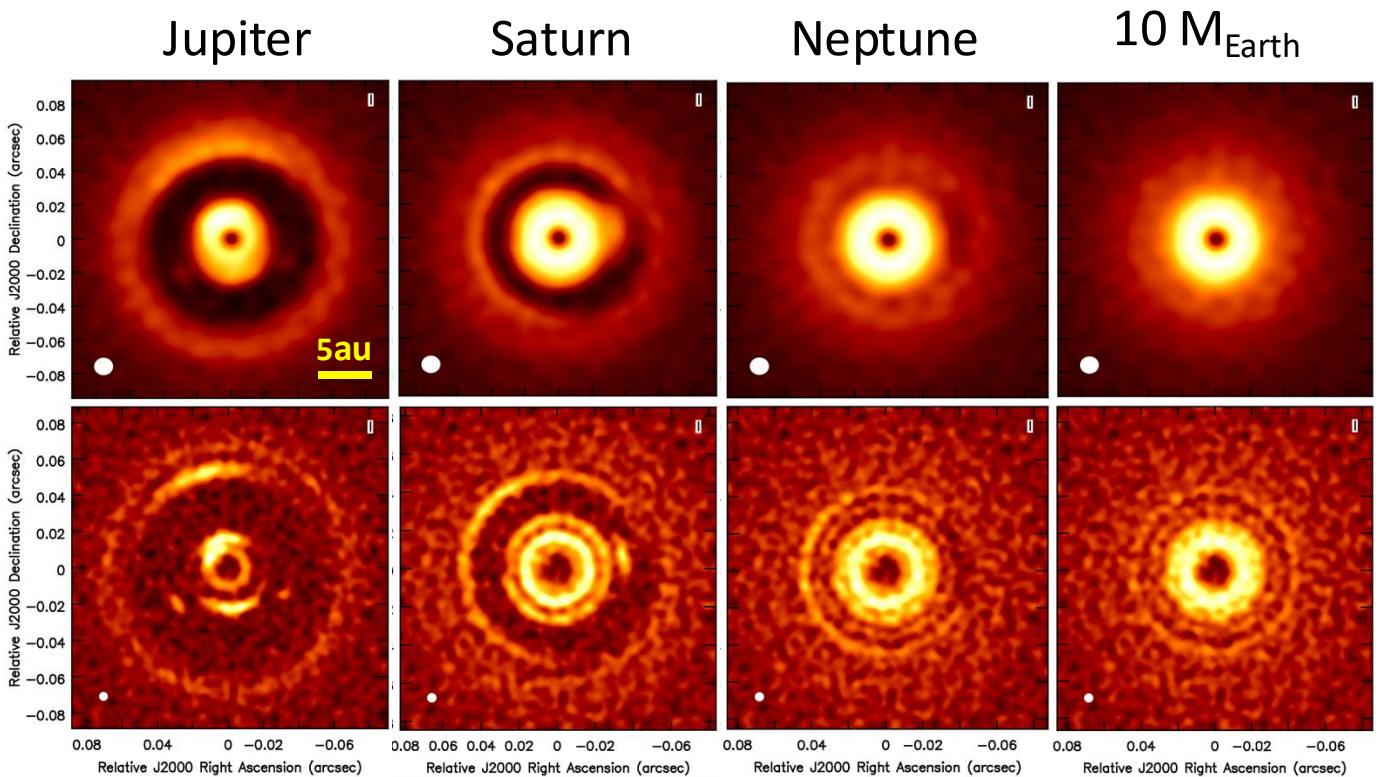


# Planets at 5AU

ALMA @ 0.87mm

ngVLA @ 3mm

5 mas = 0.7 AU  
rms =  $5 \times 10^{-7}$  Jy/beam

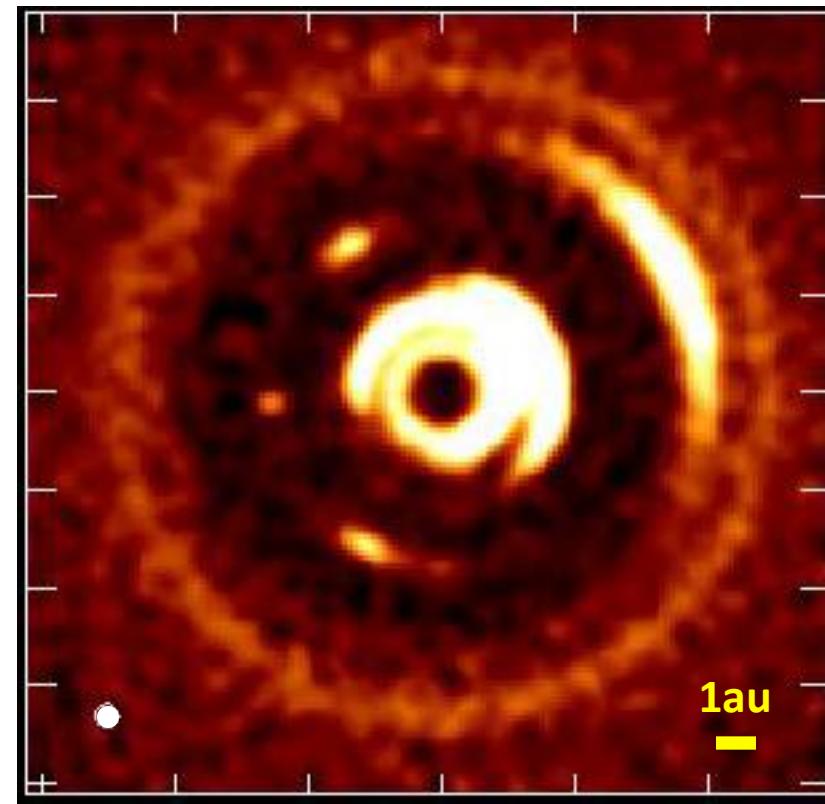


Ricci et al. 2018

ngVLA identifies gaps/substructures down to  $\sim 5\text{-}10 M_{\text{Earth}}$

# ngVLA: Proper motions

Jupiter at 5 AU



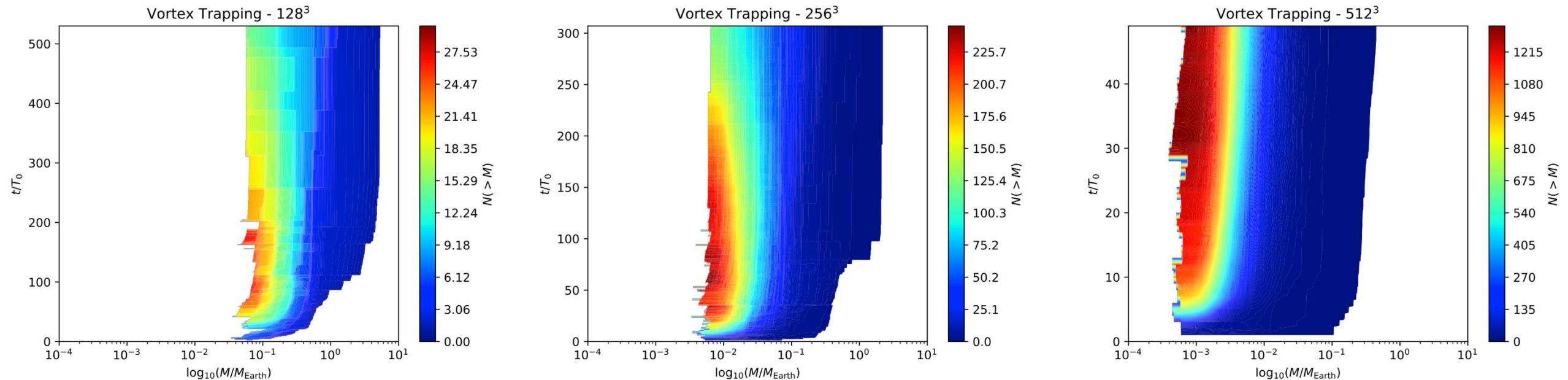
## Conclusions

- Two routes for planet formation (streaming instability and vortices, complementary)
  - Does turbulence help (concentration at large scales) or hinder (diffusion at small scales)?
  - Three dynamical instabilities in the Ohmic dead zone
    - Different regimes of opacity, operate in different regions
    - Saturate into vortices
  - Dust trapped in drag-diffusion equilibrium explains the observations
- **Issues:**
- Are the dynamical instabilities (chiefly the Vertical Shear Instability) responsible for the observed crescents?
  - Overlap between instabilities unclear
  - Global model of Convective Overstability needed
  - Relevance of Resonant Buoyant Instability (“zombie vortex”) unclear/unlikely.
  - Planet formation properties / Synergy with streaming instability

ngVLArocks!

	ZVI	COV	VSI
Global model	✗	✗	✓
Vertical Stratification	✓	✗	✓
Boundaries with other instabilities	✗	✗	✗
Interaction with dust	✗	✓	✓
Observational Validation/Rule out	✗	✗	✗
Planet Forming Properties	✗	✗	✗

# Convergence



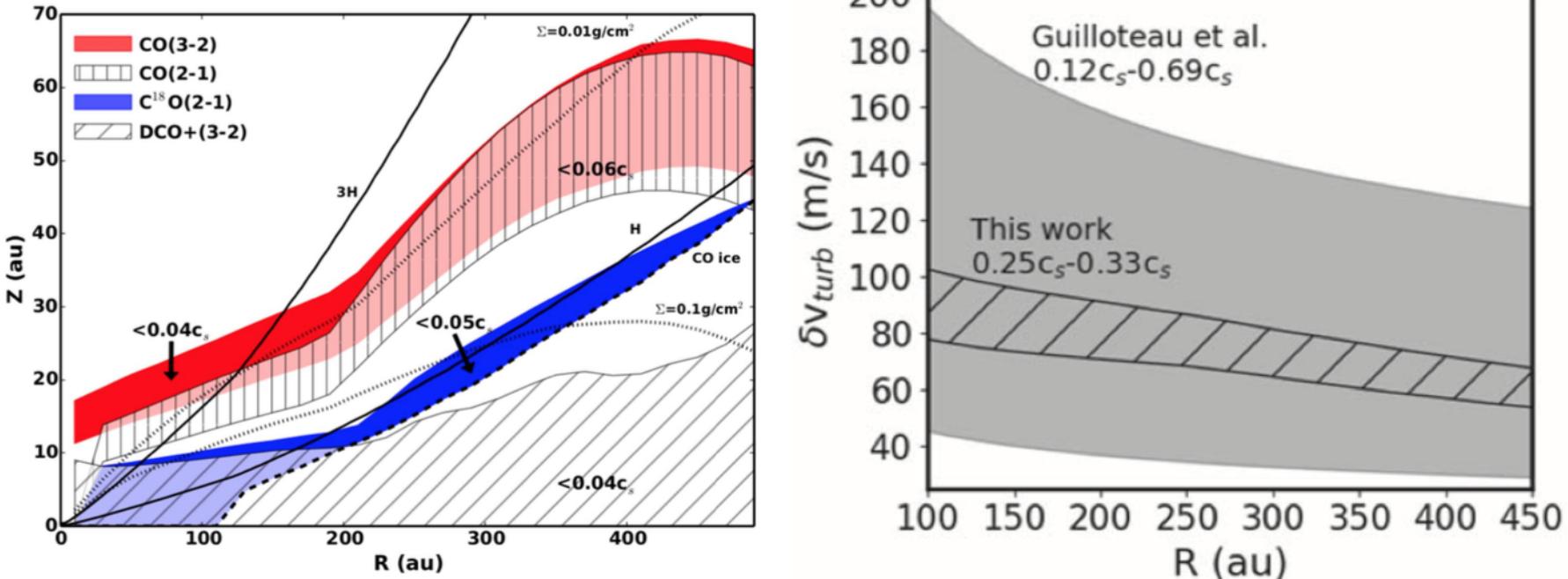
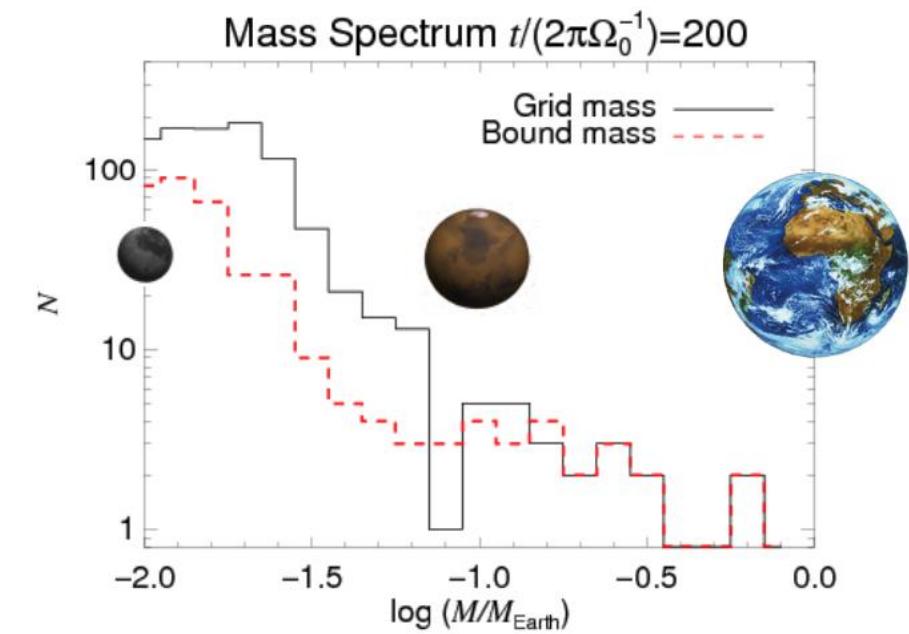
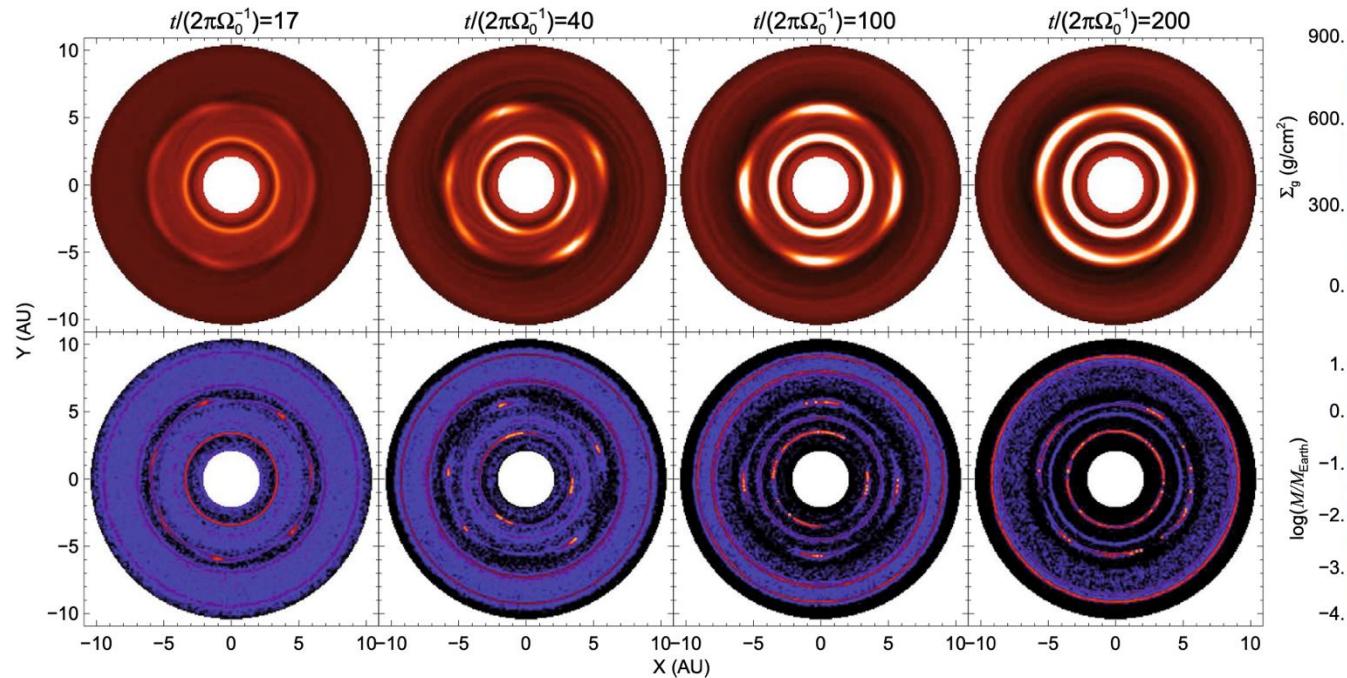
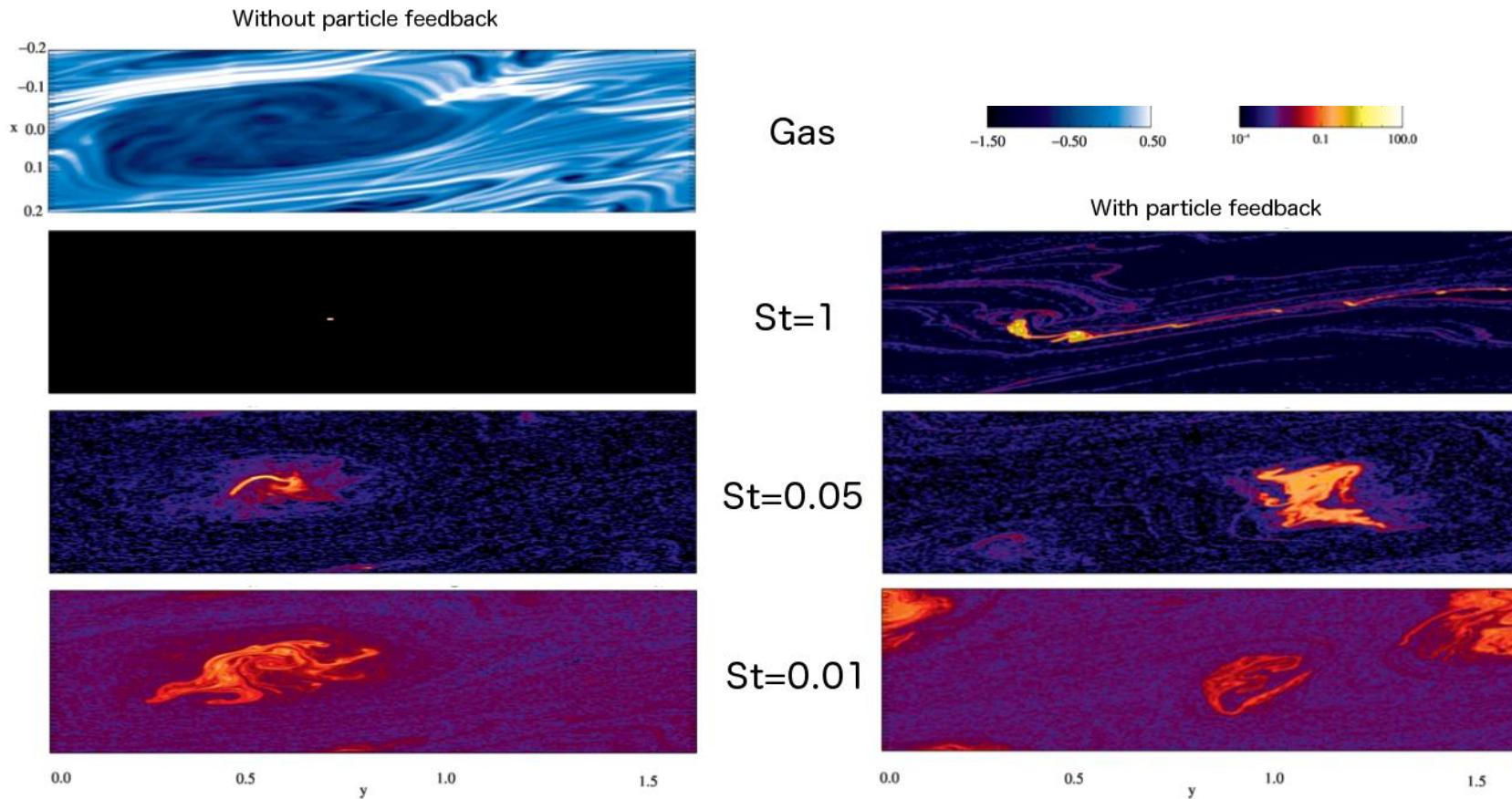


Fig. 7.— *Left:* Upper limits to turbulent velocities in HD 163296 as a function of radius  $R$  and mid-plane height  $z$ . The colors denote the species from which there is a majority of emission; the CO transitions are at large  $z$  whereas  $\text{C}^{18}\text{O}$  and  $\text{DCO+}$  are from lower in the disk. Also included on the plot are lines of constant  $\Sigma$ ,  $H$  and  $3H$  ( $H$  being the gas scale height) and where CO is ice. In this source, turbulence is at most a few percent of the sound speed. From [Flaherty et al. \(2017\)](#). *Right:* The turbulent velocity as a function of radius as measured from CO emission in DM Tau (hashed lines), compared to the results from previous work using CS ([Guilloteau et al. 2012](#); grey shaded region). As opposed to HD 163296, DM Tau exhibits strong turbulence, consistent with theoretical predictions [Flaherty et al. \(2020\)](#).

# Vortices and Planet Formation



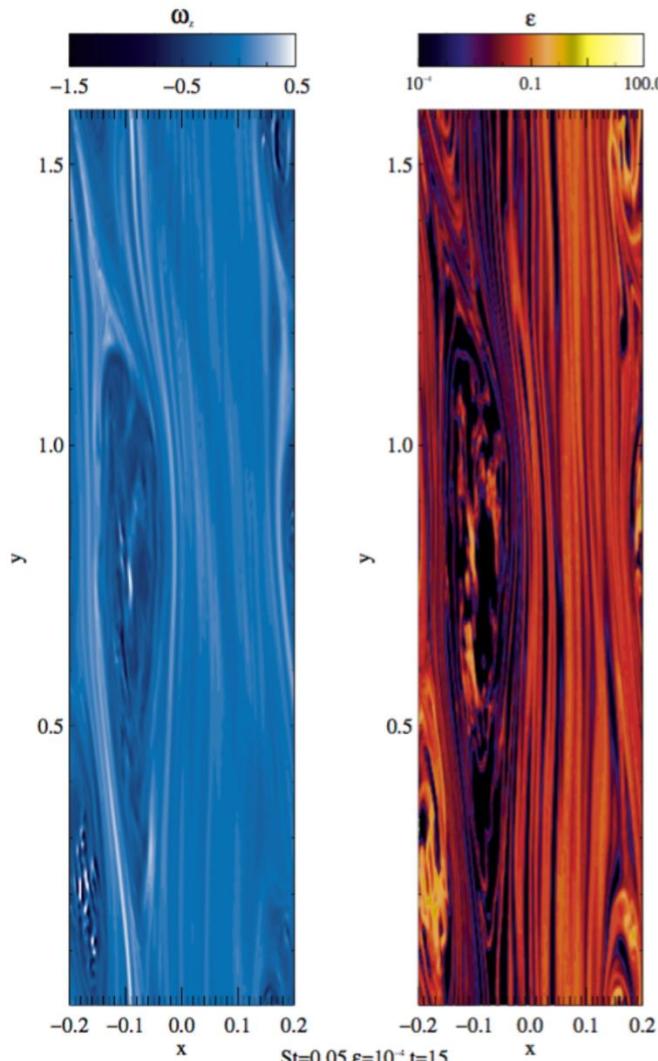
# Pebble trapping in vortices in LOCAL models



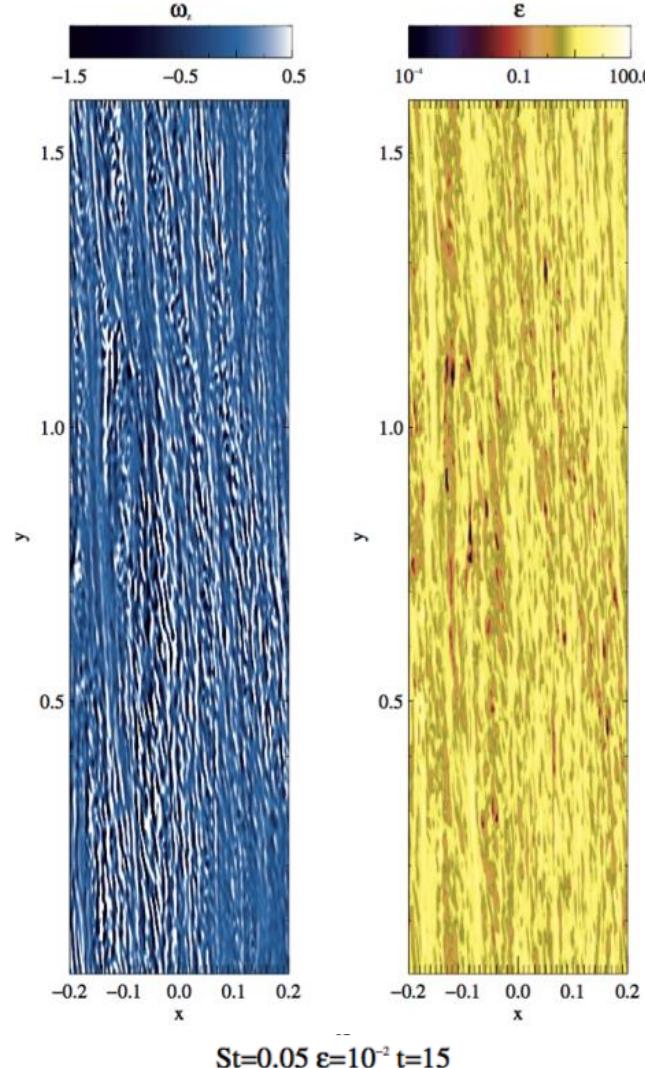
Raettig et al (2015)

# Vortex destruction at high dust load?

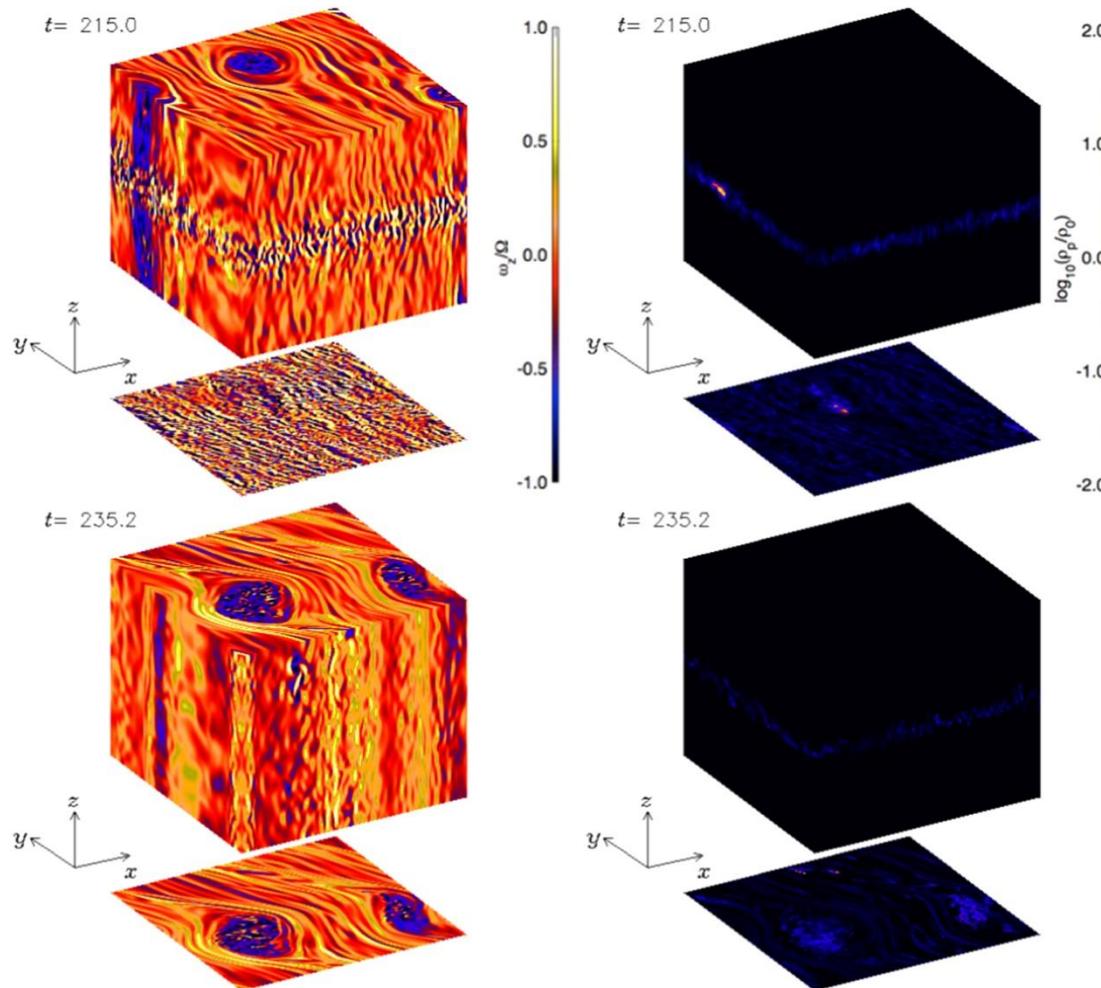
Dust to gas ratio  $10^{-4}$



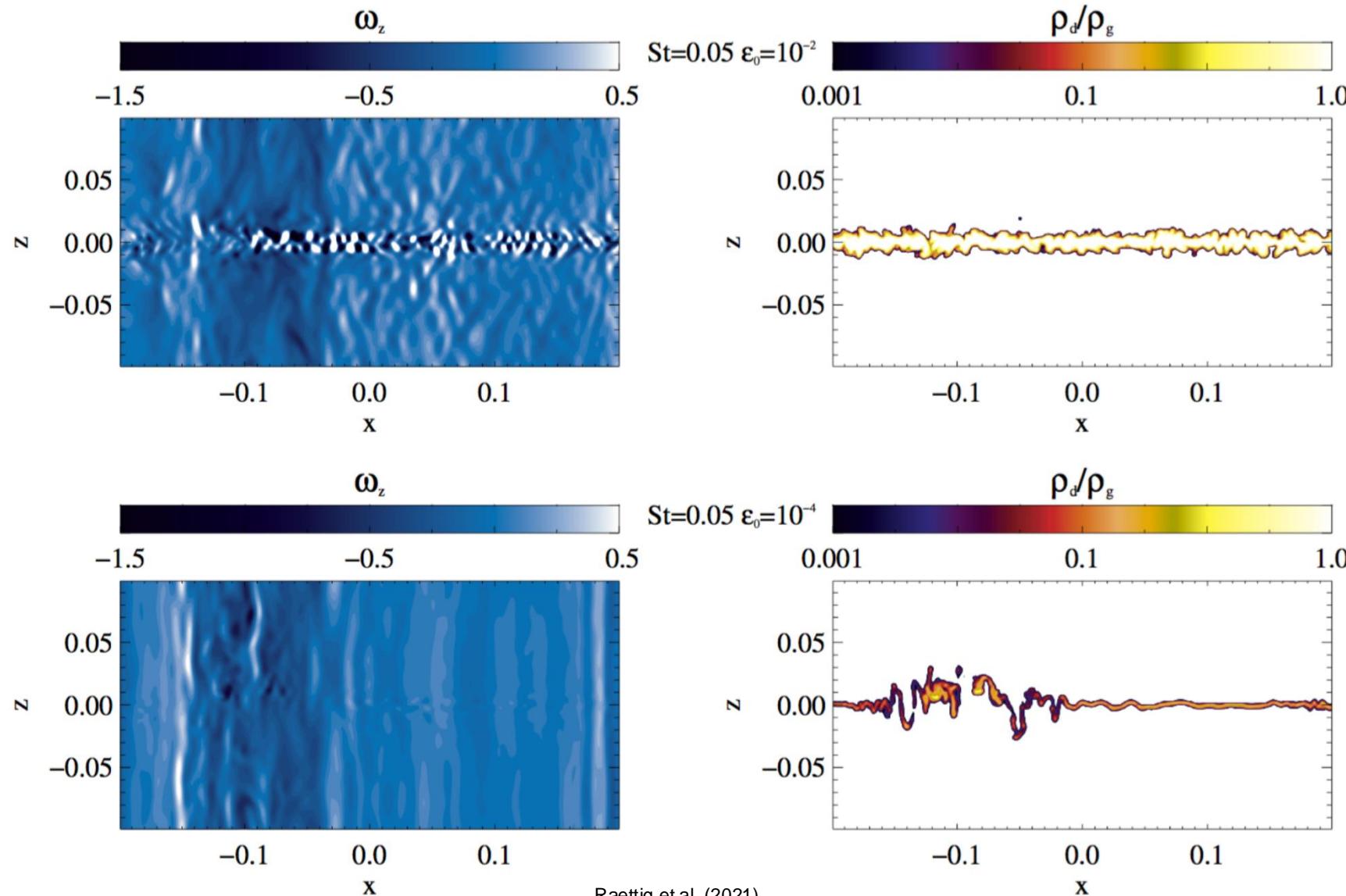
Dust to gas ratio  $10^{-2}$



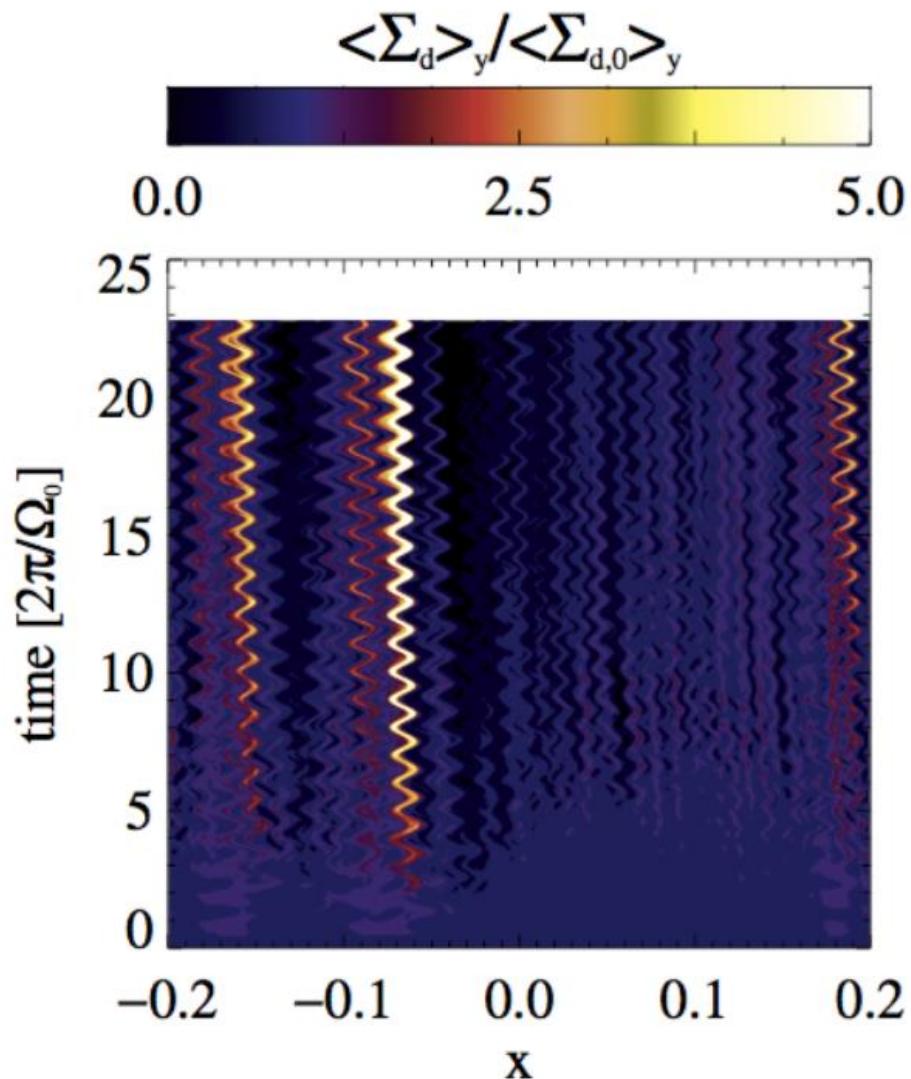
# Pebble trapping does not destroy vortices



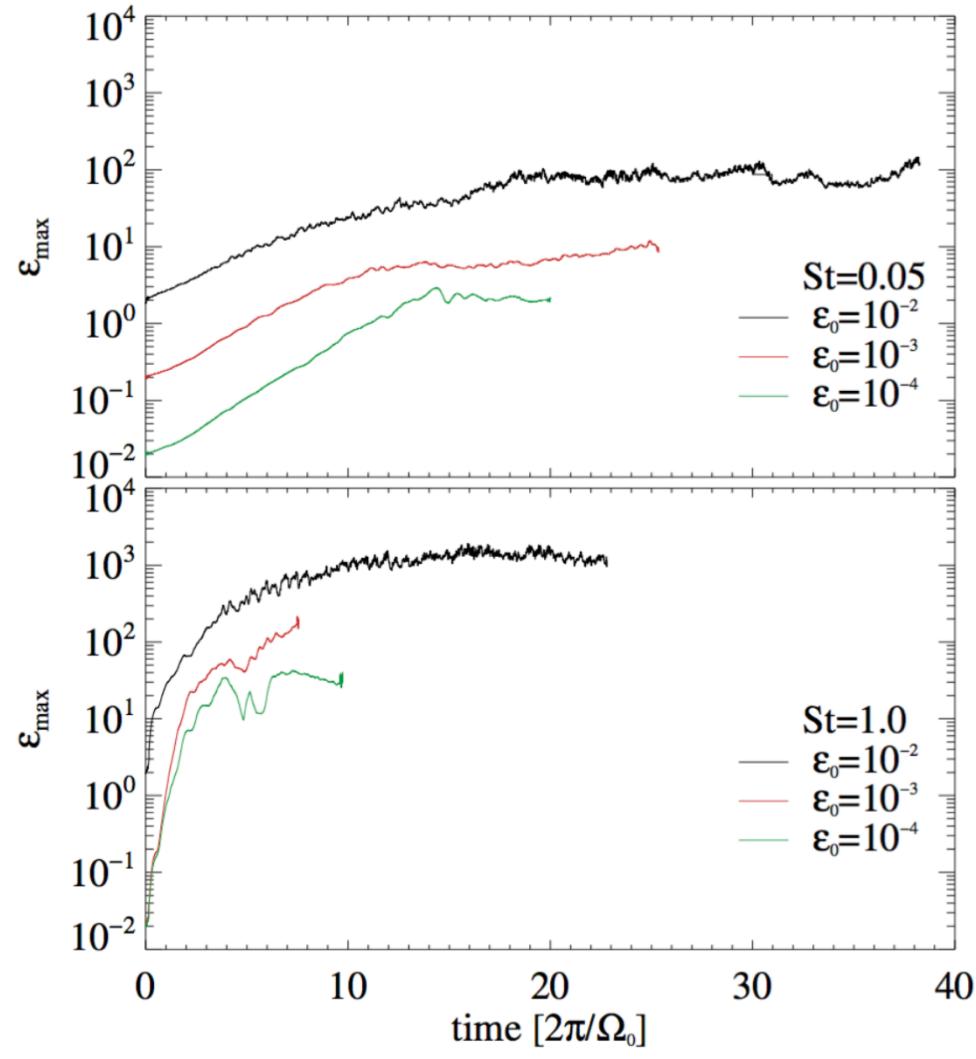
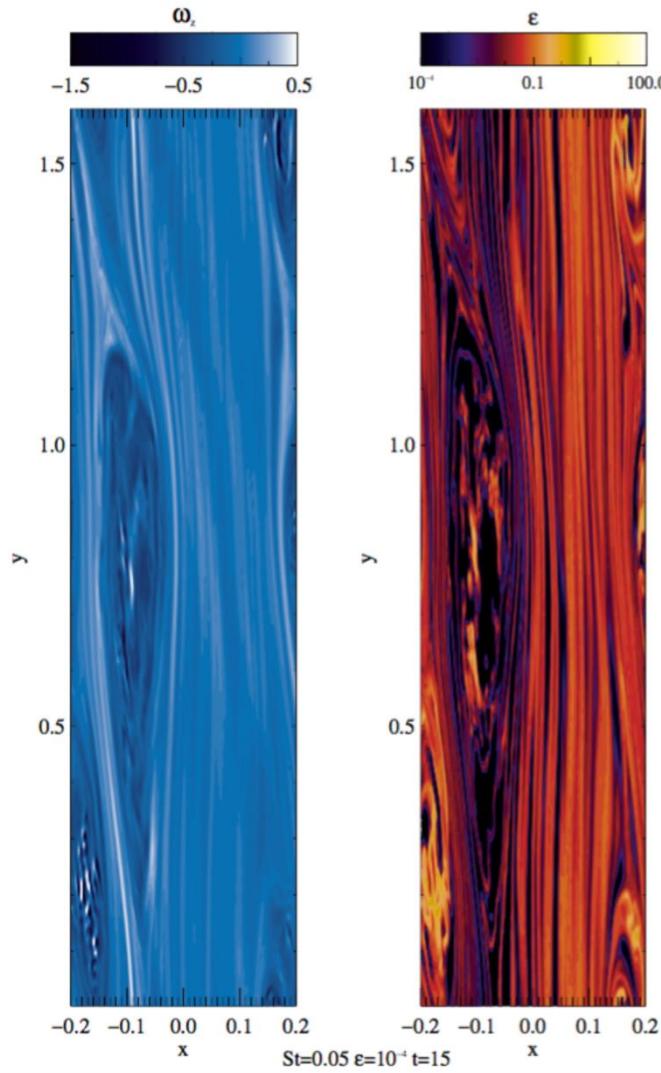
# Vortex column disrupted only around the midplane



# Pebble drift: follows vortex



# Pebble trapping in 3D vortices

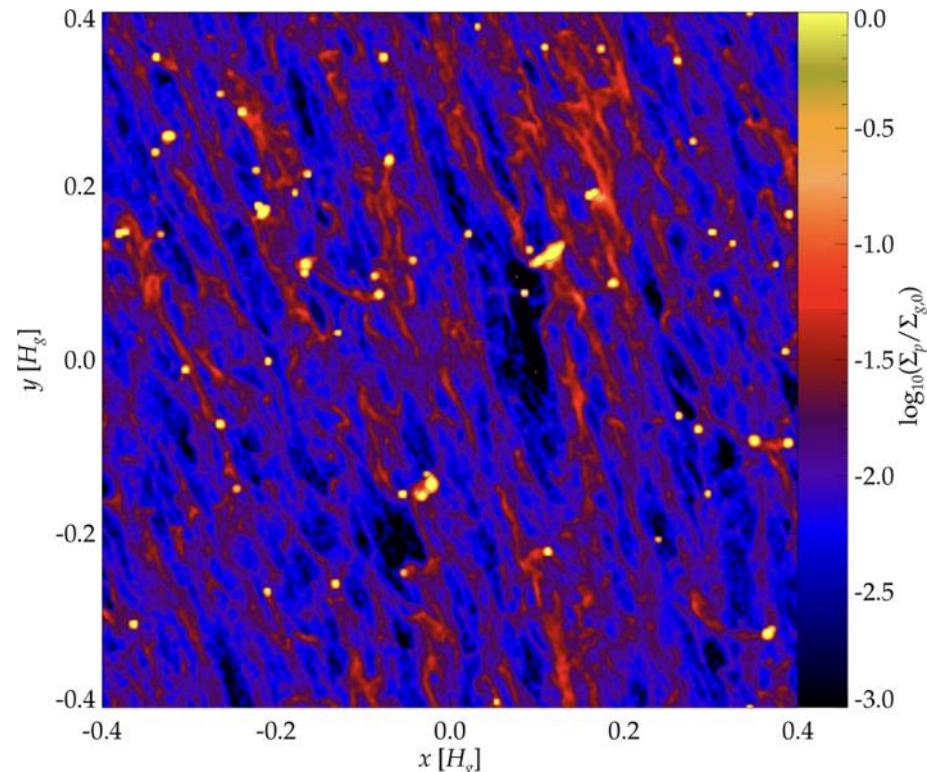
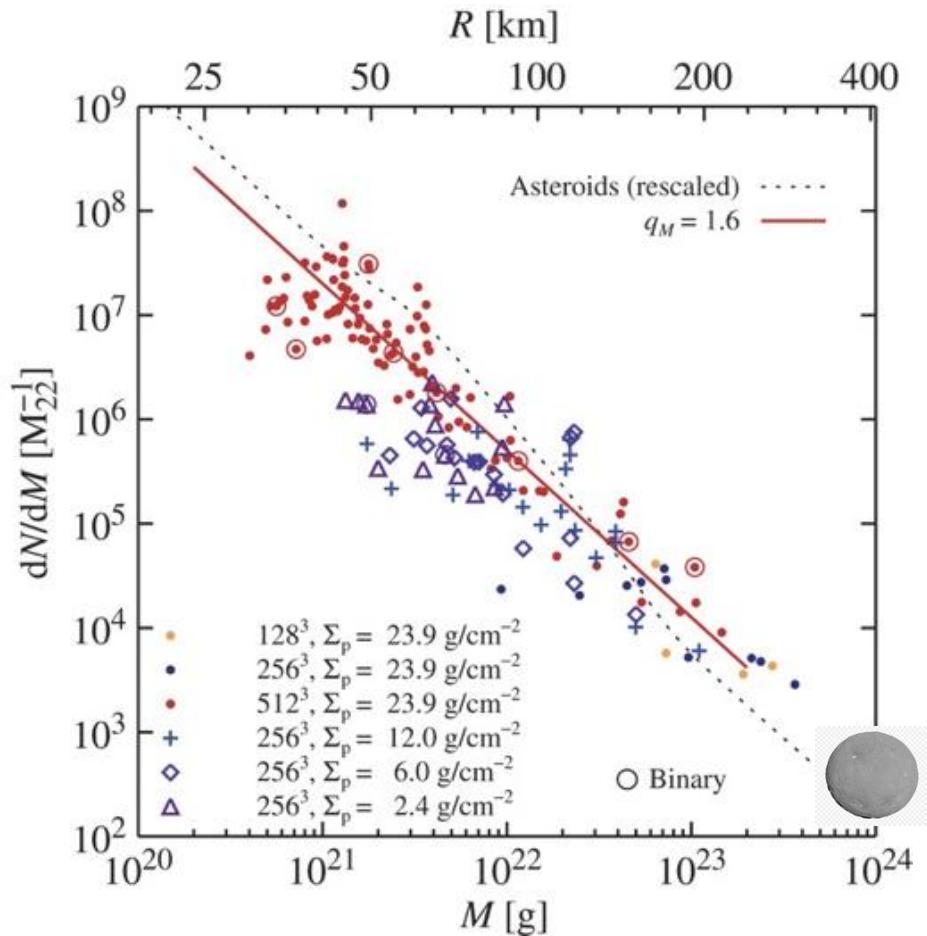




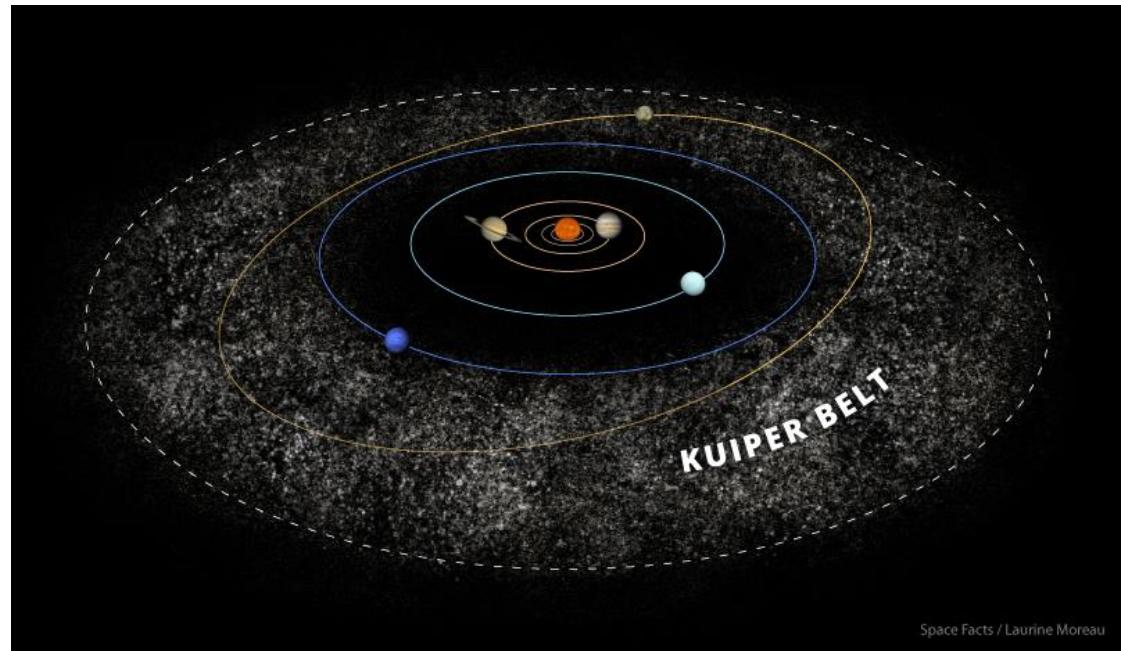
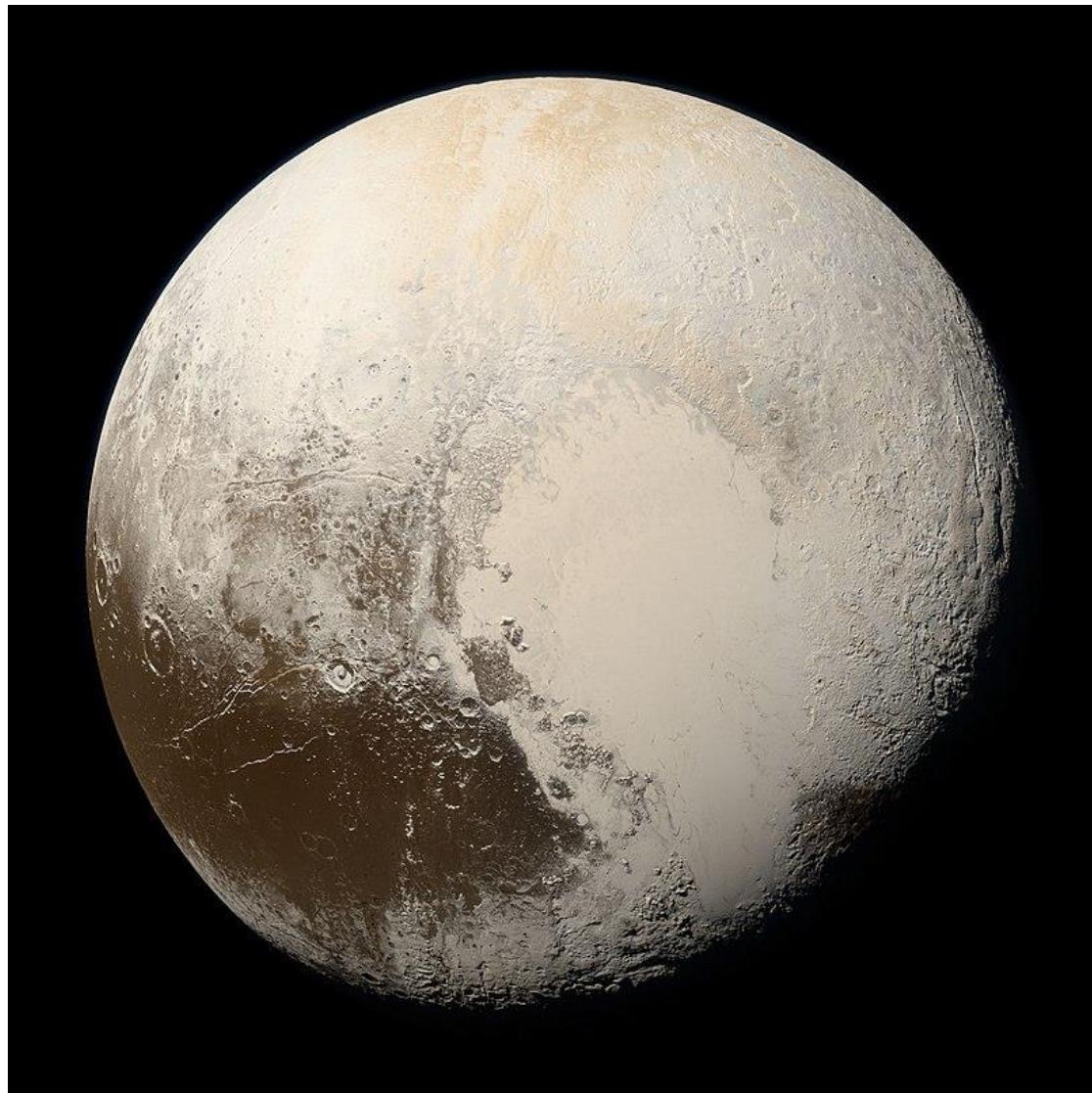
Fingerprints of  
streaming instability

**How can we verify the  
streaming instability  
hypothesis?**

# Planetesimal Formation

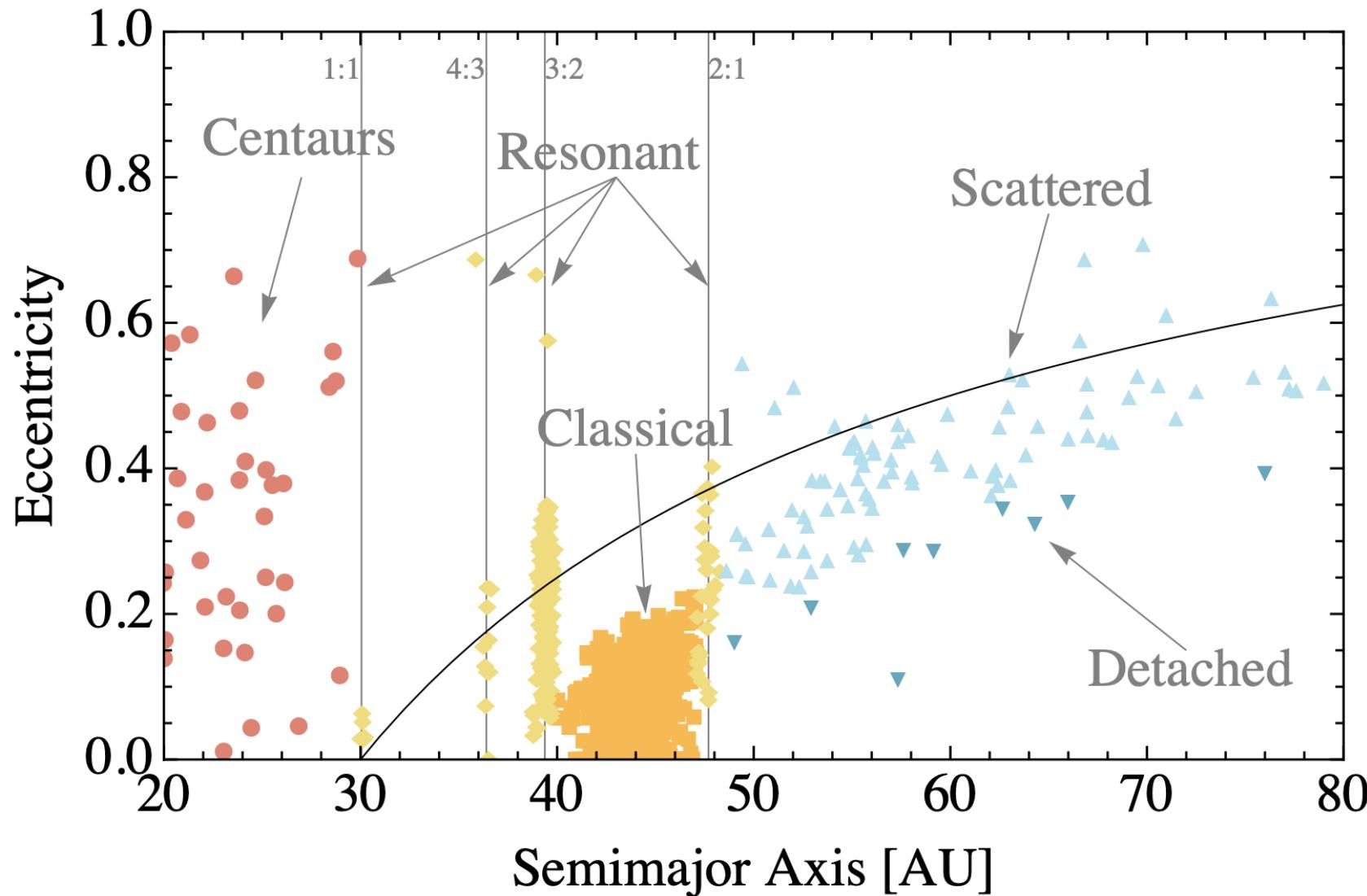


Initial mass function consistent with mass distribution of asteroid belt. Slope 1.6

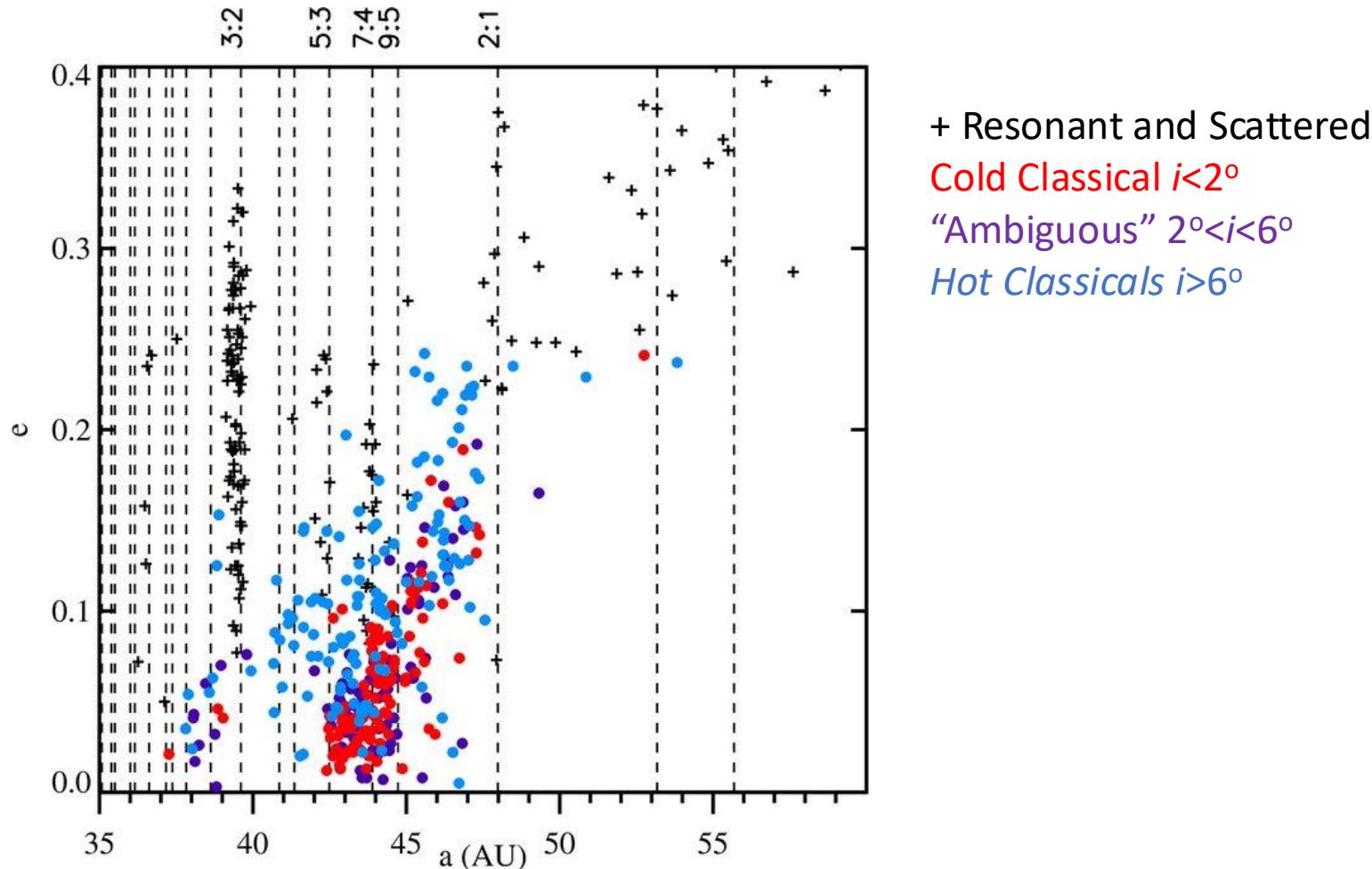


Space Facts / Laurine Moreau

# Structure of the Kuiper Belt

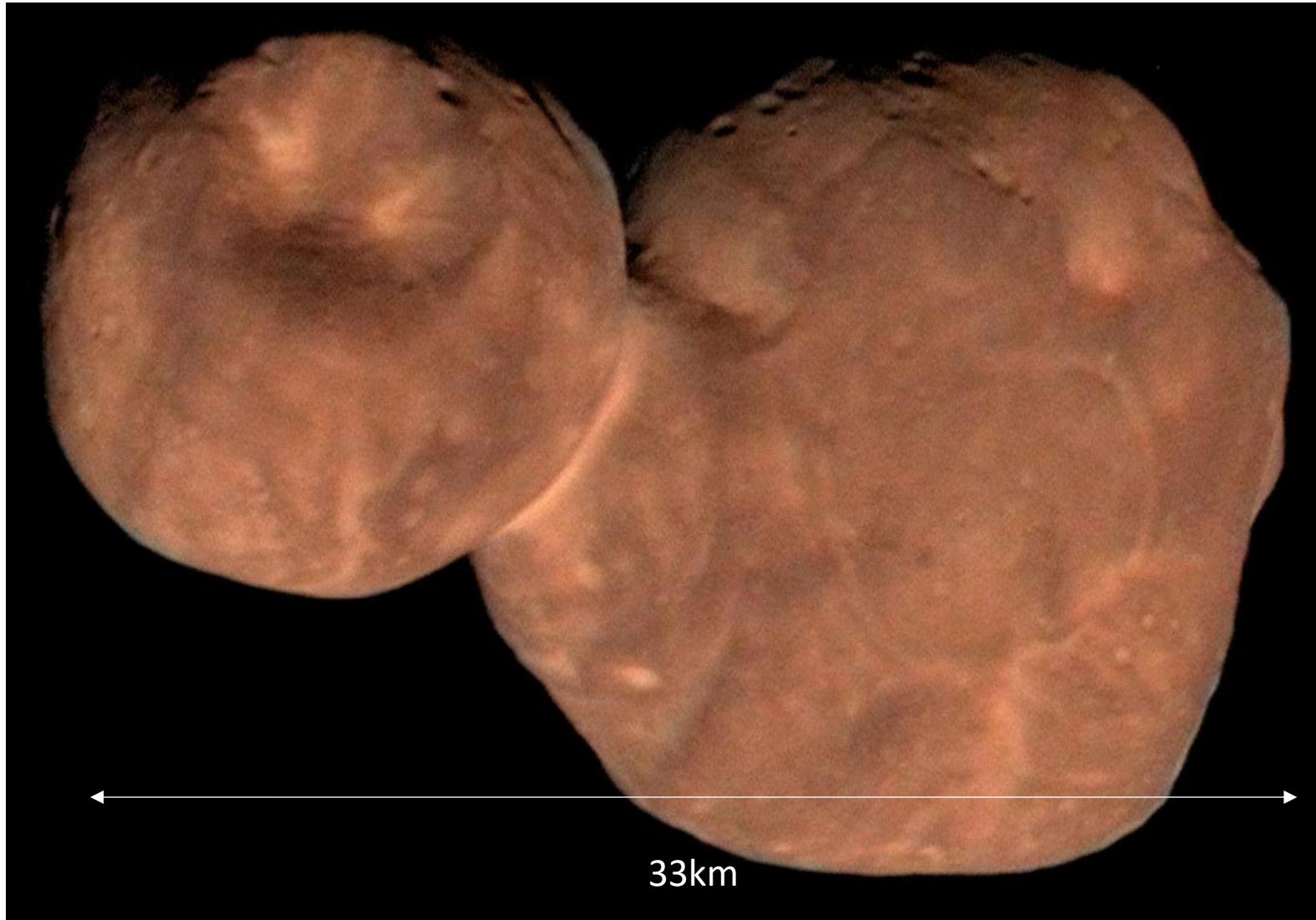


# Structure of the Kuiper Belt



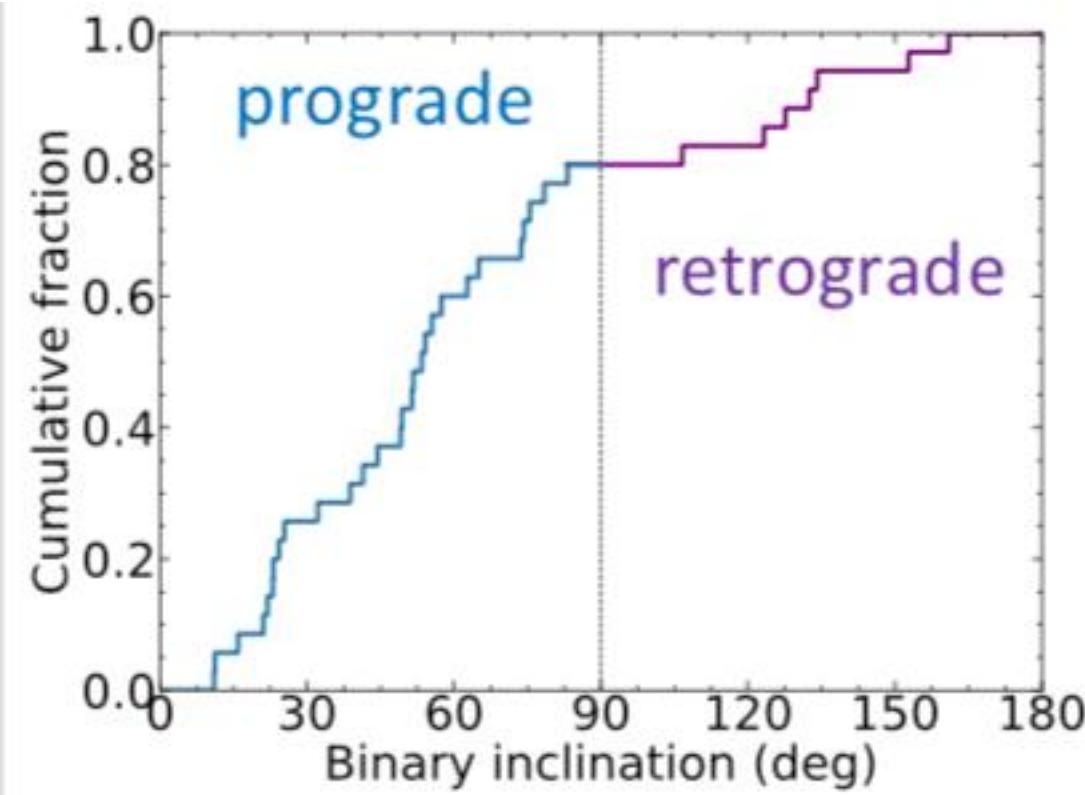
Cold Classicals: Presumably  
pristine planetesimals

# Arrokoth (MU<sub>69</sub>)

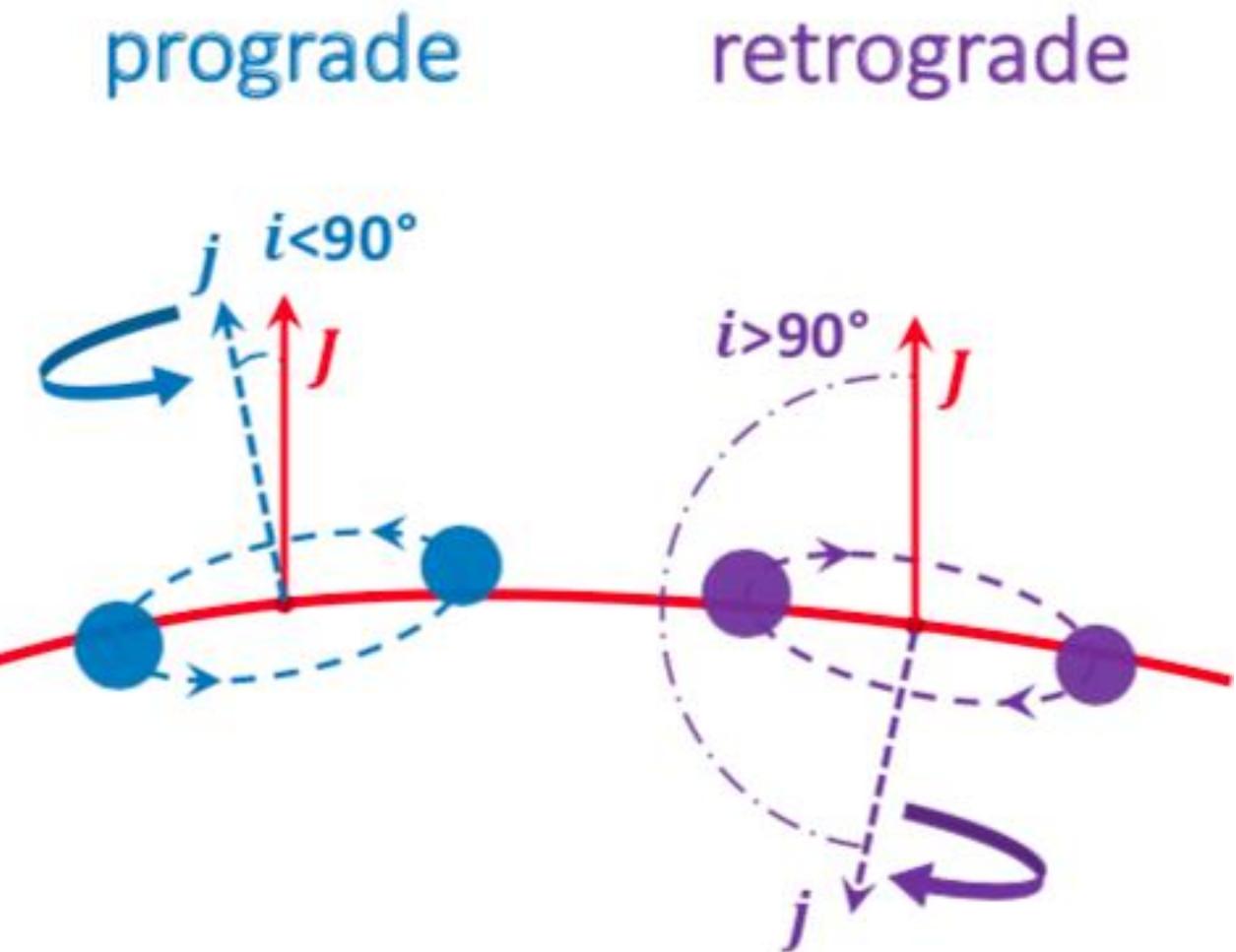


New Horizons Flyby, Jan 2019

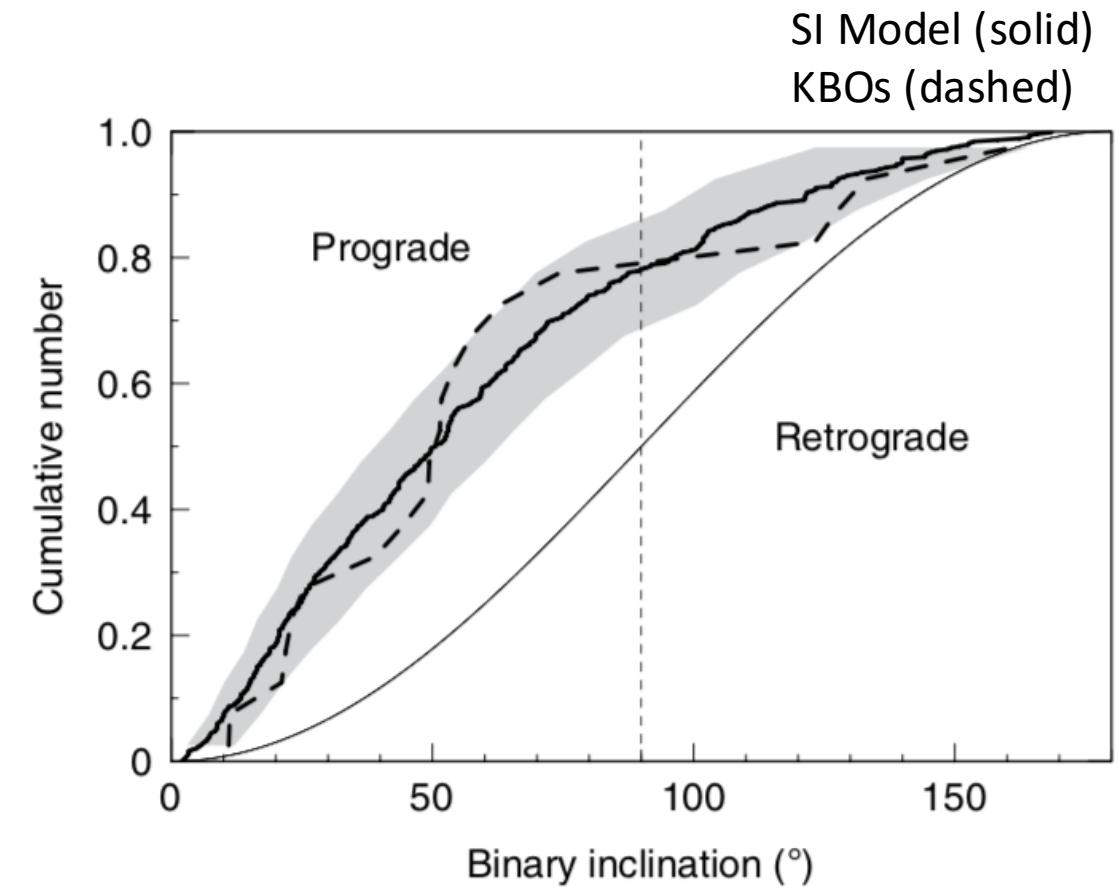
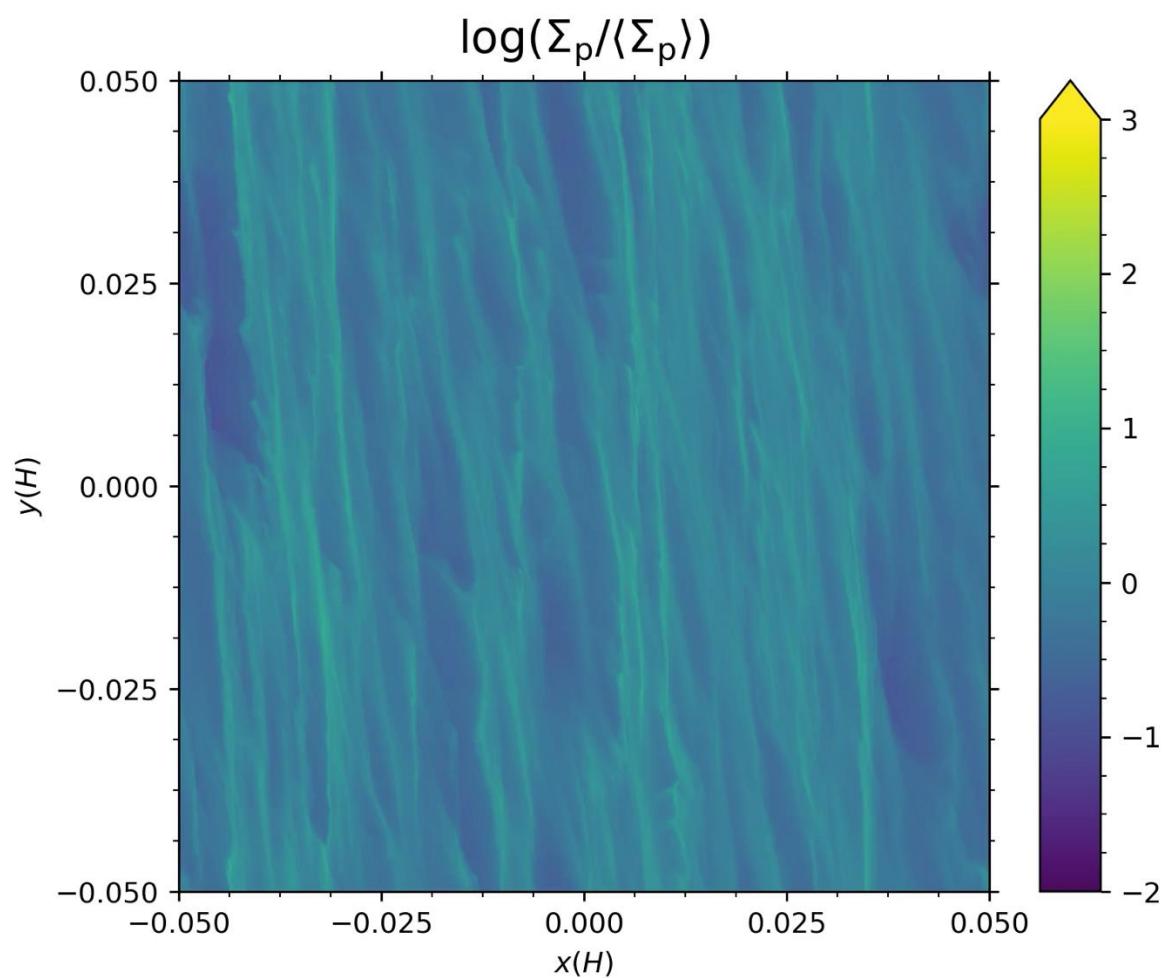
# Cold Classical KBOs: Preference for Prograde



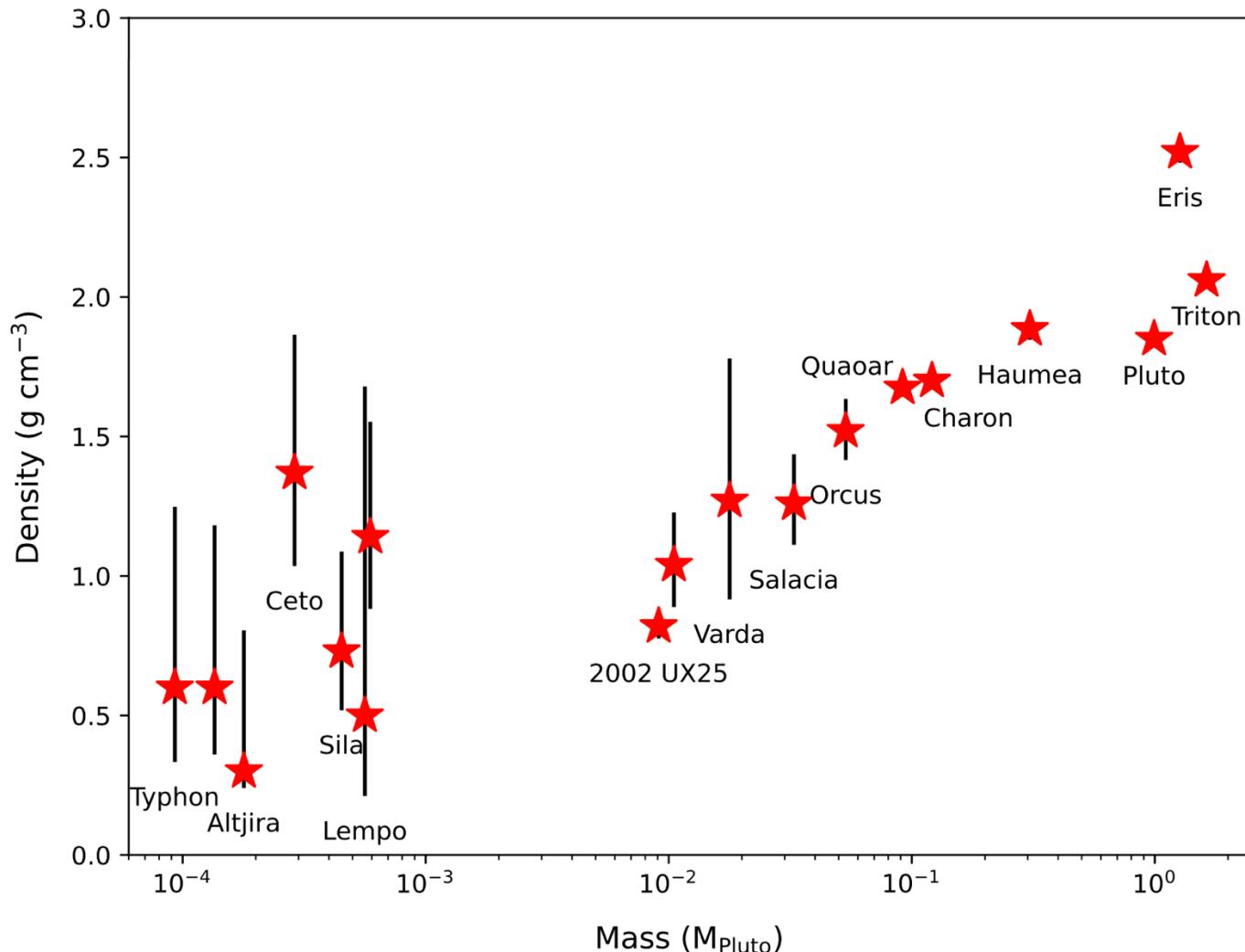
orbiting around the Sun



# Counting binaries: Preference for Prograde (~80%)

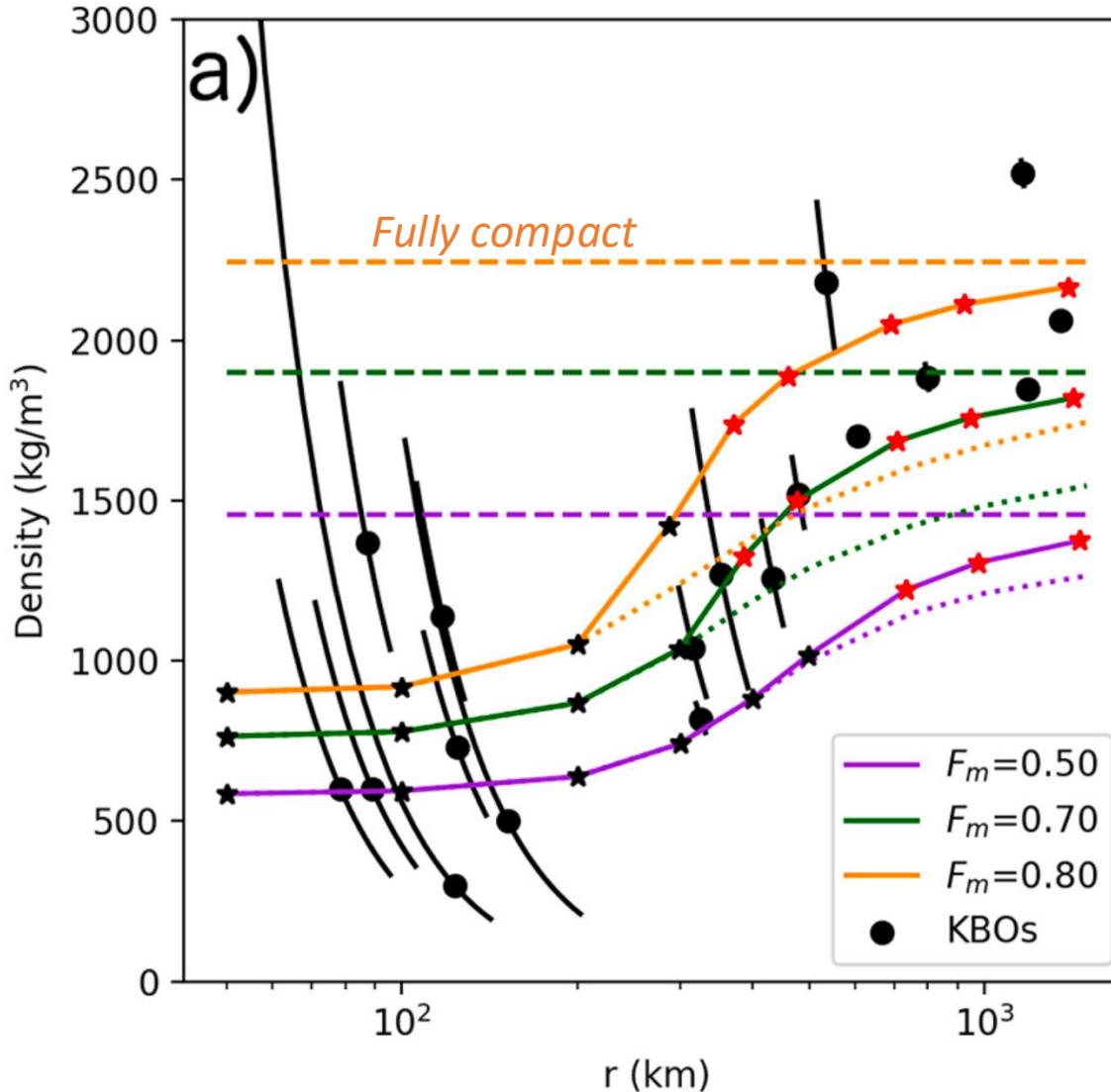


# The density dichotomy of Kuiper Belt objects



# Possible Solution?

- Assumptions
  - Constant composition at birth and growth
  - Porosity removal by gravitational compaction

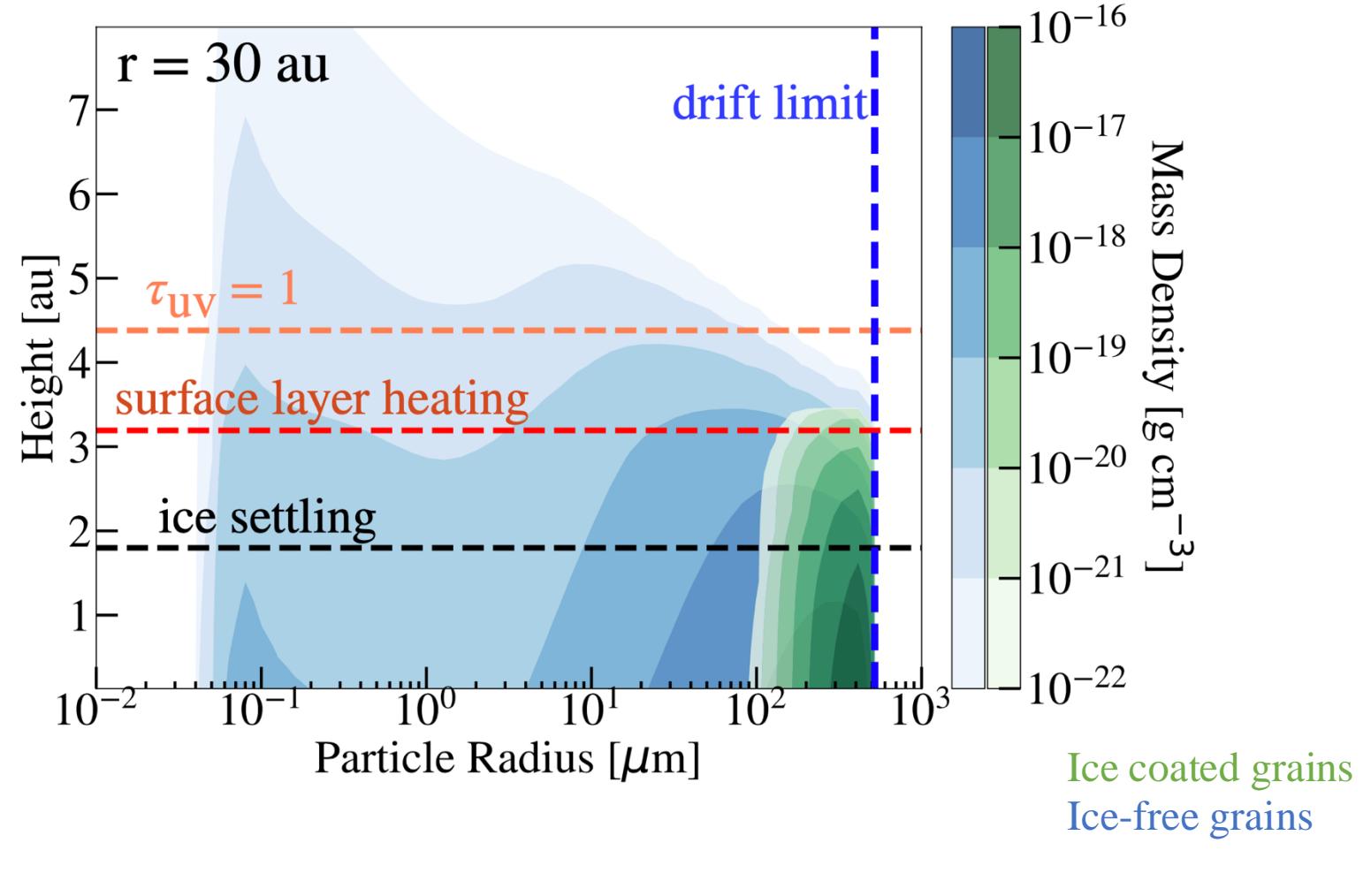


- Problems
  - Low-mass objects need to be unreasonably porous
  - Timing!  $^{26}\text{Al}$  would melt if formed within 4 Myr

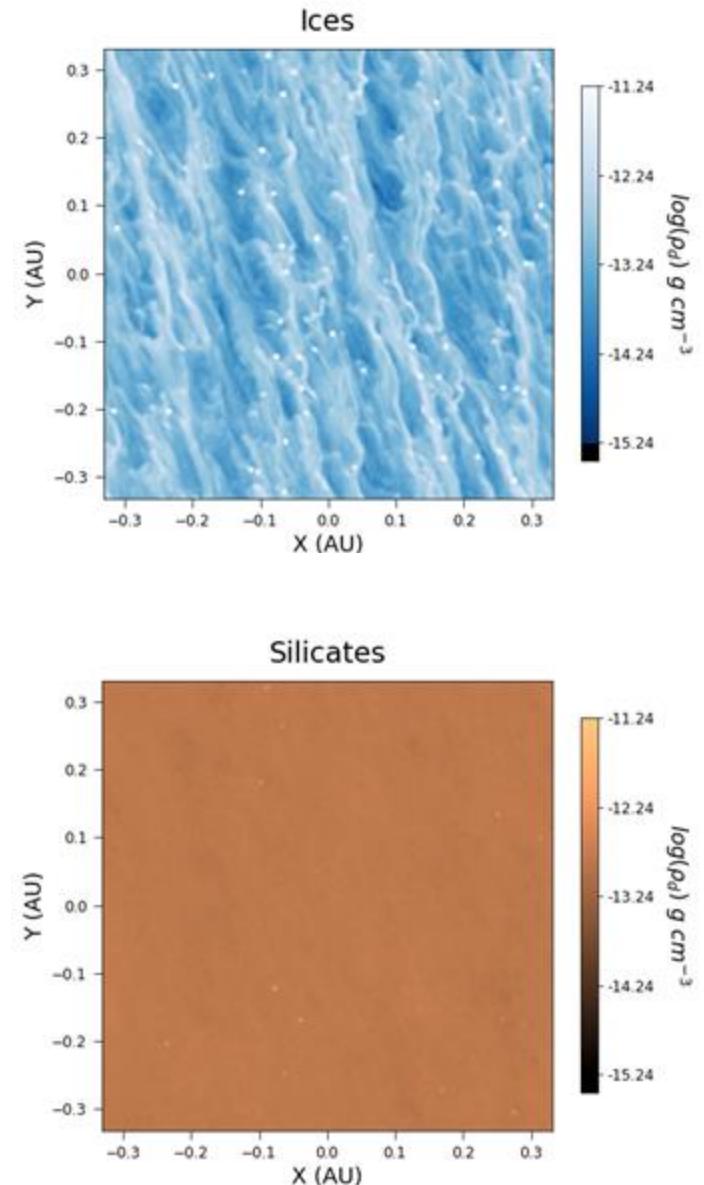
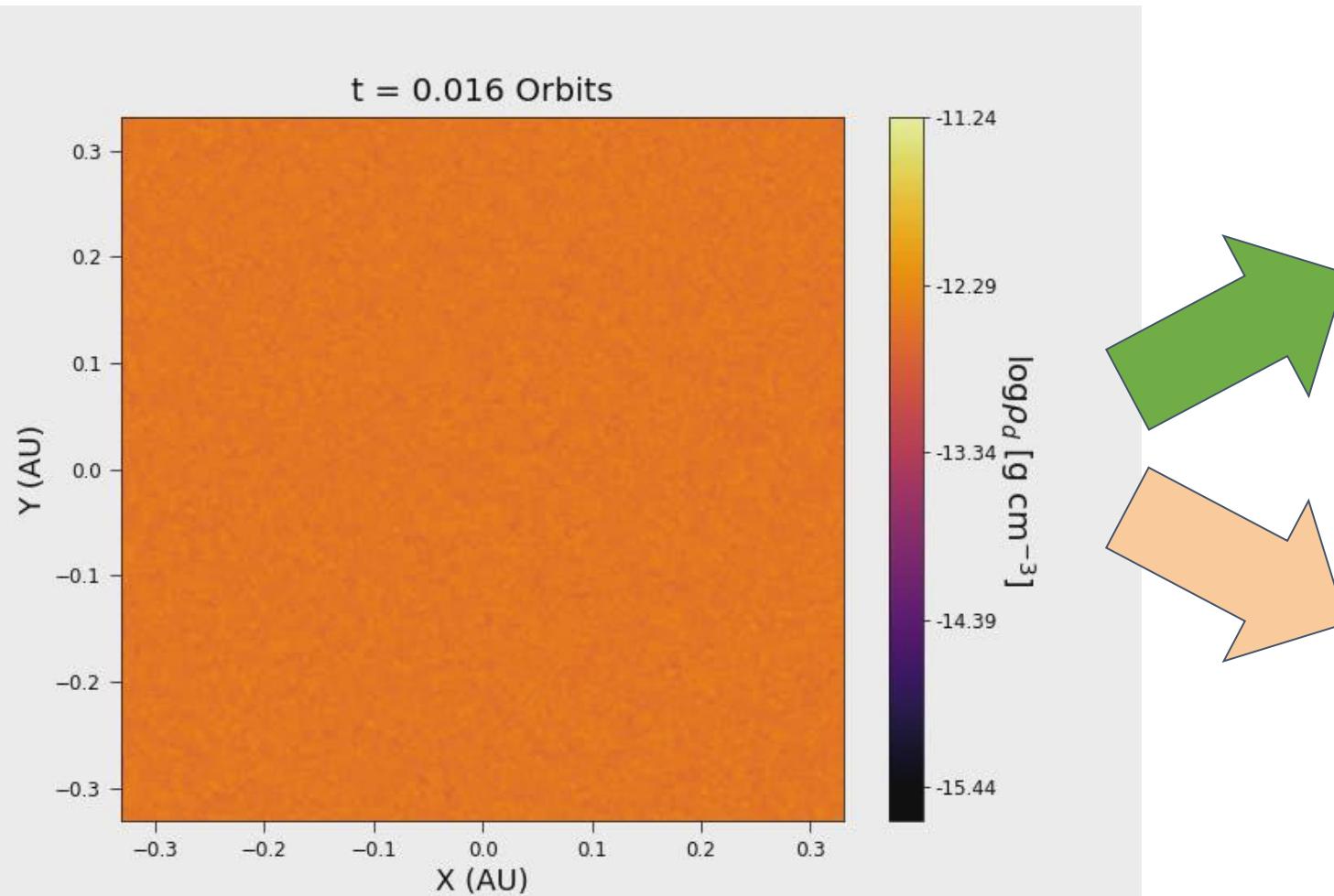
# Abandoning Constant Composition

Heating and UV irradiation remove ice on Myr timescales

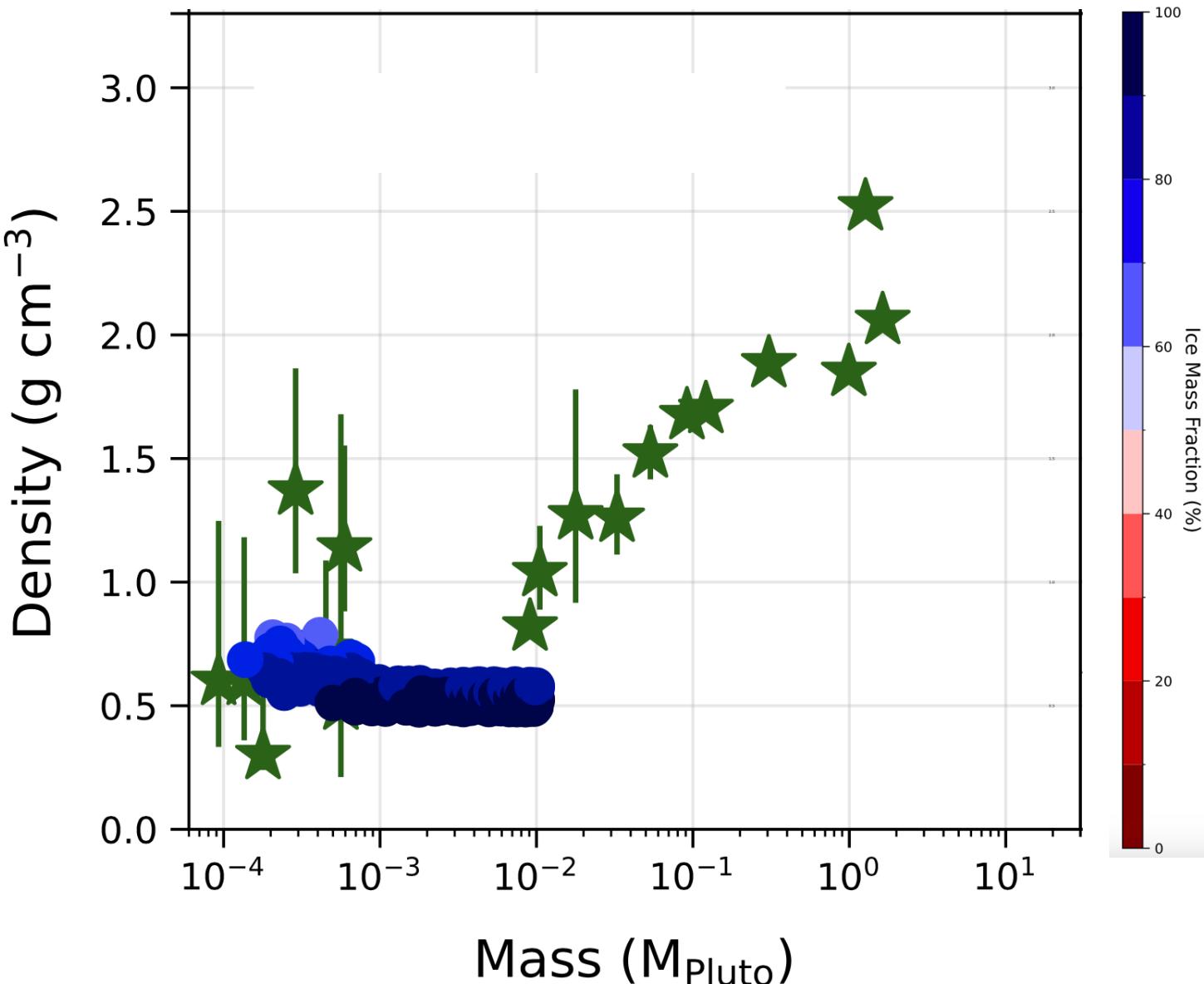
- Small grains lofted in the atmosphere lose ice
- Big grains are shielded and remain icy.



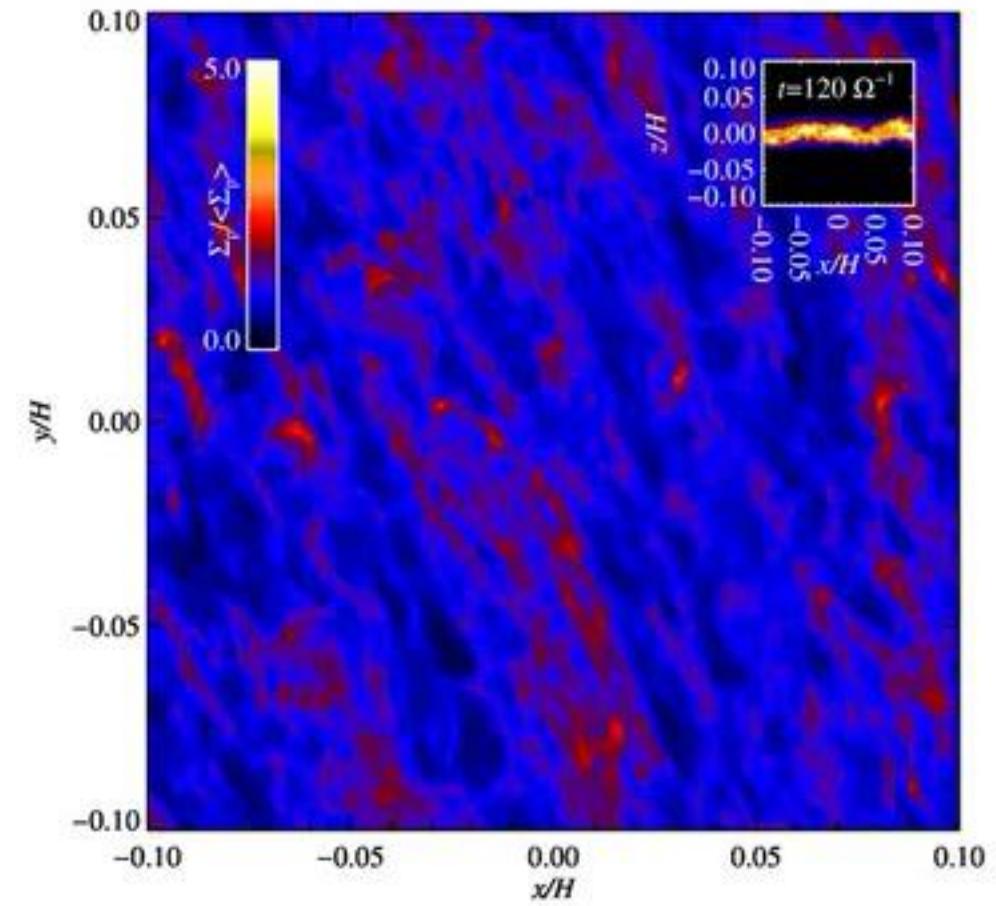
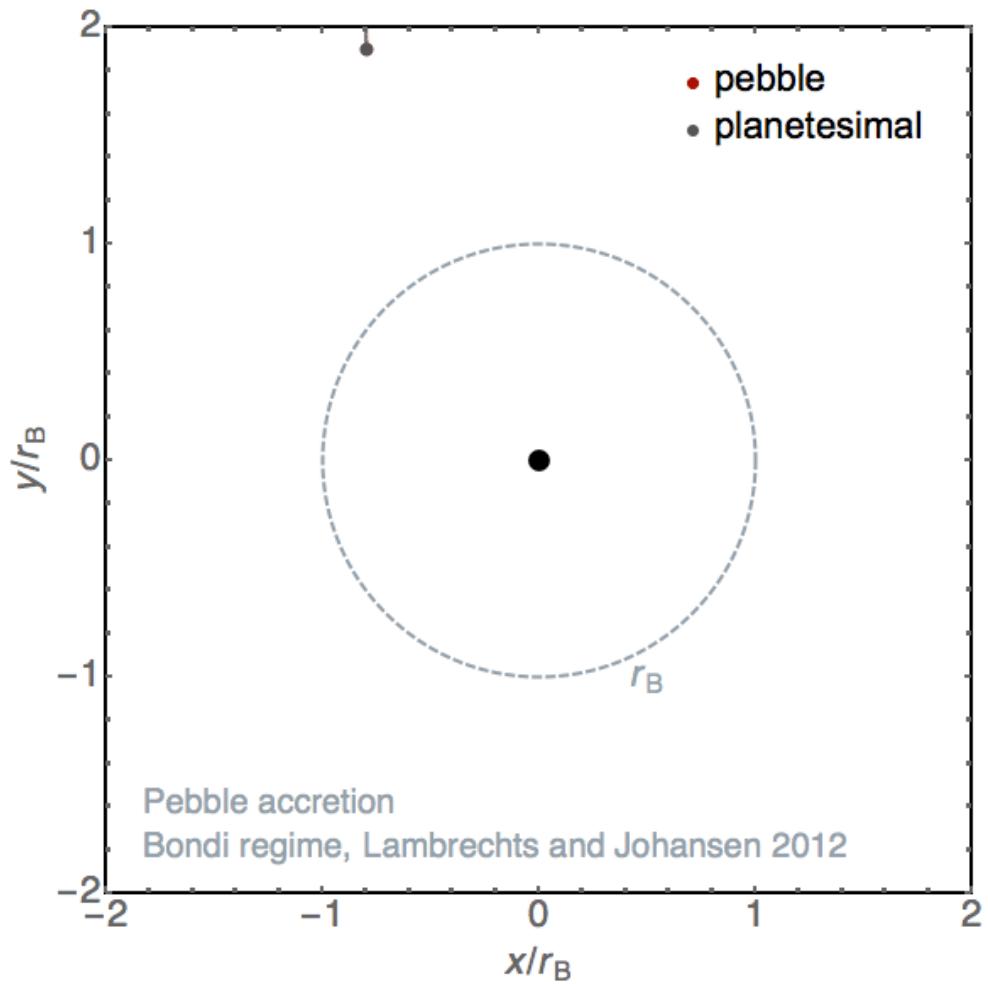
# Split into icy and silicate pebbles



# The first planetesimals are icy



# Pebble Accretion



Lyra+ '08, '09, '23, Ormel & Klahr '10, Lambrechts & Johansen '12  
See Johansen & Lambrechts '17 for a review

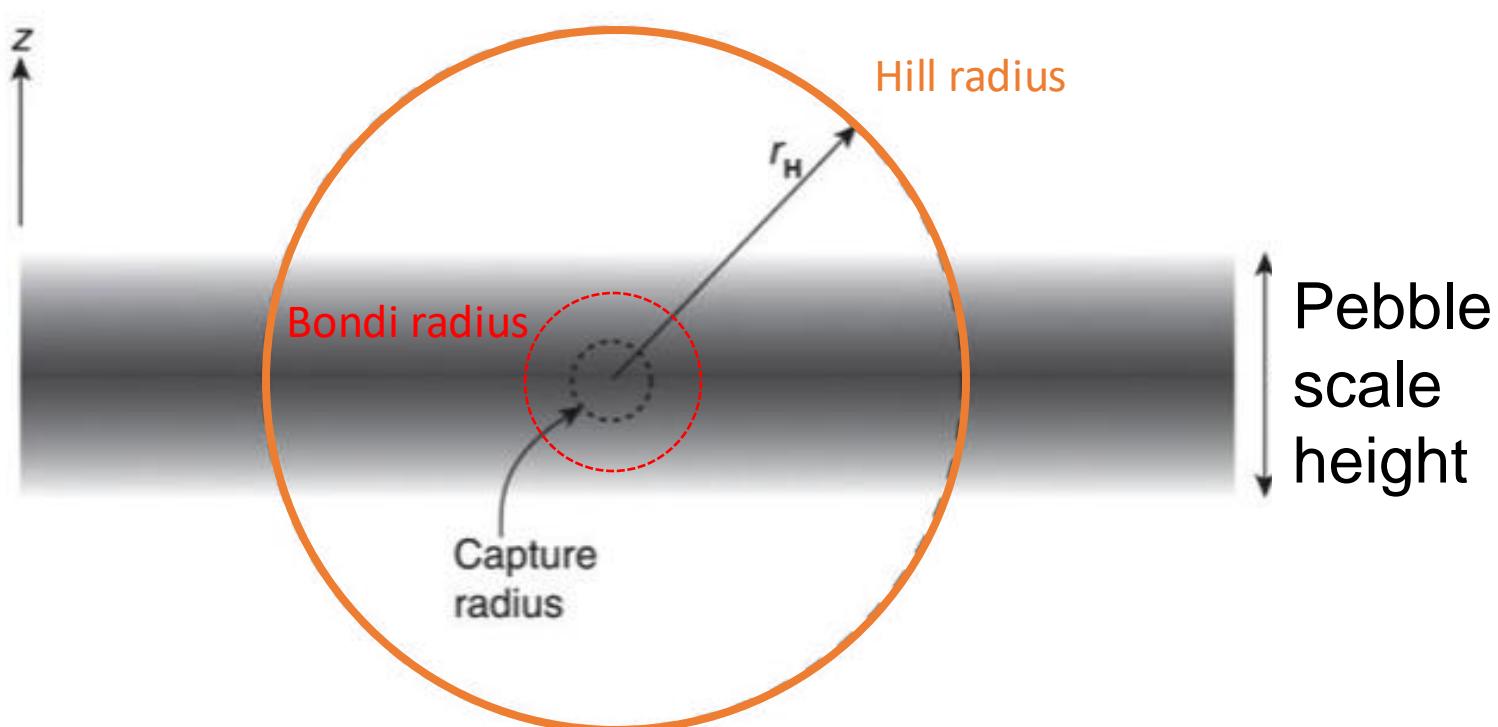
## Pebble Accretion: Geometric, Bondi, and Hill regime

**Bondi** accretion - Bound against thermal (dynamic) **kinetic energy**

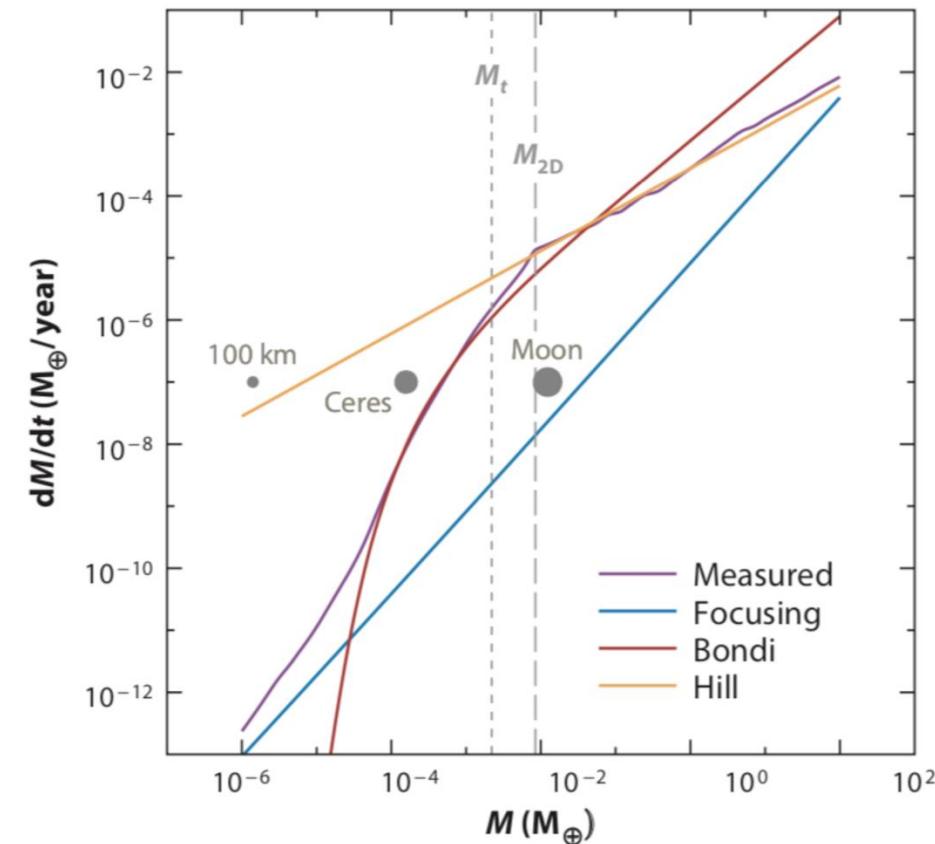
**Hill** accretion - Bound against **stellar tide**

$$\xi \equiv \left( \frac{R_{\text{acc}}}{2H_d} \right)^2 \quad \dot{M}_{3D} = \lim_{\xi \rightarrow 0} \dot{M} = \pi R_{\text{acc}}^2 \rho_{d0} \delta v,$$

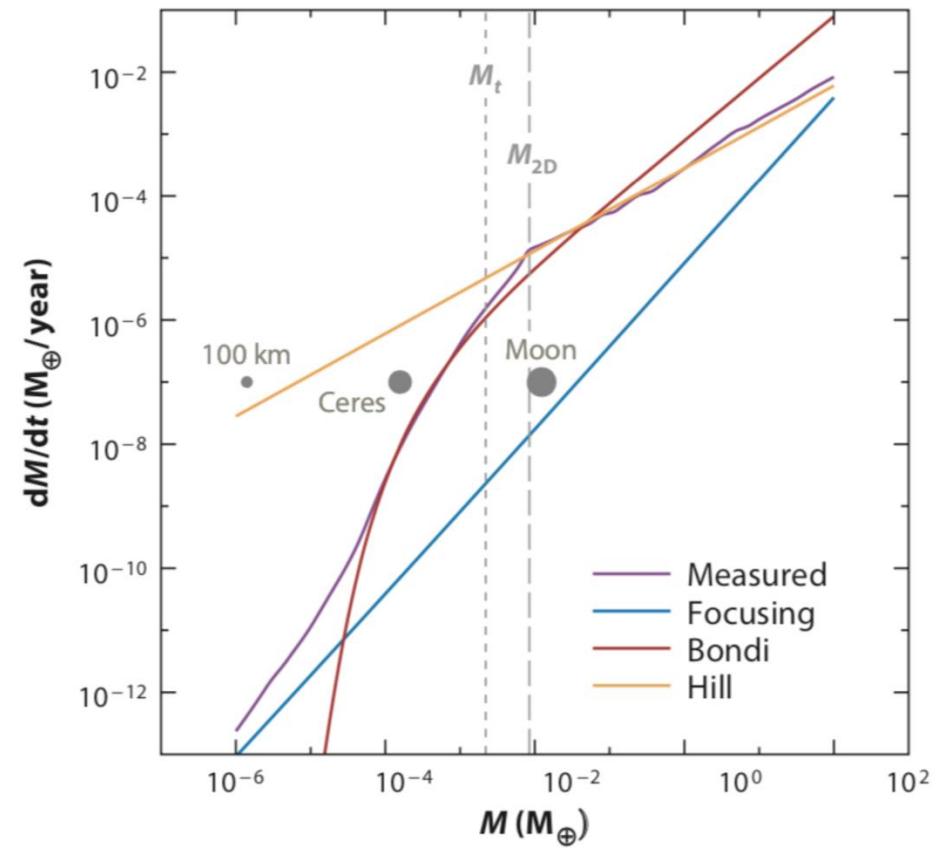
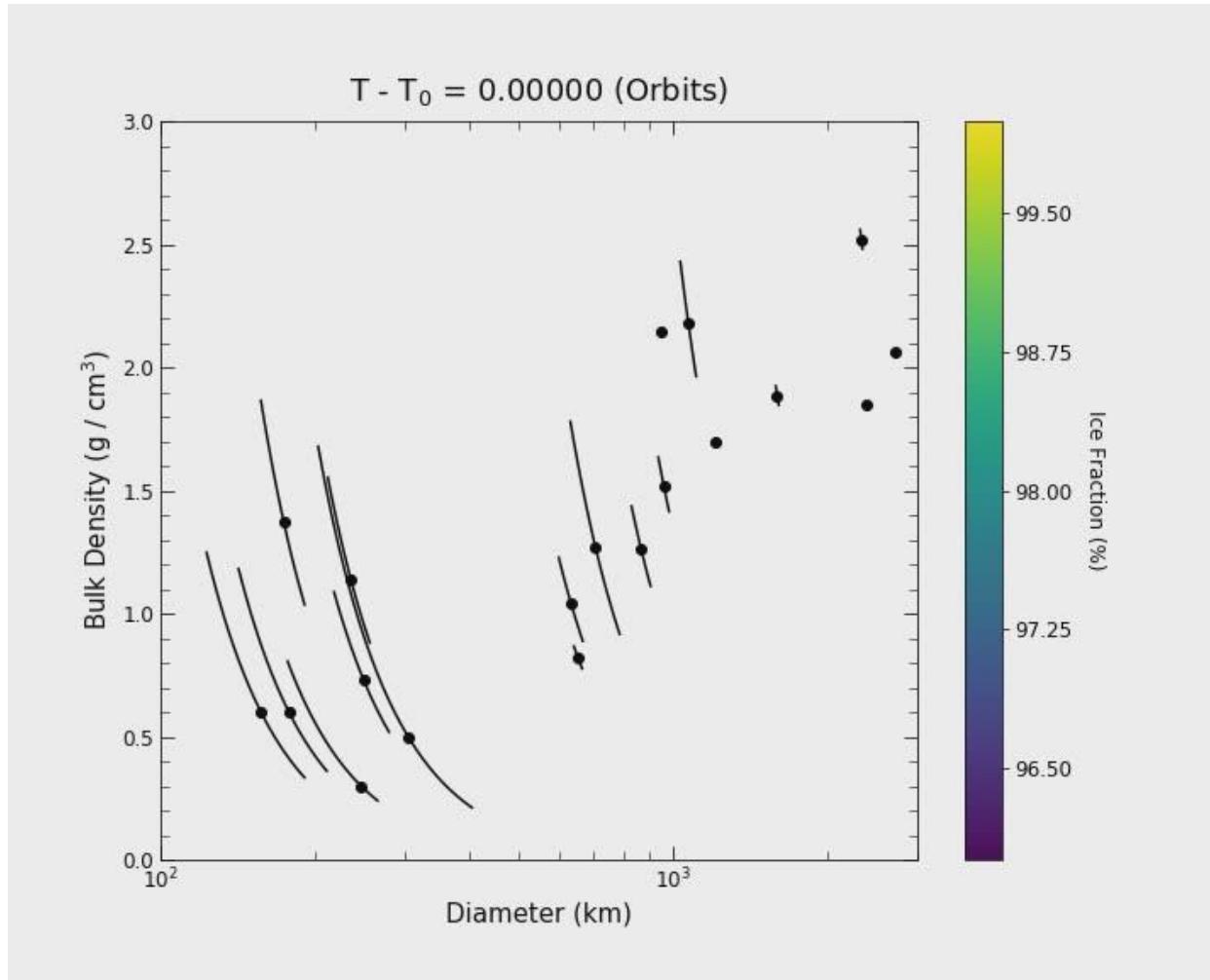
$$\dot{M}_{2D} = \lim_{\xi \rightarrow \infty} \dot{M} = 2R_{\text{acc}} \Sigma_d \delta v,$$



Mass Accretion rates

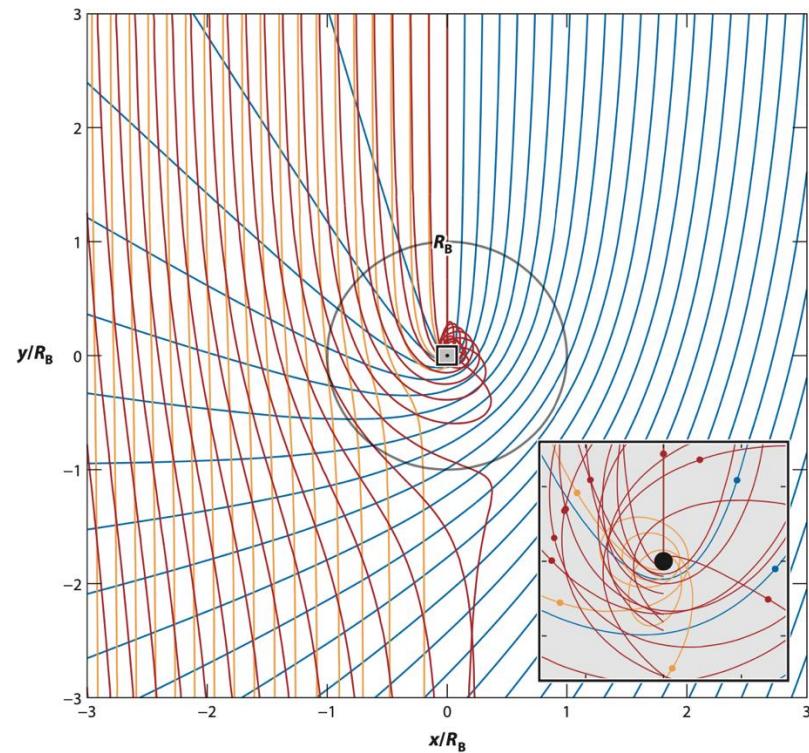


## Integrate pebble accretion



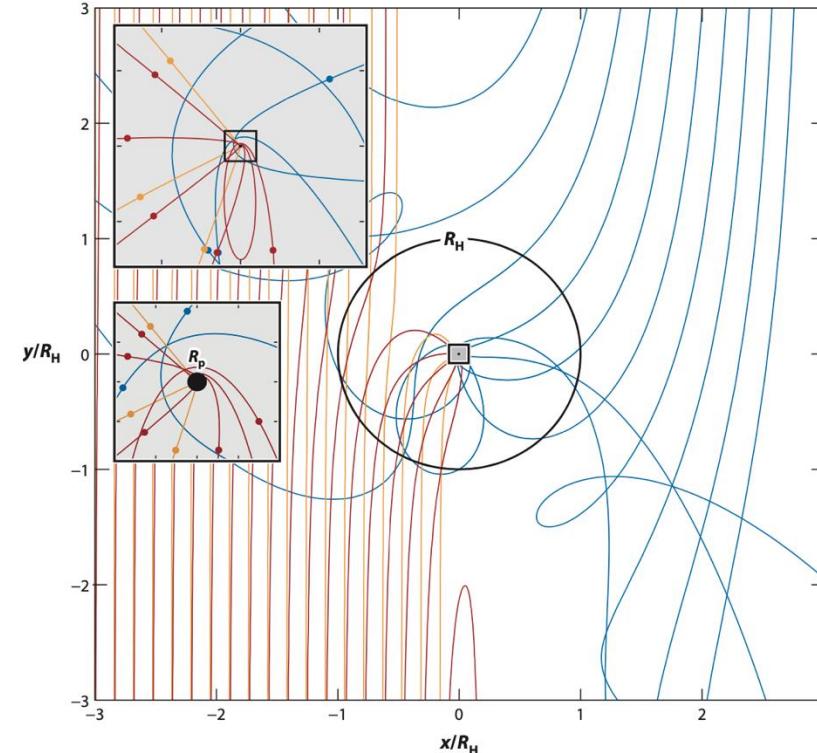
## Pebble Accretion: Pebbles of different size accrete differently

Bondi Regime



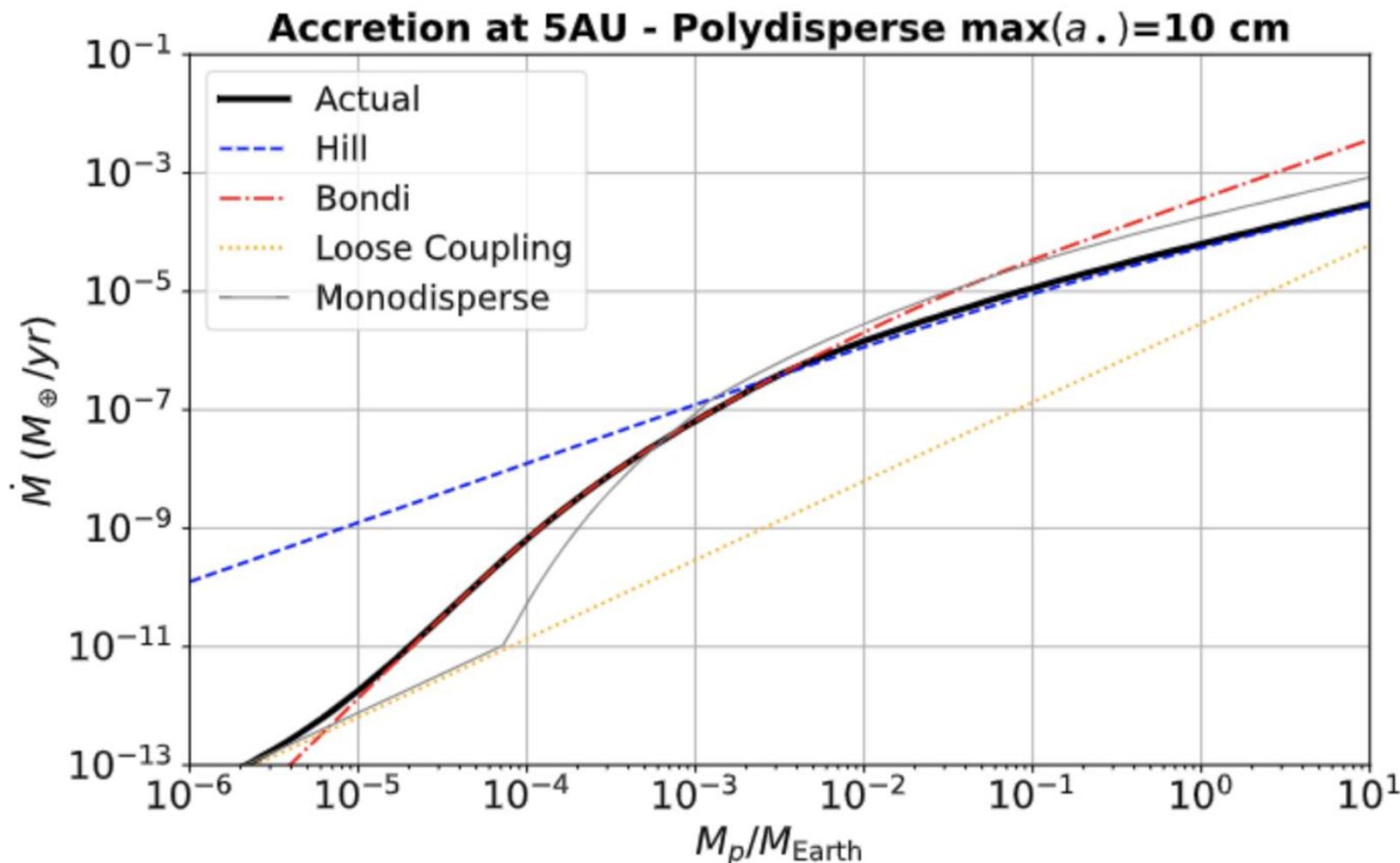
Best accreted  
Drag time = Time to cross Bondi sphere

Hill Regime



Best accreted  
Drag time ~ Orbital Time

## Accretion Rates



# Analytical theory of polydisperse (multi-species) pebble accretion

## Monodisperse (single species)

$$\dot{M}_{3D} = \xi \lim_{\xi \rightarrow 0} \dot{M} = \pi R_{acc}^2 \rho_{d0} \delta v,$$

$$\dot{M}_{2D} = \lim_{\xi \rightarrow \infty} \dot{M} = 2R_{acc} \Sigma_d \delta v,$$

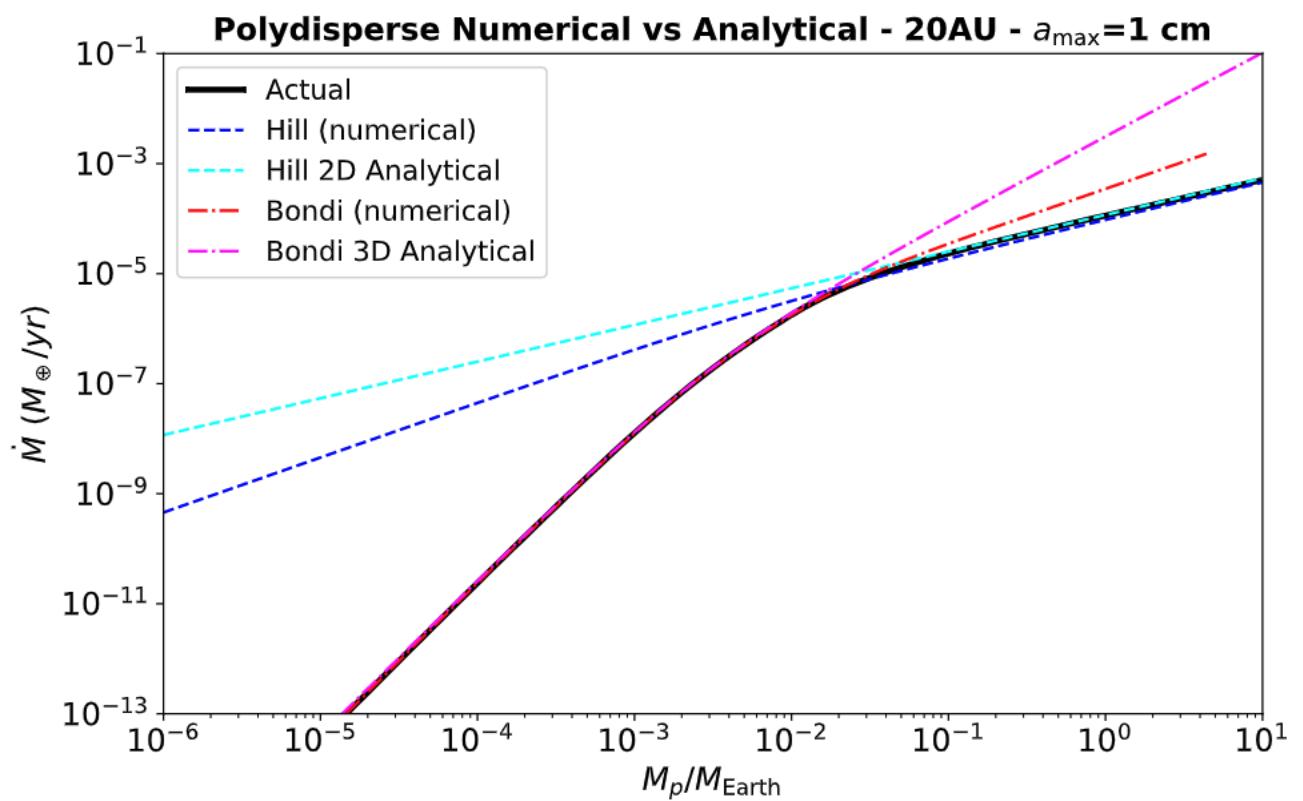
Lambrechts & Johansen (2012)

## Polydisperse (multiple species)

$$\dot{M}_{2D,Hill} = \frac{6(1-p)}{14-5q-3k} \left( \frac{St_{max}}{0.1} \right)^{2/3} \Omega R_H^2 Z \Sigma_g$$

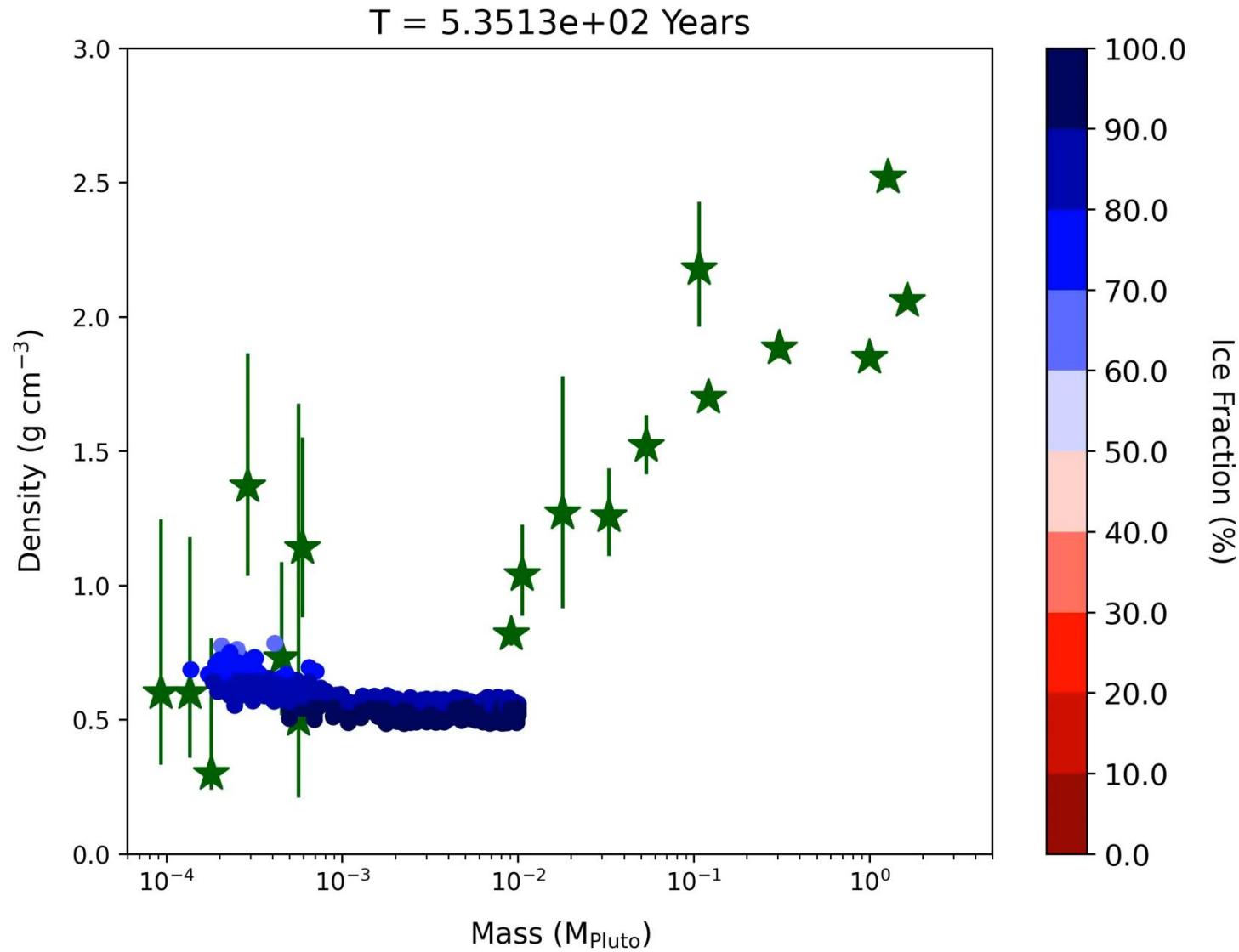
$$\begin{aligned} \dot{M}_{3D,Bondi} \approx & C_1 \frac{\gamma_l \left( \frac{b_1+1}{s}, j_1 a_{max}^s \right)}{s j_1^{(b_1+1)/s}} + C_2 \frac{\gamma_l \left( \frac{b_2+1}{s}, j_2 a_{max}^s \right)}{s j_2^{(b_2+1)/s}} + \\ & C_3 \frac{\gamma_l \left( \frac{b_3+1}{s}, j_3 a_{max}^s \right)}{s j_3^{(b_3+1)/s}} + C_4 \frac{\gamma_l \left( \frac{b_4+1}{s}, j_4 a_{max}^s \right)}{s j_4^{(b_4+1)/s}}, \end{aligned}$$

Lyra et al. (2023)



Lyra et al. 2023

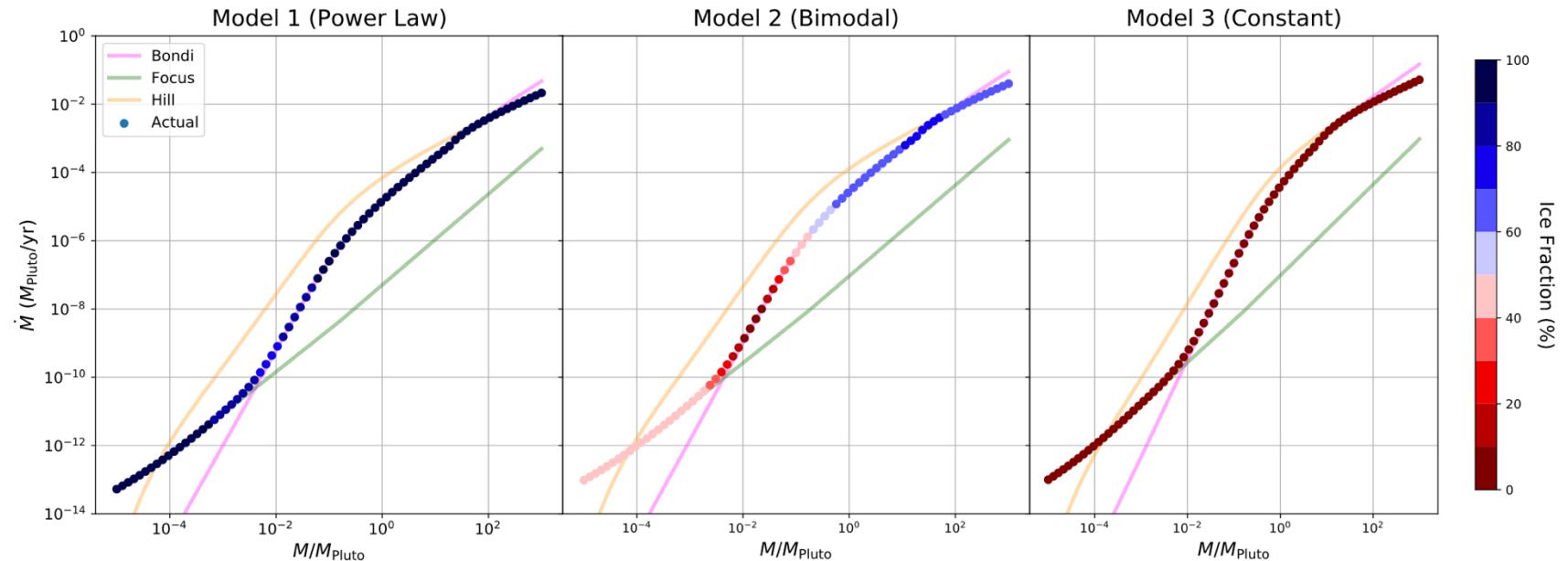
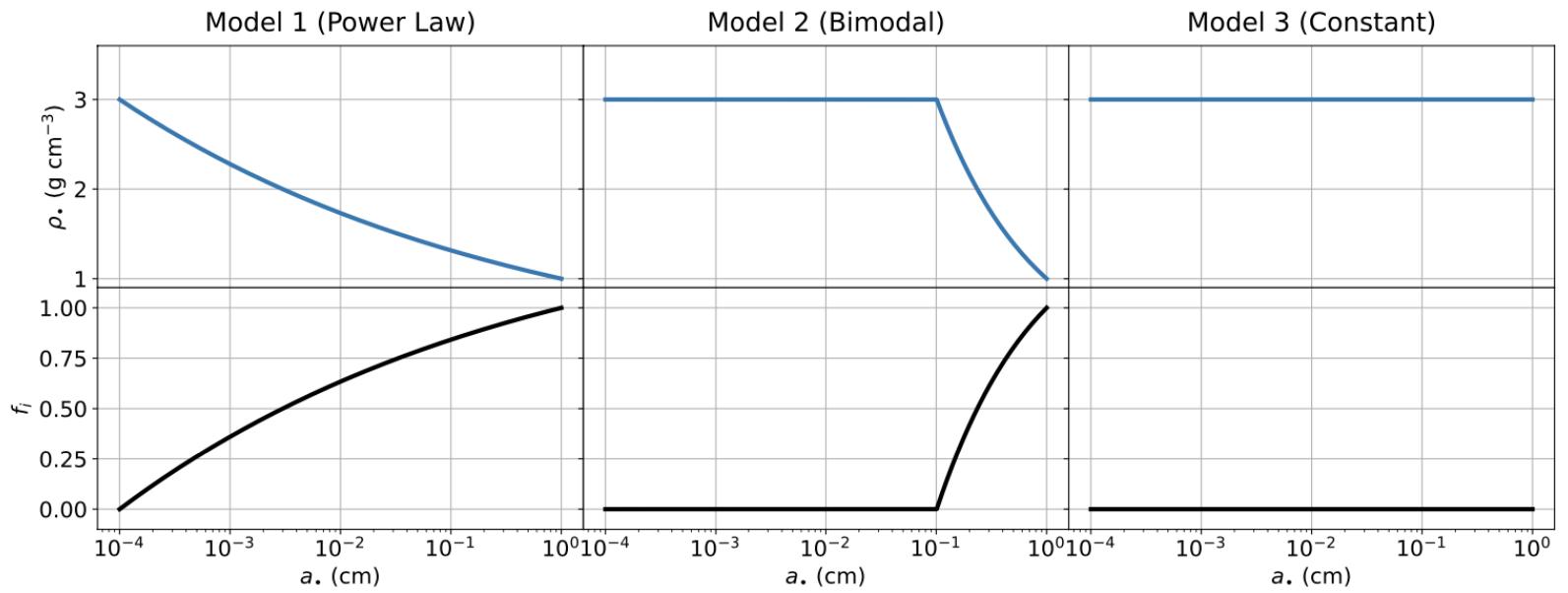
# Growing Pluto by silicate pebble accretion



**Pebble Density**

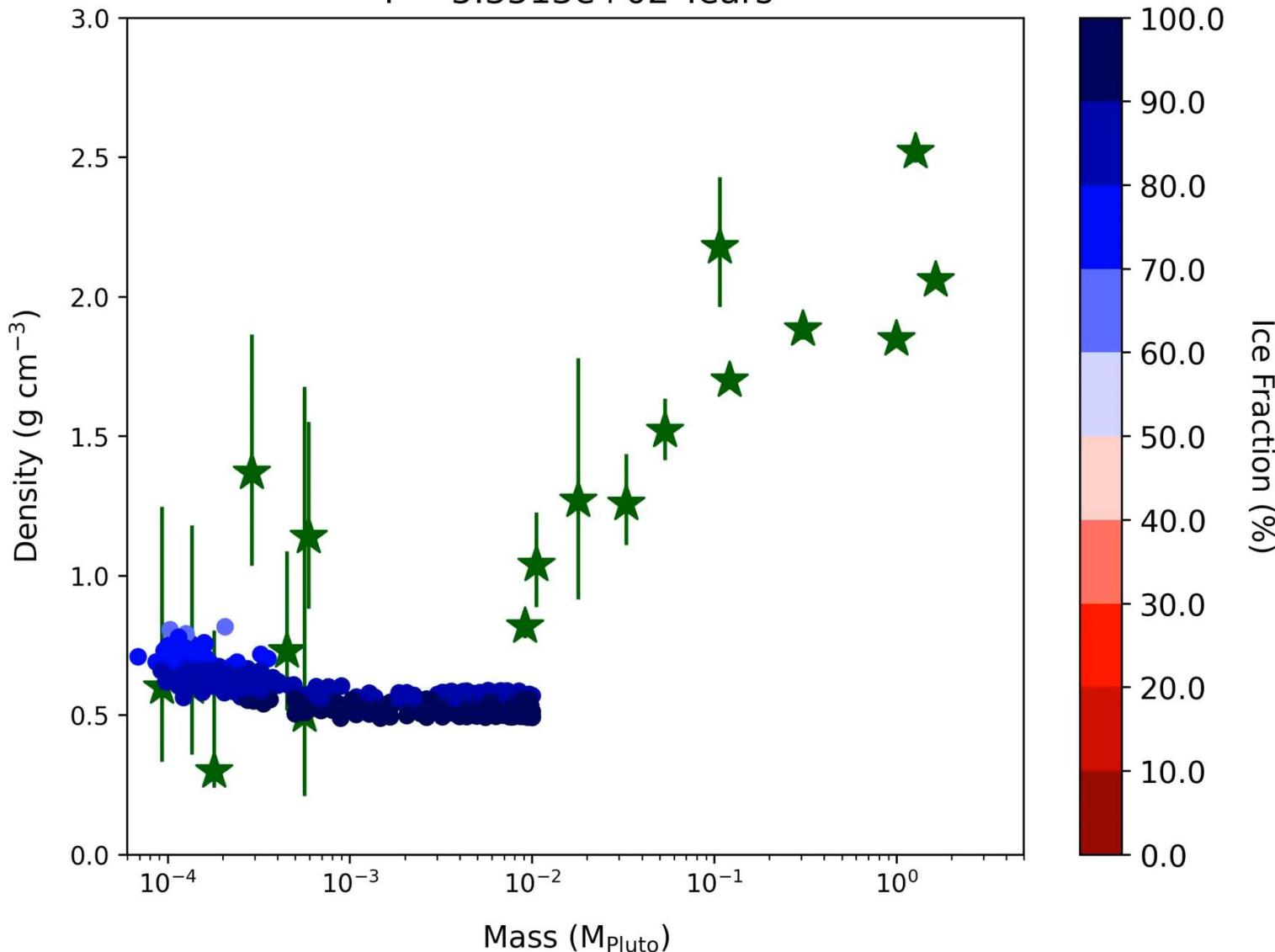
**Ice Fraction**

**Mass Accretion rate**

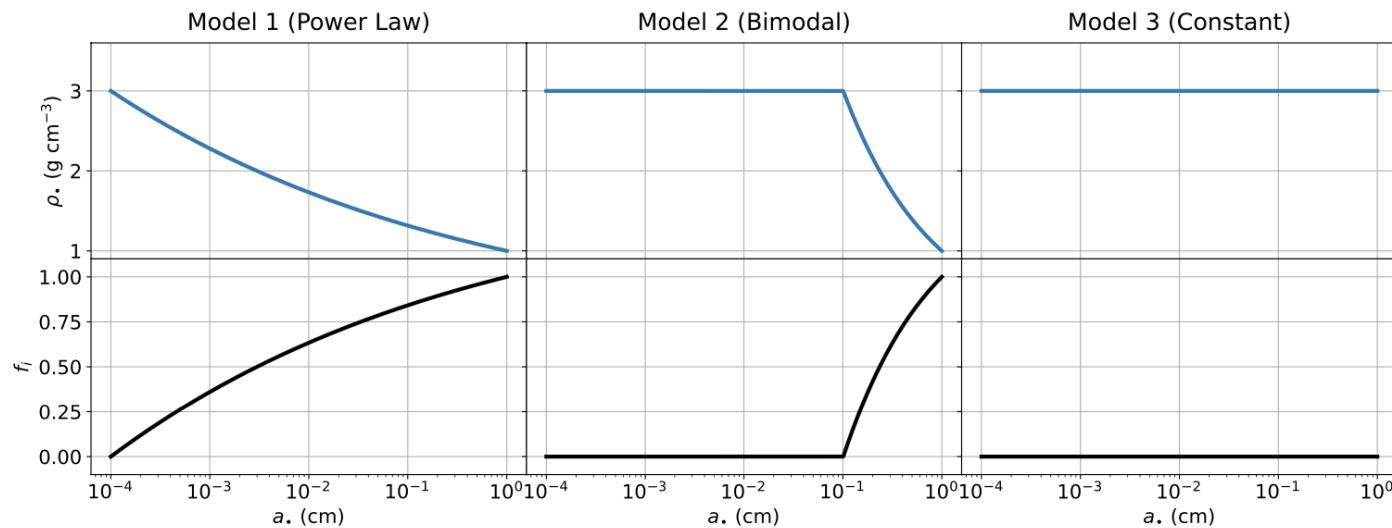


## Growing Pluto by silicate pebble accretion

$$T = 5.3513e+02 \text{ Years}$$



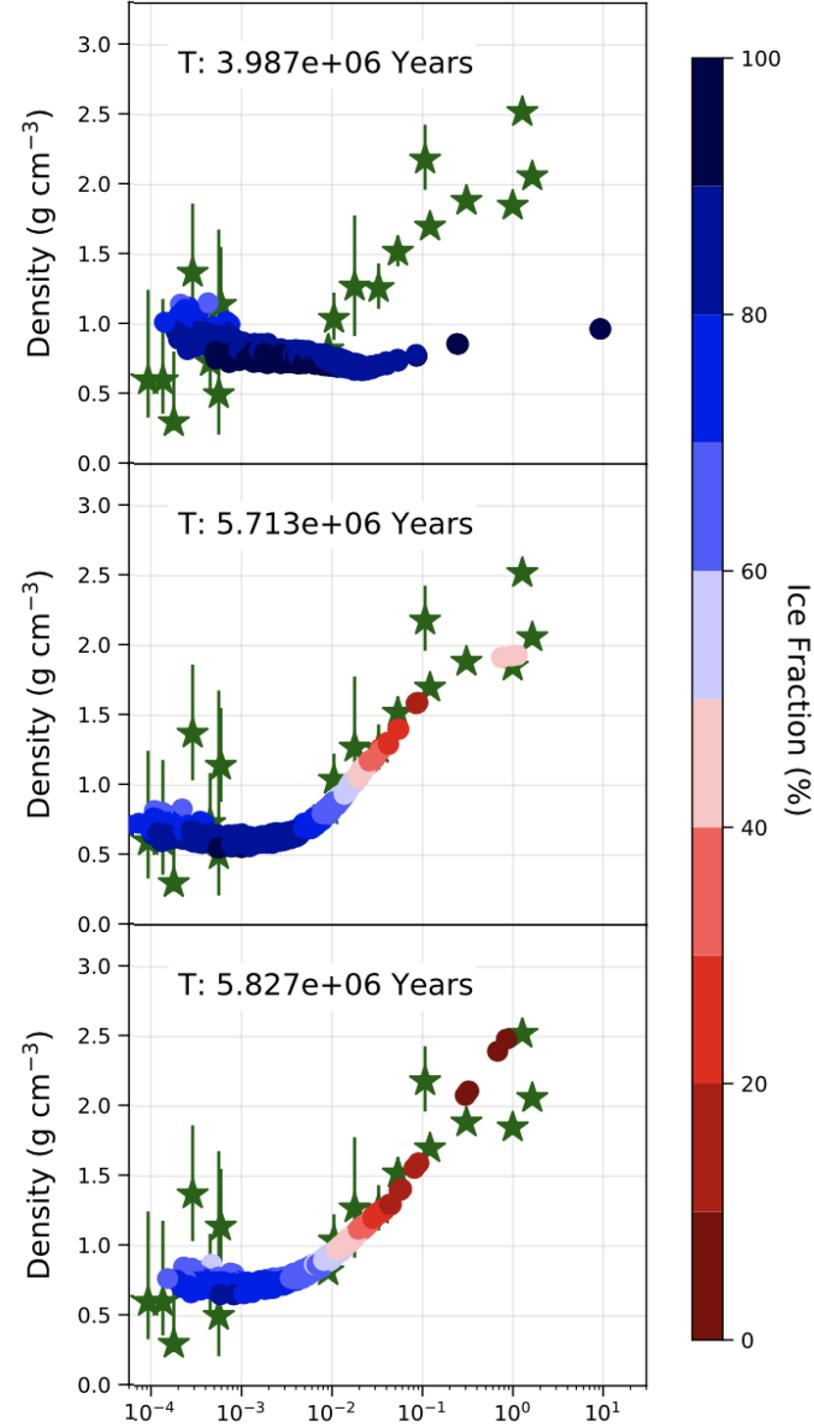
## Resulting Densities vs Mass relations



**Model 1 (Power Law)**

**Model 2 (Bimodal)**

**Model 3 (Constant)**



## Take-home message

- Streaming Instability fits
  - slope of asteroid belt distribution,
  - prograde-retrograde distribution of Kuiper belt objects
  - Low density of small classical Kuiper belt objects
- Pebble accretion is a very efficient planetary growth mechanism
  - Polydisperse Bondi accretion 1-2 orders of magnitude more efficient than monodisperse
  - Silicate pebble accretion explains densities of high-mass Kuiper belt objects

- Polydisperse Bondi accretion 1-2 orders of magnitude more efficient than monodisperse
  - Best accreted pebbles are those of drag time  $\sim$  Bondi time, not the largest ones
  - The largest ones dominate the mass budget, but accrete poorly
- Onset of Bondi accretion 1-2 orders of magnitude lower in mass compared to monodisperse
  - Reaches 100-350km objects within Myr timescales
  - Bondi accretion possible on top of Streaming Instability planetary embryos within disk lifetime
- Analytical solution to
  - Polydisperse 2D Hill and 3D Bondi

## Problem: wrong number density

