

Evolution of circumstellar disks and planet formation



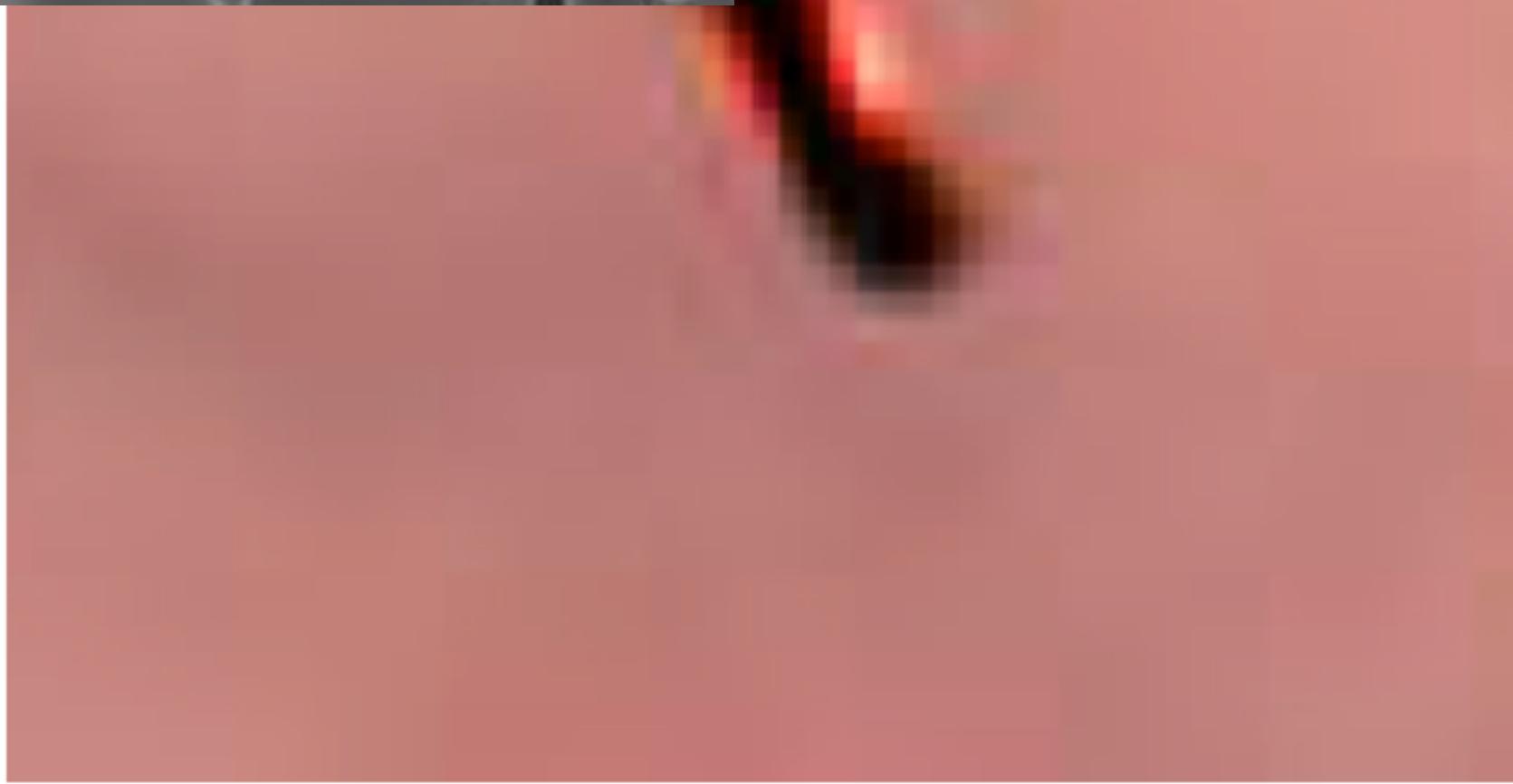
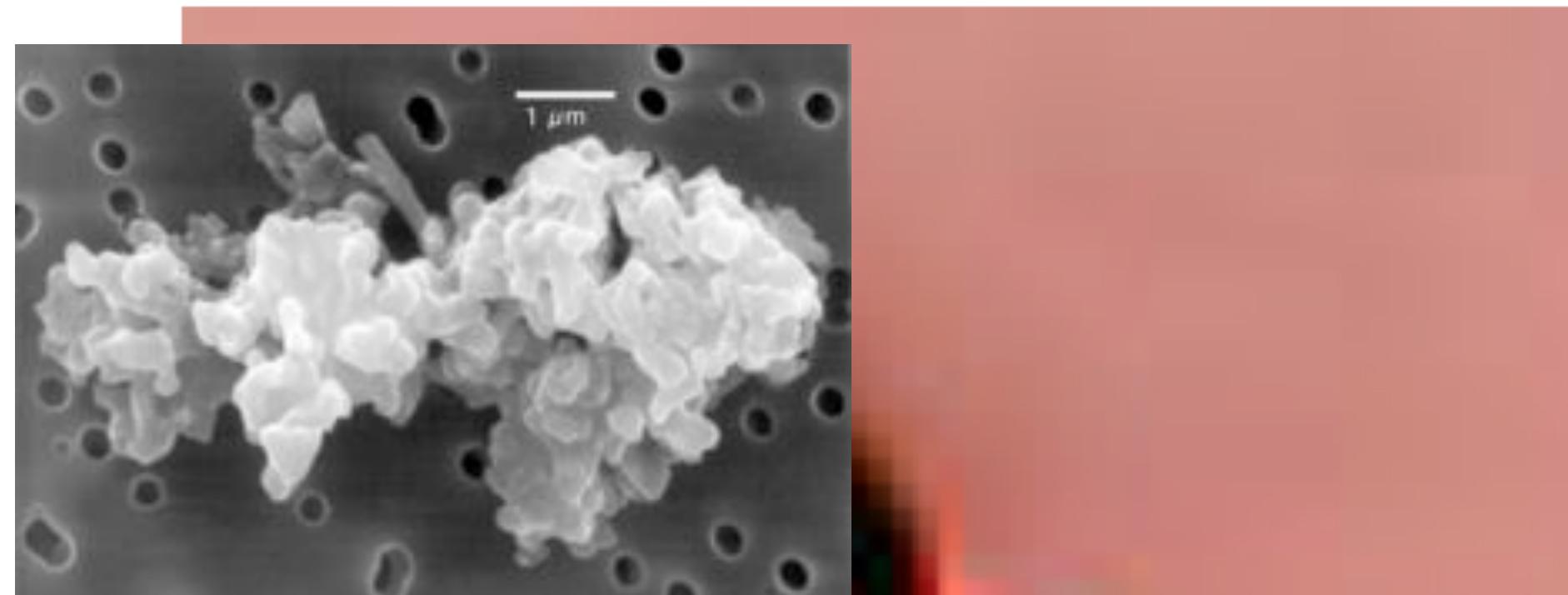
Collaborators

Aaron Boley (Vancouver), Axel Brandenburg (Stockholm), Kees Dullemond (Heidelberg), Anders Johansen (Lund), Tobias Heinemann (KITP), Hubert Klahr (Heidelberg), Min-Kai Lin (ASU), Mordecai-Mark Mac Low (AMNH), Colin McNally (Copenhagen), Krzysztof Mizerski (Warsaw), Sijme-Jan Paardekooper (London), Nikolai Piskunov (Uppsala), Natalie Raettig (Heidelberg), Alex Richert (PSU), Neal Turner (JPL), Miguel de Val-Borro (Princeton), Andras Zsom (MIT).



Outline

- Turbulence
 - Active and dead zones
 - Magneto-rotational and baroclinic instability
 - Vortices and elliptic instability
- Active/dead boundary
 - Rossby wave instability
- Vortex-mode of planet formation
- Observational constraints



Protoplanetary Disks



PP disk fact sheet

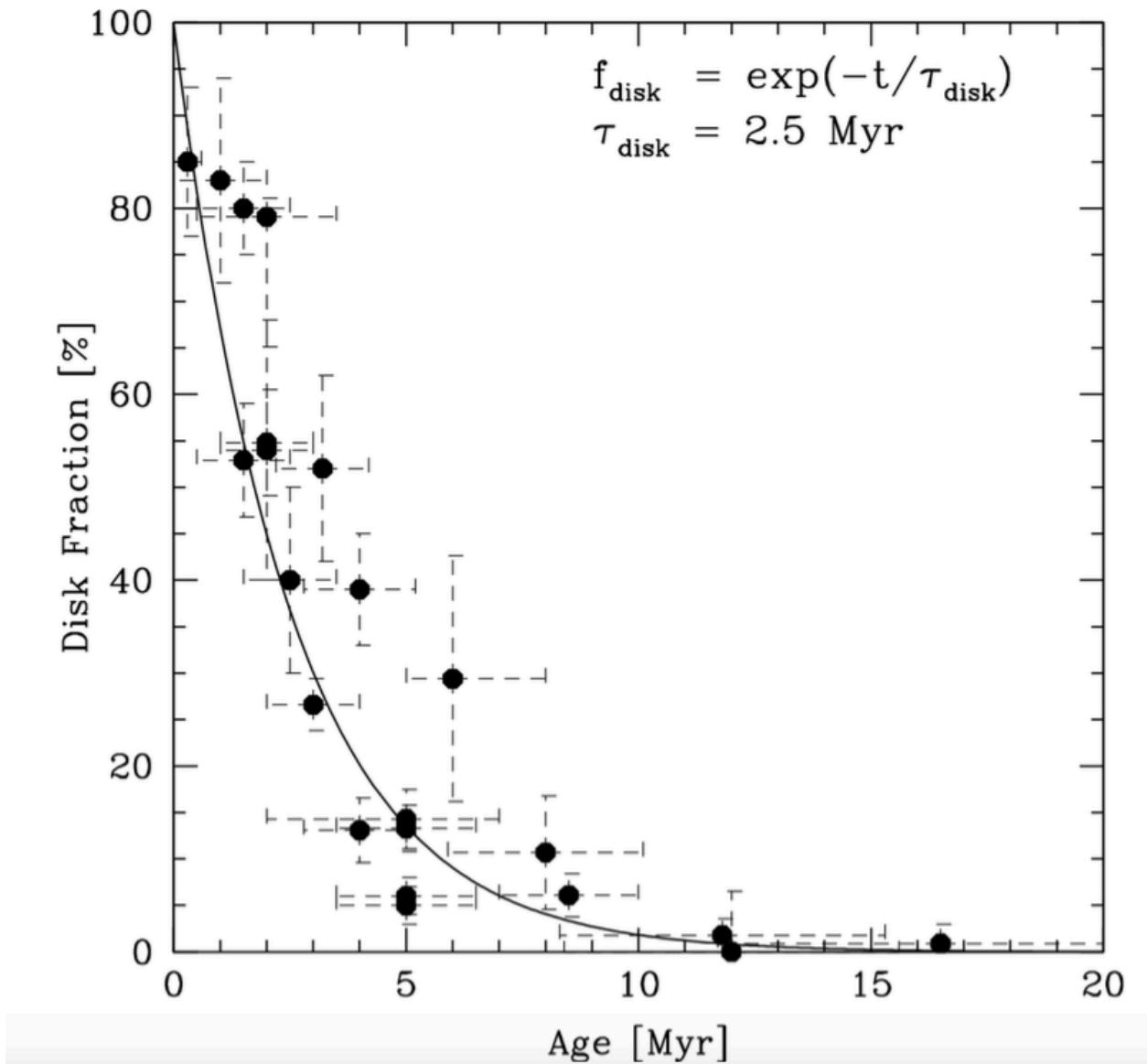
Density: $10^{13} - 10^{15} \text{ cm}^{-3}$
(Air: 10^{21} cm^{-3})

Temperature: 10-1000 K

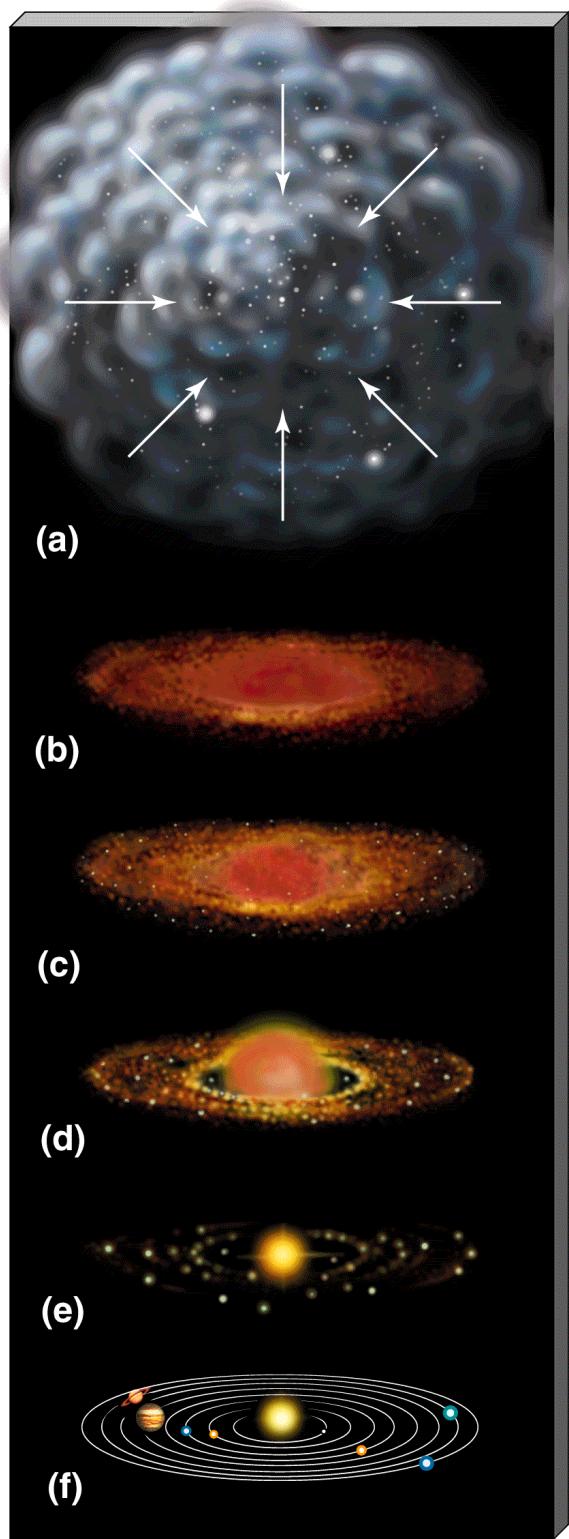
Scale: 0.1-100AU
(1 AU = $1.49 \times 10^{13} \text{ cm}$)

Mass: $10^{-3} - 10^{-1} M_{\text{sun}}$
($1 M_{\text{sun}} = 2 \times 10^{33} \text{ g}$)

Disk lifetime



Disks dissipate with an e-folding time of 2.5 Myr



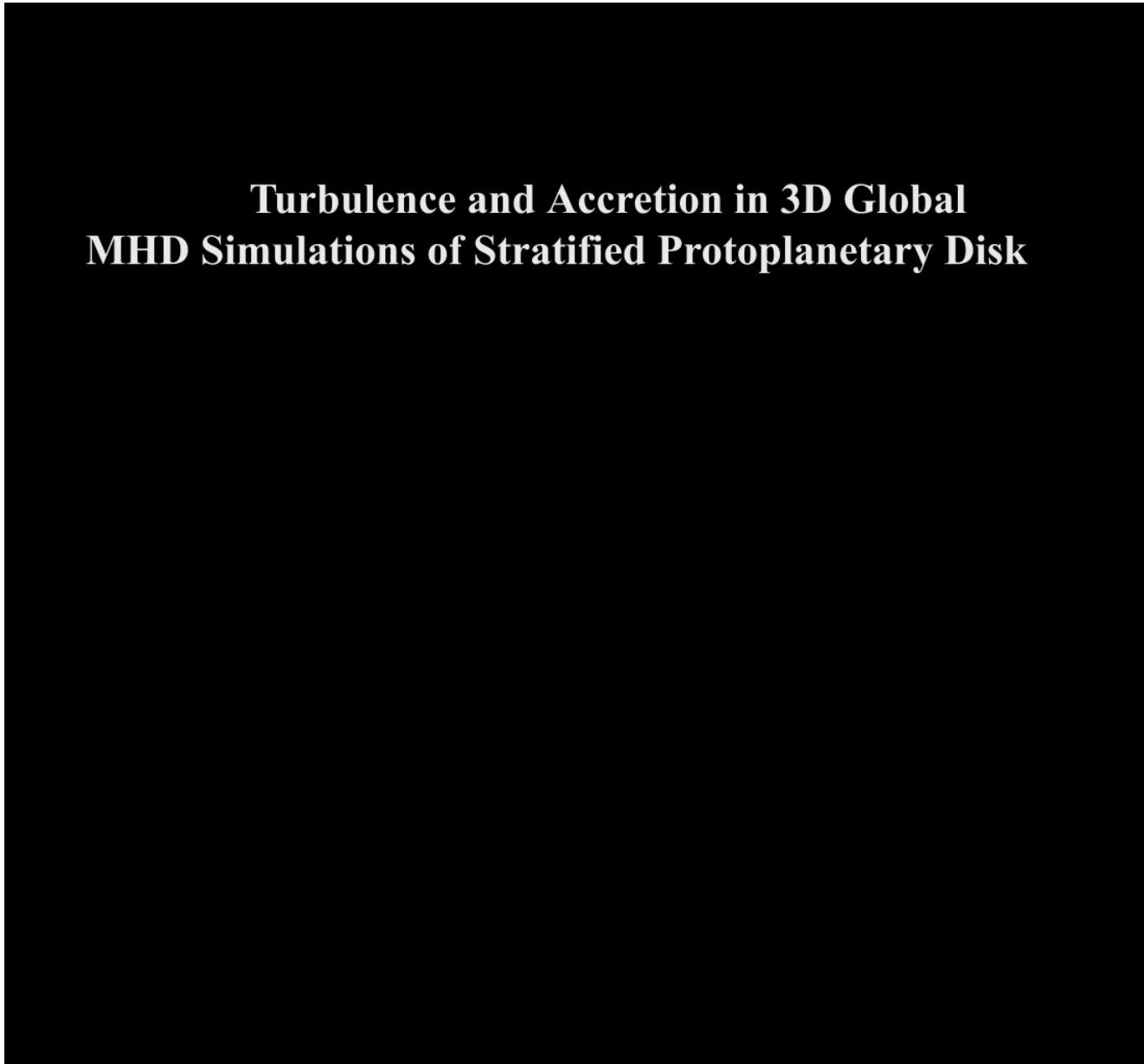
Disk evolution

Gas-rich phase (< 10 Myr)
Primordial Disks

Transition phase (~10 Myr)
Transitional Disks

Gas-poor phase (>10 Myr)
Debris Disks

Magneto-Rotational Instability



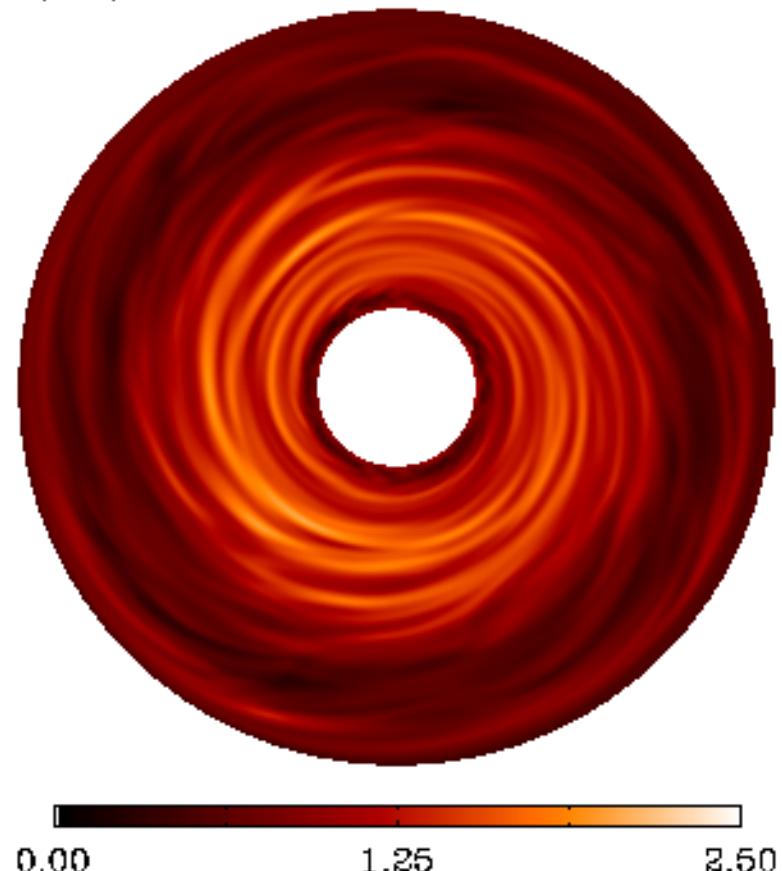
**Turbulence and Accretion in 3D Global
MHD Simulations of Stratified Protoplanetary Disk**

Video credit: Mario Flock (MPIA/CEA)

Accretion in disks occurs via turbulent viscosity

Turbulence in disks is enabled by
the Magneto-Rotational Instability

$t=46.3/88\text{yr}$



Slower
Rotation

Stretching
amplifies
B-field

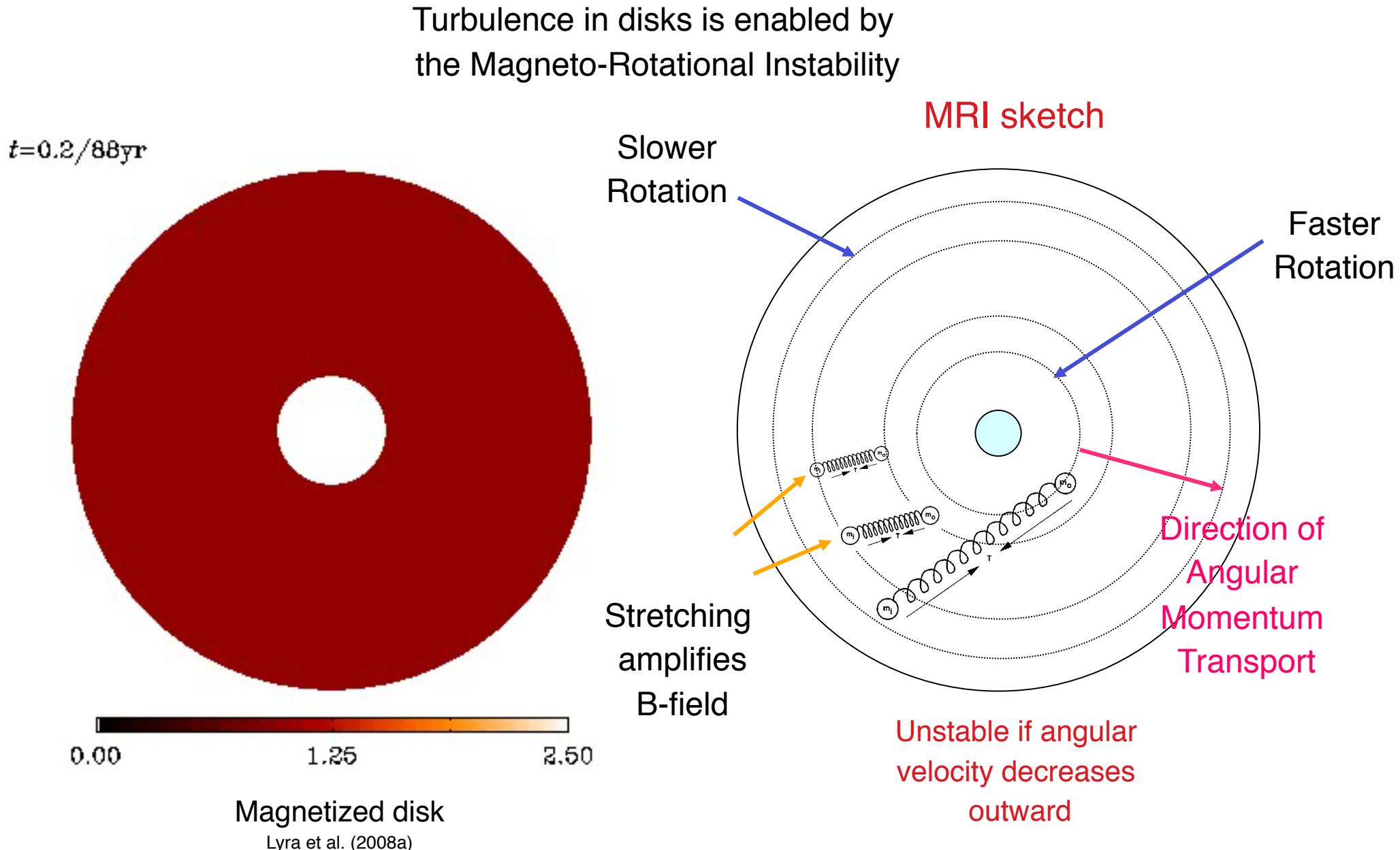
MRI sketch

Unstable if angular
velocity decreases
outward

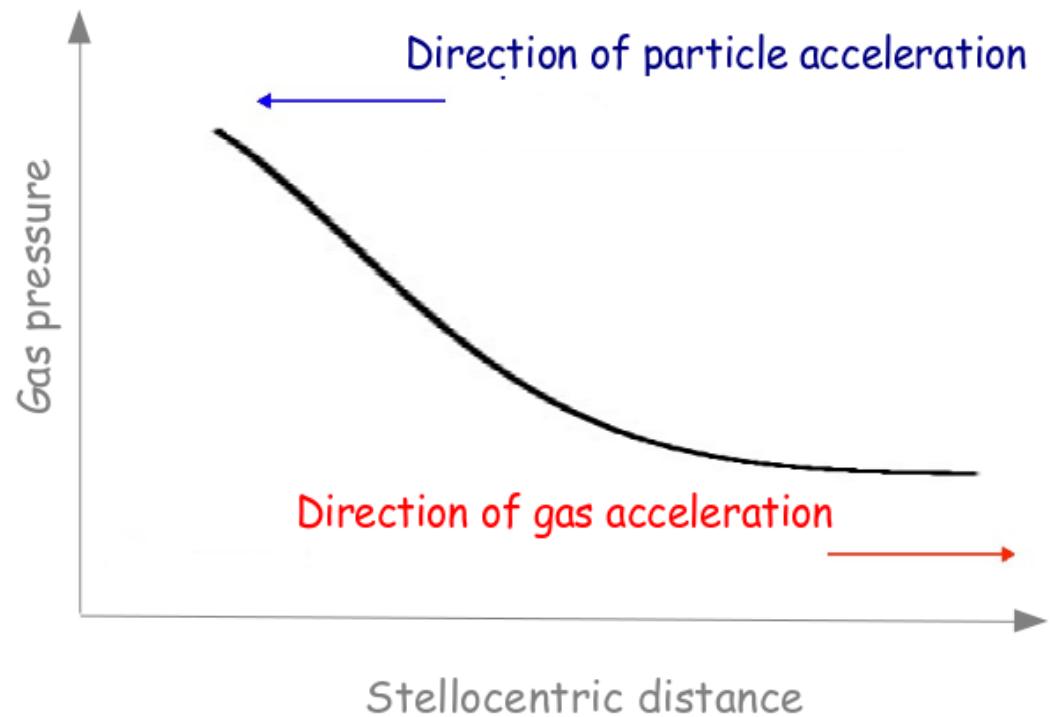
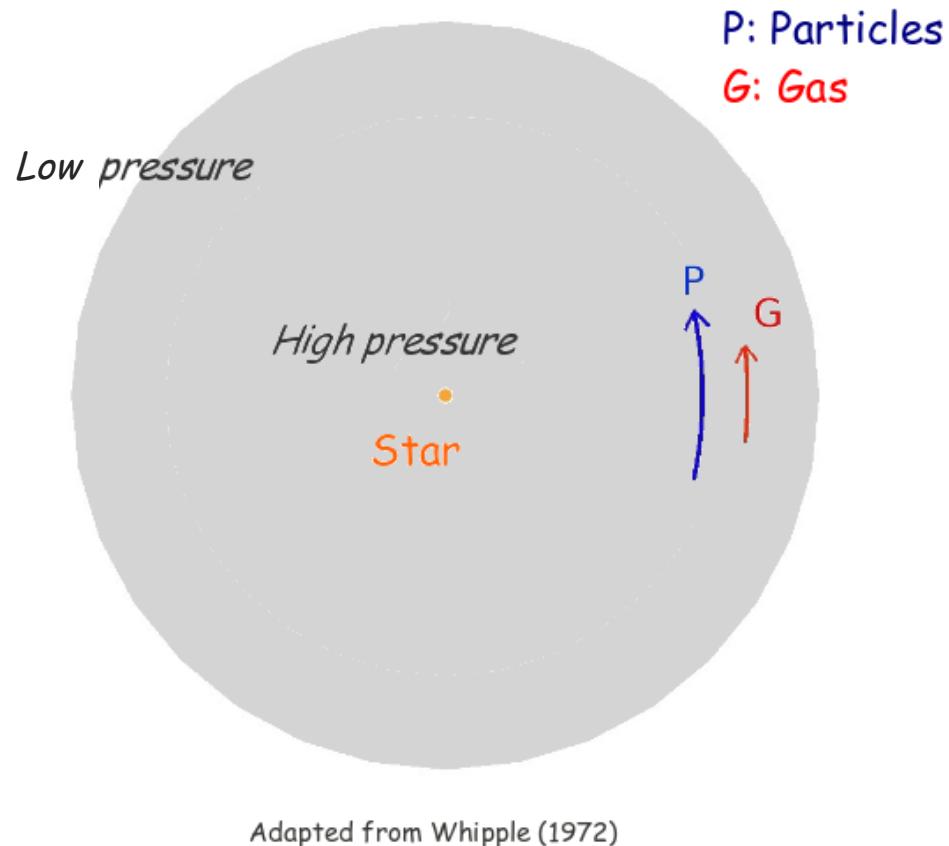
Faster
Rotation

Direction of
Angular
Momentum
Transport

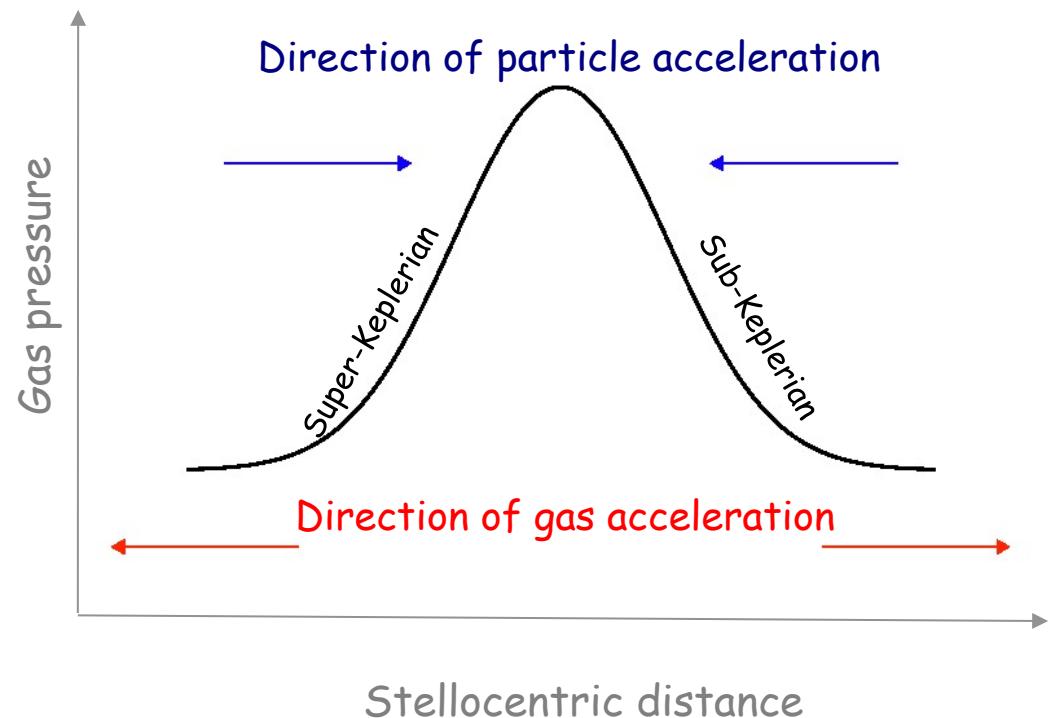
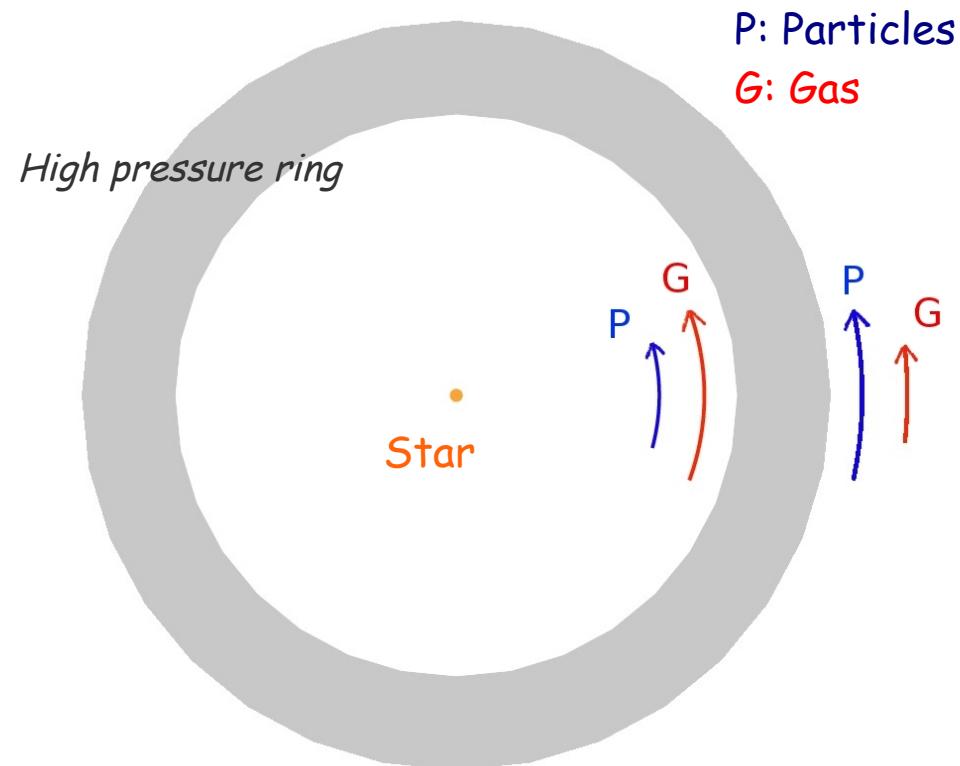
Accretion in disks occurs via turbulent viscosity



Particle drift

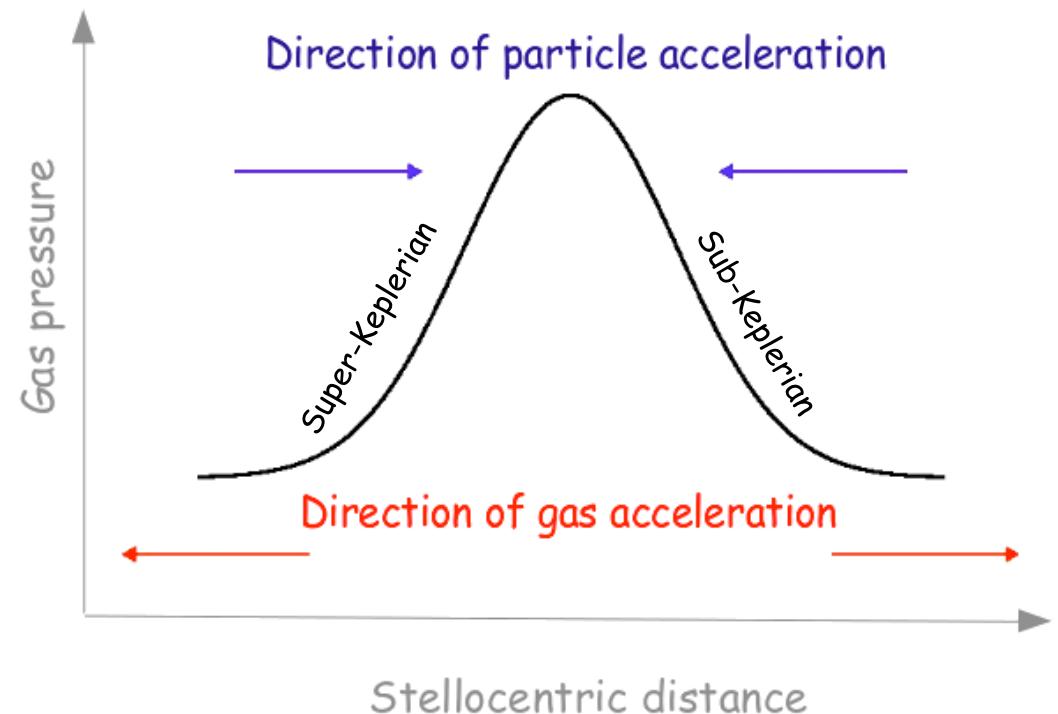
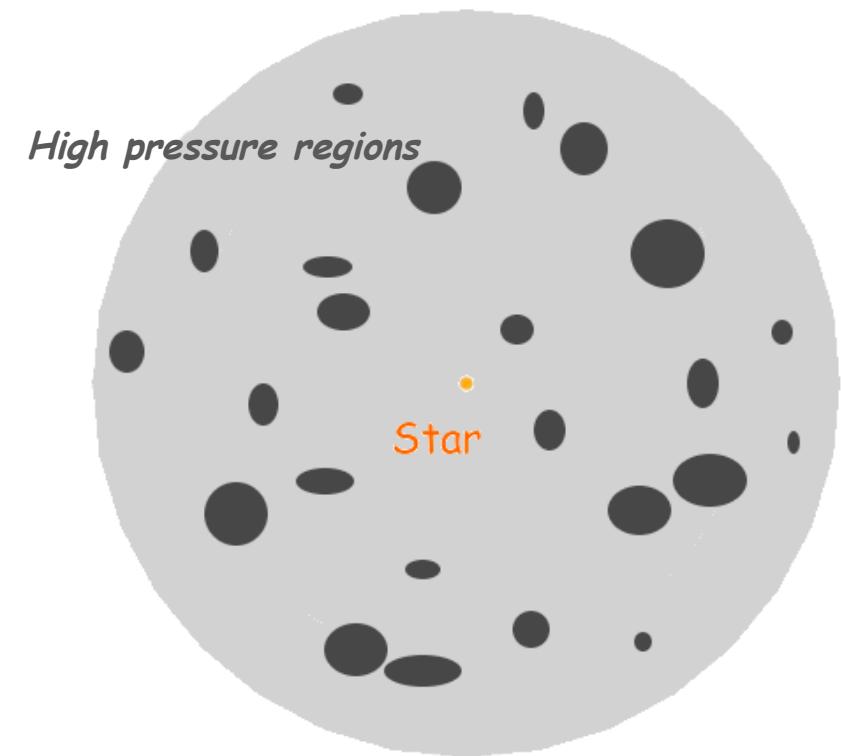


Pressure Trap

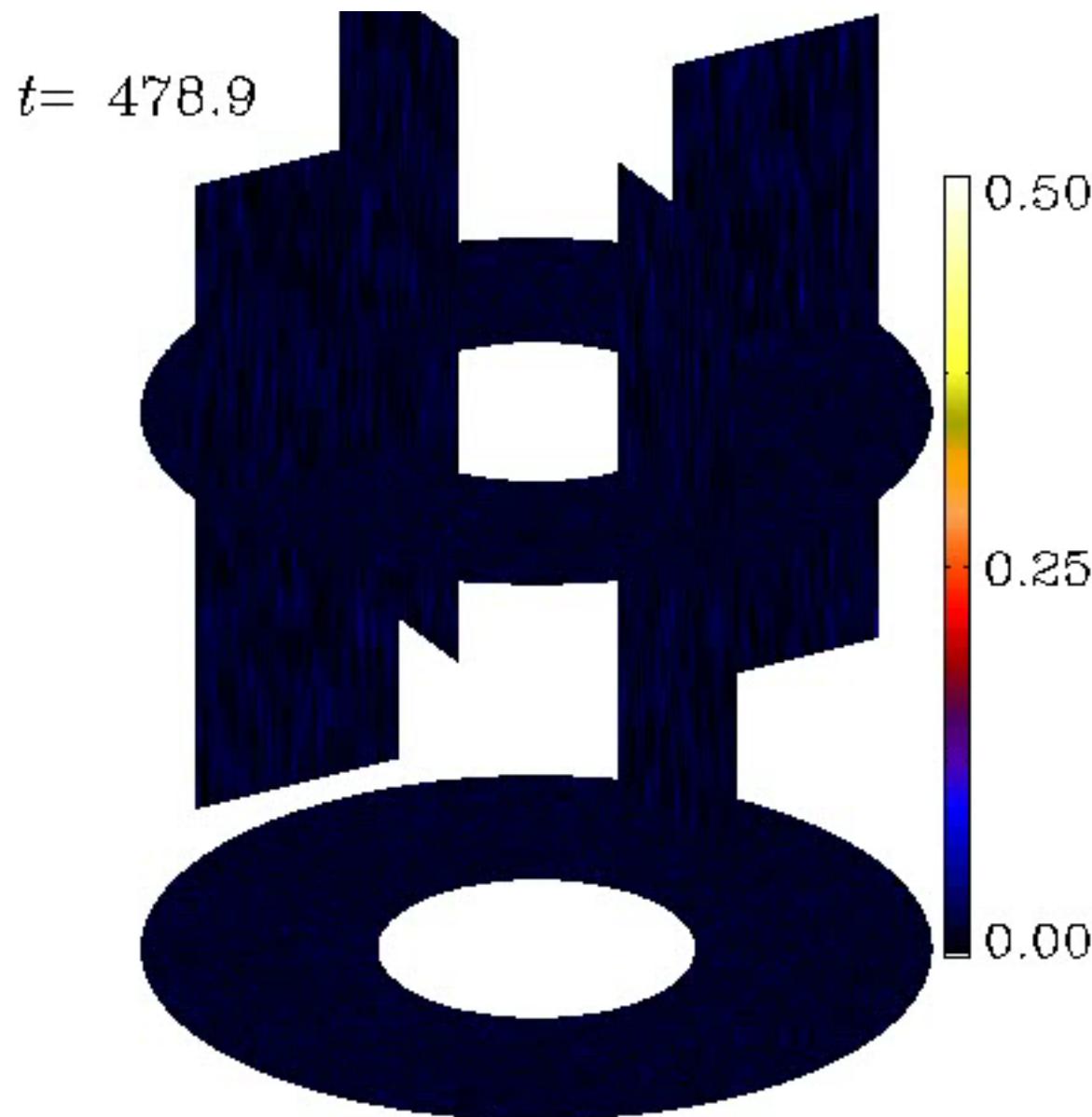


Adapted from Whipple (1972)

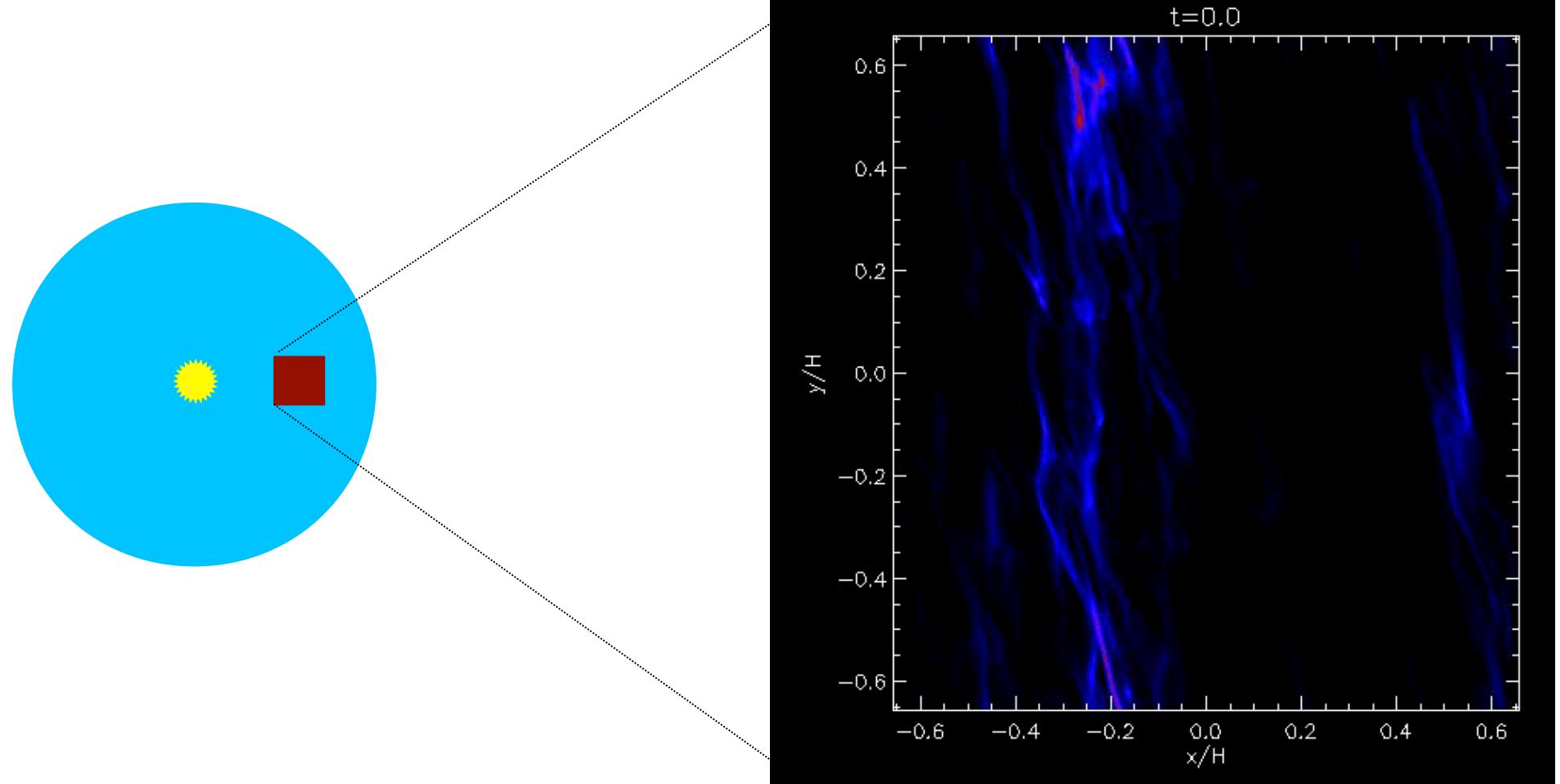
Pressure Trap



Turbulence concentrates solids mechanically in pressure maxima

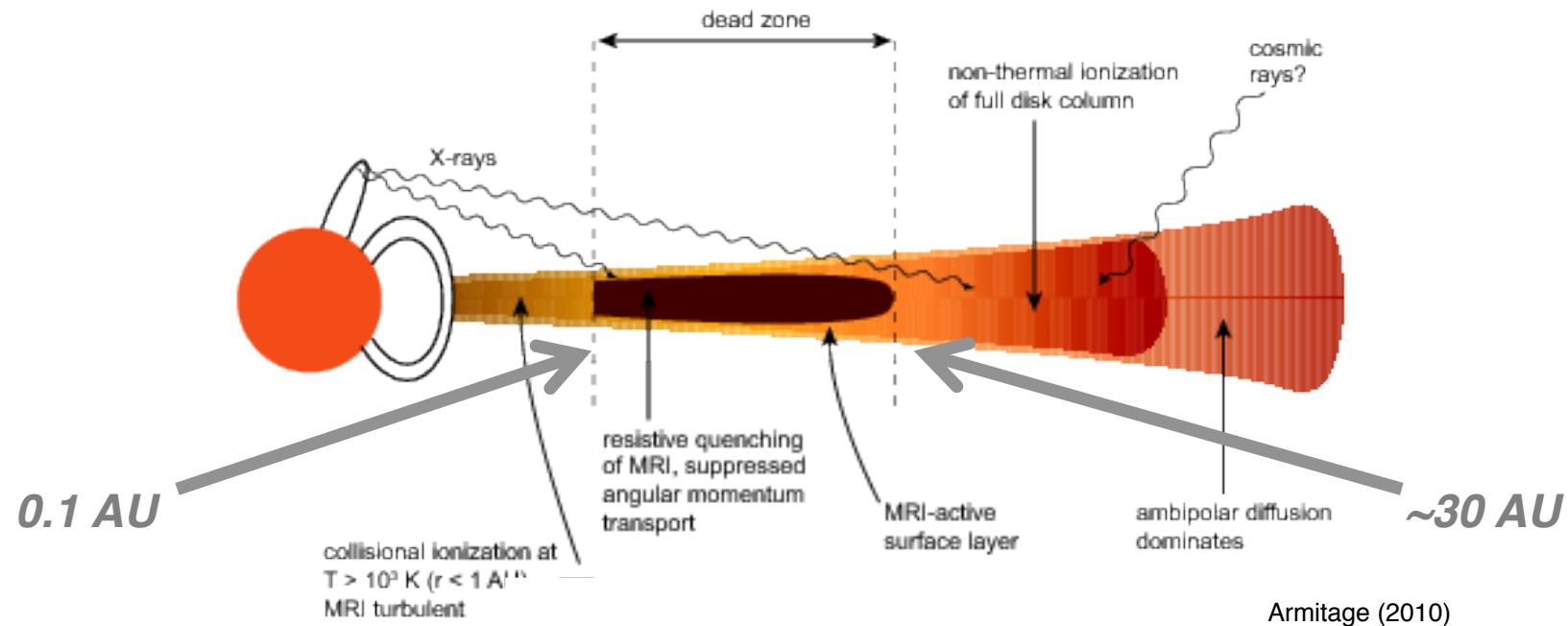


Gravitational collapse into planetesimals



Johansen et al. (2007)

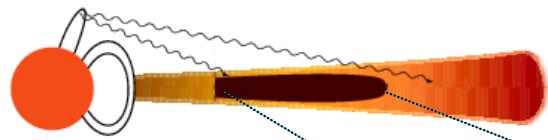
Dead zones are robust features of protoplanetary disks



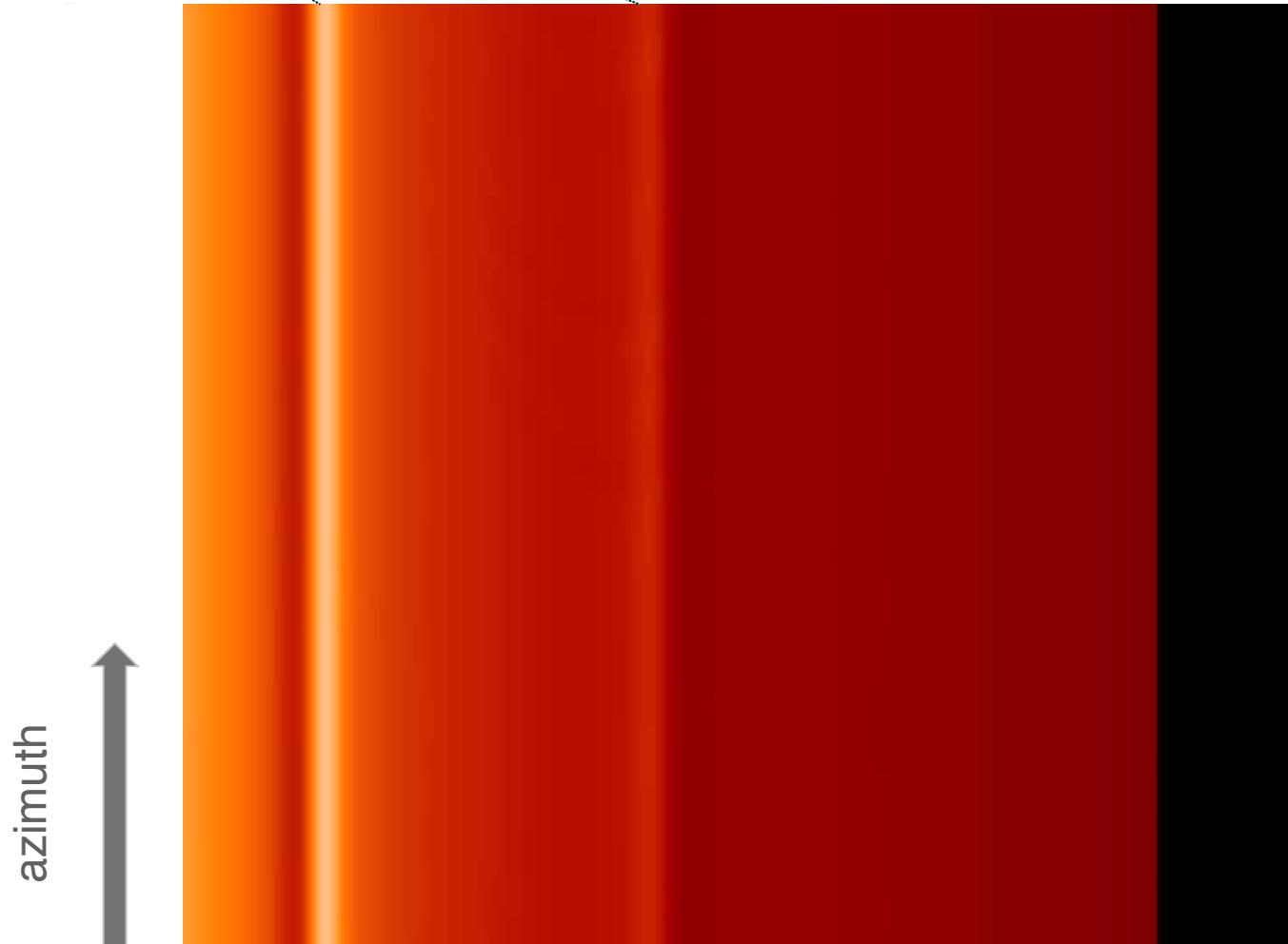
Disks are cold and thus poorly ionized
(Blaes & Balbus 1994)

Therefore, accretion is **layered**
(Gammie 1996)

There should be a **magnetized, active zone**,
and a **non-magnetic, dead zone**.



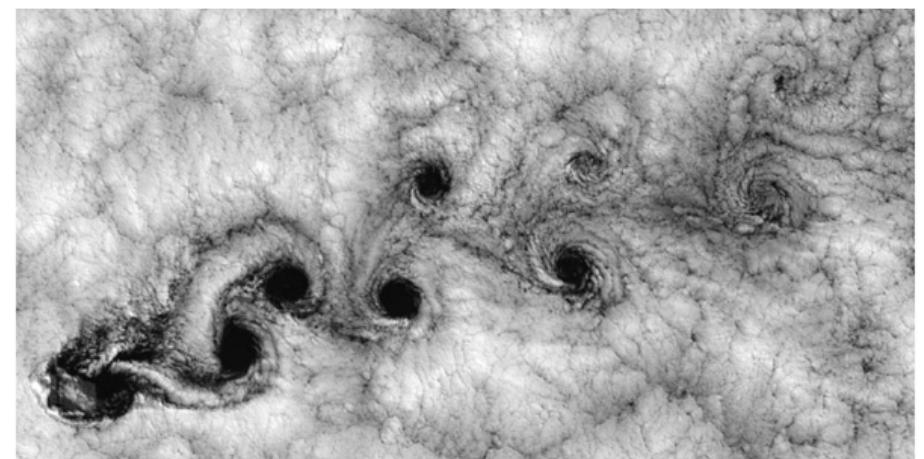
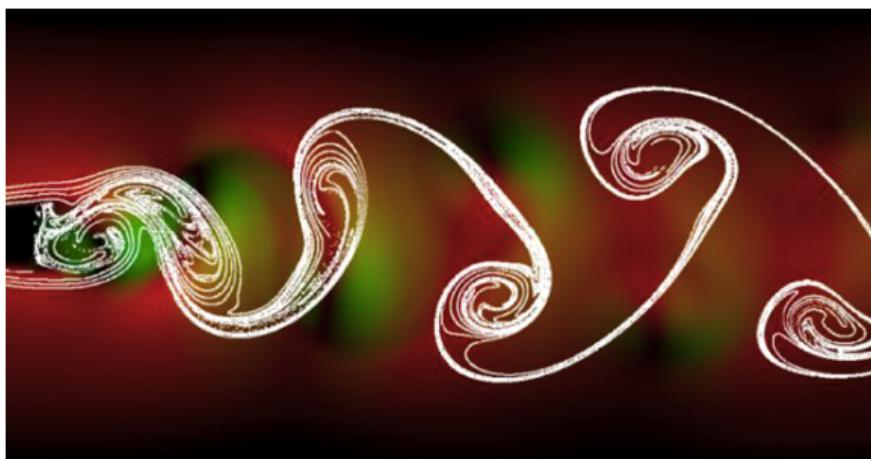
A simple dead zone model



radius

Lyra et al. (2008b, 2009a);
See also Varniere & Tagger (2006)

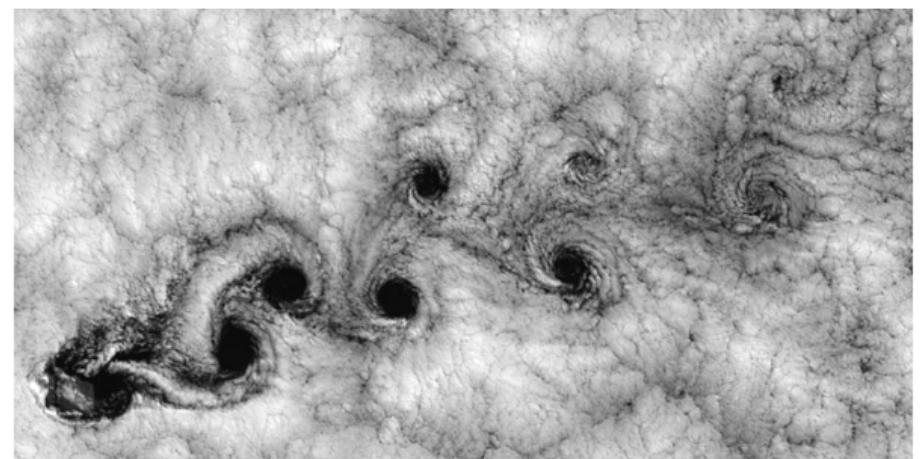
Vortices – an ubiquitous fluid mechanics phenomenon



Vortices – an ubiquitous fluid mechanics phenomenon

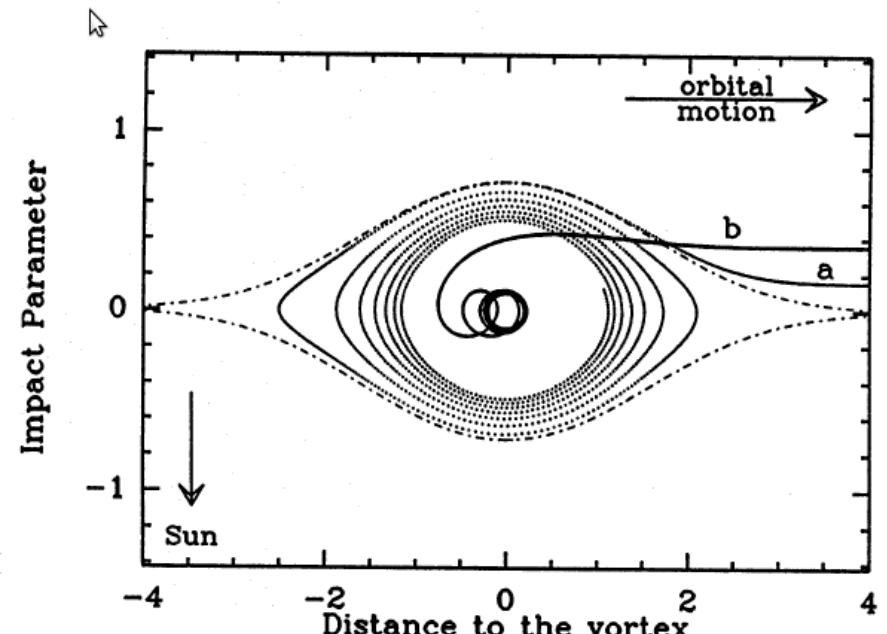
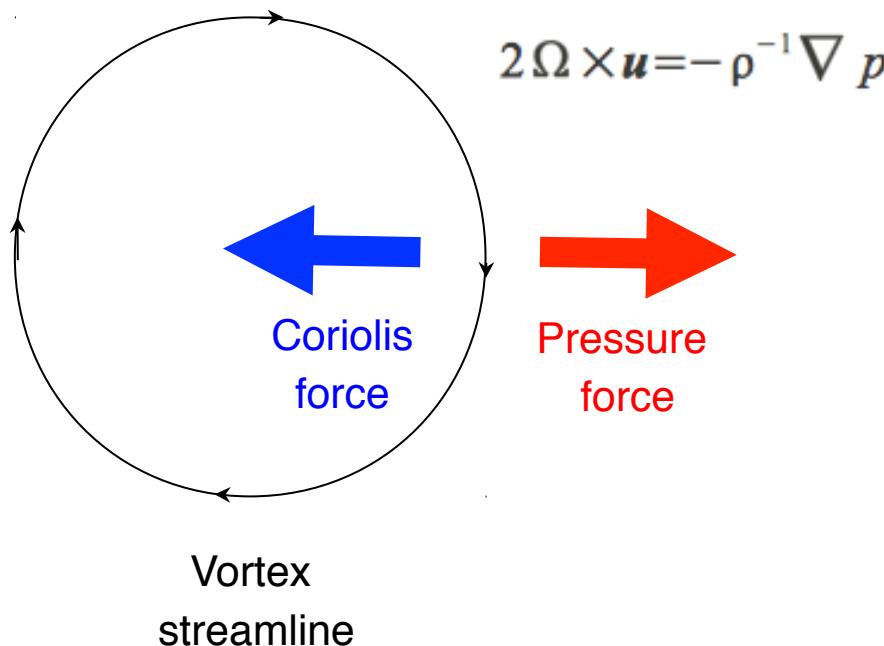


Von Kármán *vortex street*



The Tea-Leaf effect

Geostrophic balance:



Barge & Sommeria (1995)

Particles do not feel the pressure gradient.
They sink towards the center, where they accumulate.

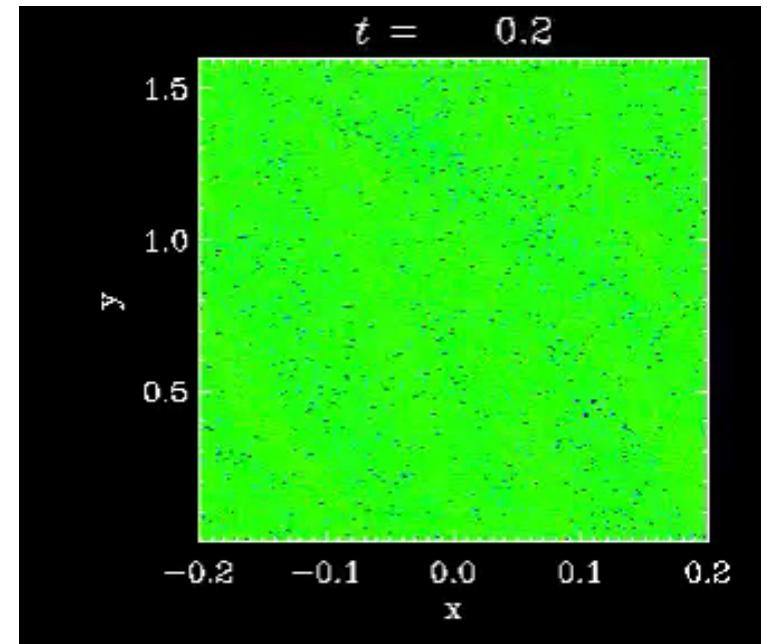
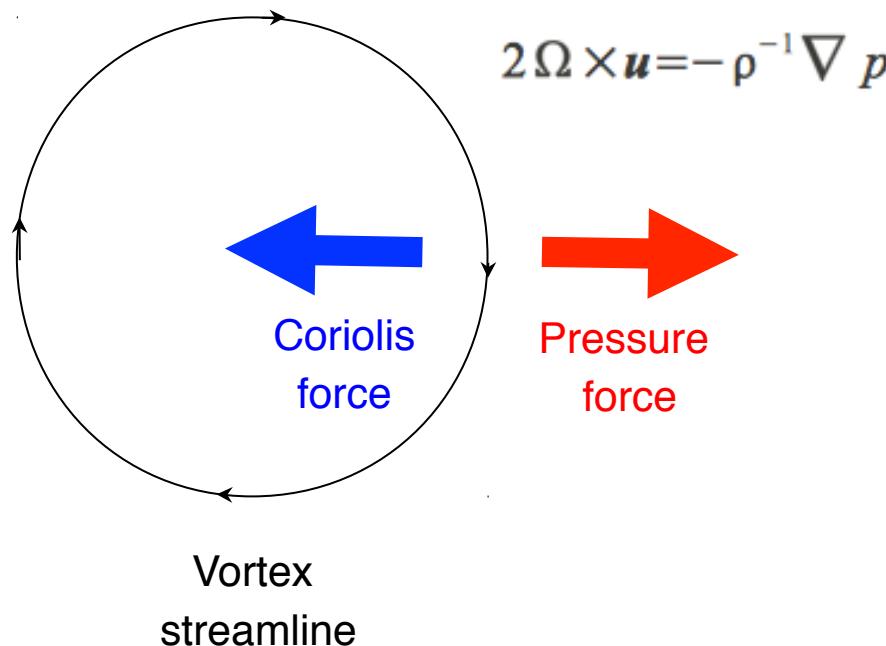
Aid to planet formation

(Barge & Sommeria 1995, Adams & Watkins 1996, Tanga et al. 1996)

Speed up planet formation enormously
(Lyra et al. 2008b, 2009ab, Raettig et al. 2012)

The Tea-Leaf effect

Geostrophic balance:



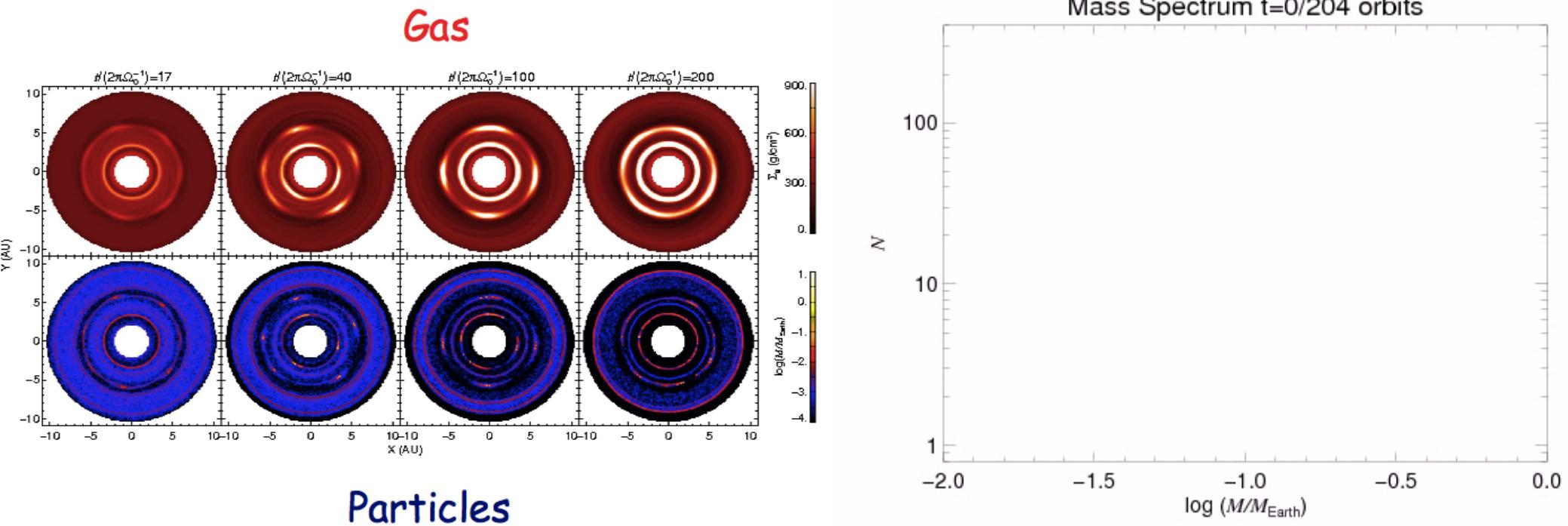
Raettig et al. (2012)

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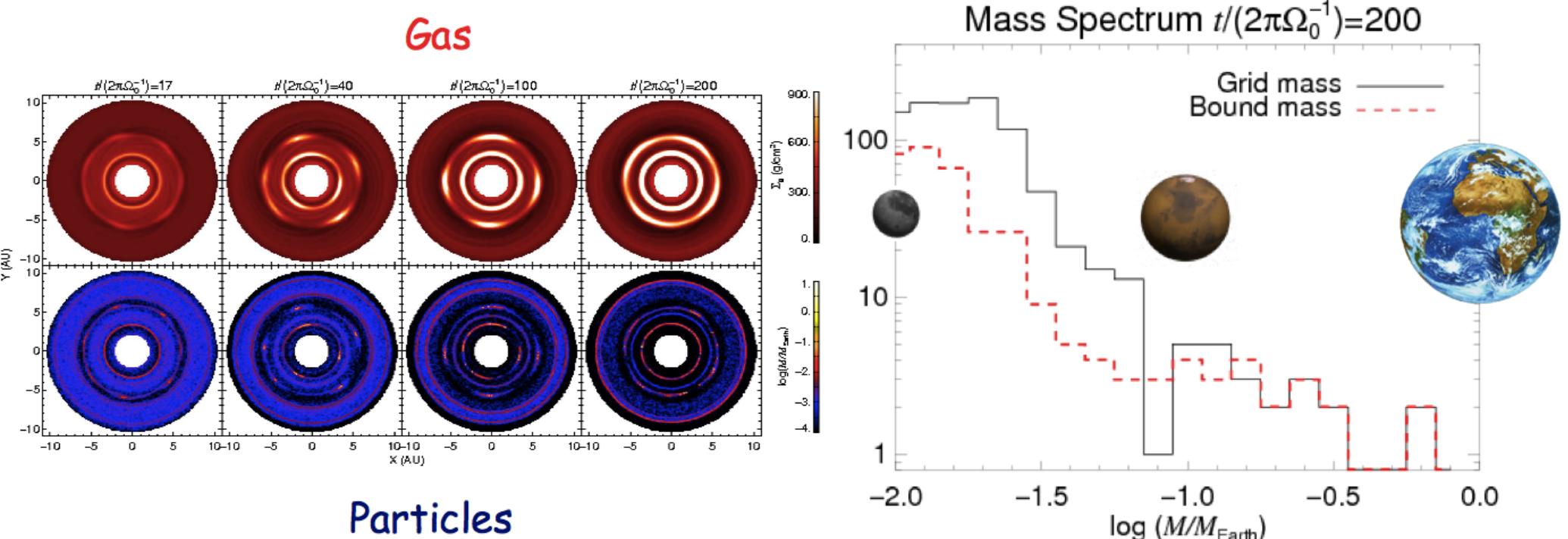
Vortices and Planet Formation



Collapse into Mars mass objects

(Lyra et al. 2008b, 2009a,
see also Lambrechts & Johansen 2012)

Vortices and Planet Formation

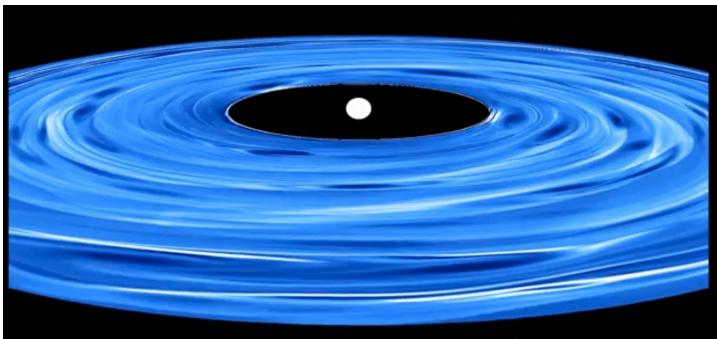


Collapse into Mars mass objects

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see also Lambrechts & Johansen 2012)

Sustaining vortices in disks

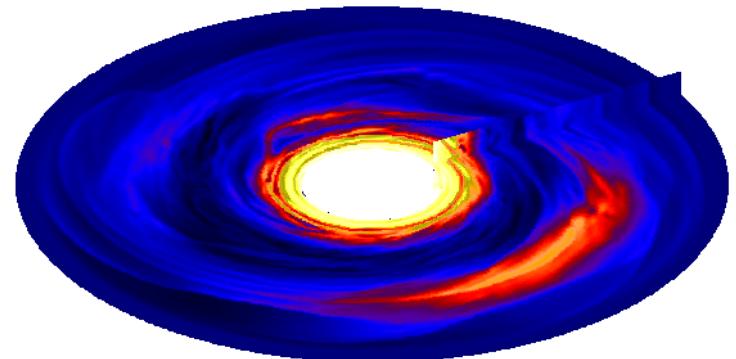
Baroclinic instability (*Convective overstability*)



Klahr & Bodenheimer (2003), Klahr (2004),
Johnson & Gammie (2005), Petersen et al. (2007ab),
Lesur & Papaloizou (2010), Lyra & Klahr (2011), Raettig et al. (2013)
Klahr & Hubbard (2014), Lyra (2014)

Powered by:
Buoyancy, thermal diffusion
(baroclinic source term)

Rossby wave instability

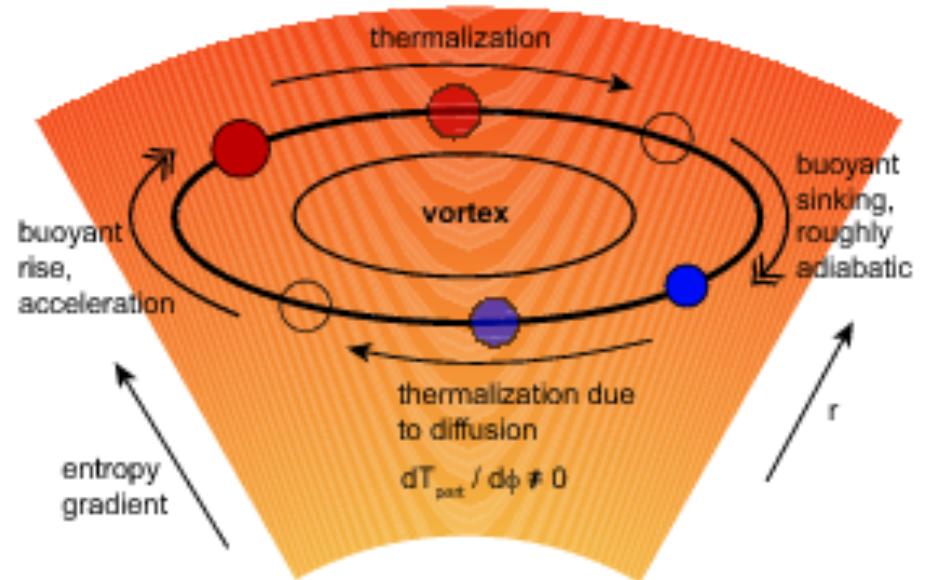


Lovelace & Hohlfield (1978), Toomre (1981), Papaloizou & Pringle (1984, 1985), Hawley et al. (1987), Lovelace et al. (1999), Li et al. (2000, 2011), Tagger (2001), Varniere & Tagger (2006), de Val-Borro et al. (2007), Lyra et al. (2008b, 2009ab), Mehuet et al. (2010, 2012abc), Lin & Papaloizou (2011ab, 2012), Lyra & Mac Low (2012), Regaly et al. (2012, 2013), Lin (2012ab, 2013), Ataiee et al. (2013, 2014), Lyra et al. (2014)

Powered by:
Modification of shear profile
(external vorticity reservoir)

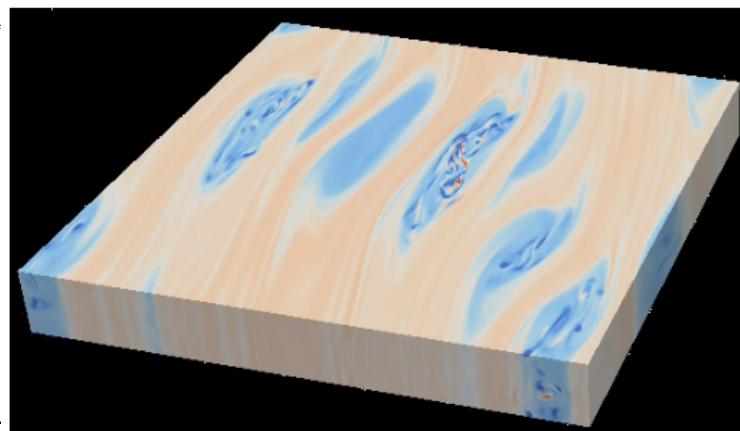
Baroclinic Instability – Excitation and self-sustenance of vortices

Sketch of the
Baroclinic Instability

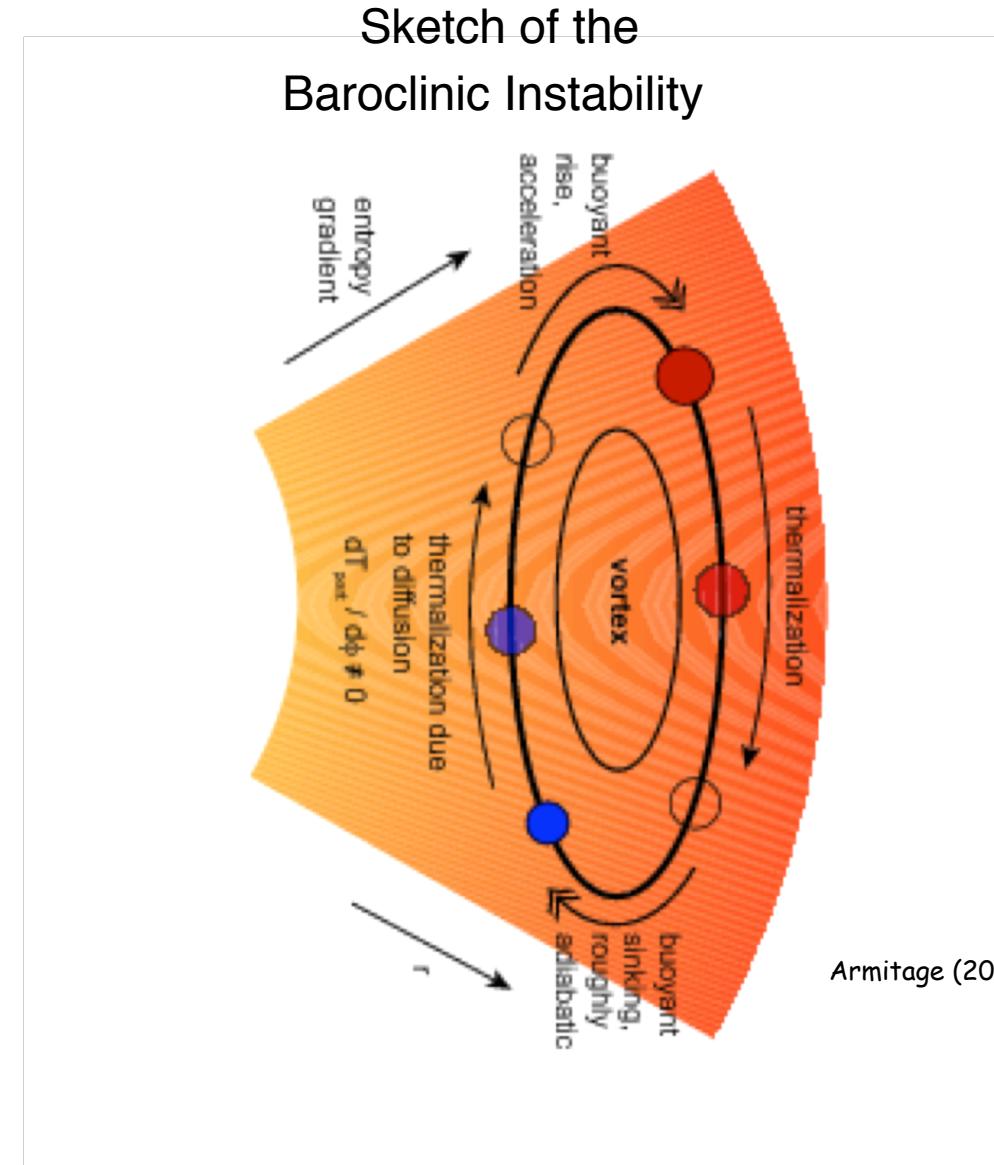
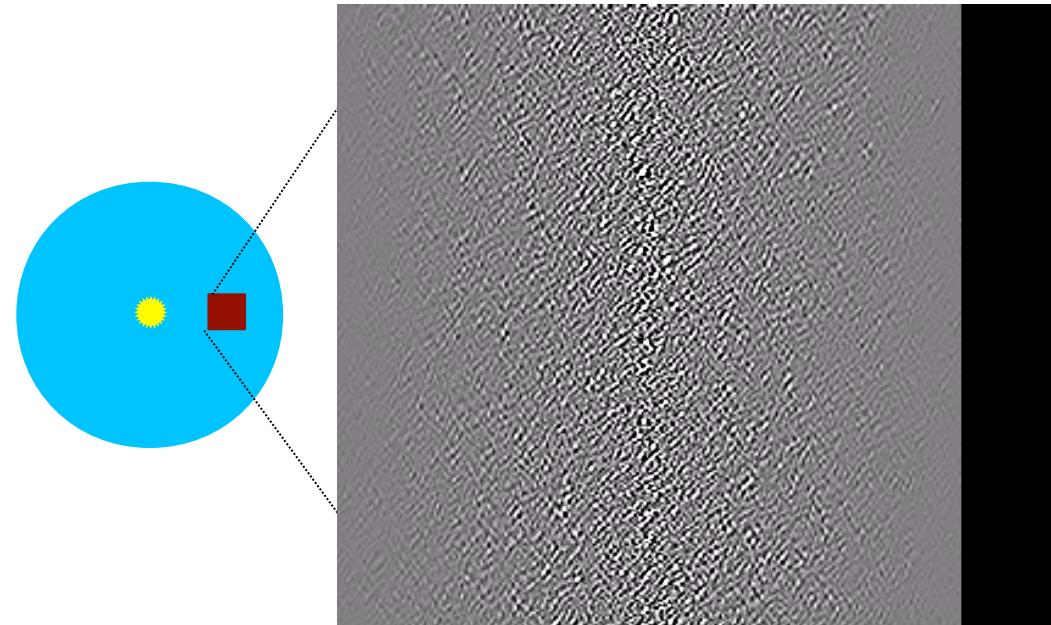


Lesur & Papaloizou (2010)

Armitage (2010)

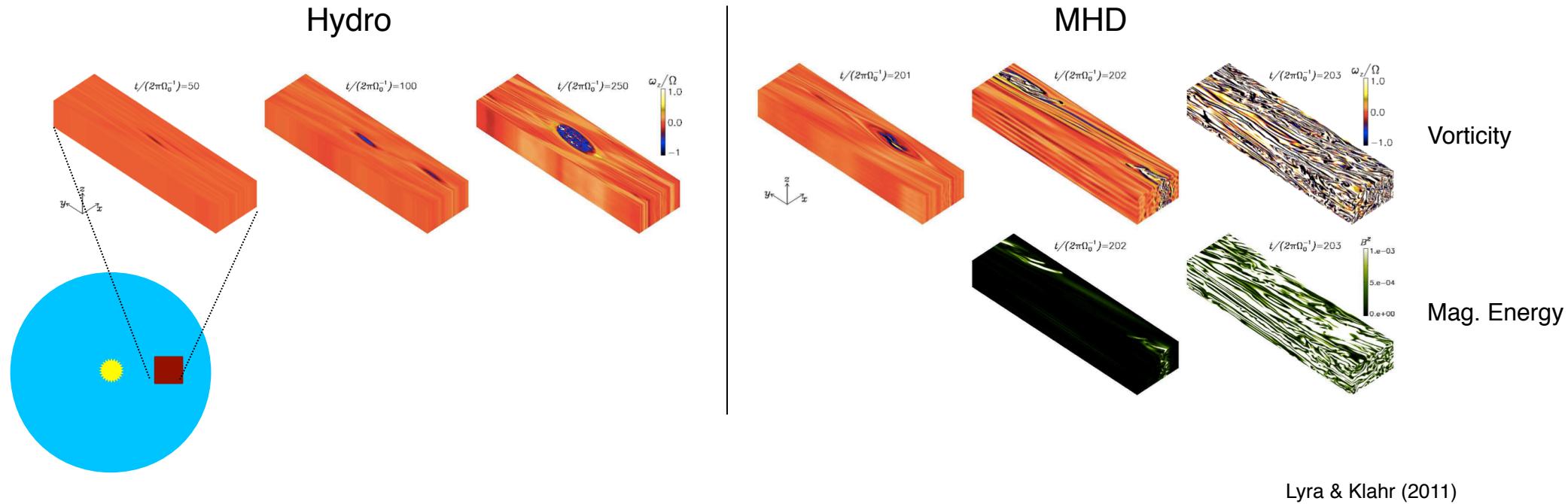


Baroclinic Instability – Excitation and self-sustenance of vortices



Baroclinic instability and layered accretion

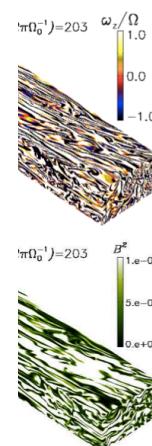
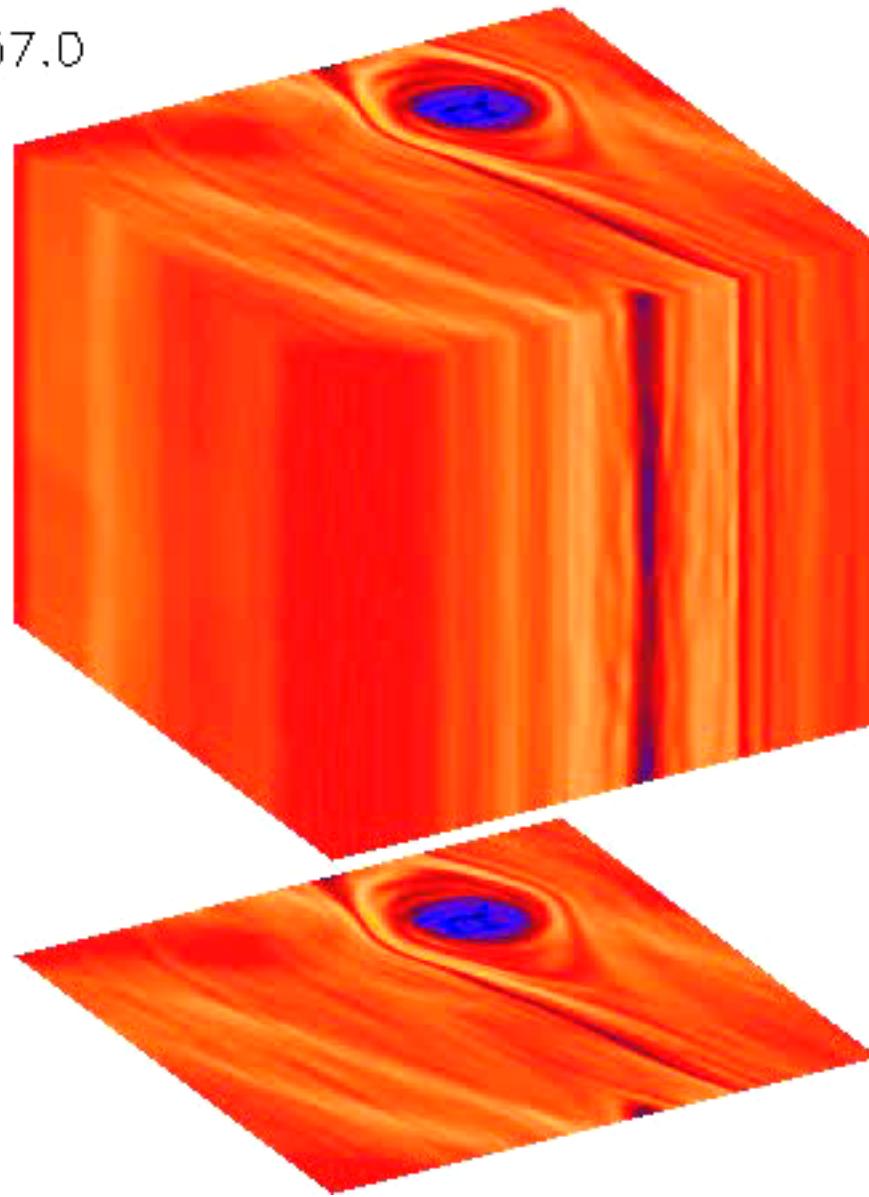
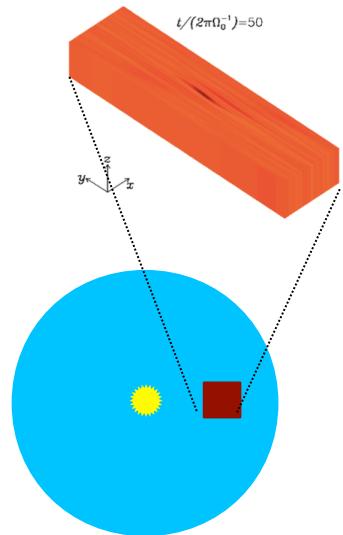
What happens when the vortex is magnetized?



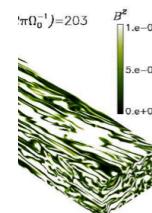
Lyra & Klahr (2011)

Baroclinic instability and layered accretion

$t=1257.0$



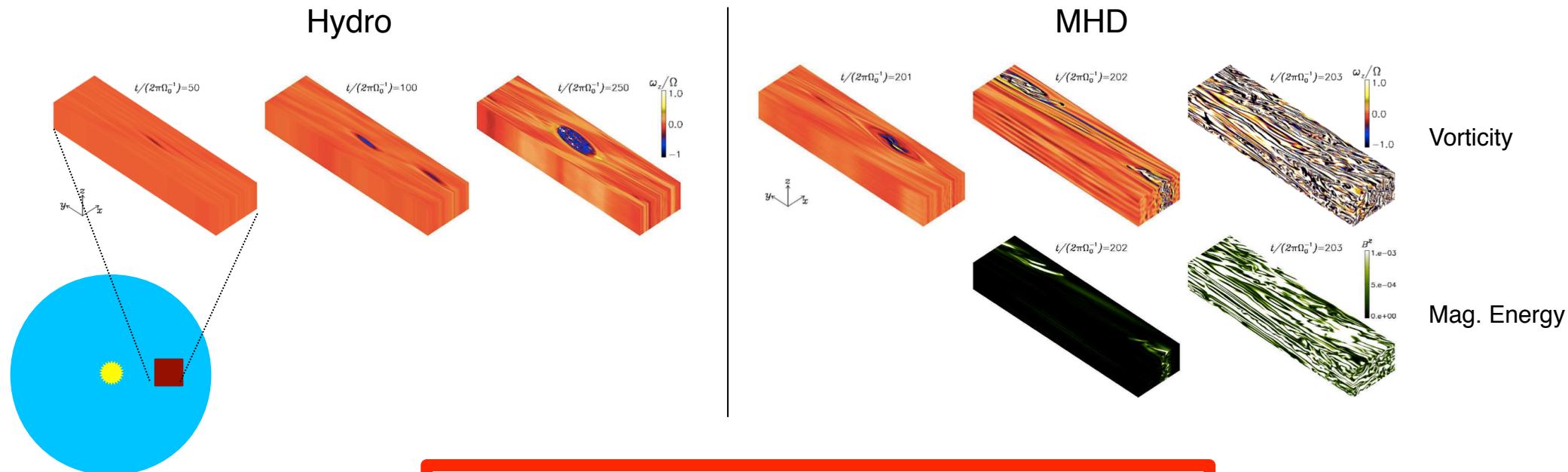
Vorticity



Mag. Energy

Baroclinic instability and layered accretion

What happens when the vortex is magnetized?



Baroclinic vortices
do **not** survive magnetization

Lyra & Klahr (2011)

The “Baroclinic Instability” is LINEAR (Convective Overstability)

Klahr & Hubbard (2014), Lyra (2014)

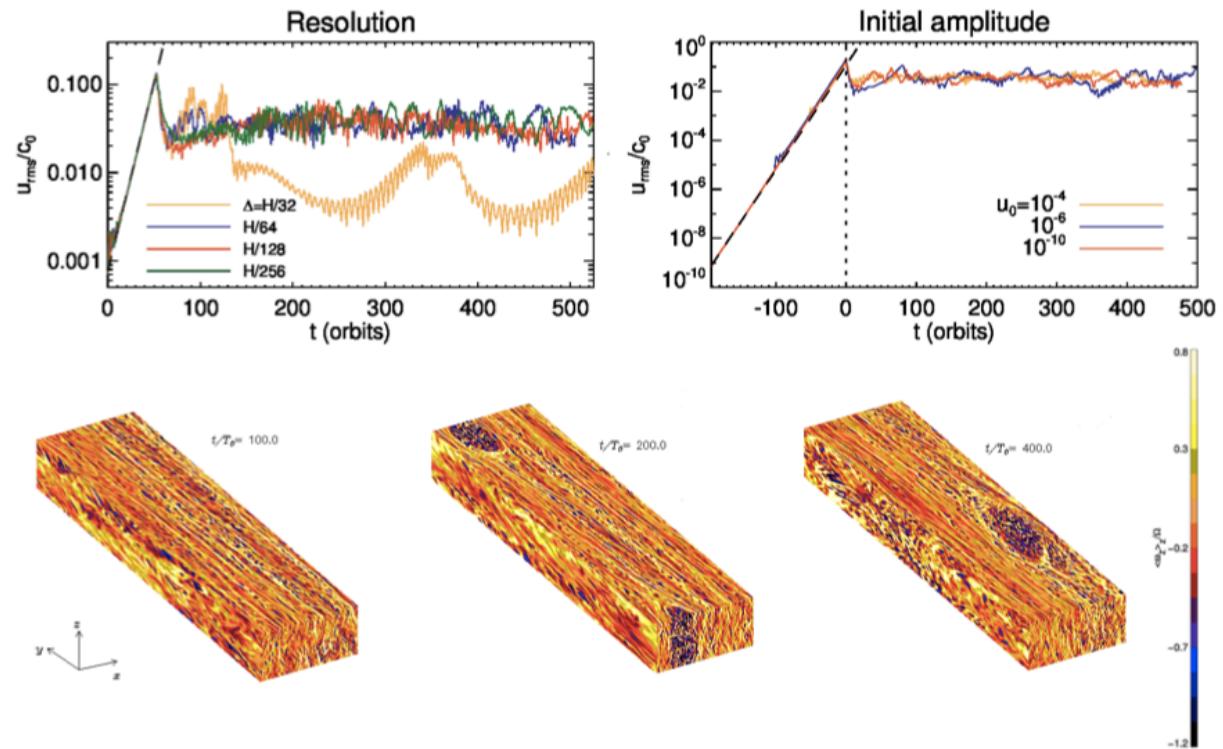
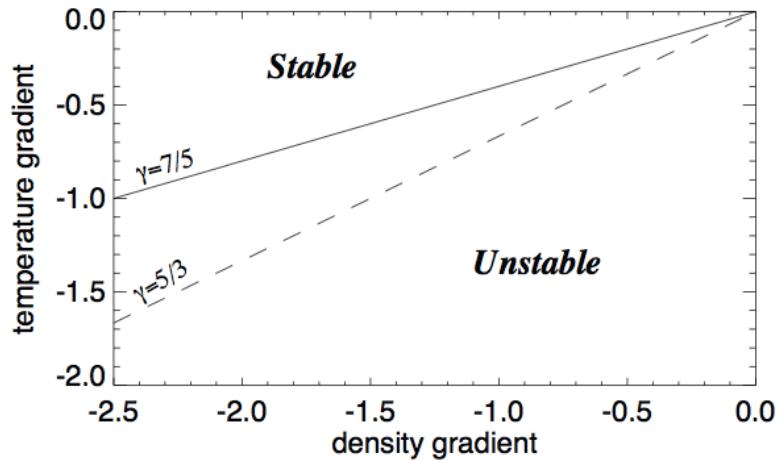
$$\begin{aligned}\frac{\partial \rho}{\partial t} + (\mathbf{u} \cdot \nabla) \rho &= -\rho \nabla \cdot \mathbf{u}, \\ \frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} &= -\frac{1}{\rho} \nabla p + \mathbf{g}, \\ \frac{\partial p}{\partial t} + (\mathbf{u} \cdot \nabla) p &= -\gamma p \nabla \cdot \mathbf{u} - \frac{p}{T} \frac{(T - T_0)}{\tau},\end{aligned}$$

$$\bar{\omega}^3 + i\zeta\bar{\omega}^2 - \bar{\omega}\mu^2(\kappa^2 + N^2) - i\zeta\kappa^2\mu^2 = 0,$$

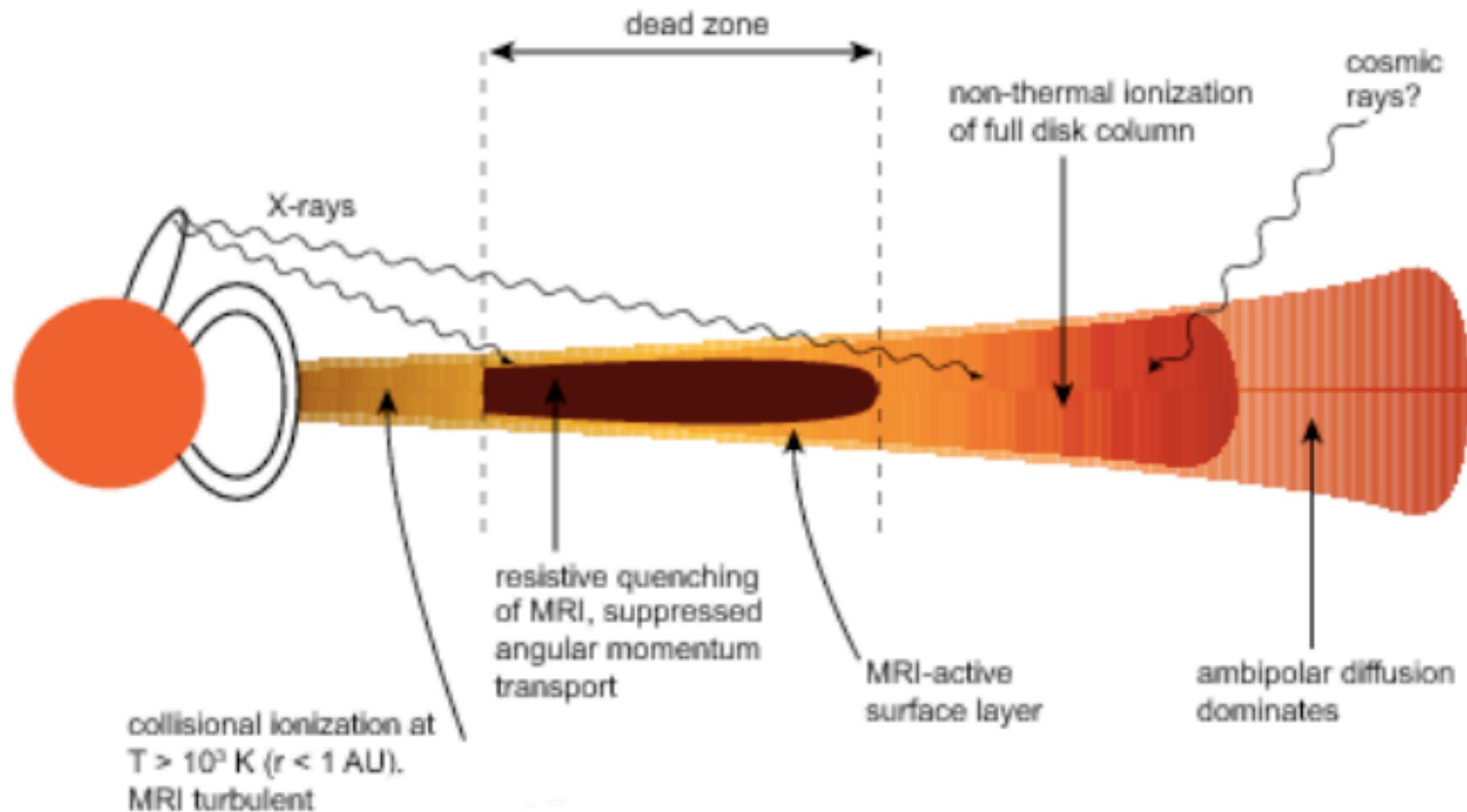
$$\zeta = 1/\gamma\tau \quad \mu^2 = k_z^2/k^2.$$

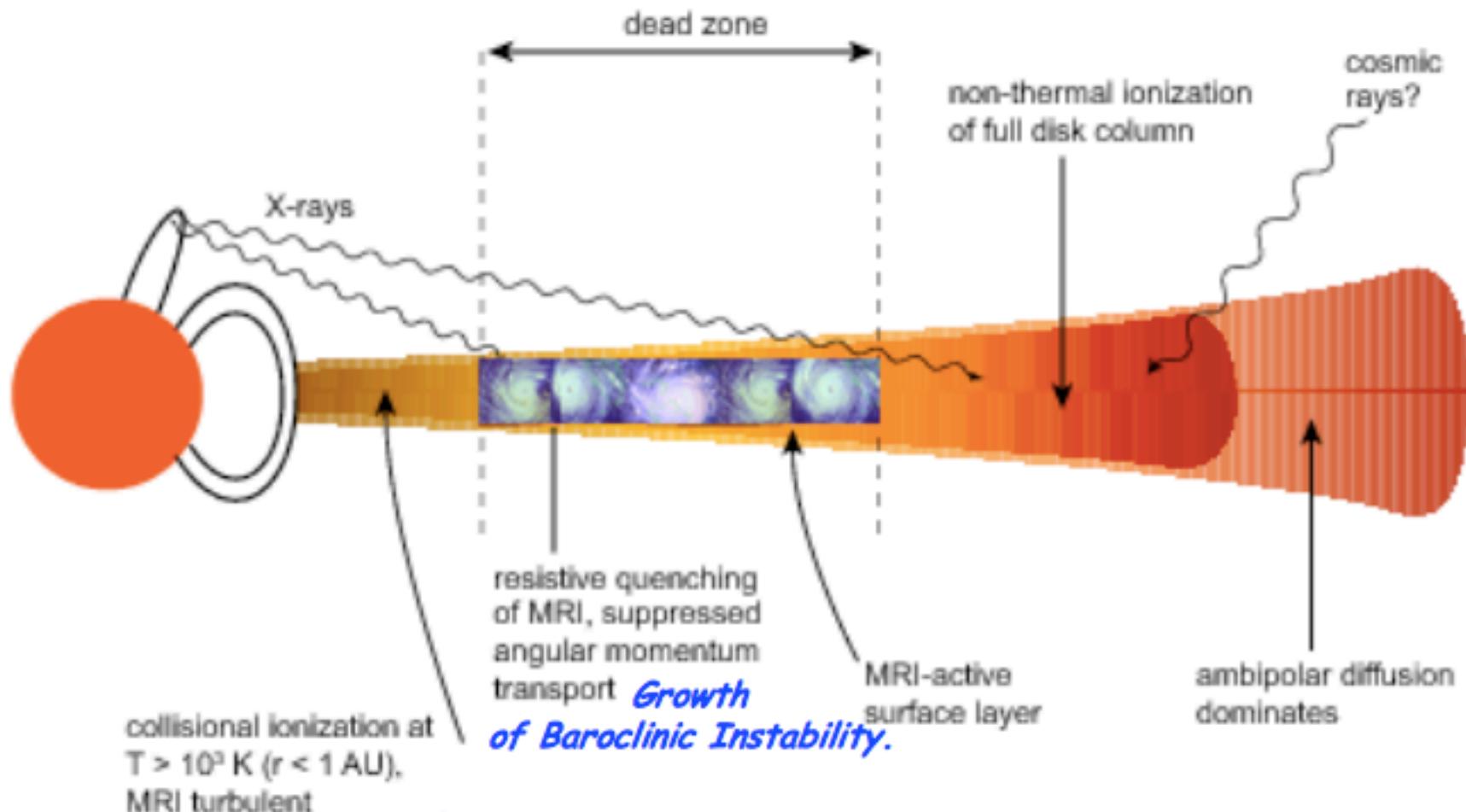
$$\tau_{\max} = \frac{1}{\gamma} \left| \frac{k}{k_z} \right| \frac{1}{\sqrt{\kappa^2 + N^2}}$$

$$\sigma_{\max} = -\frac{1}{4} \left| \frac{k_z}{k} \right| \frac{N^2}{\sqrt{\kappa^2 + N^2}}$$



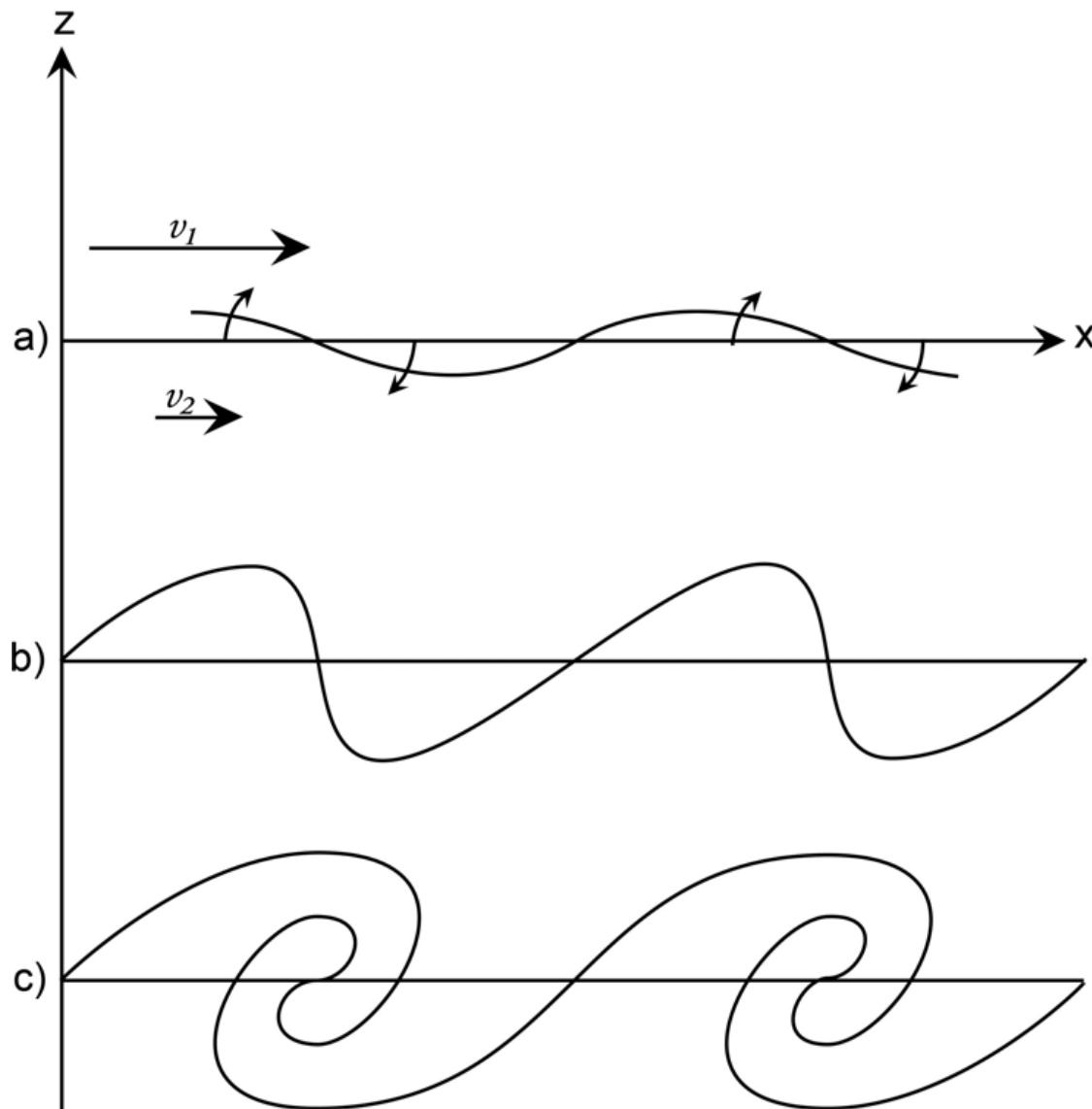
Lyra (2014)





Rossby Wave Instability

(or... Kelvin-Helmholtz in rotating disks)

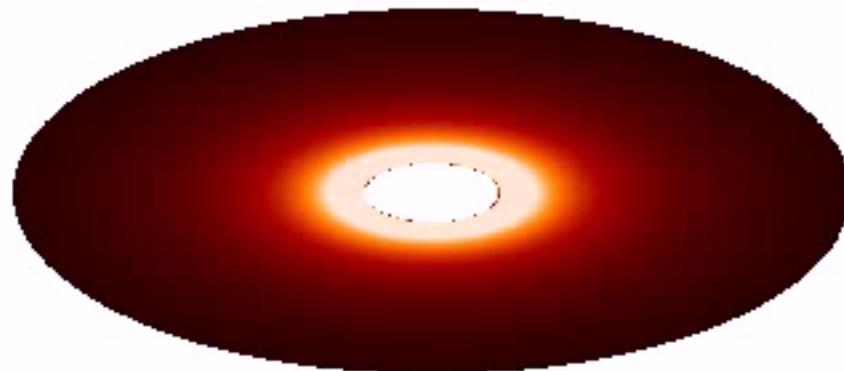
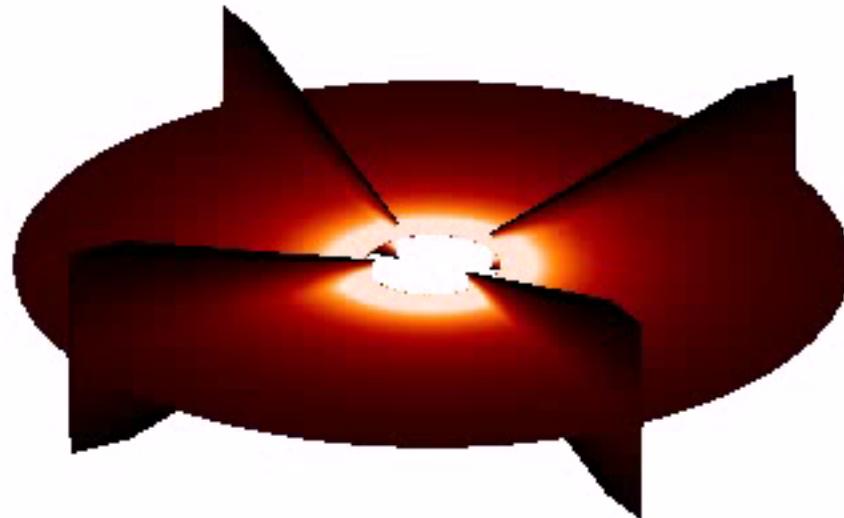


© Brooks Martner

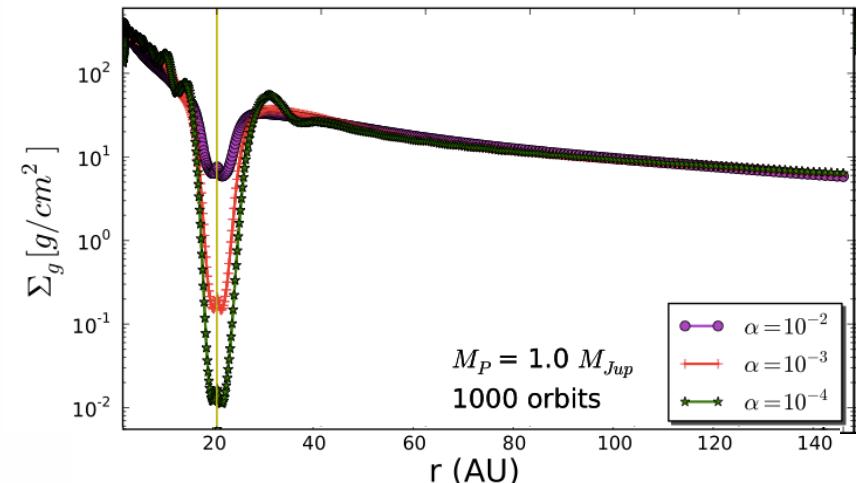
Planetary gap RWI

(de Val-Borro et al. 2006, 2007)

$t = 0.1$



Lyra (2009)



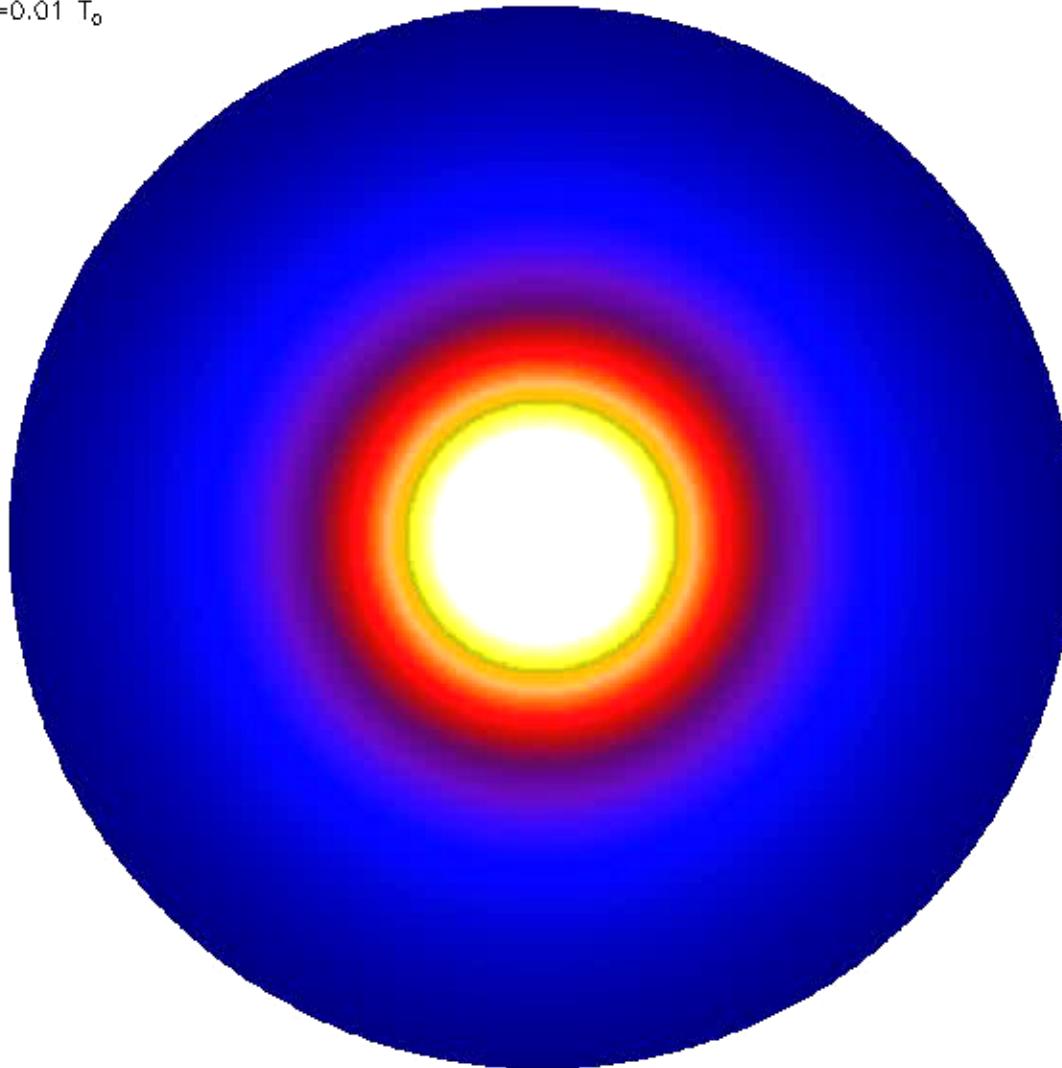
Pinilla et al. (2012)

Planet tides carve gap

Gap walls are unstable to
Kelvin-Helmholtz instability

Active/dead zone boundary

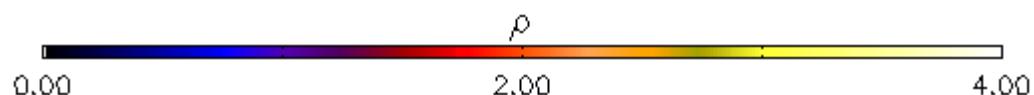
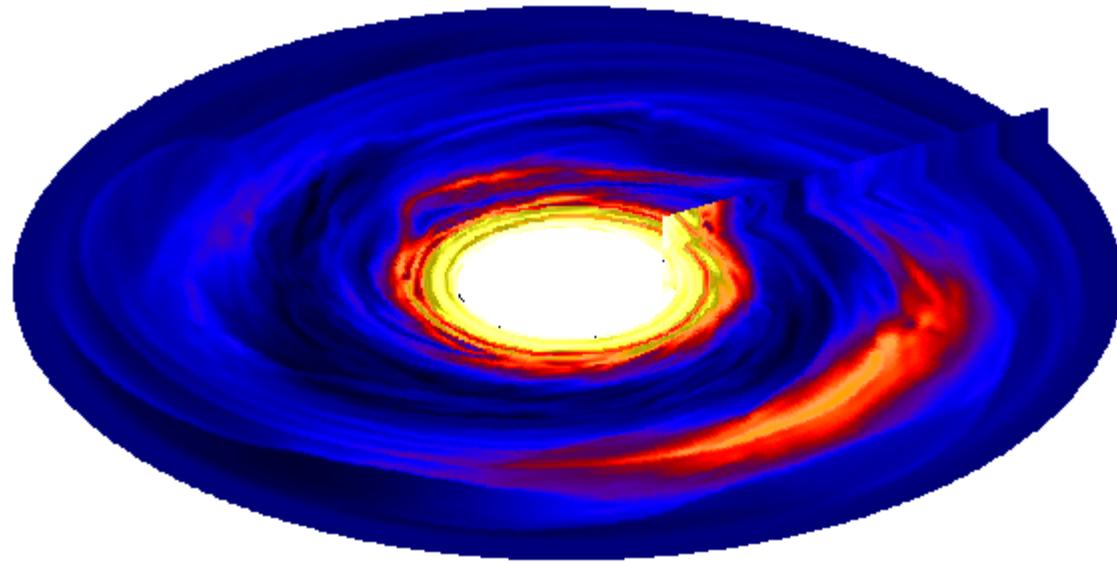
$t=0.01 T_0$



Magnetized inner disk + resistive outer disk
Lyra & Mac Low (2012)

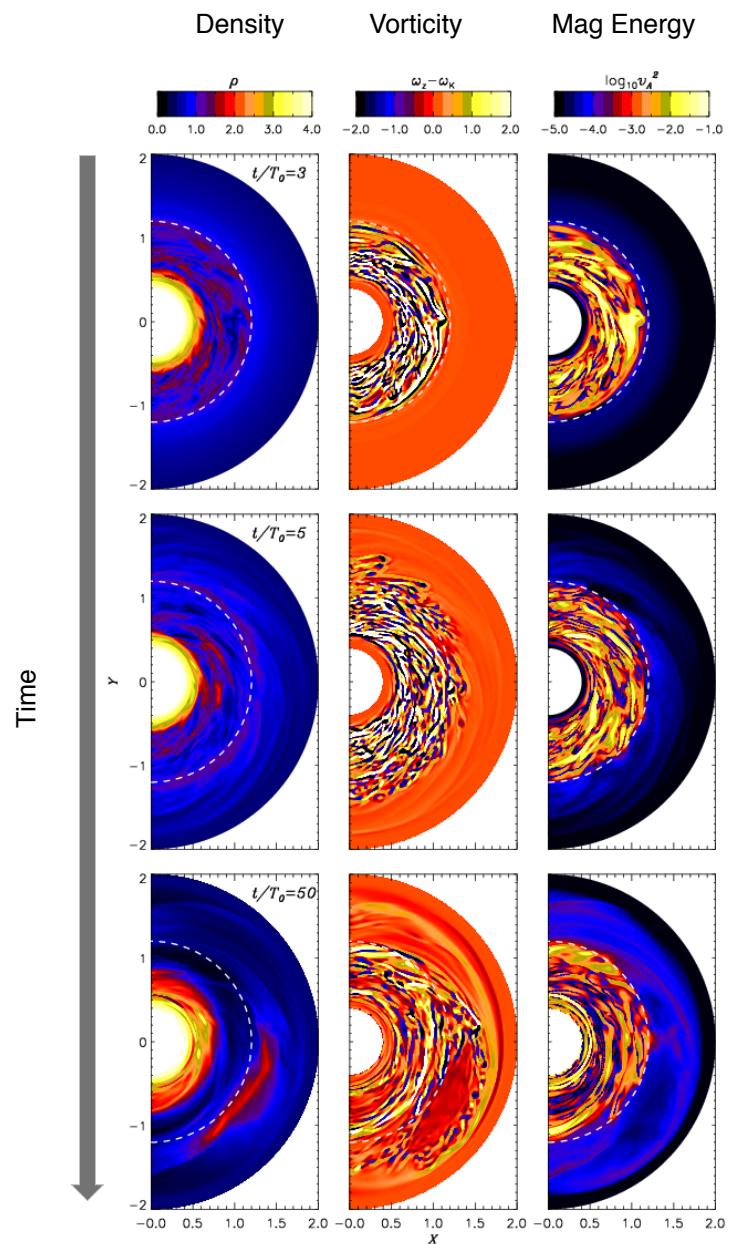
Active/dead zone boundary

$t=22.28 T_0$



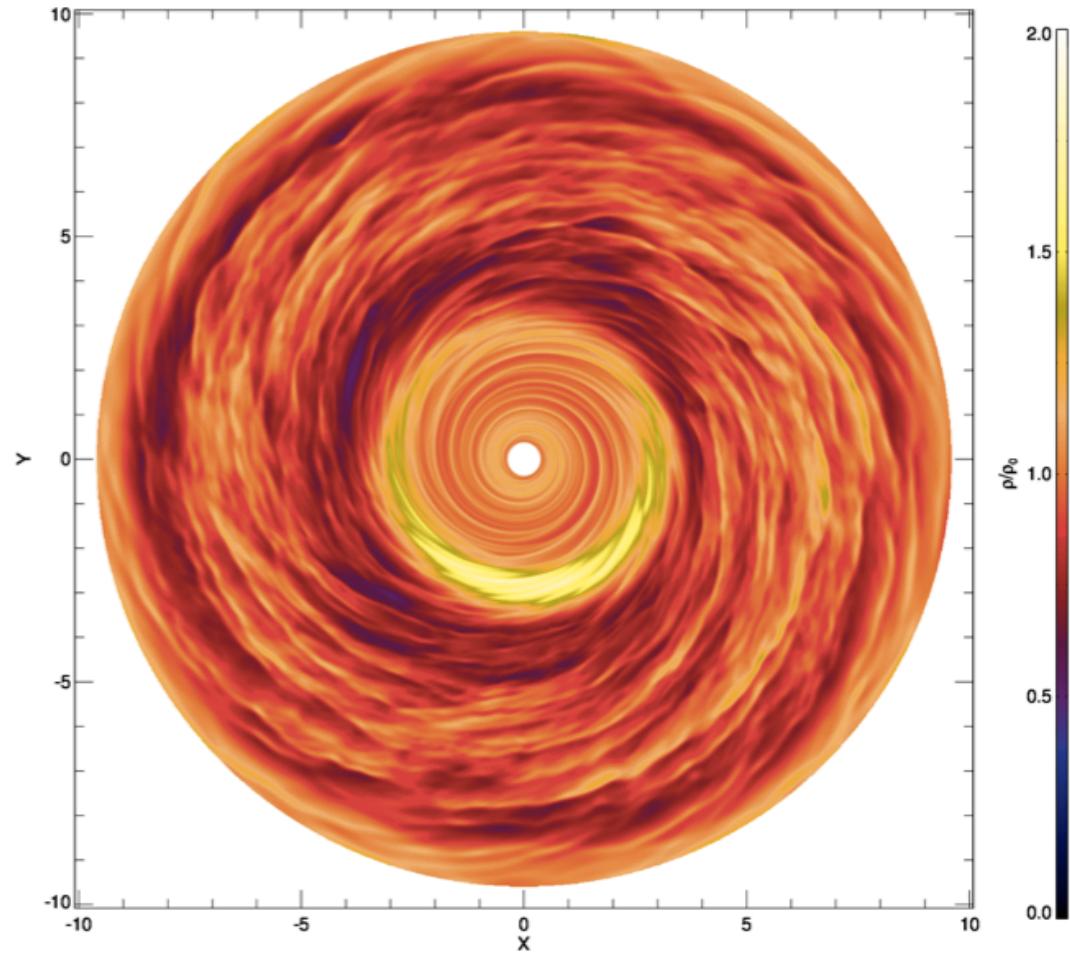
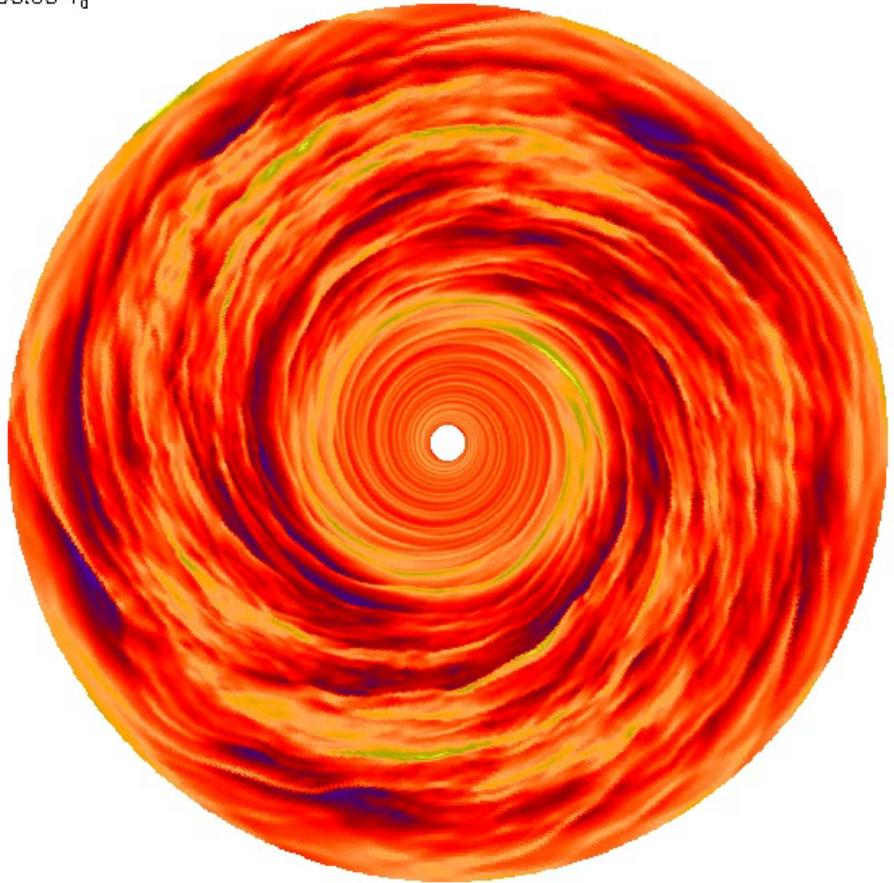
Magnetized inner disk + resistive outer disk

Lyra & Mac Low (2012)



Outer Dead/Active zone transition RWI

$t=95.58 T_0$



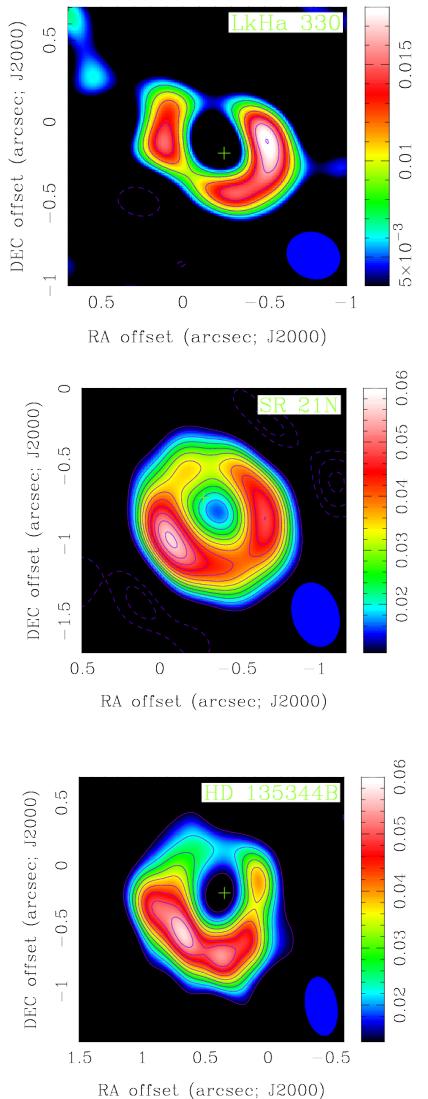
Resistive inner disk + magnetized outer disk

Lyra, Turner, & McNally (2015)

A possible detection of vortices in disks?

Observations

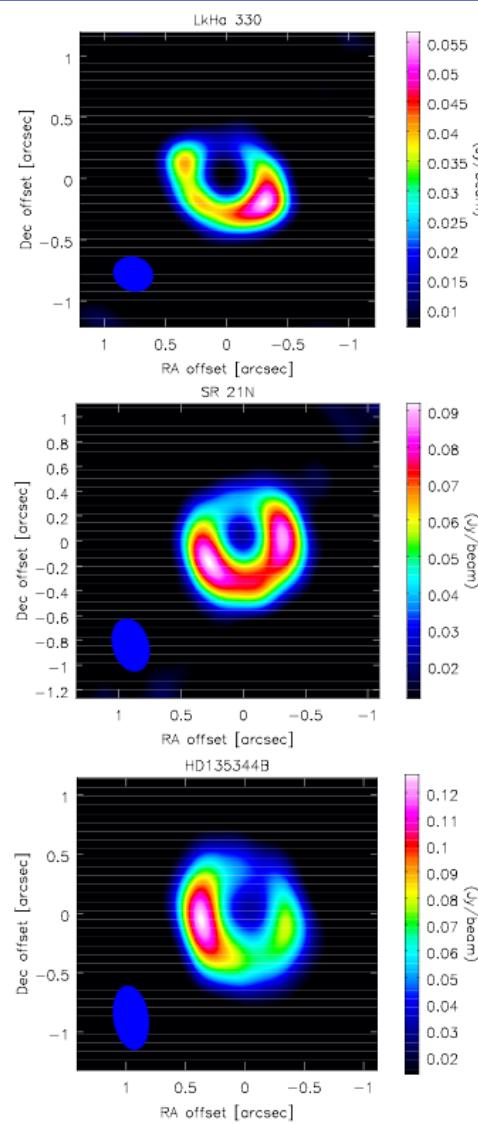
Brown et al. (2009)



Models

Simulated observations
of Rossby vortices

Regaly, Sándor
et al. (2012)



Oph IRS 48

Down



A Major Asymmetric Dust Trap in a Transition Disk

Nienke van der Marel,^{1,*} Ewine F. van Dishoeck,^{1,2} Simon Bruderer,² Til Birnstiel,³ Paola Pinilla,⁴ Cornelis P. Dullemond,⁴ Tim A. van Kempen,^{1,5} Markus Schmalzl,¹ Joanna M. Brown,³ Gregory J. Herczeg,⁶ Geoffrey S. Mathews,¹ Vincent Geers⁷

The statistics of discovered exoplanets suggest that planets form efficiently. However, there are fundamental unsolved problems, such as excessive inward drift of particles in protoplanetary disks during planet formation. Recent theories invoke dust traps to overcome this problem. We report the detection of a dust trap in the disk around the star Oph IRS 48 using observations from the Atacama Large Millimeter/submillimeter Array (ALMA). The 0.44-millimeter-wavelength continuum map shows high-contrast crescent-shaped emission on one side of the star, originating from millimeter-sized grains, whereas both the mid-infrared image (micrometer-sized dust) and the gas traced by the carbon monoxide 6-5 rotational line suggest rings centered on the star. The difference in distribution of big grains versus small grains/gas can be modeled with a vortex-shaped dust trap triggered by a companion.

Although the ubiquity of planets is confirmed almost daily by detections of new exoplanets (*1*), the exact forma-

tion mechanism of planetary systems in disks of gas and dust around young stars remains a long-standing problem in astrophysics (*2*). In

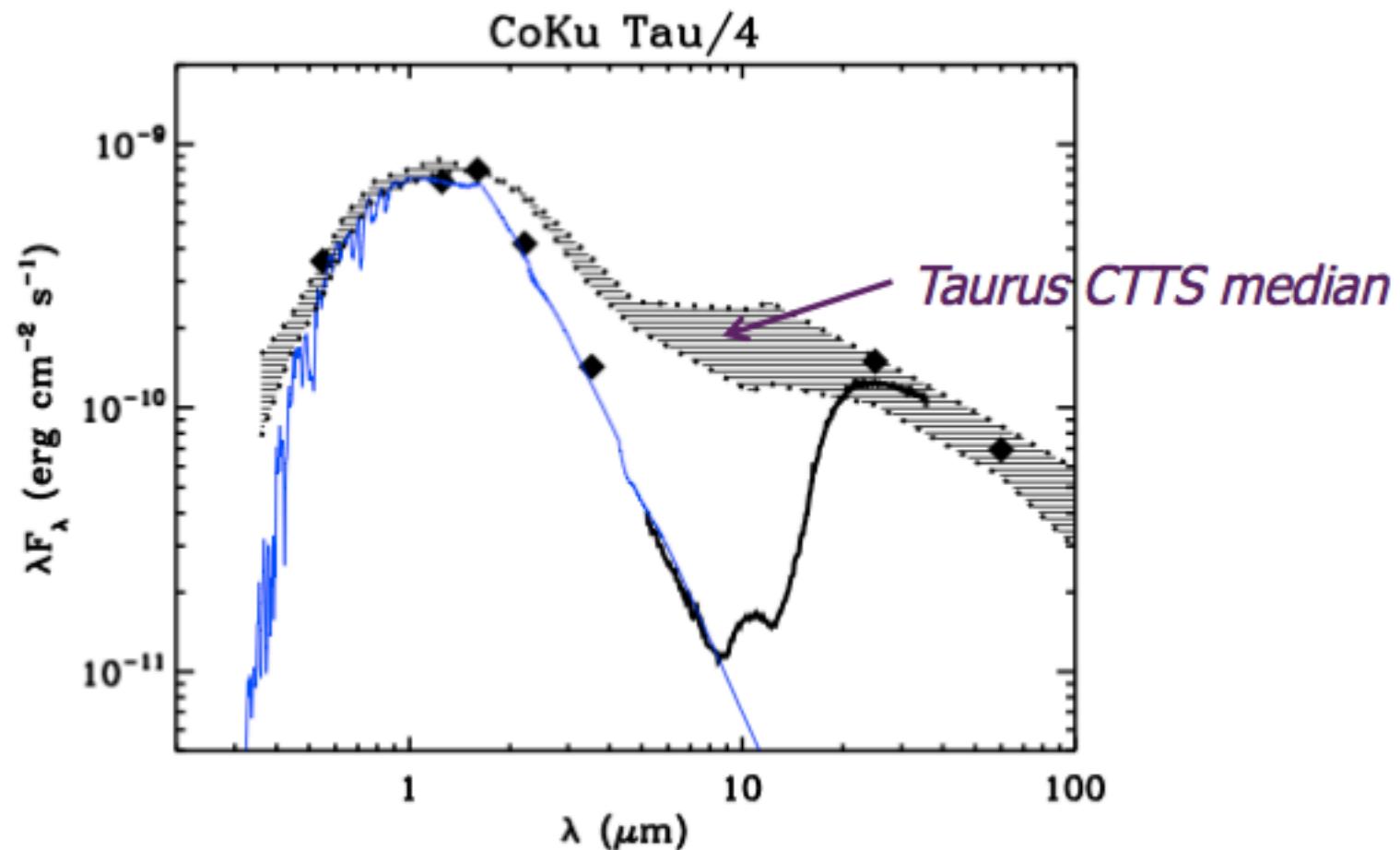
iencemag.org SCIENCE VOL 340 7 JUNE 2013

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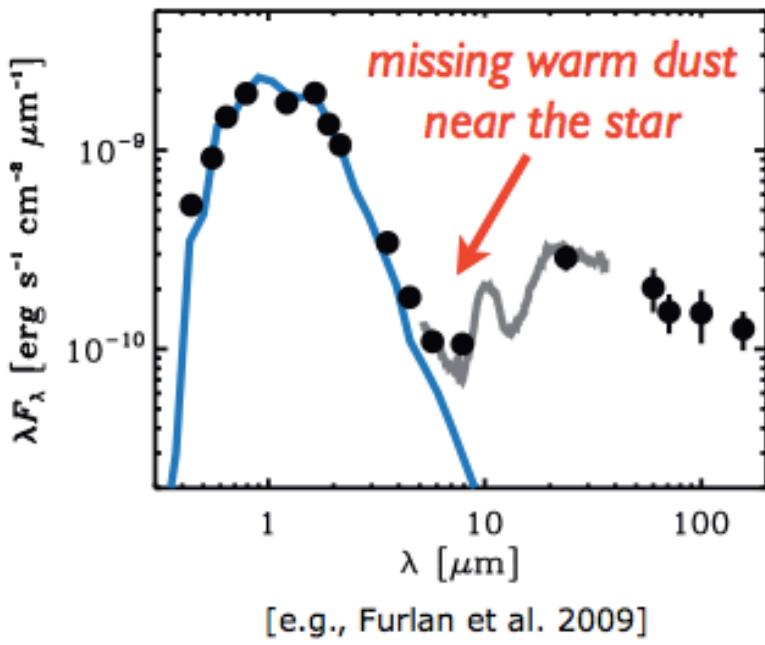
van der Marel et al. 2013

A possible huge vortex observed with ALMA

Transition Disks: Disks with missing hot dust.



the “transition” disks (and what that means)



“These objects represent...disks whose inner regions are relatively devoid of distributed matter, although the outer regions still contain substantial amounts of dust.”

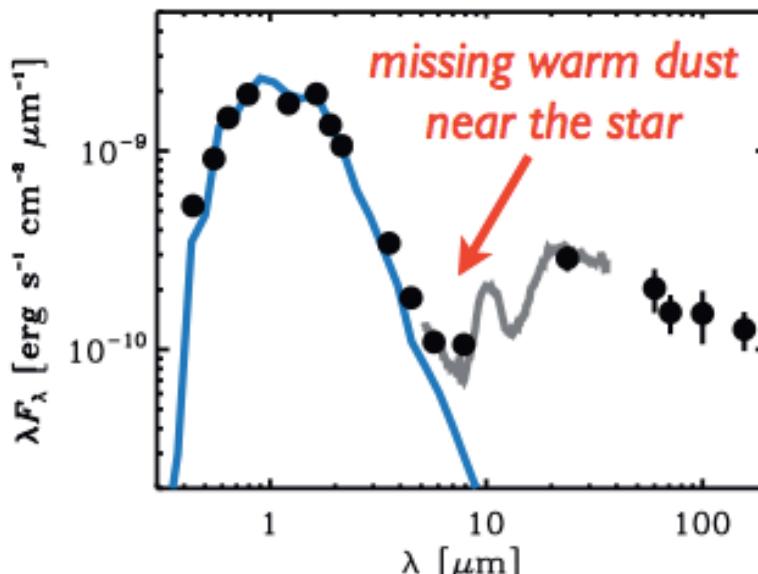
[Strom et al. 1989]

what I mean:

a disk with a large reduction in optical depth near the star
(i.e., a “cavity” or “hole”)



the “transition” disks (and what that means)



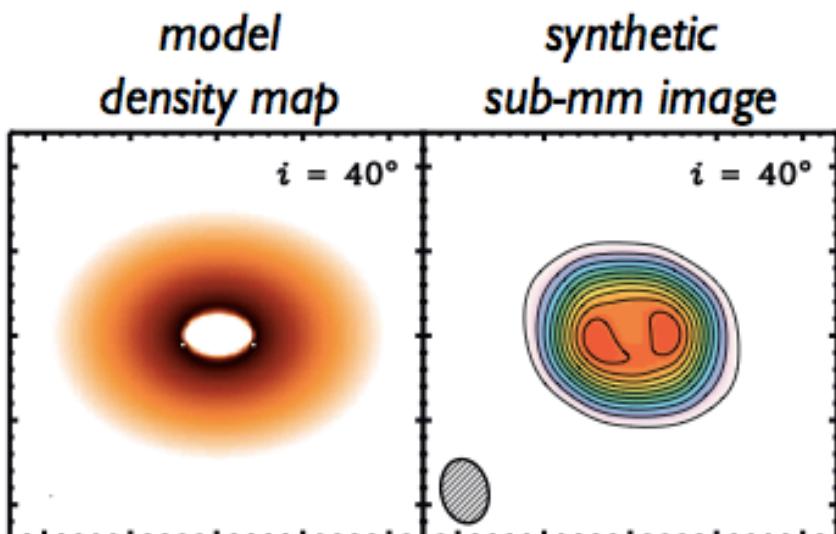
[e.g., Furlan et al. 2009]

“These objects represent...disks whose inner regions are relatively devoid of distributed matter, although the outer regions still contain substantial amounts of dust.”

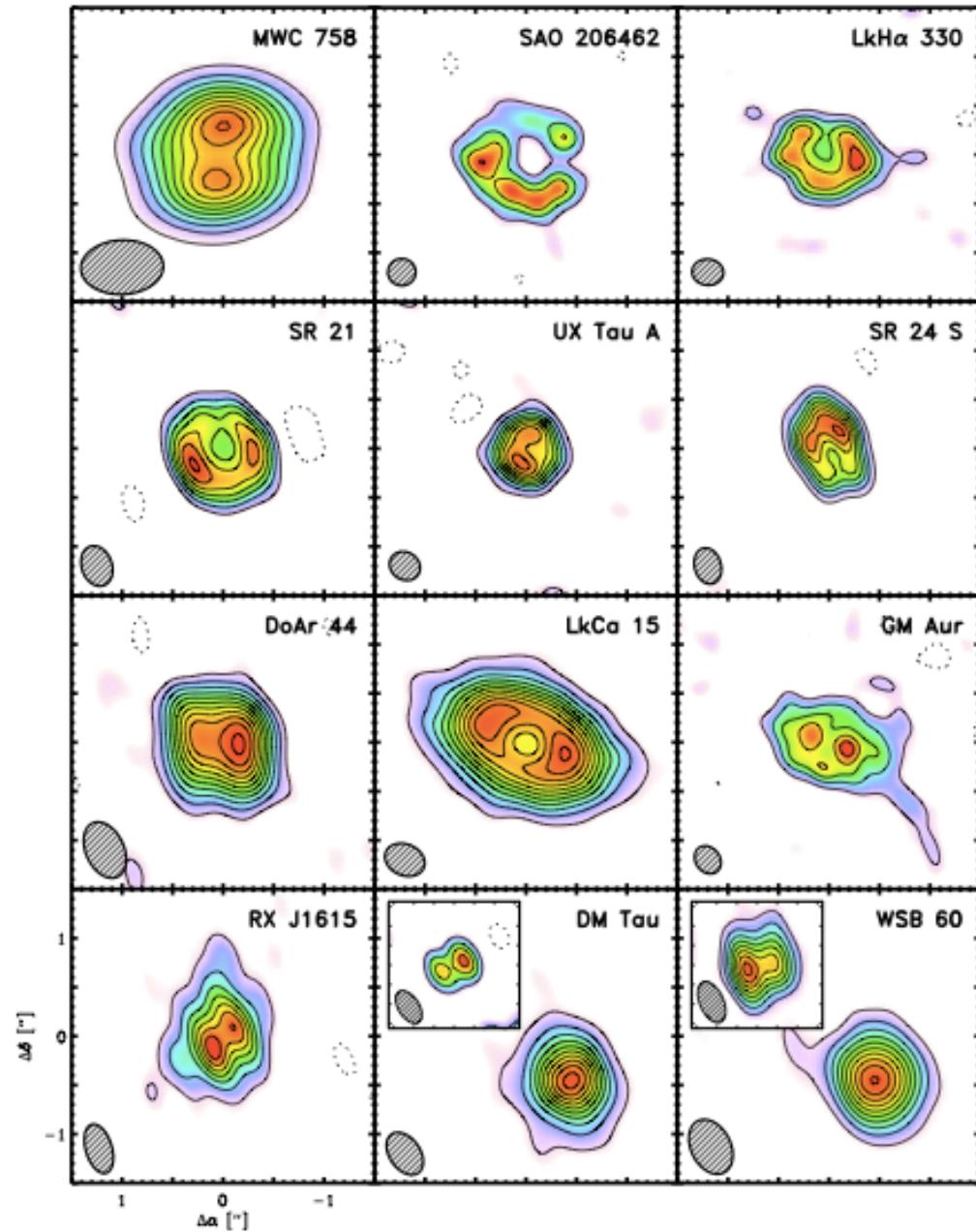
[Strom et al. 1989]

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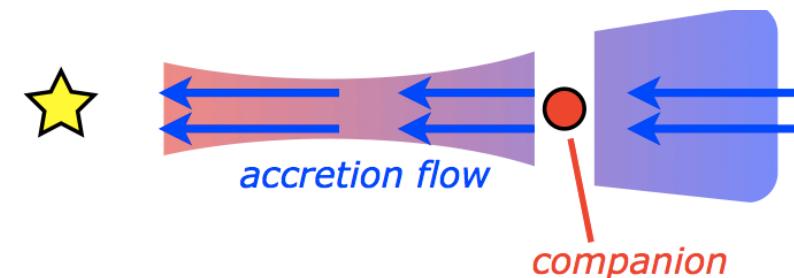
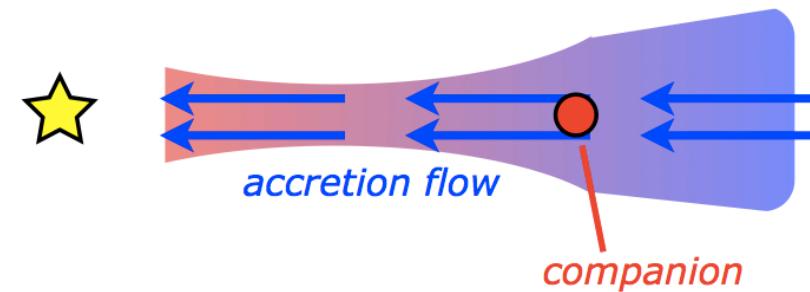
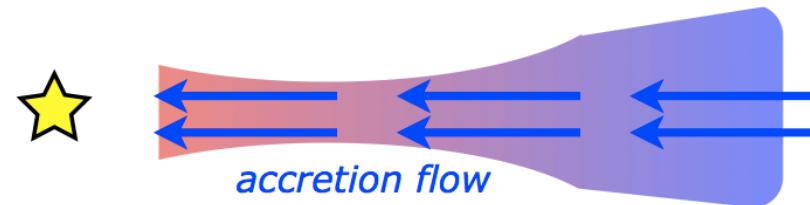


Resolved transition disks with SMA



0.85mm
0.3" ~ 20 AU resolution

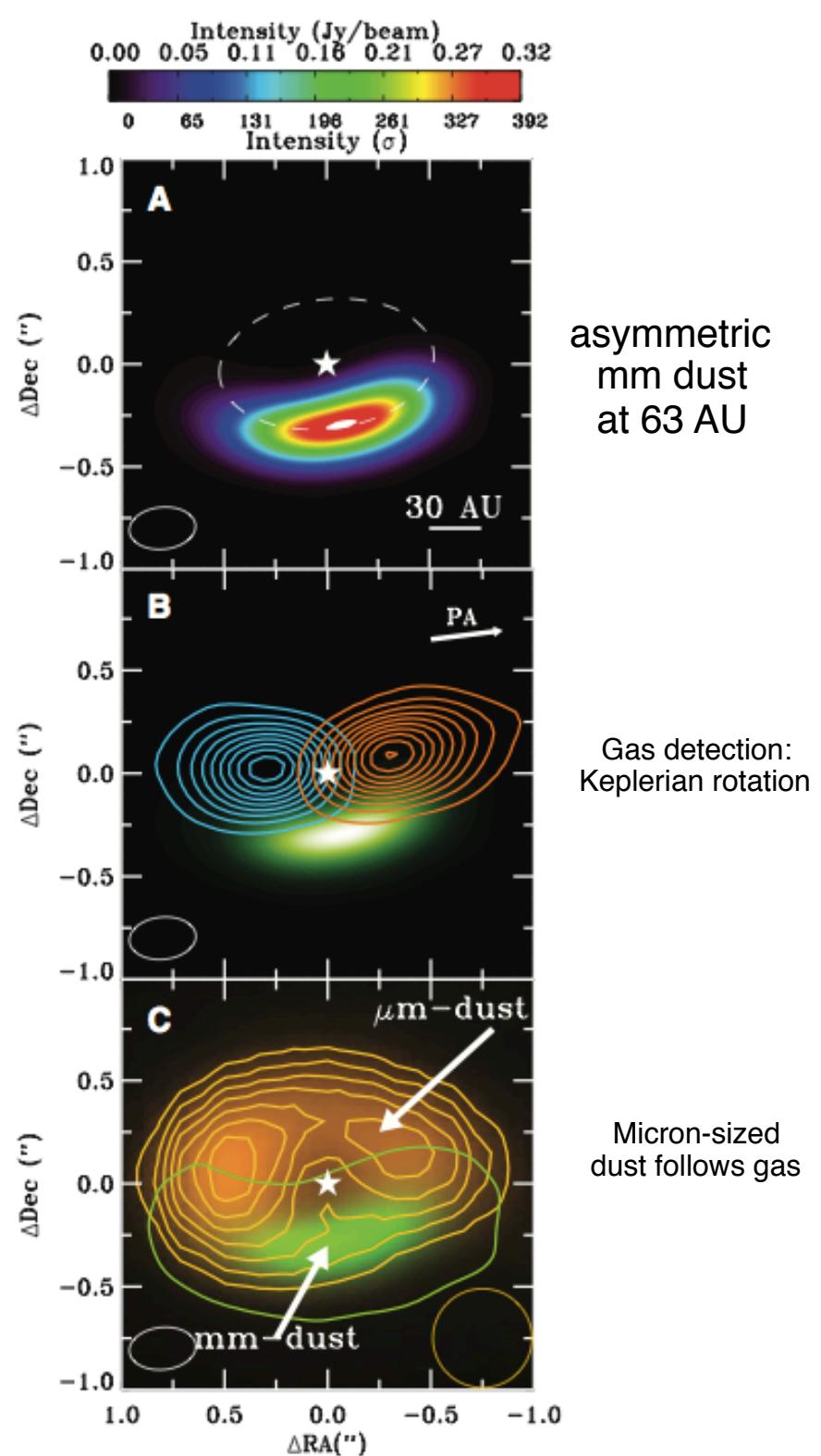
Planetary companion



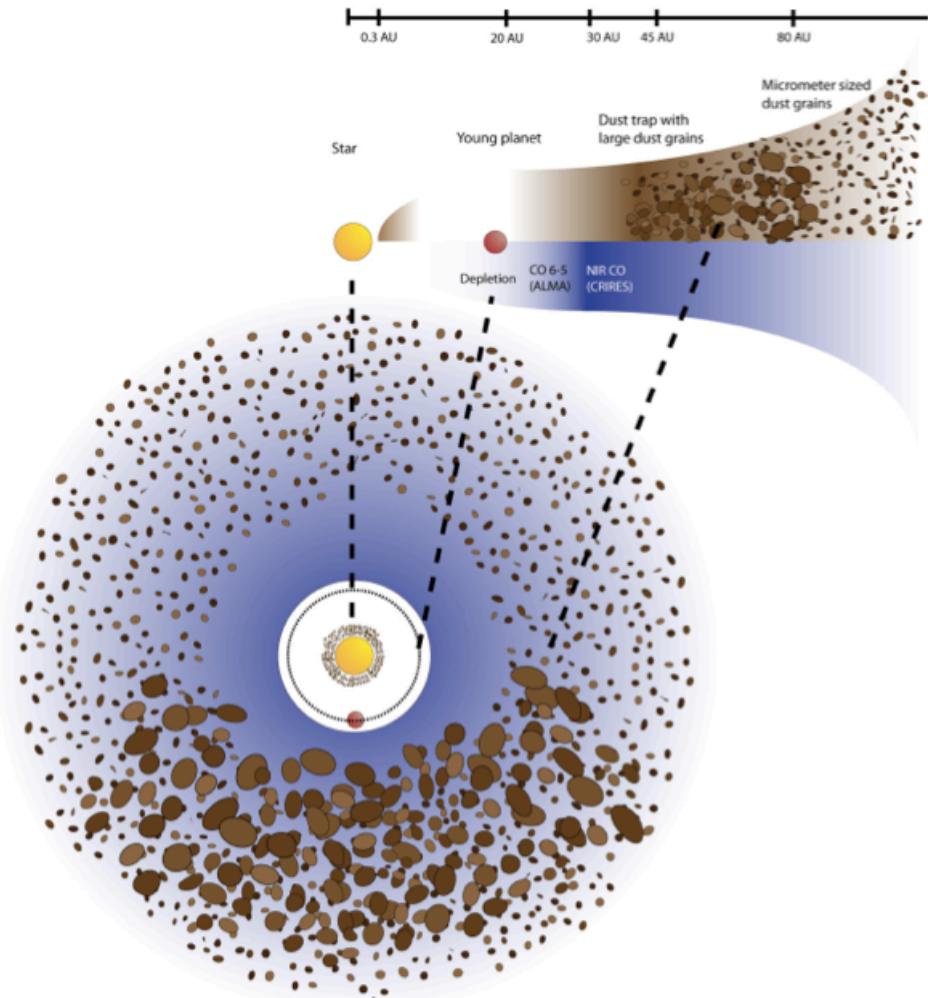
See James Owen's talk

The Oph IRS 48 “dust trap”

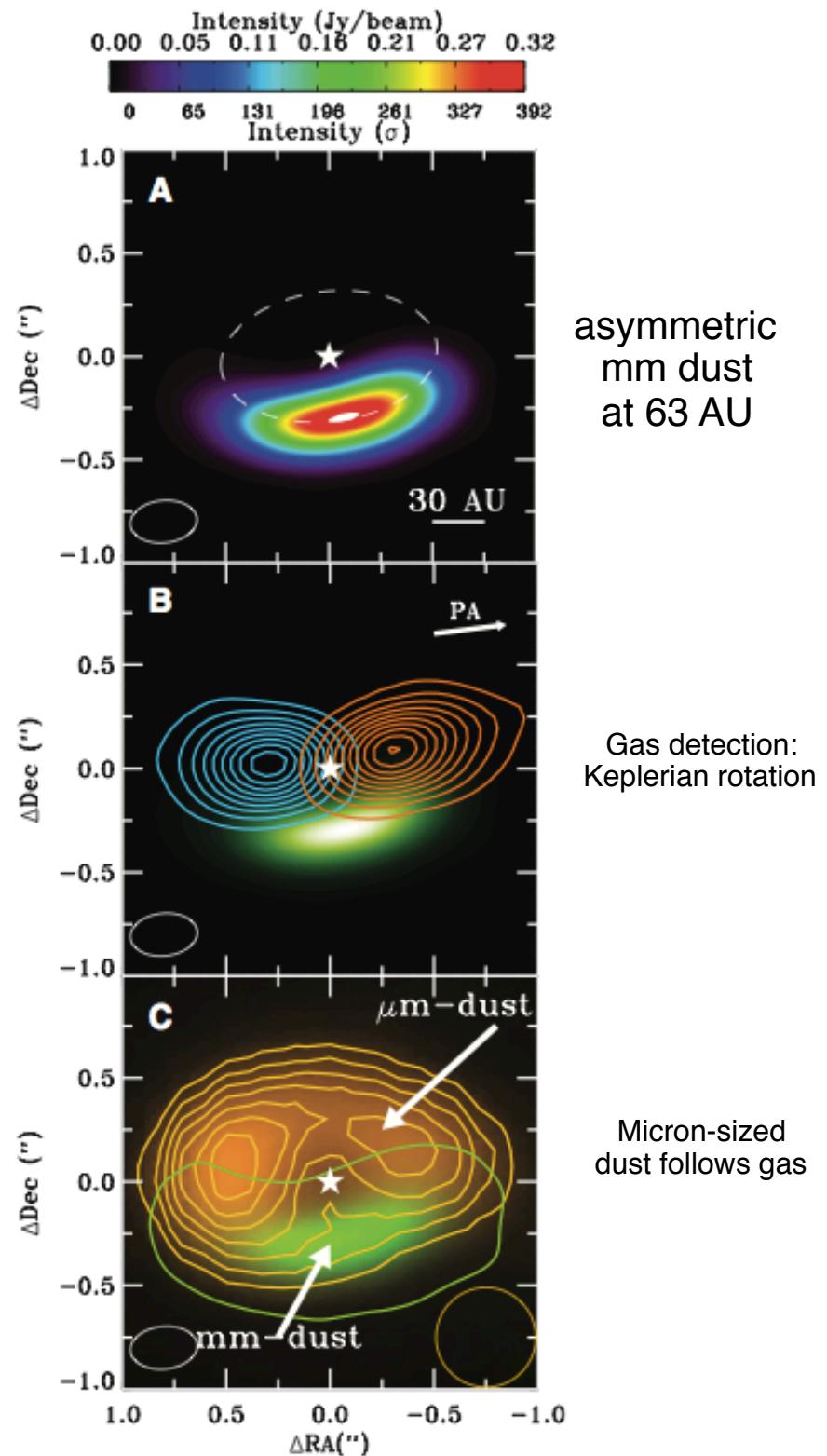
van der Marel et al. (2013)



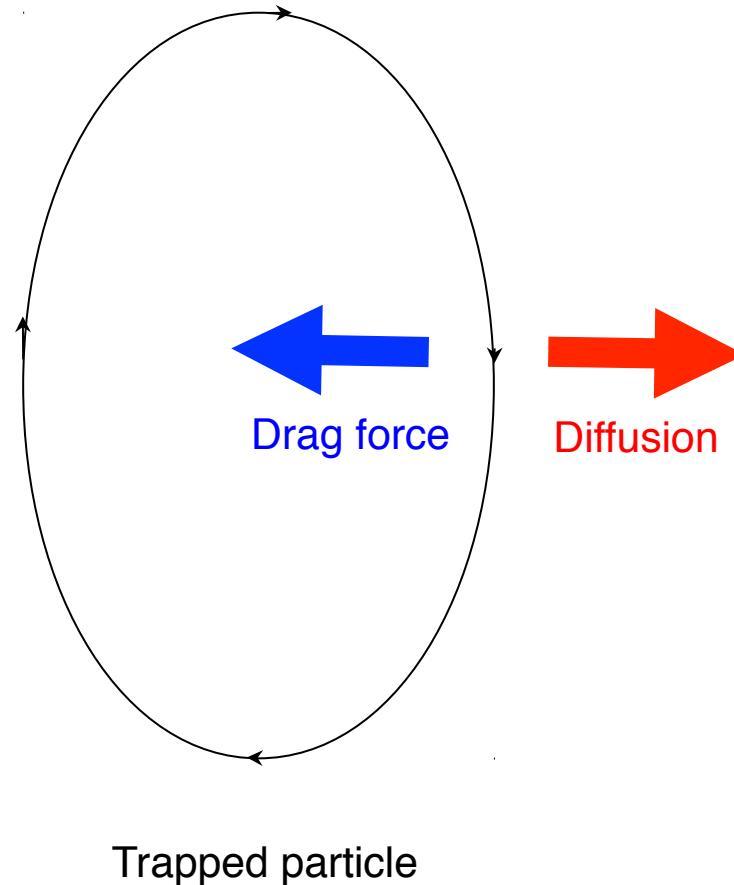
The Oph IRS 48 “dust trap”



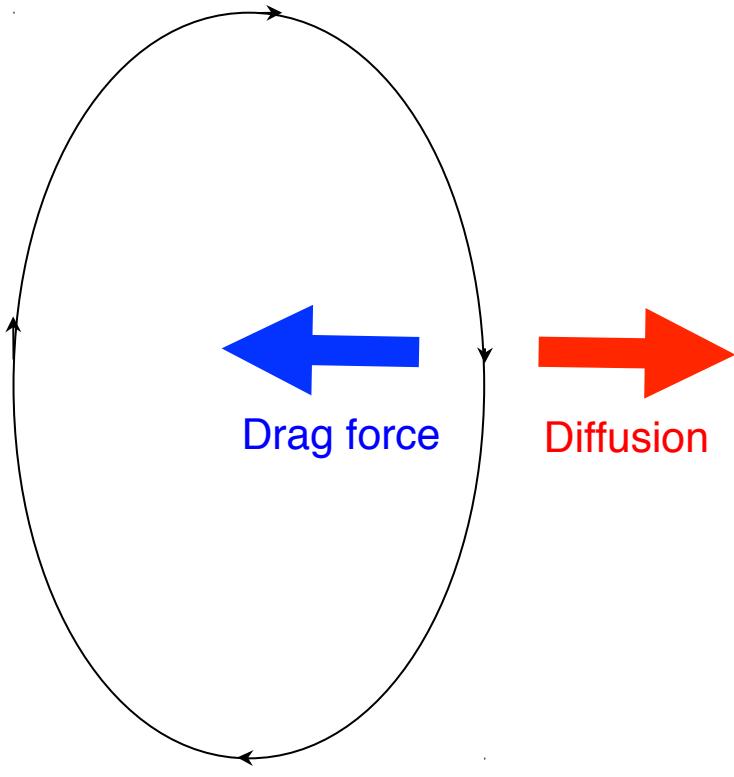
van der Marel et al. (2013)



Drag-Diffusion Equilibrium



Drag-Diffusion Equilibrium



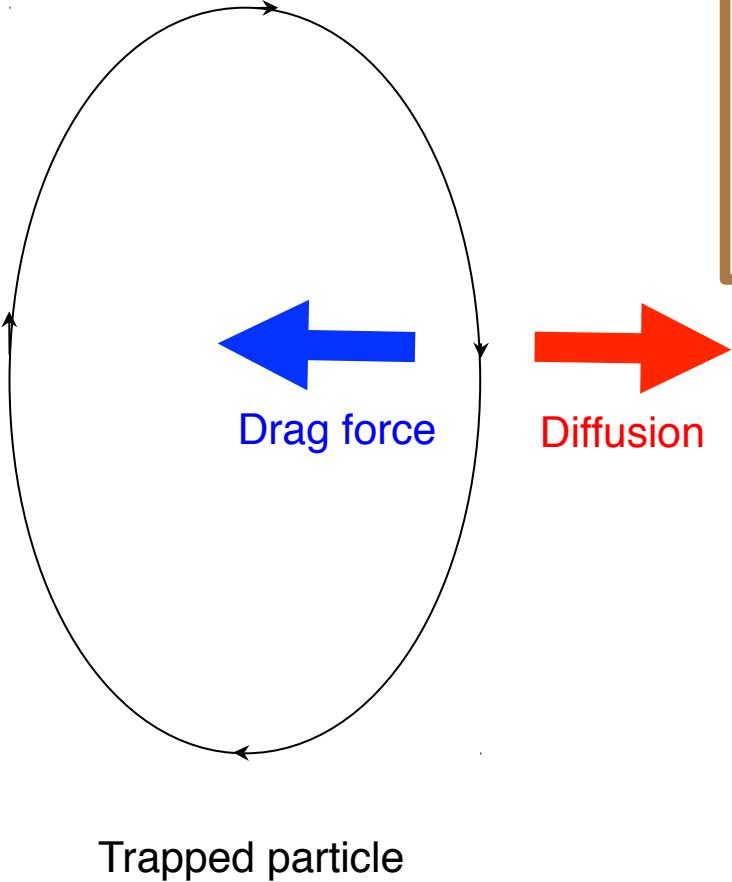
Trapped particle

Dust continuity equation

$$\frac{\partial \rho_d}{\partial t} = -(\mathbf{v} \cdot \nabla) \rho_d - \rho_d \nabla \cdot \mathbf{v} + D \nabla^2 \rho_d,$$

advection compression diffusion

Drag-Diffusion Equilibrium



Steady-state solution

$$\rho_d(a,z) = \epsilon \rho_0 (S + 1)^{3/2} \exp \left\{ - \frac{[a^2 f^2(\chi) + z^2]}{2H^2} (S + 1) \right\}$$

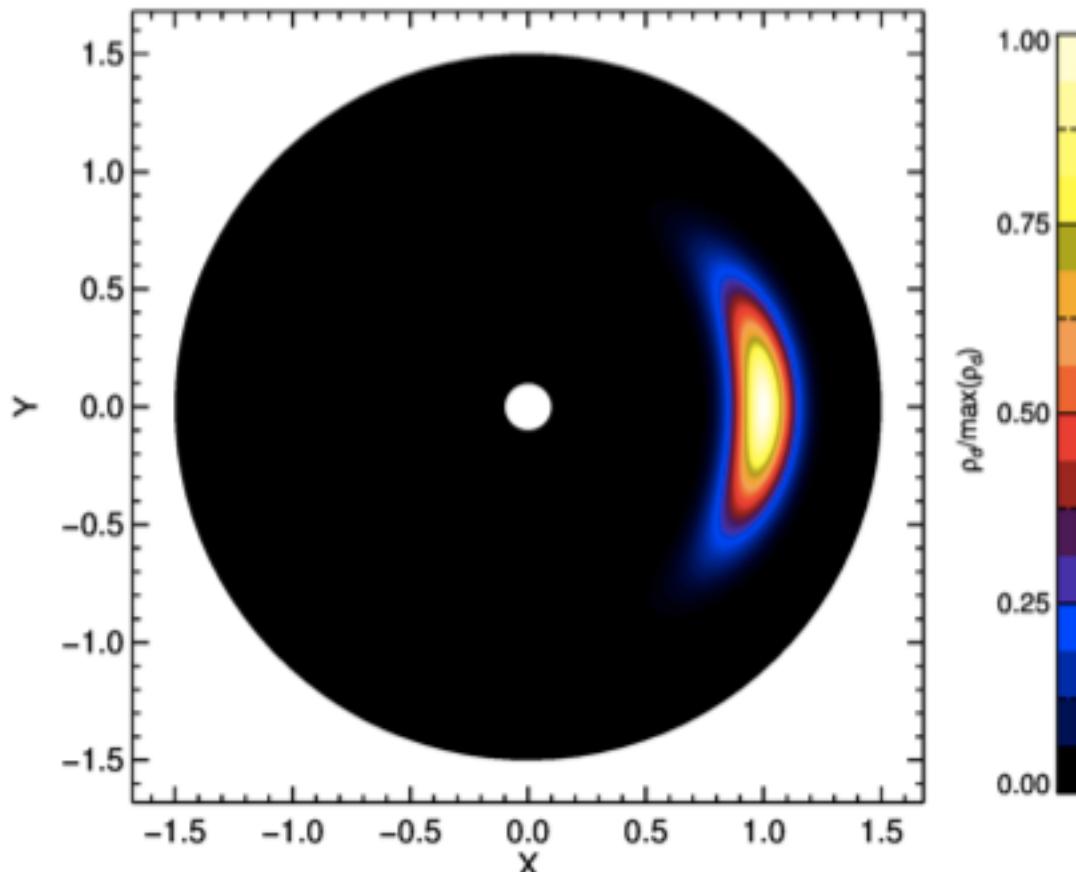
Lyra & Lin (2013)

$$S = \frac{St}{\delta}$$

$$\delta = v_{\text{rms}}^2 / c_s^2,$$

a = vortex semi-minor axis
 H = disk scale height (temperature)
 χ = vortex aspect ratio
 δ = diffusion parameter
 St = Stokes number (particle size)
 $f(\chi)$ = model-dependent scale function

Analytical solution for dust trapping



Solution for

$$H/r=0.1 \quad \chi=4 \quad S=1$$

Solution

$$\rho_d(a) = \rho_{d\max} \exp\left(-\frac{a^2}{2H_V^2}\right),$$

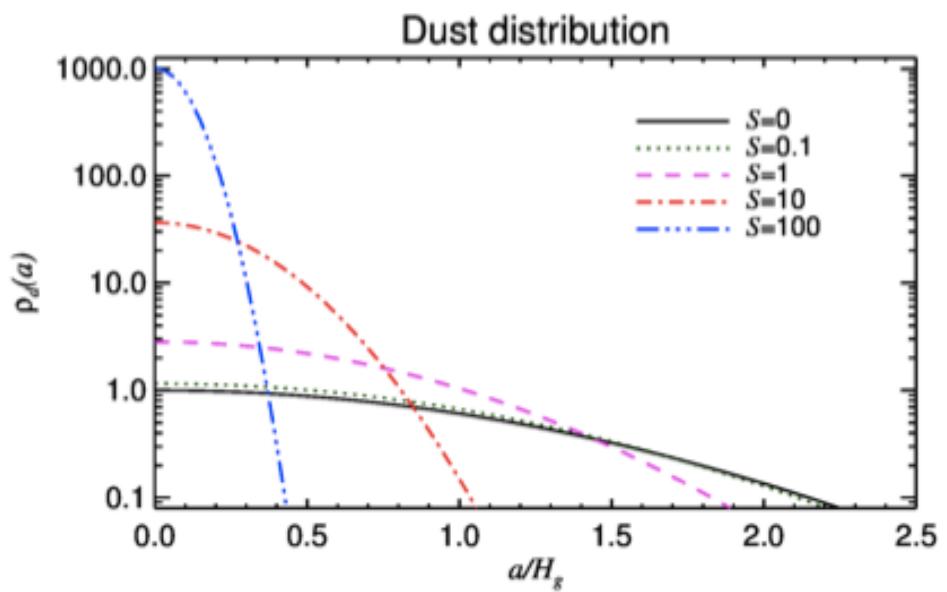
$$H_V = \frac{H}{f(\chi)} \sqrt{\frac{1}{S+1}}$$

$$S = \frac{St}{\delta}$$

$$\delta = v_{\text{rms}}^2 / c_s^2,$$

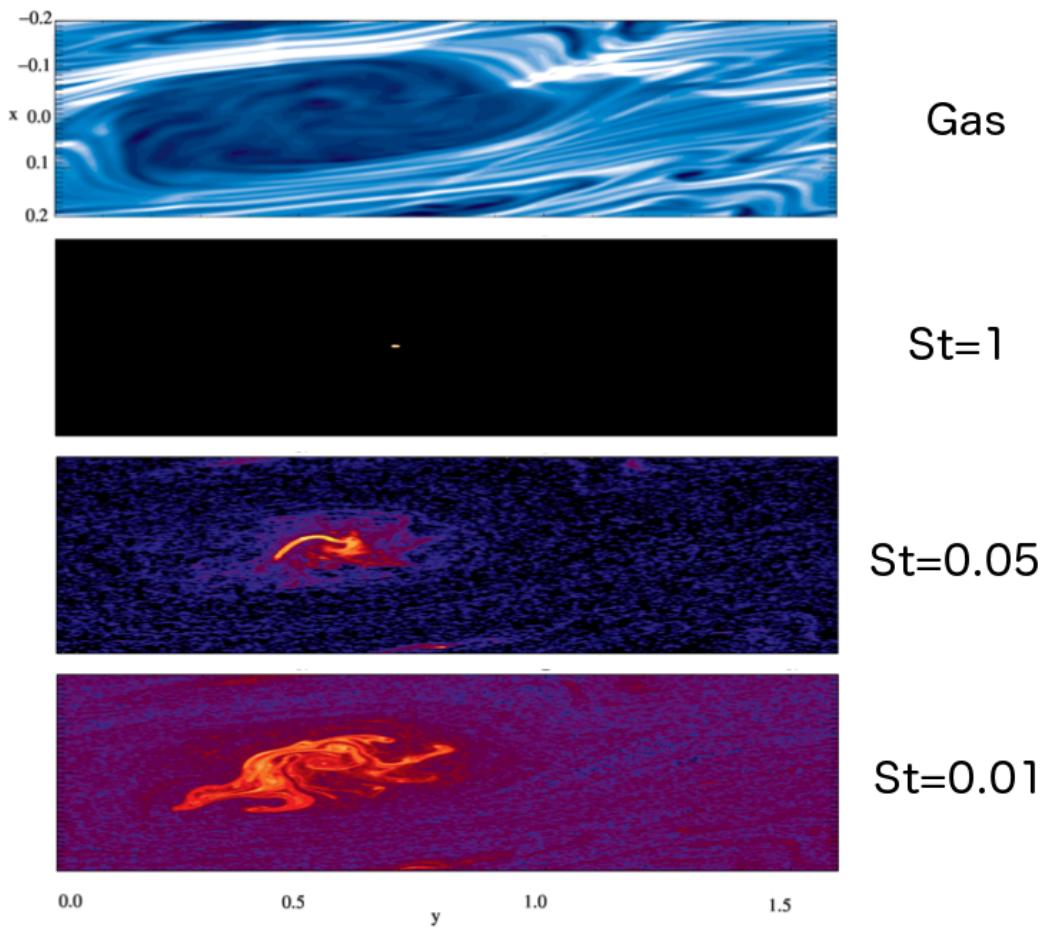
- a = vortex semi-minor axis
 H = disk scale height (temperature)
 χ = vortex aspect ratio
 δ = diffusion parameter
St = Stokes number (particle size)
 $f(\chi)$ = model-dependent scale function

Analytical vs Numerical



$$S = \frac{St}{\delta} \quad \delta = v_{\text{rms}}^2 / c_s^2,$$

Lyra & Lin (2013)



Raettig et al (2015)

Derived quantities

$$\rho_d(a, z) = \epsilon \rho_0 (S + 1)^{3/2} \exp \left\{ - \frac{[a^2 f^2(\chi) + z^2]}{2H^2} (S + 1) \right\}$$

Lyra & Lin (2013)

Gas distribution

$$\rho_g(a) = \rho_{g\max} \exp \left(- \frac{a^2}{2H_g^2} \right),$$

Maximum dust density

$$\rho_{d\max} = \epsilon \rho_0 (S + 1)^{3/2}$$

Gas contrast

$$\frac{\rho_{g\max}}{\rho_{g\min}} = \exp \left[\frac{f^2(\chi)}{2\chi^2 \omega_V^2} \right],$$

Dust contrast

$$\frac{\rho_{d\max}}{\rho_{d\min}} = \frac{\rho_{g\max}}{\rho_{g\min}} \exp(S),$$

Total trapped mass

$$\int \rho_d(a, z) dV = (2\pi)^{3/2} \epsilon \rho_0 \chi H H_g^2$$

Vortex size

$$a_s = H(\chi \omega_V)^{-1}$$

H = disk scale height (temperature)
 χ = vortex aspect ratio
 δ = diffusion parameter

St = Stokes number (particle size)
 $f(\chi)$ = model-dependent scale function
 ϵ = dust-to-gas ratio

Applying the model to Oph IRS 48

Observed parameters

Aspect ratio: 3.1

Dust contrast: 130

Temperature: 60K

Trapped mass: $9 M_{Earth}$

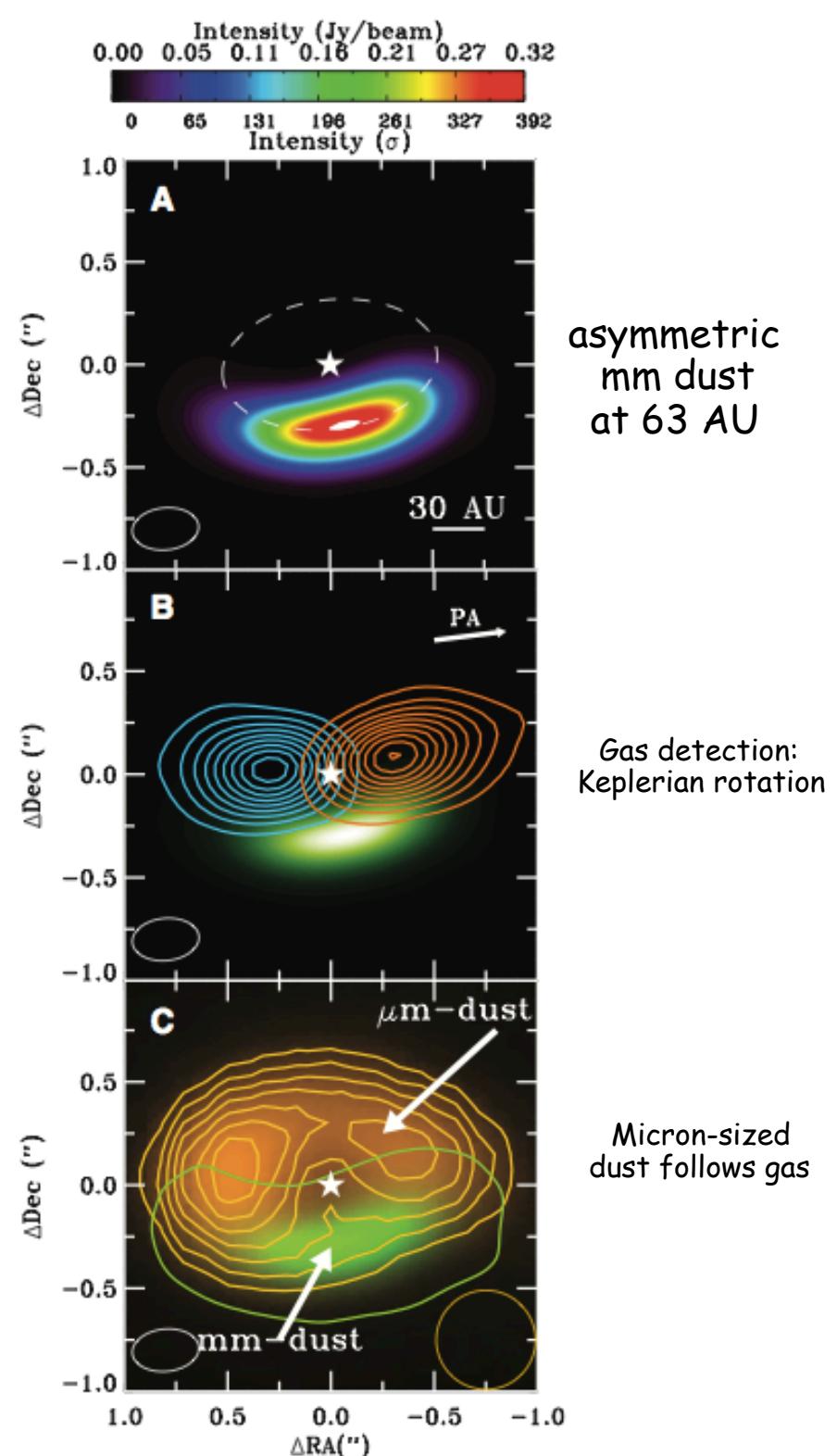
Derived parameters

S=4.8

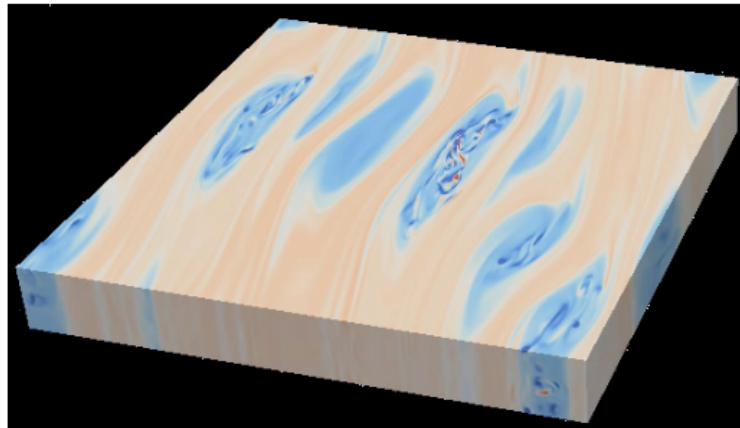
Stokes number, St=0.008

$\delta = 0.005$, $V_{rms} = 4\% C_s$

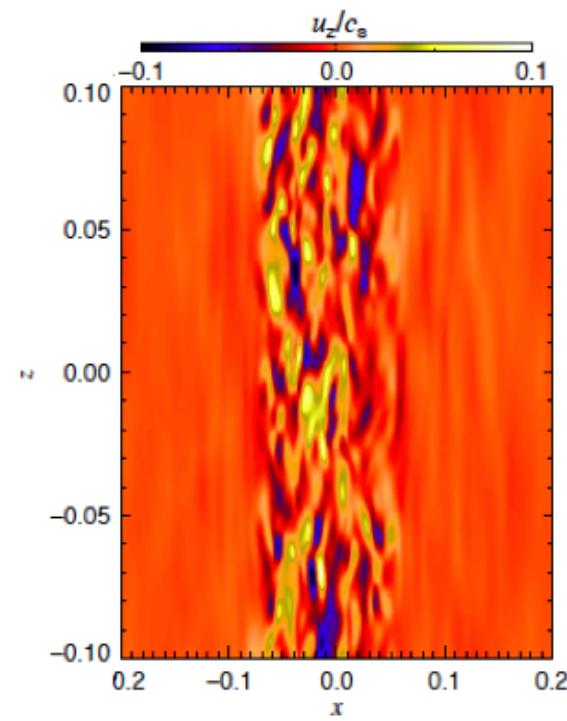
Trapped mass: $11 M_{Earth}$



Turbulence in vortex cores



Lesur & Papaloizou (2010)



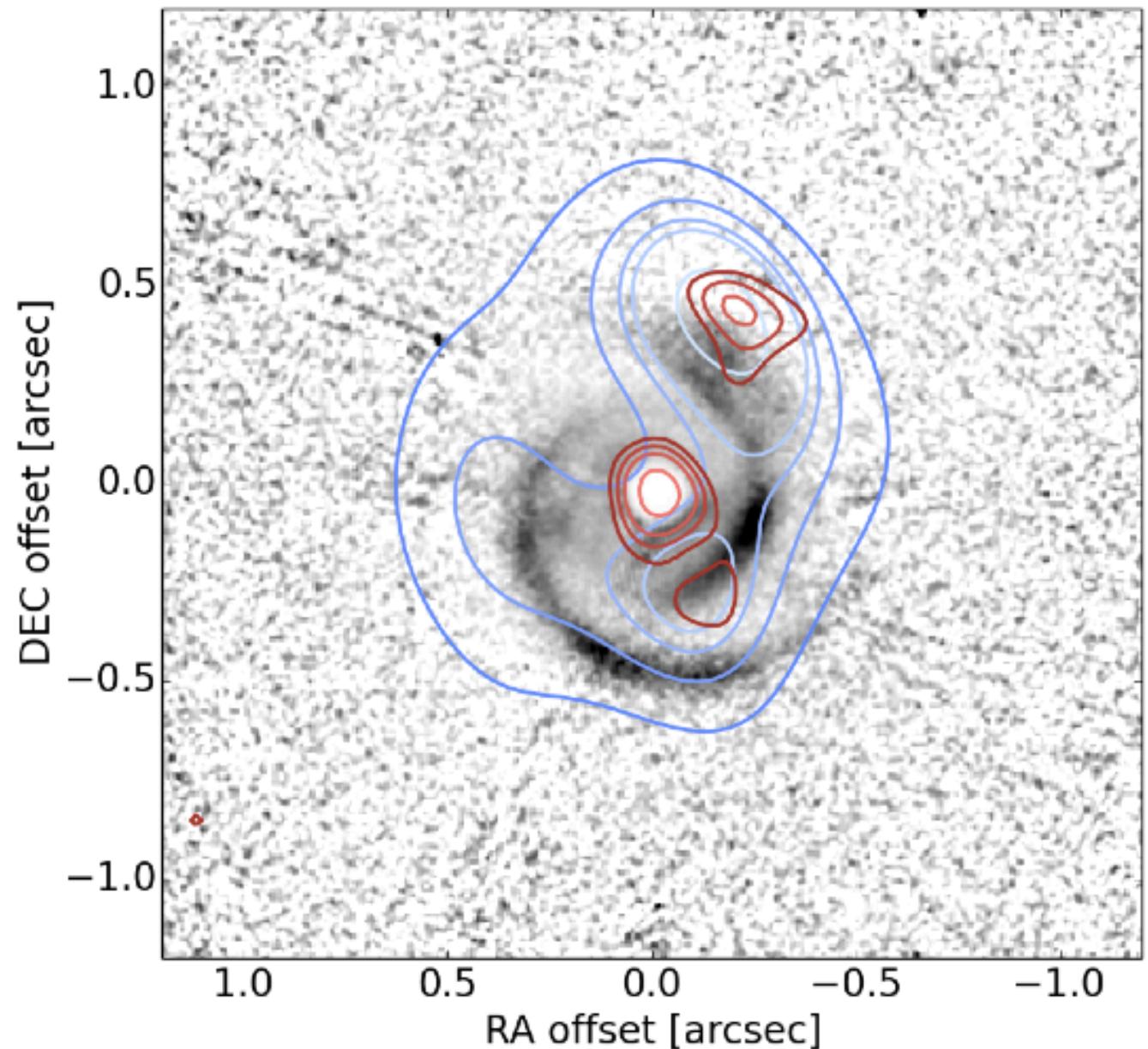
Lyra & Klahr (2011)

Turbulence in vortex cores:

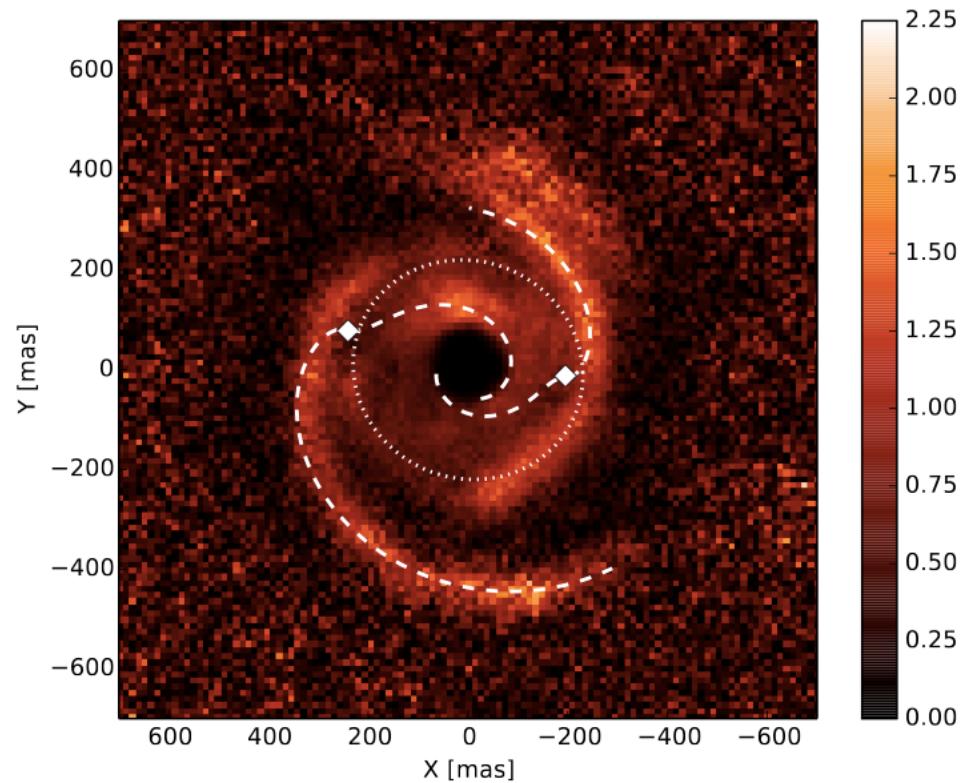
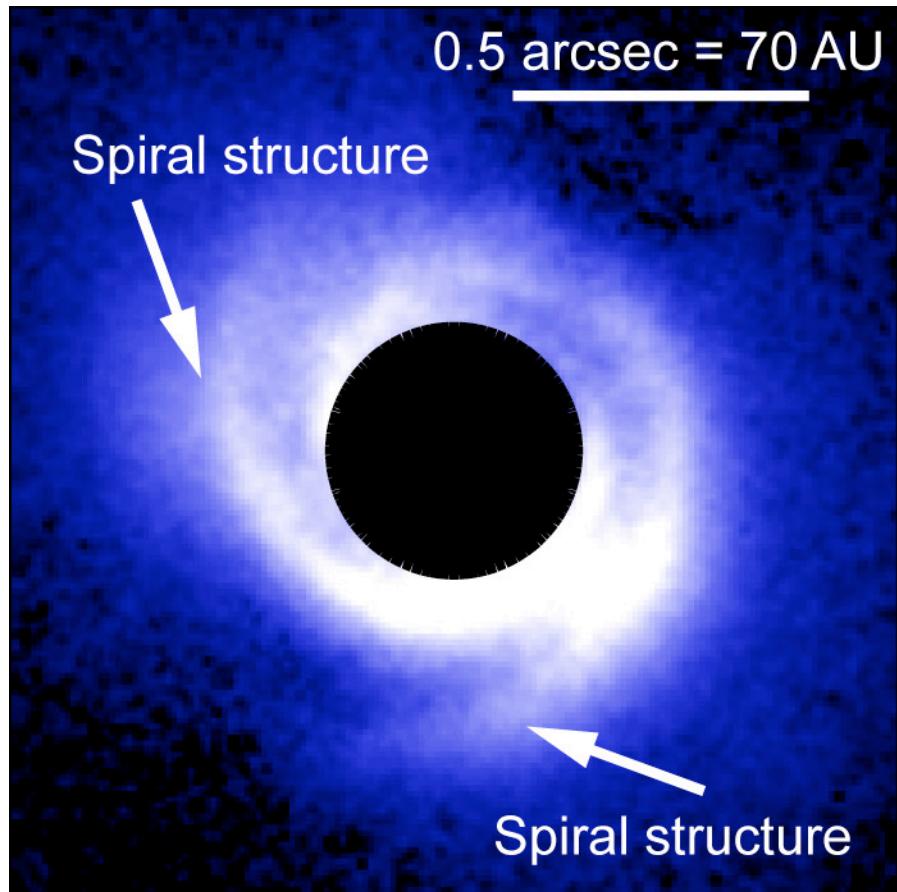
max at ~10% of sound speed
rms at ~3% of sound speed

SPHERE-ALMA-VLA overlay of MWC 758

SPHERE (μm)
ALMA (mm)
VLA (m)

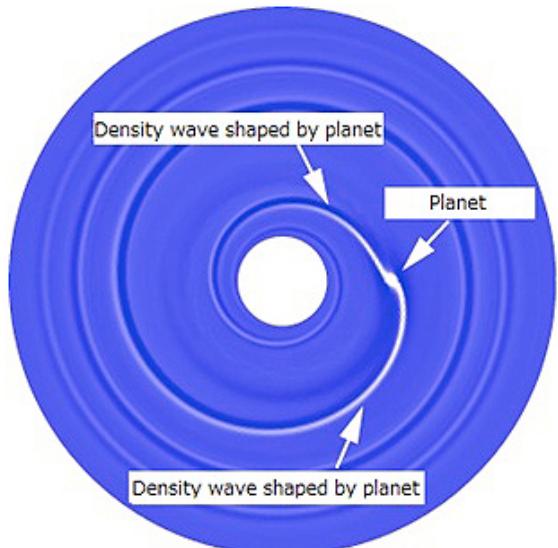


Observational evidence: Spirals



Spiral arm fitting leads to problems

Analytical spiral fit

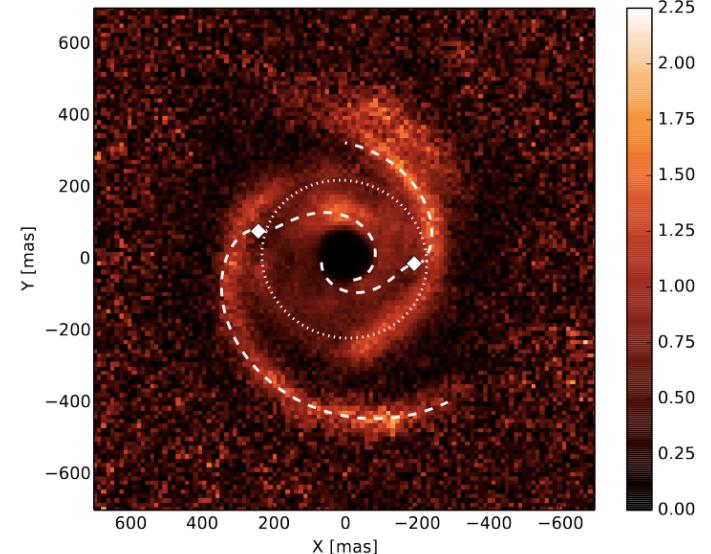


$$\theta(r) = \theta_c + \frac{\text{sgn}(r - r_c)}{h_c} \times \left\{ \left(\frac{r}{r_c} \right)^{1+\beta} \left[\frac{1}{1+\beta} - \frac{1}{1-\alpha+\beta} \left(\frac{r}{r_c} \right)^{-\alpha} \right] - \left(\frac{1}{1+\beta} - \frac{1}{1-\alpha+\beta} \right) \right\},$$

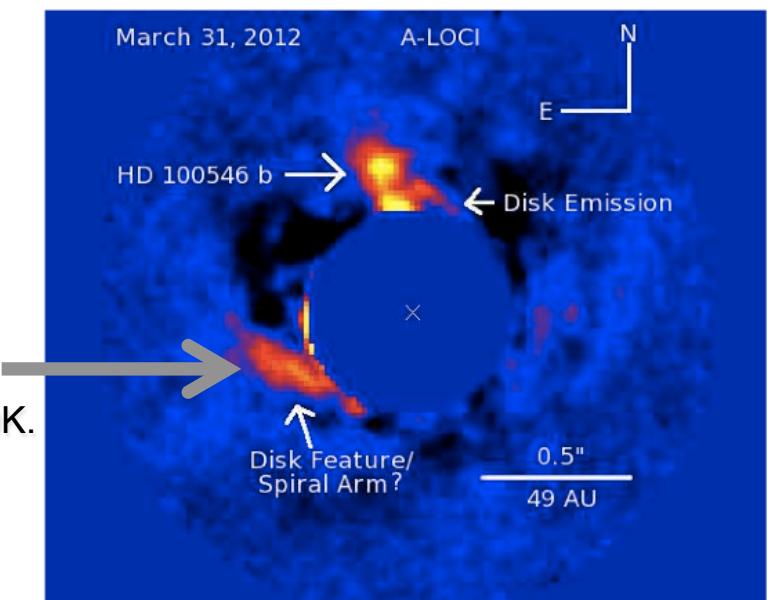
Rafikov (2002)

Muto et al. (2012)

Spirals are too wide
hotter (300K) than
ambient gas (50K)

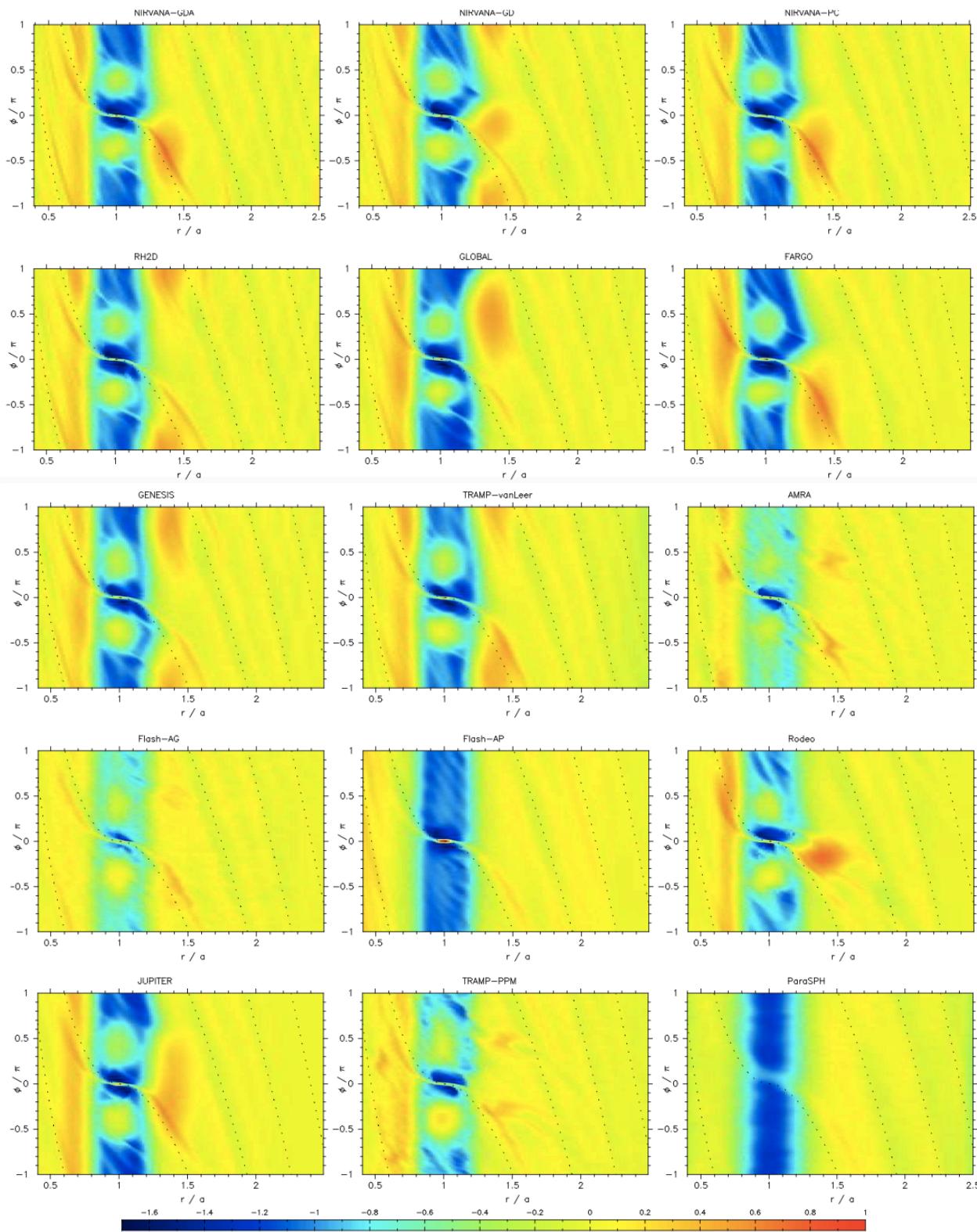


Spiral has little
polarization. Must be
thermal emission at 1000K.



The code comparison project of 2006 (de Val-Borro et al. 2006)

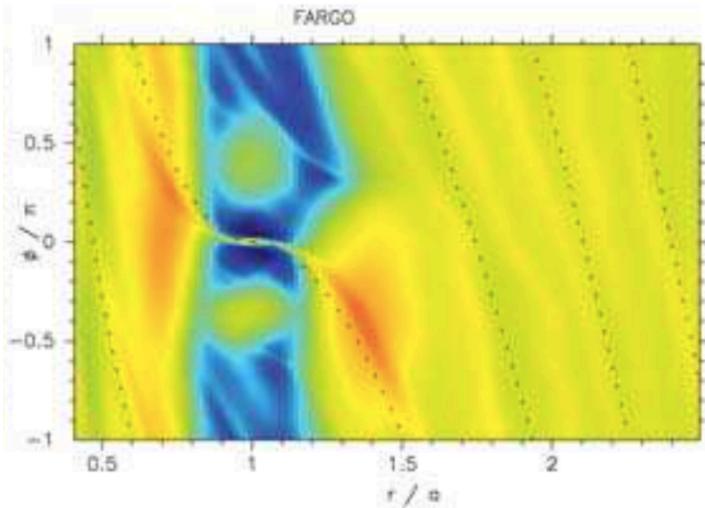
Problem of choice:
2D ‘vanilla’ planet-disk interaction.



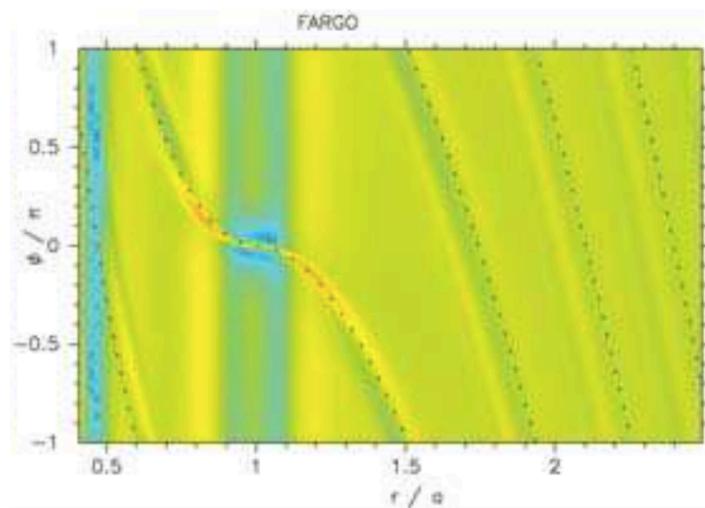
The “hot spiral problem” has never been a problem

Wakes of high-mass planets are not sonic, but *supersonic*.

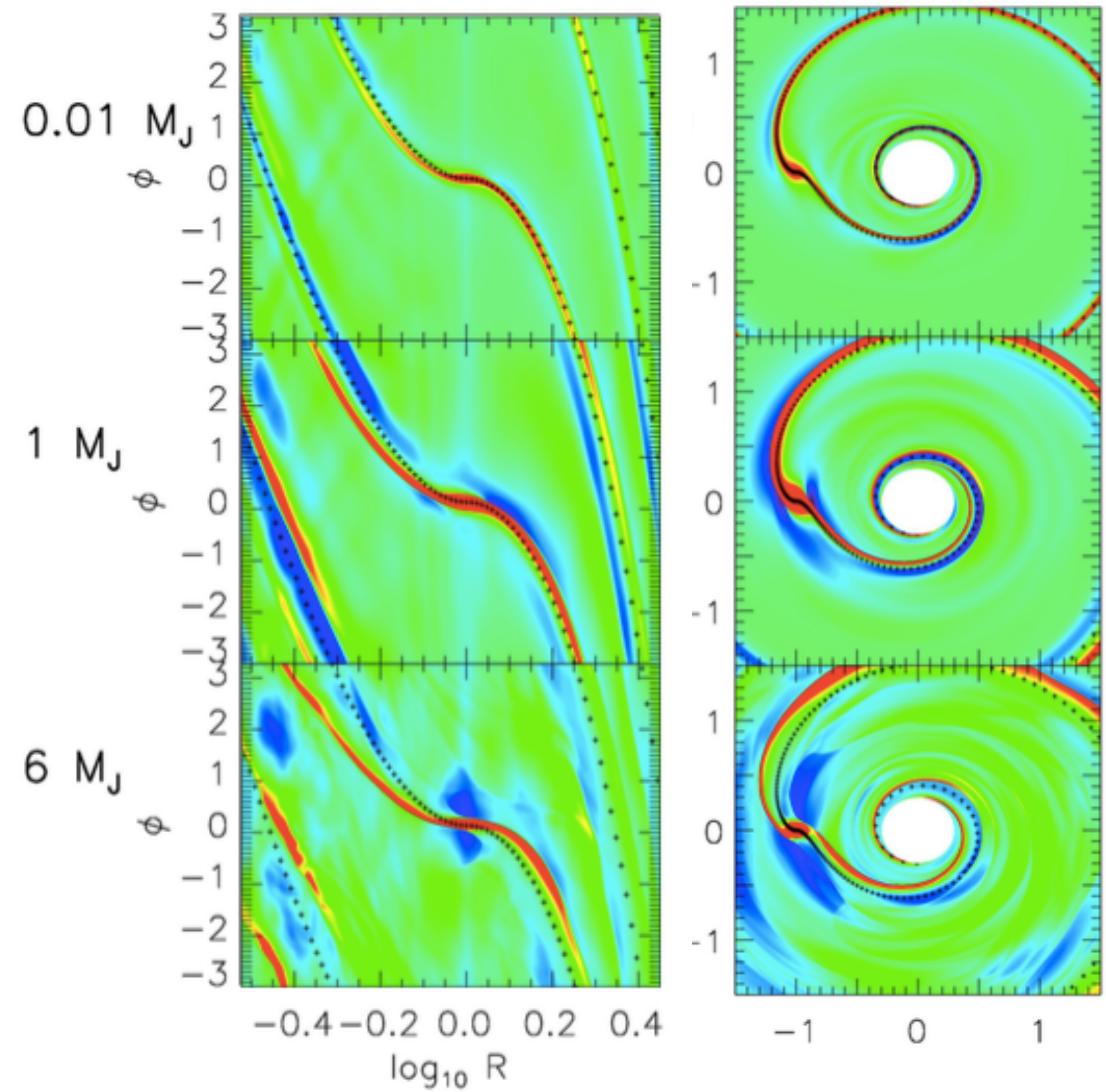
Jupiter-mass (non-linear)



Neptune-mass (linear)

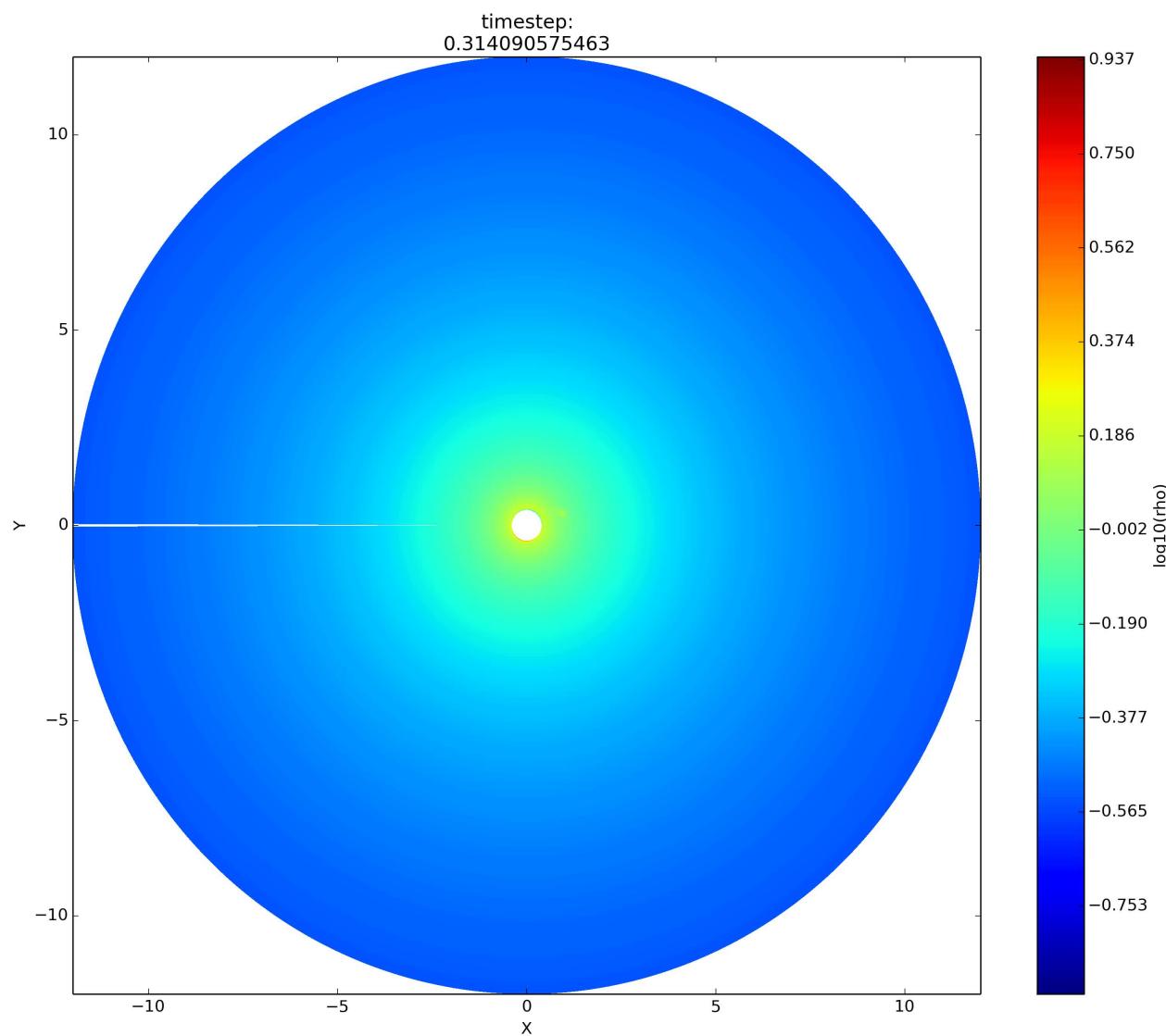


de Val-Borro al. (2006)



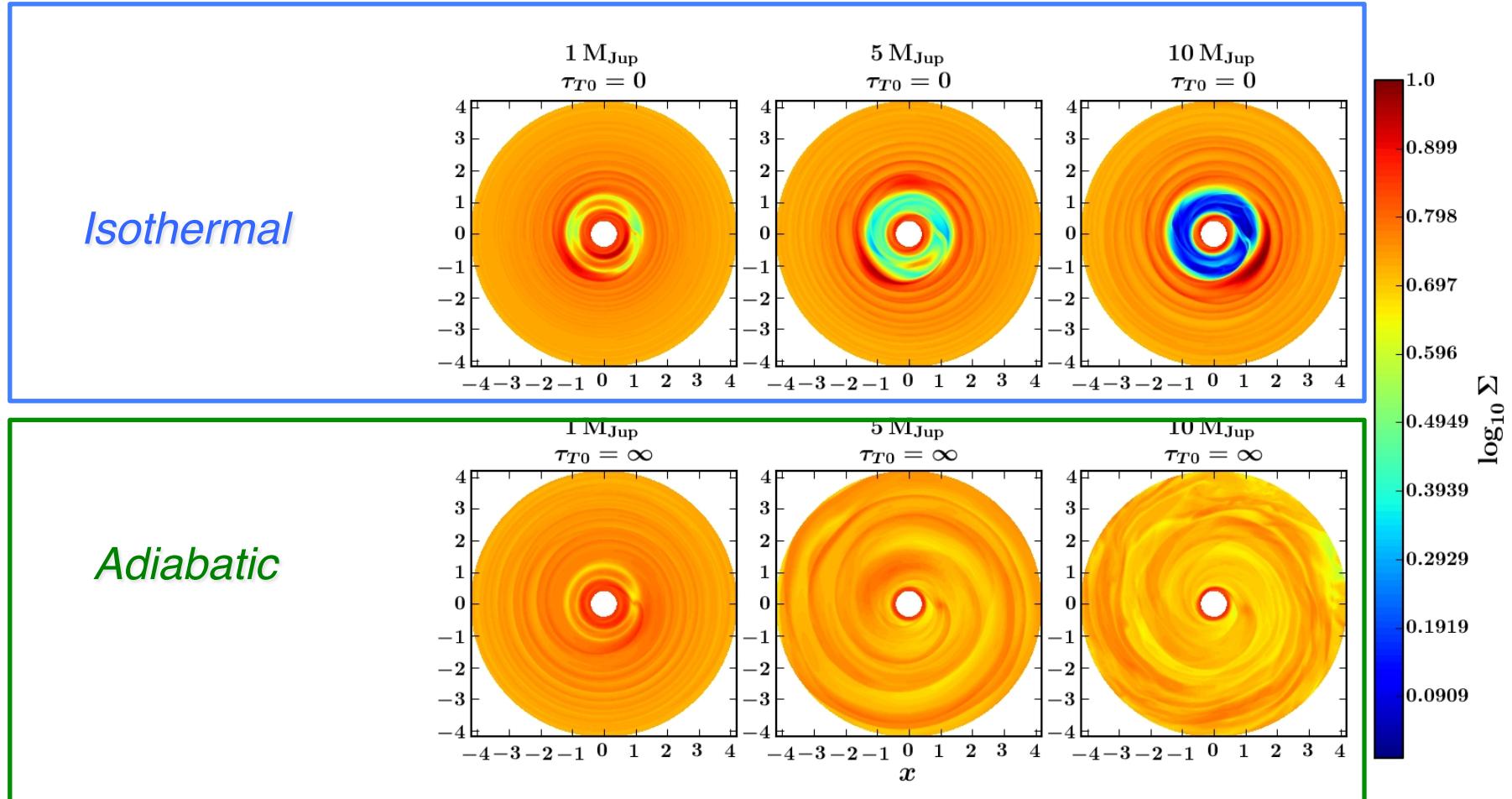
Zhu et al. (2015)

Spiral wake of high-mass planets in non-isothermal disks

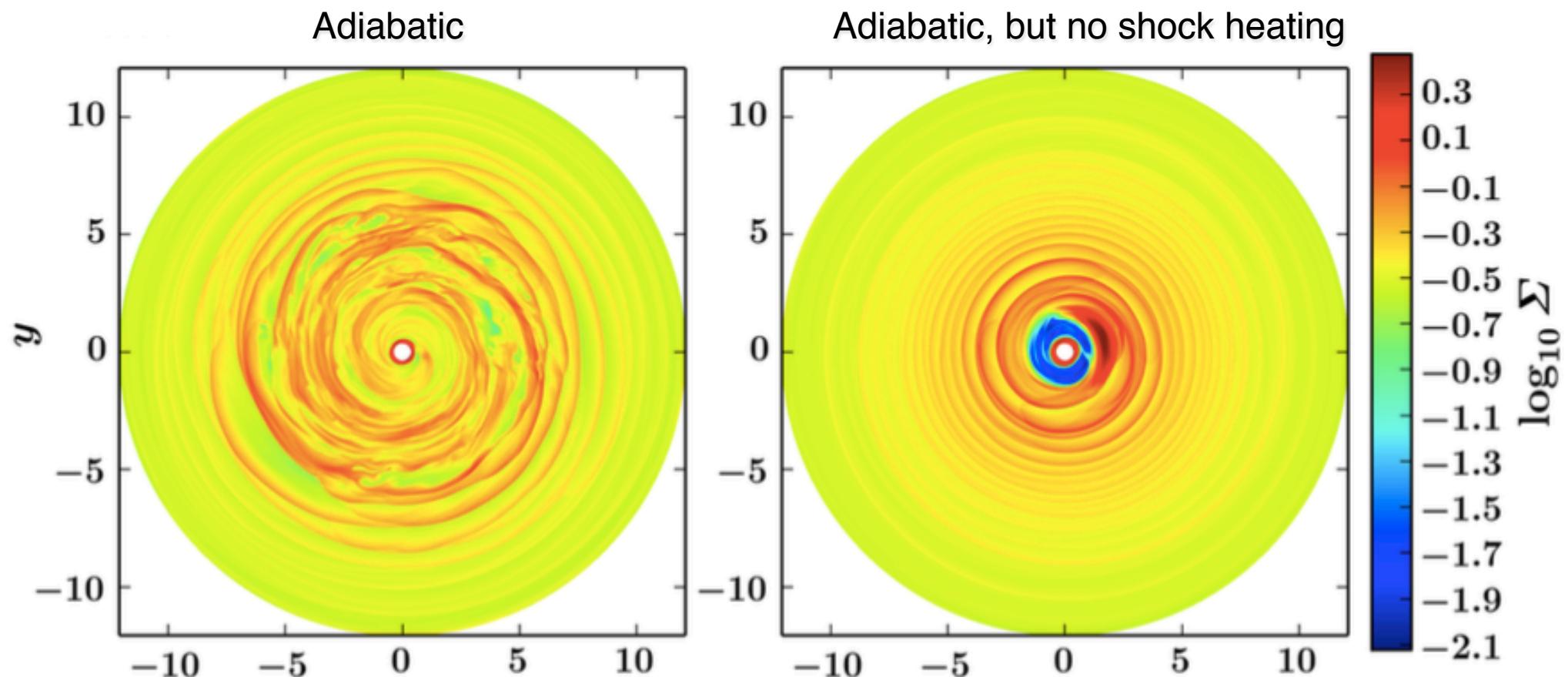


Richert et al. (2015)

Shows up for high-mass planets in adiabatic disks



The energy source: shock heating!



Disk structure

$$T \frac{Ds}{Dt} = -c_V \frac{(T - T_{\text{ref}})}{t_{\text{cool}}} + \Gamma_{\text{sh}},$$

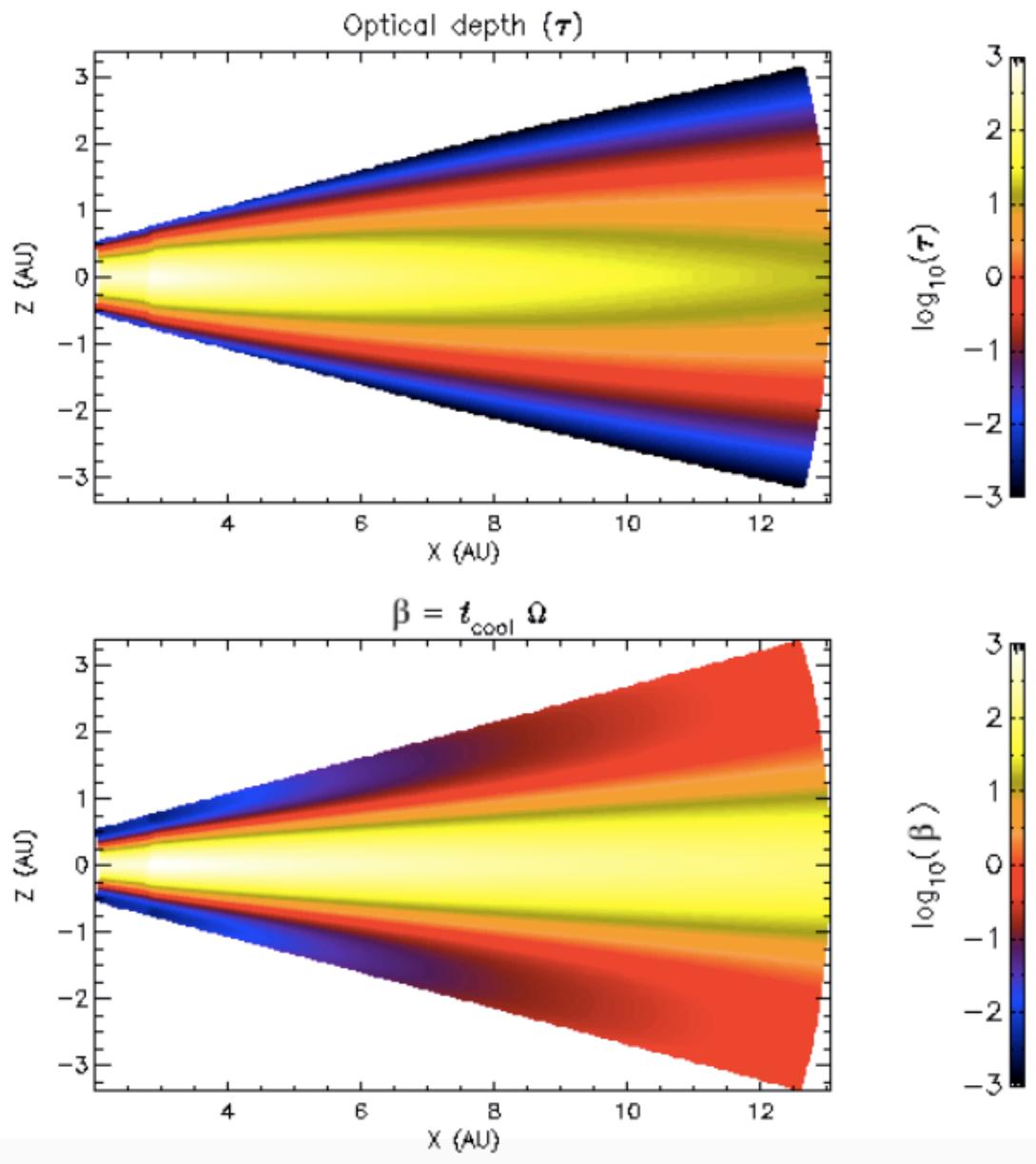
$$t_{\text{rad}} = E / \dot{E}$$

$$\dot{E} = \nabla \cdot F$$

$$t_{\text{cool}} \equiv \frac{\int E dV}{\int F \hat{n} \cdot dA}.$$

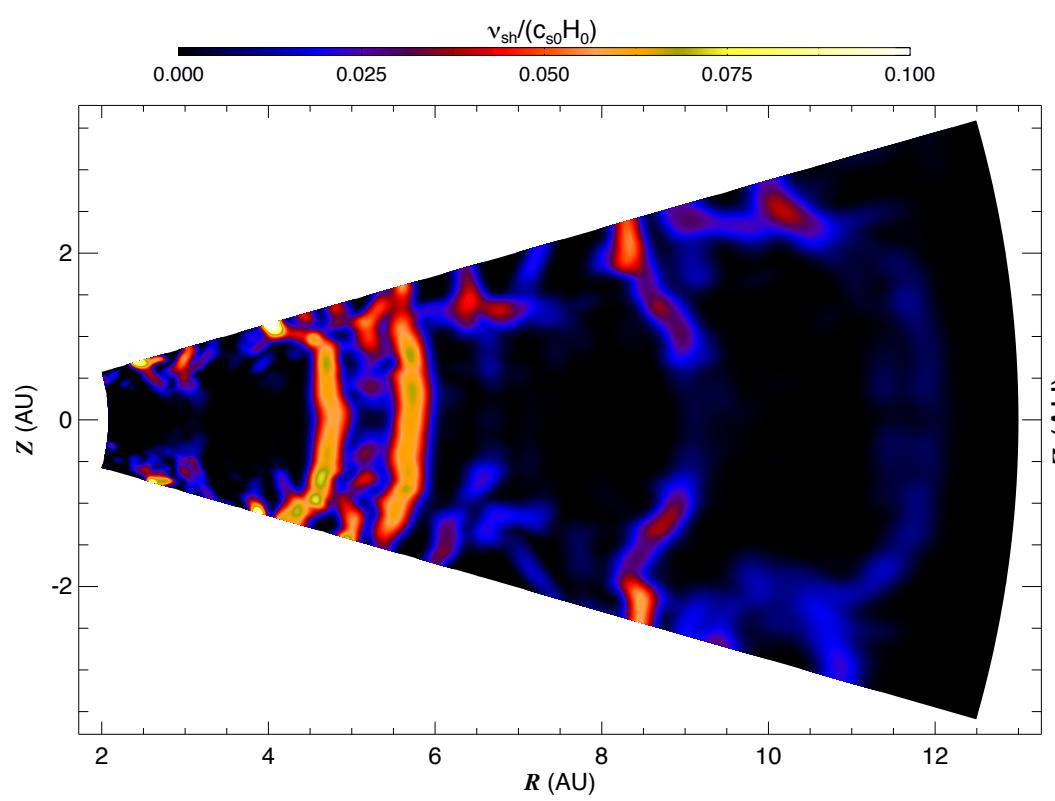
$$t_{\text{cool}} = \frac{c_V \rho H \tau_{\text{eff}}}{3\sigma T^3}.$$

$$\tau_{\text{eff}} = \frac{3\tau}{8} + \frac{\sqrt{3}}{4} + \frac{1}{4\tau}.$$

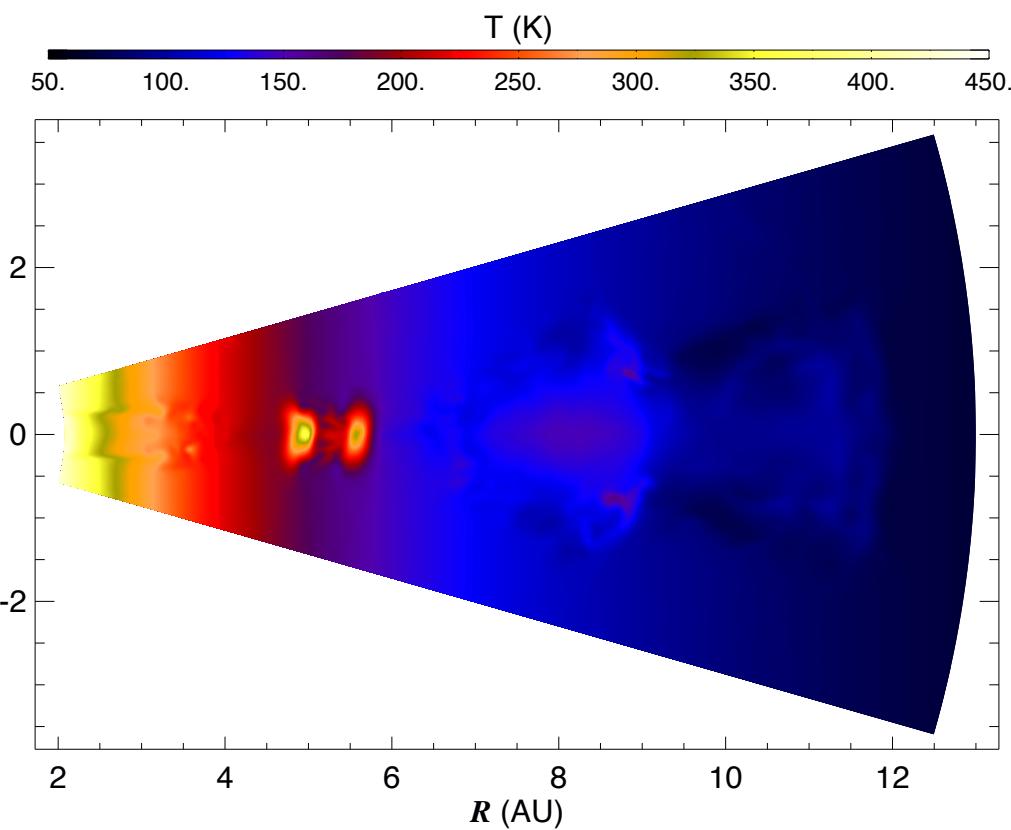


Shock bores

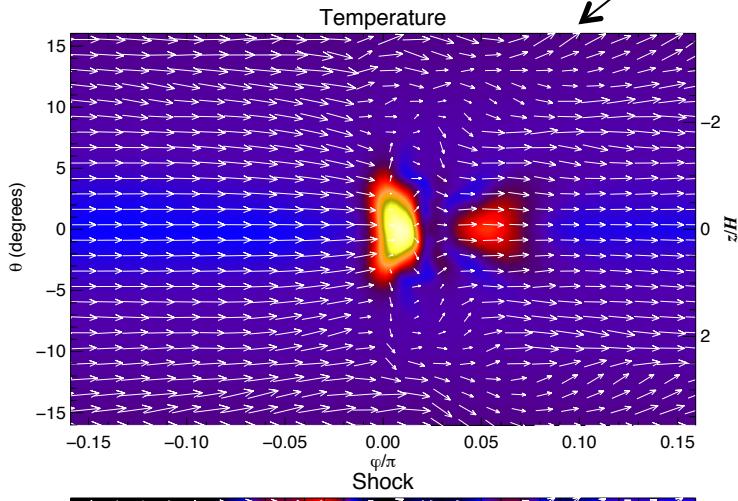
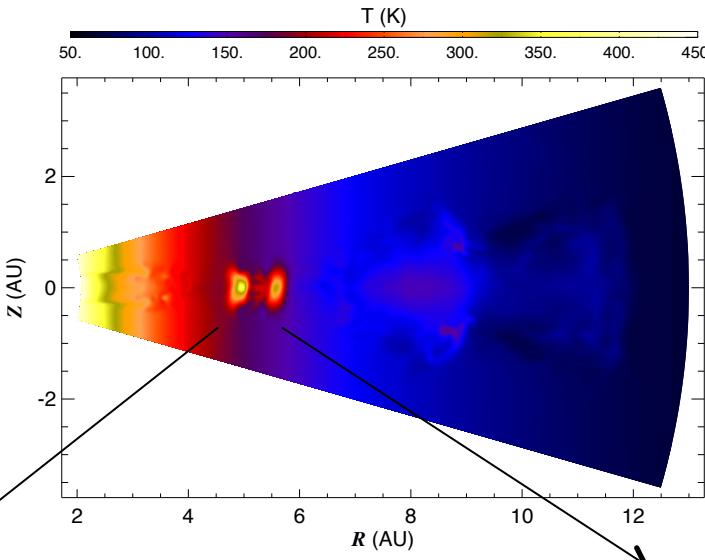
Velocity convergence



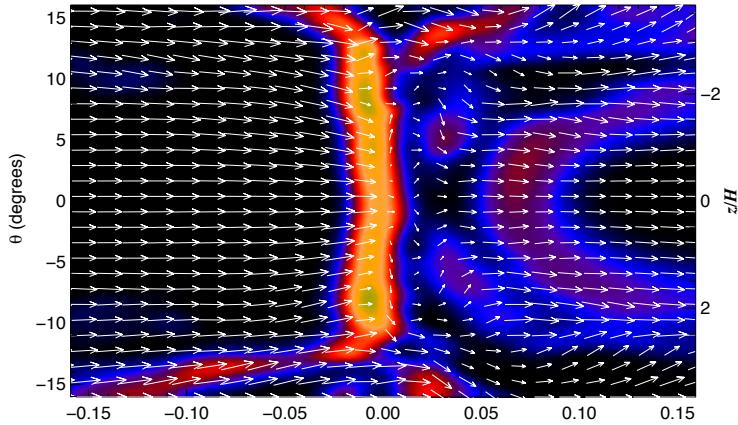
Temperature



3D shocks: bores and breaking waves

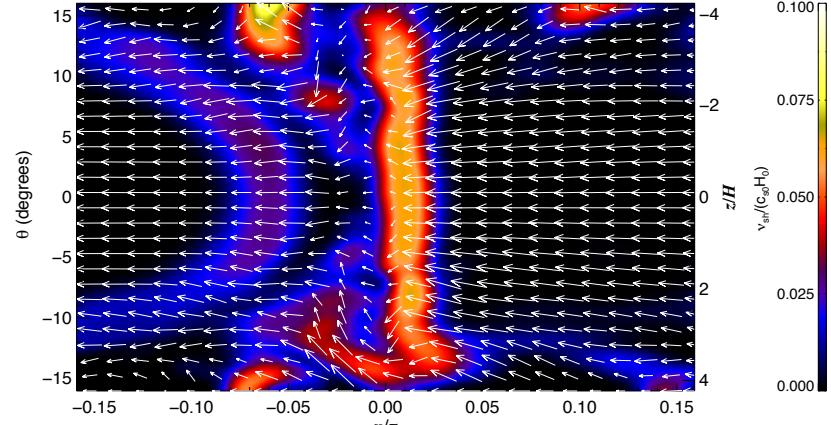
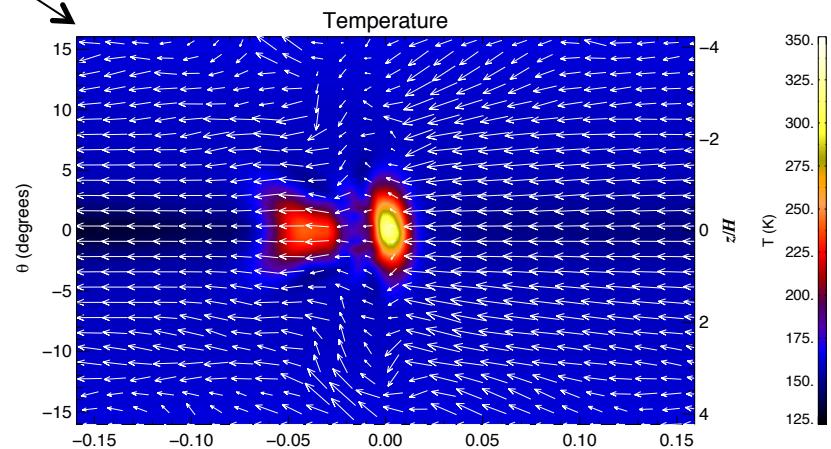


Temperature



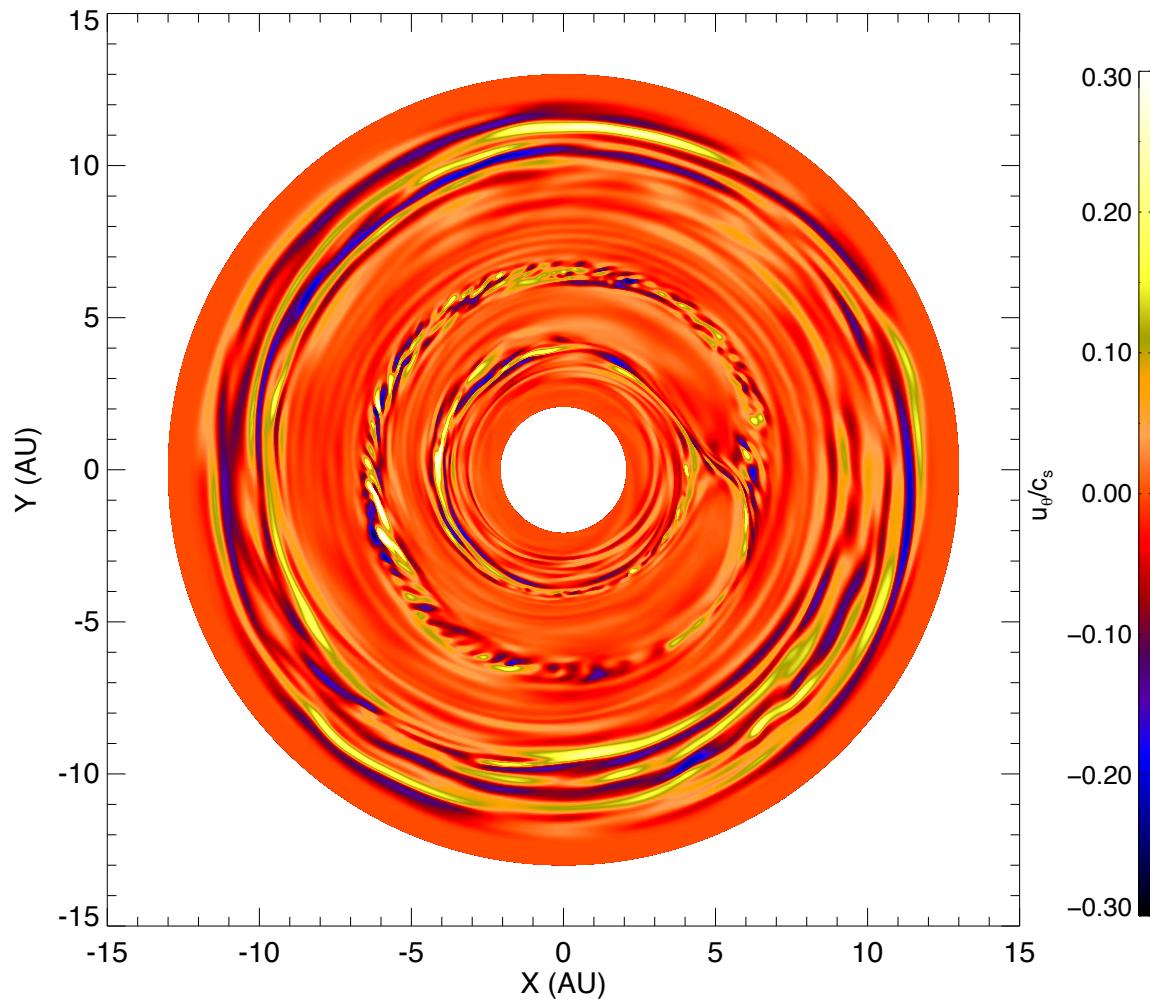
Shock

Div u
(shock)

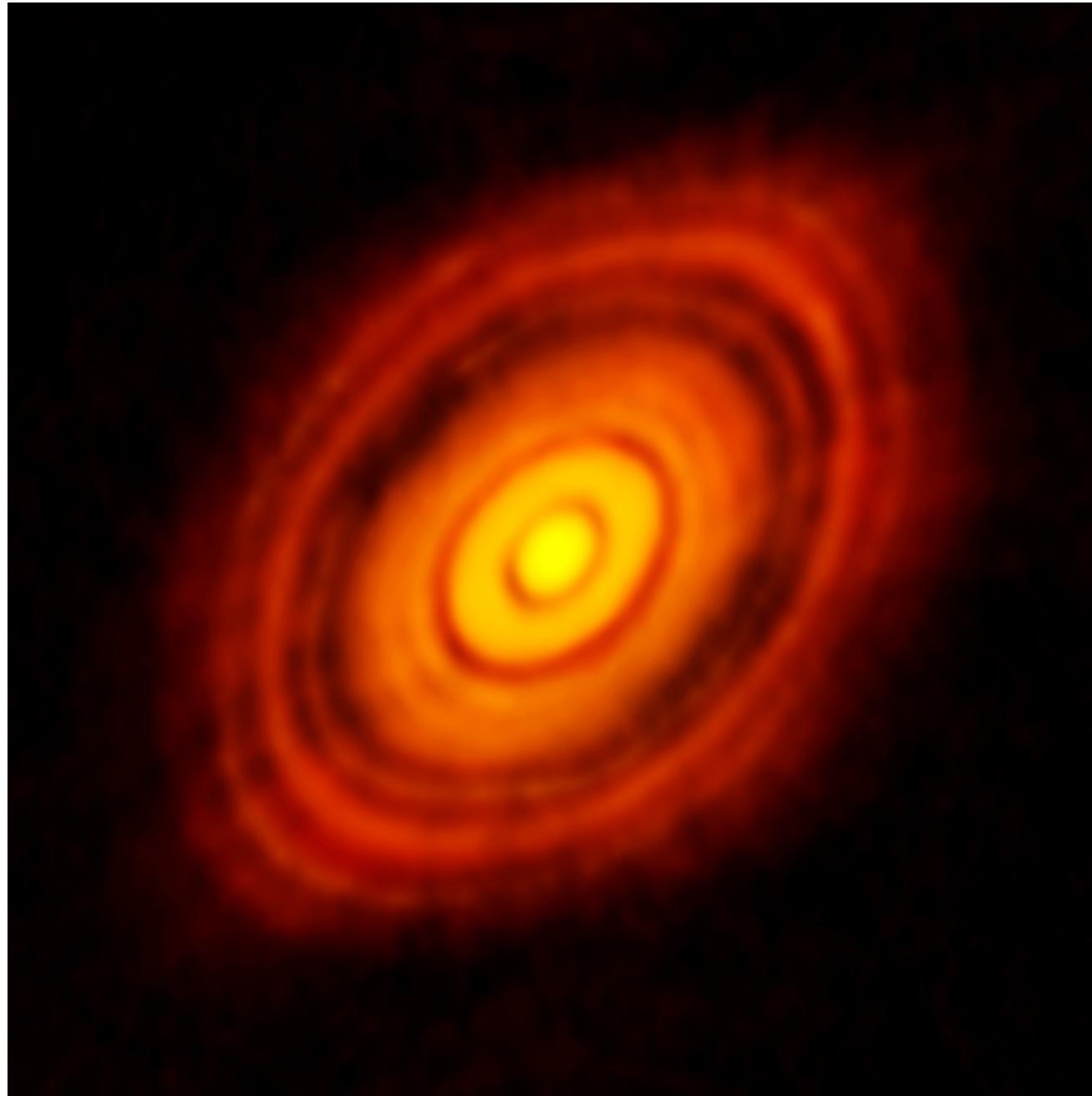


Lyra et al. (2015b, submitted)

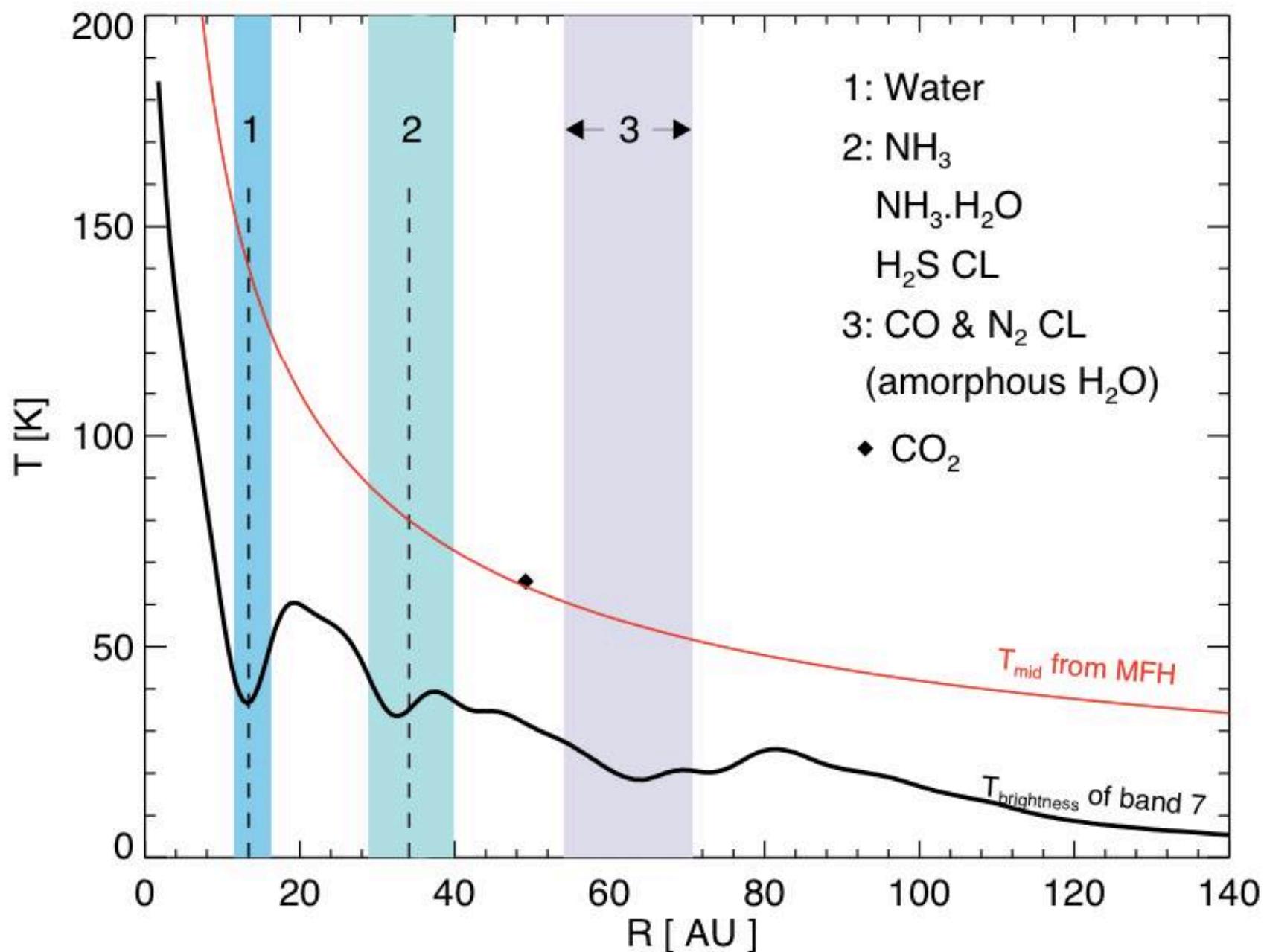
Turbulent surf



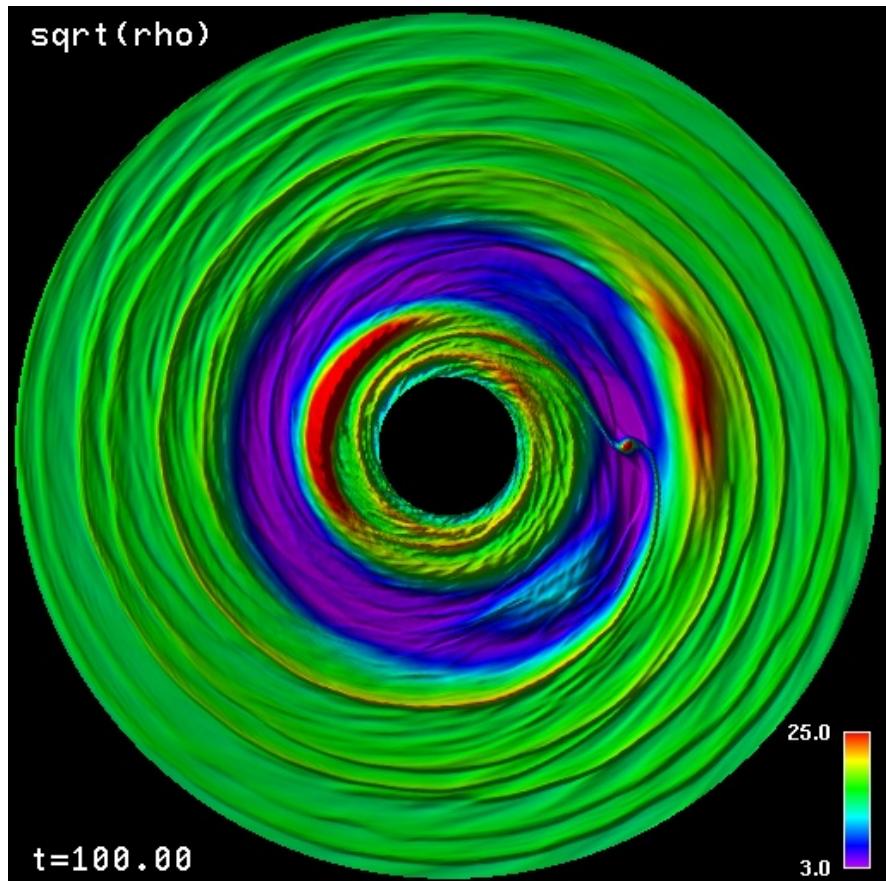
HL Tau



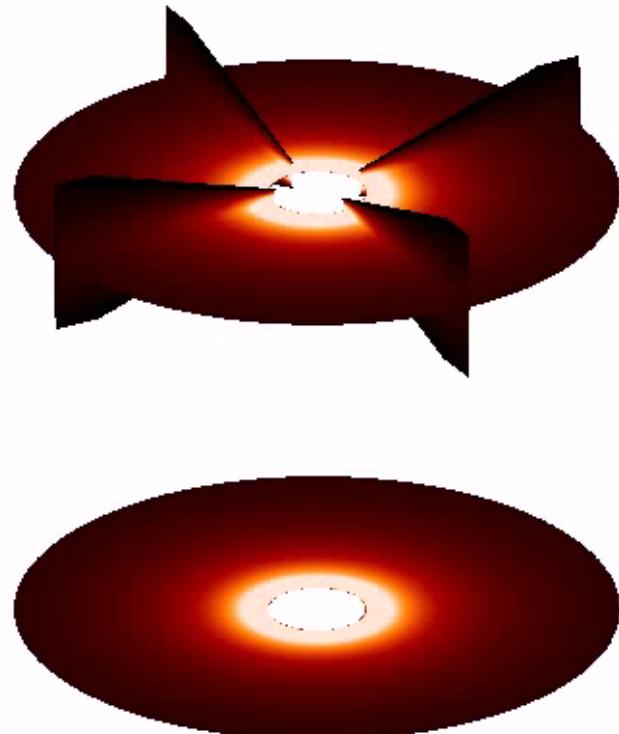
HL Tau



Planet-disk interaction: gaps, spirals, and vortices.



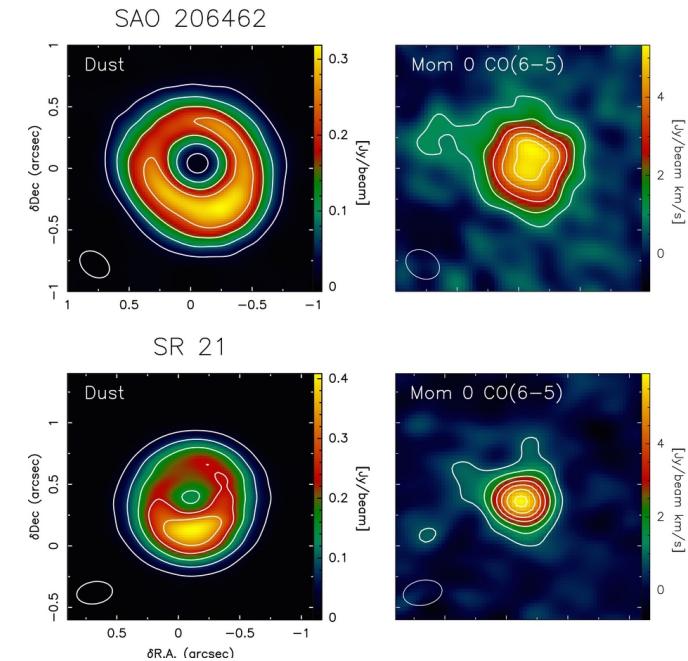
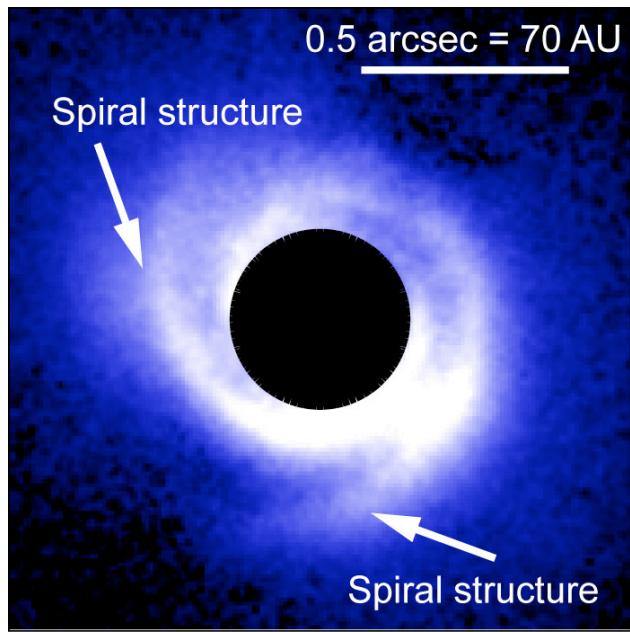
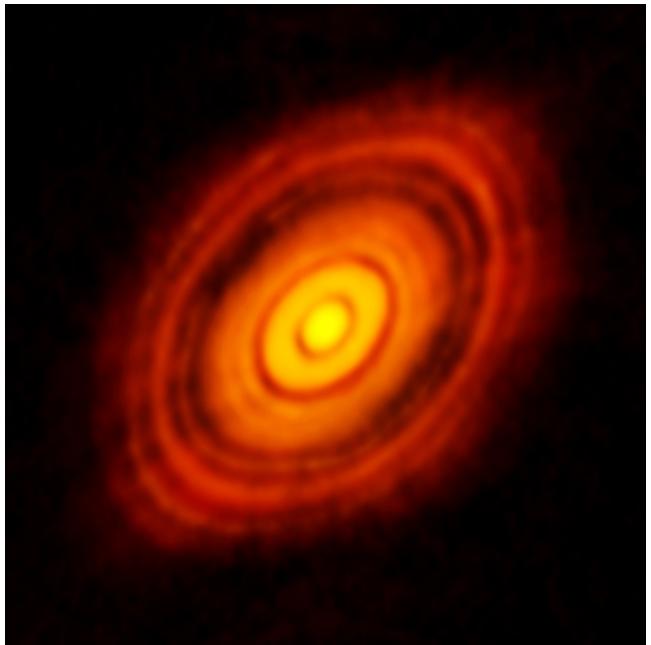
$t = 0.1$



Lyra (2009)

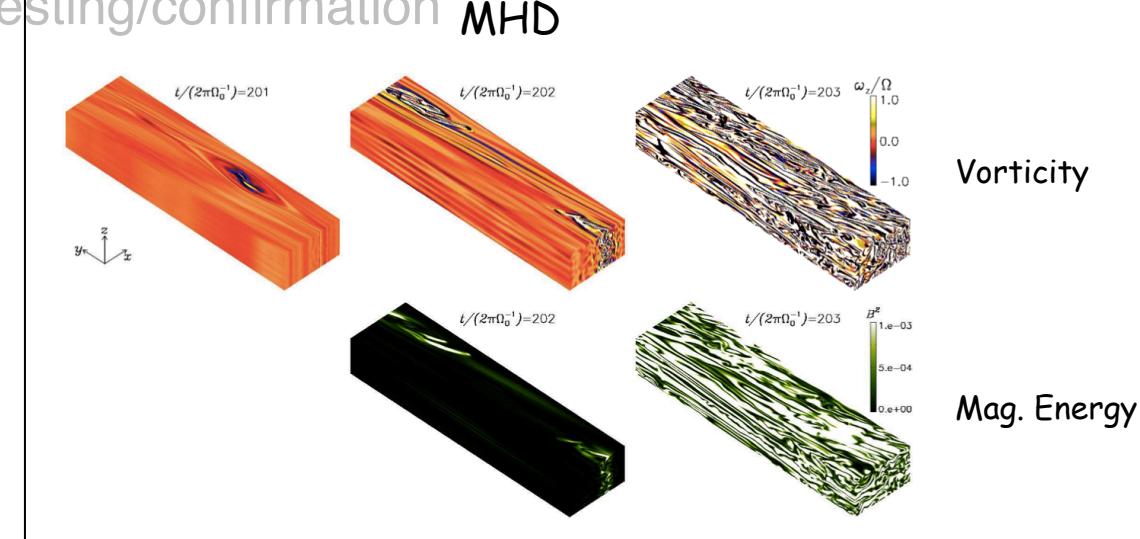
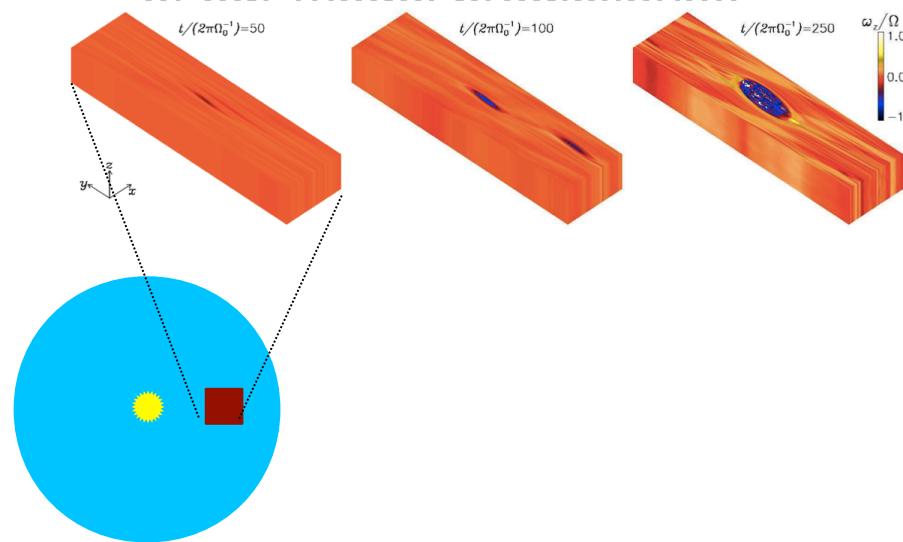
See Clement Baruteau's talk

Observational evidence: gaps, spirals, and vortices



Conclusions

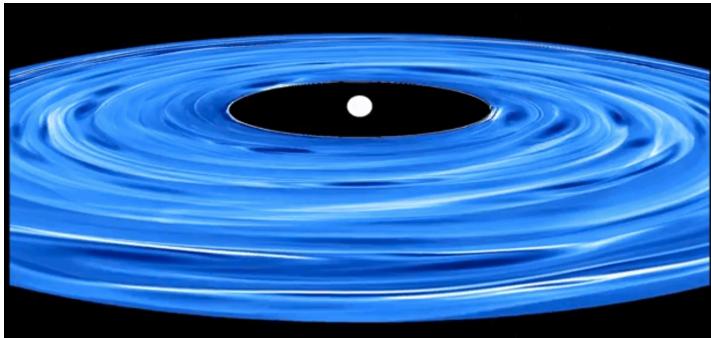
- Vortices exist in the dead zone only
- Two sustenance modes: Kelvin-Helmholtz Instability and Convective Overstability
- Vortex-assisted and streaming instability are complementary
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Rossby wave instability may be the culprit of these dust traps
- We're in the era of observational testing/confirmation **Hydro MHD** of our model predictions!!



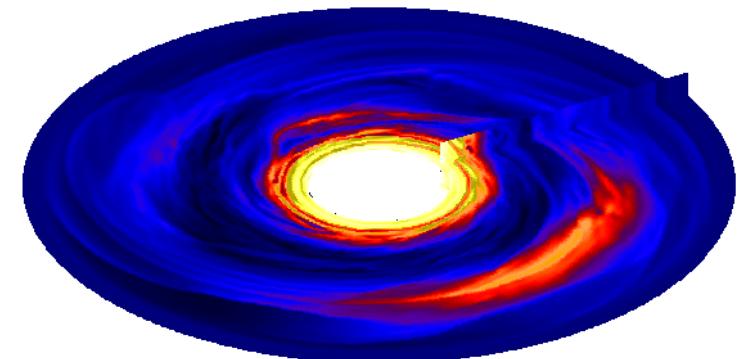
Conclusions

- Vortices exist in the dead zone only
- Two sustenance modes: Kelvin-Helmholtz Instability and Convective Overstability
- Vortex-assisted is a complementary formation mode to streaming instability
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Rossby wave instability may be the culprit of these dust traps
- We're in the era of observational testing/cor

Baroclinic instability



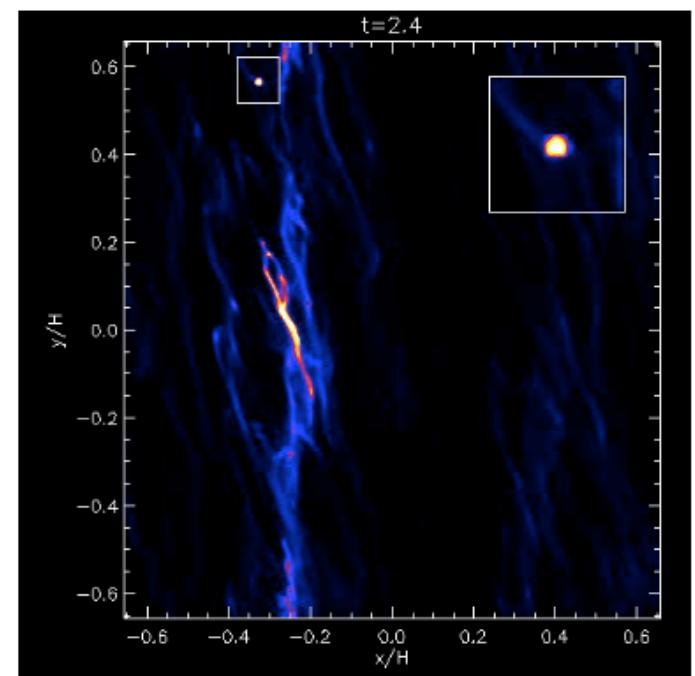
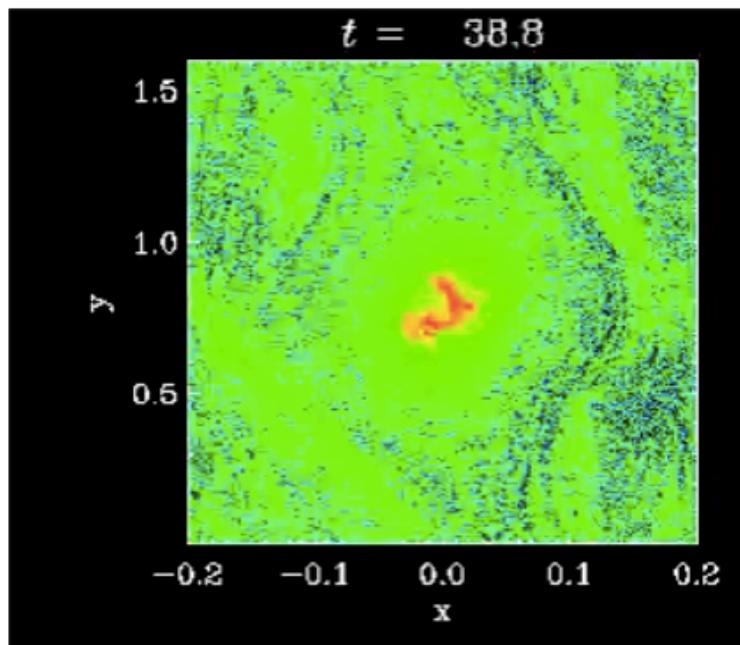
Rossby wave instability



Conclusions

- Vortices exist in the dead zone only
- Two sustenance modes: Kelvin-Helmholtz Instability and Convective Overstability
- Vortex-assisted and streaming instability are complementary
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Kelvin-Helmholtz instability may be the culprit of these dust traps

VI. VORTEX MODELLING PREDICTIONS:

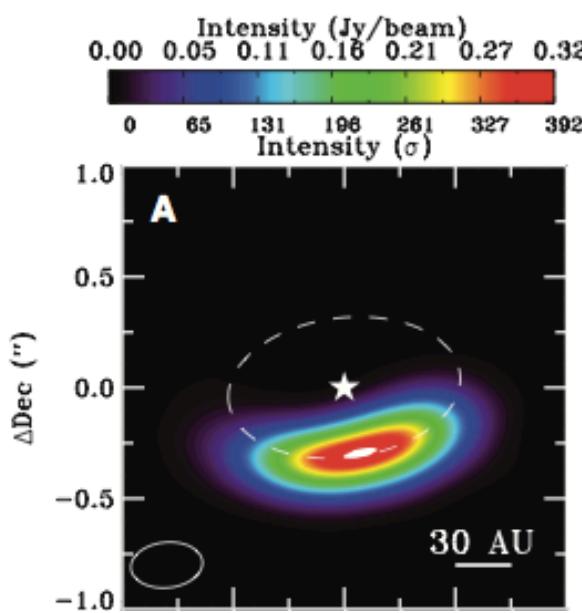
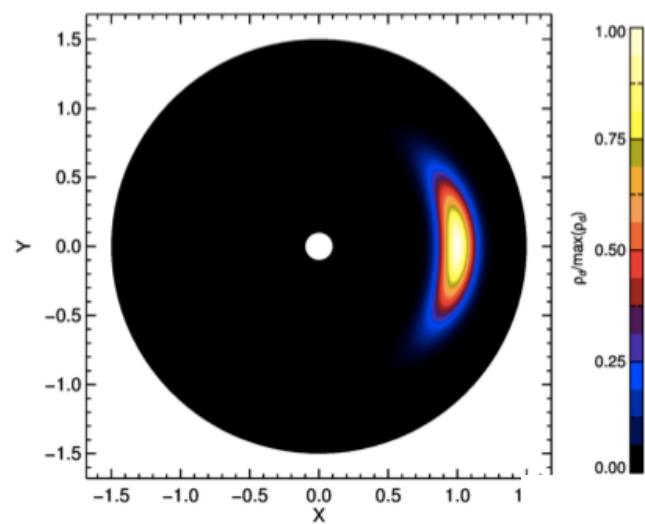


Conclusions

- Vortices exist in the dead zone
- Two sustenance modes: Rossby wave and vortex
- Vortex-assisted and streamwise diffusion
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Rossby wave instability may be the culprit of these dust traps
- We're in the era of observational tests of our model predictions!!

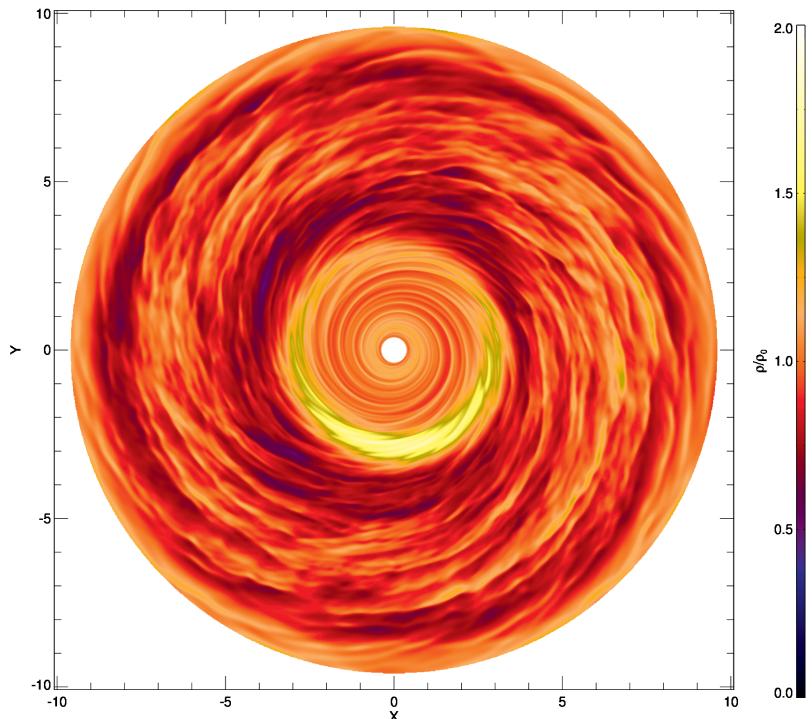
$$\rho_d(a,z) = \epsilon \rho_0 (S+1)^{3/2} \exp \left\{ - \frac{[a^2 f^2(\chi) + z^2]}{2H^2} (S+1) \right\}$$

Lyra & Lin (2013)



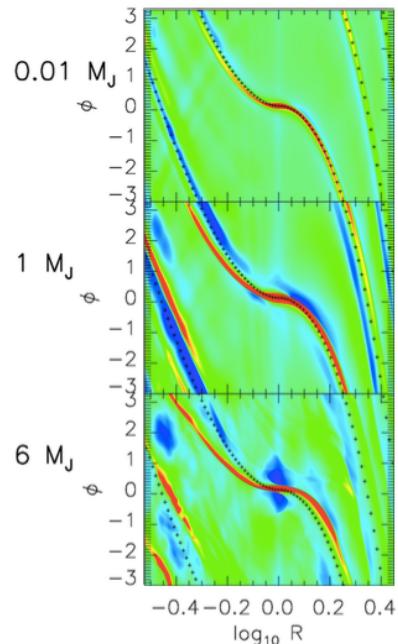
Conclusions

- Vortices exist in the dead zone only
- Two sustenance modes: Kelvin-Helmholtz Instability and Convective Overstability
- Vortex-assisted and streaming instability are complementary
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- **Kelvin-Helmholtz instability may be the culprit of these dust traps**
- We're in the era of observational testing/coin of our model predictions!!

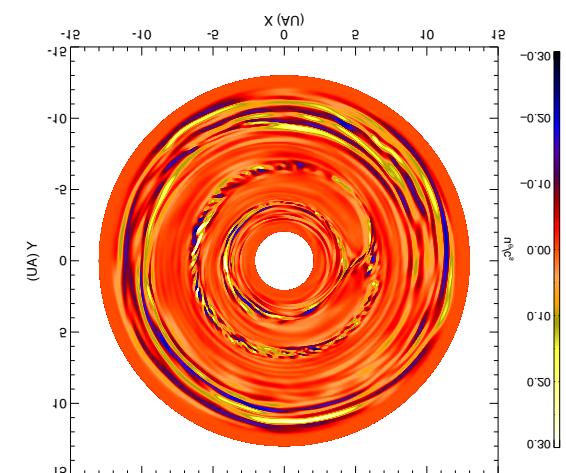
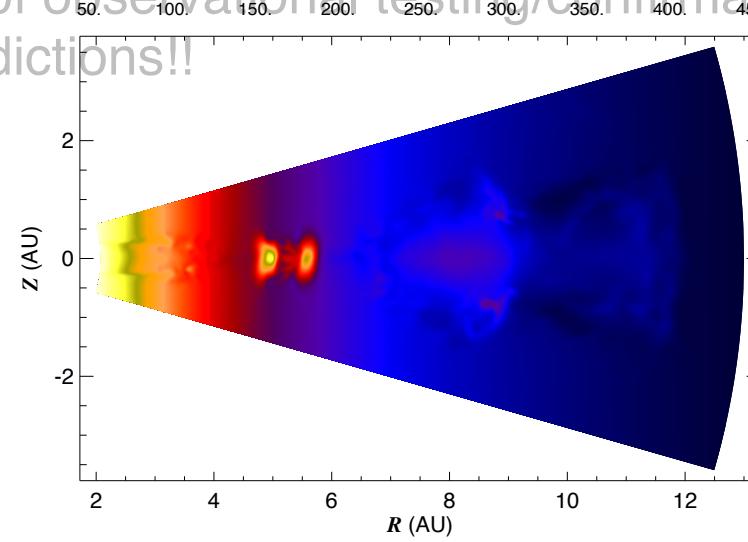


Conclusions

- Vortices exist in the dead zone only
- Two sustenance modes: Kelvin-Helmholtz Instability and Convective Overstability
- Vortex-assisted and streaming instability are complementary
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Kelvin-Helmholtz instability may be the culprit of these dust traps
- Shocks due to high mass planets yield good fits to observed spirals.

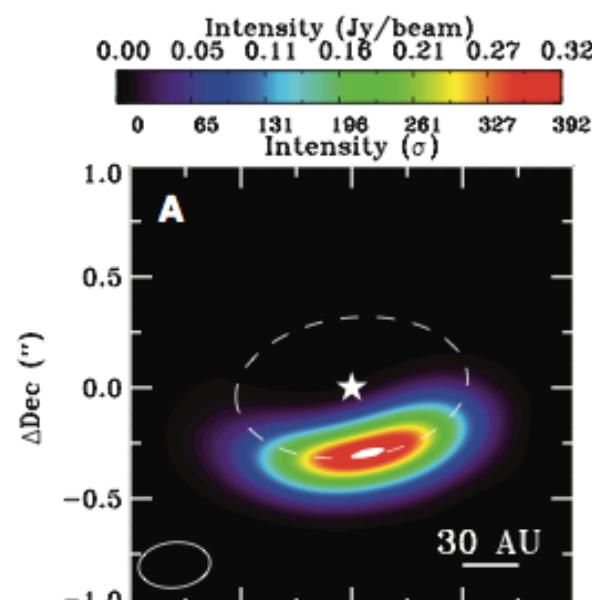
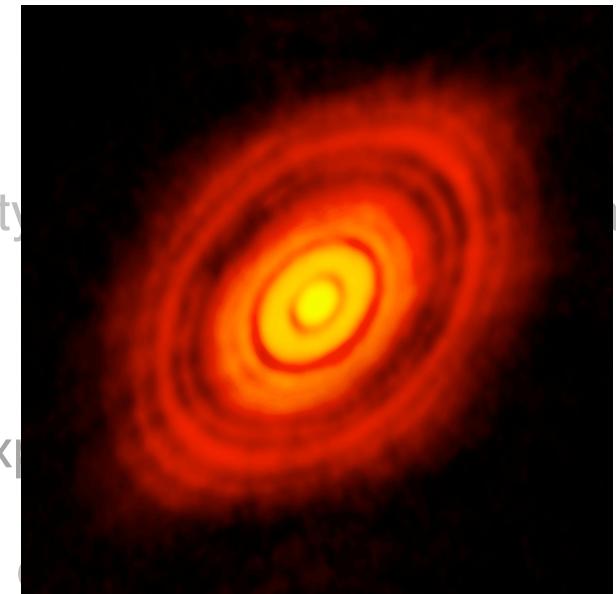
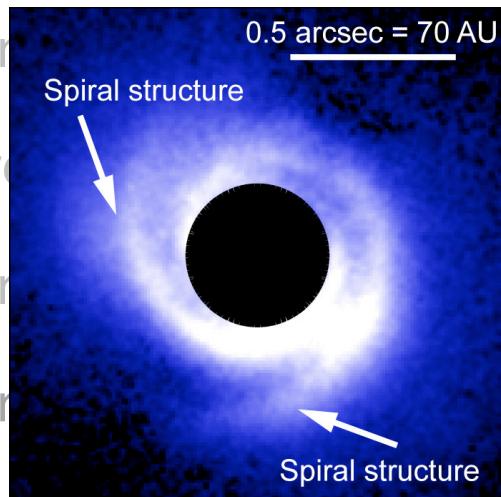


a of observational testing/confirmation predictions!!



Conclusions

- Vortices are found in the hot zone only
- Twists are associated with Kelvin-Helmholtz Instability
- Vortices are associated with vorticity
- Vortices are associated with drag-diffusion equilibrium experiments
- Rossby wave instability may be the culprit of these structures
- We're in the era of observational testing/confirmation of our model predictions!!



Conclusions

- Vortices e
- Two sustai
- Vortex-ass
- Vortex-tra
- Rossby w
- We're in th
- of our mode

