

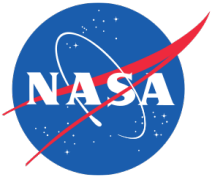
Evolution of MU69

from a binary planetesimal into contact
via Kozai-Lidov oscillations and nebular drag



Wladimir Lyra
New Mexico State University

Funding



NFDAP – 2019
XRP – 2018
XRP - 2016



NRAO - 2017



HST - 2016

Computational Facilities



EVOLUTION OF MU69 FROM A BINARY PLANETESIMAL INTO CONTACT BY KOZAI-LIDOV OSCILLATIONS AND NEBULAR DRAG

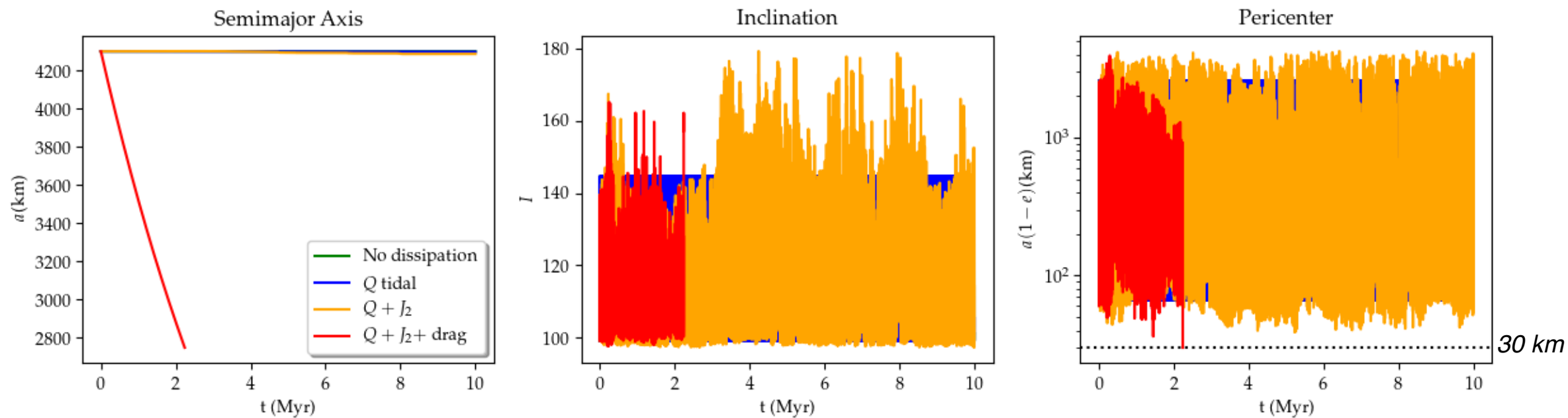
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Draft version March 2, 2020

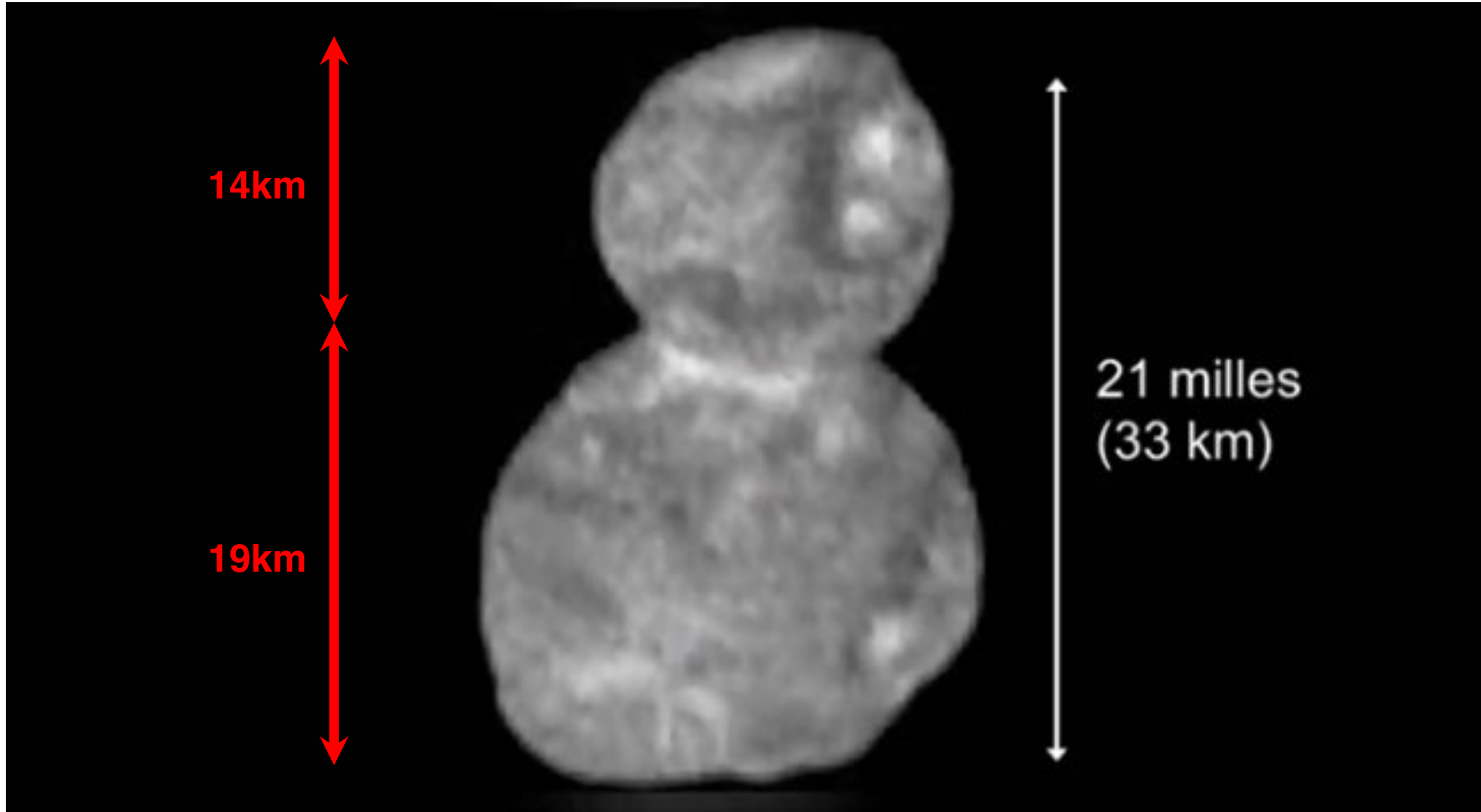
ABSTRACT

The New Horizons flyby of the cold classical Kuiper Belt object MU69 showed it to be a contact binary. The existence of other contact binaries in the 1–10 km range raises the question of how common these bodies are and how they evolved into contact. Here we consider that the pre-contact lobes of MU69 formed as a binary embedded in the Solar nebula, and calculate its subsequent orbital evolution in the presence of gas drag. We find that the sub-Keplerian wind of the disk brings the drag timescales for 10 km bodies to under 1 Myr for quadratic-velocity drag, which is valid in the asteroid belt. In the Kuiper belt, however, the drag is linear with velocity and the effect of the wind cancels out as the angular momentum gained in half an orbit is exactly lost in the other half; the drag timescales for 10 km bodies remain $\gtrsim 10$ Myr. In this situation we find that a combination of nebular drag and Kozai-Lidov oscillations is a promising channel for collapse. We analytically solve the hierarchical three-body problem with nebular drag and implement it into a Kozai cycles plus tidal friction model. The permanent quadrupoles of the pre-merger lobes make the Kozai oscillations stochastic, and we find that when gas drag is included the shrinking of the semimajor axis more easily allows the stochastic fluctuations to bring the system into contact. Evolution to contact happens very rapidly (within 10^4 yr) in the pure, double-average quadrupole, Kozai region between $\approx 85^\circ - 95^\circ$, and within 3 Myr in the drag-assisted region beyond it. The synergy between J_2 and gas drag widens the window of contact to $80^\circ - 100^\circ$ initial inclination, over a larger range of semimajor axes than Kozai and J_2 alone. As such, the model predicts a low initial occurrence of binaries in the asteroid belt, and an initial contact binary fraction of about 10% for the cold classicals in the Kuiper belt. The speed at contact is the orbital velocity; if contact happens at pericenter at high eccentricity, it deviates from the escape velocity only because of the oblateness, independently of the semimajor axis. For MU69, the oblateness leads to a 30% decrease in contact velocity with respect to the escape velocity, the latter scaling with the square root of the density. For mean densities in the range $0.3 - 0.5 \text{ g cm}^{-3}$, the contact velocity should be $3.3 - 4.2 \text{ ms}^{-1}$, in line with the observational evidence from the lack of deformation features and estimate of the tensile strength.

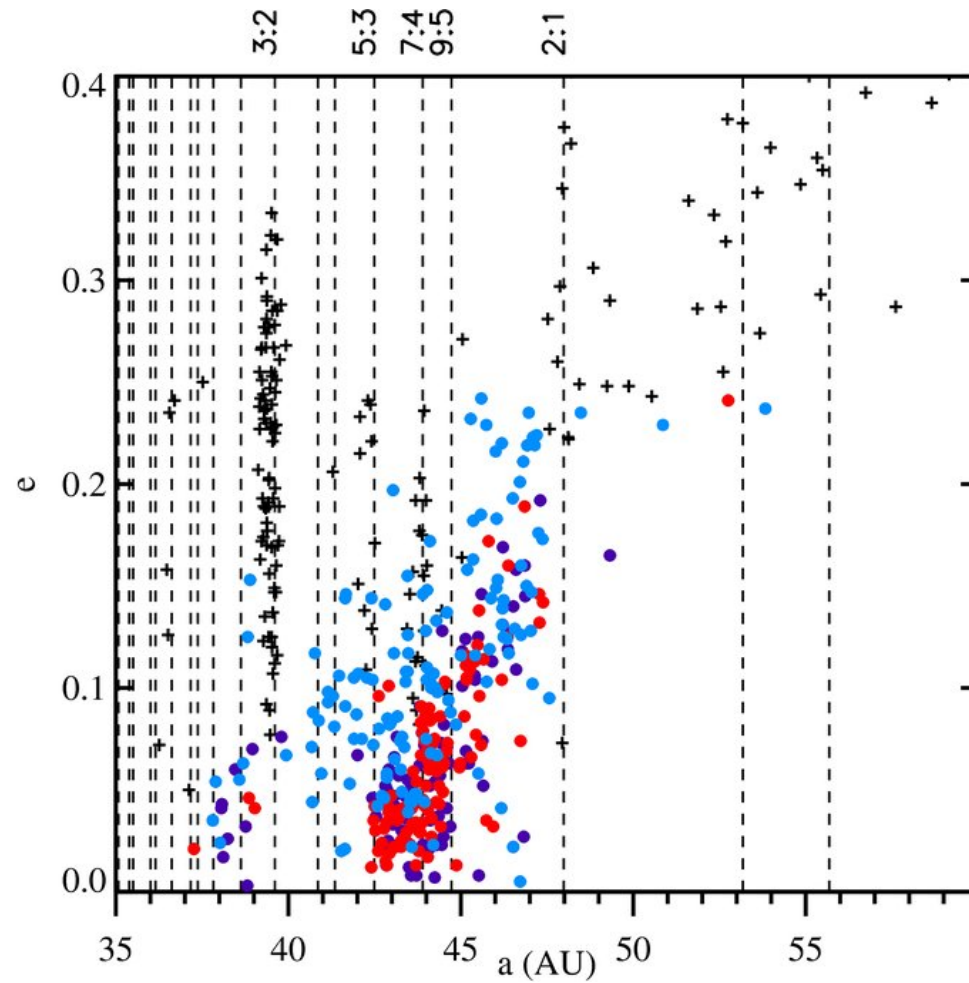
Effect of Drag



MU₆₉: Dimensions



Cold Classical Kuiper Belt Object



+ Resonant and Scattered

Cold Classical $i < 2^\circ$

"Ambiguous" $2^\circ < i < 6^\circ$

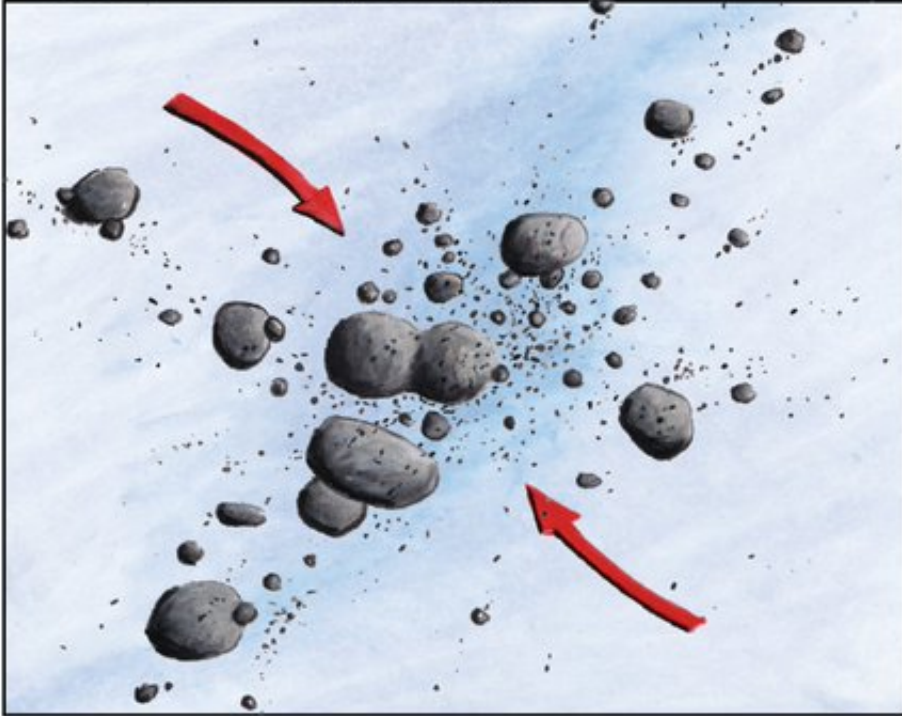
Hot Classicals $i > 6^\circ$

Presumably pristine planetesimals

The Cartoon Image

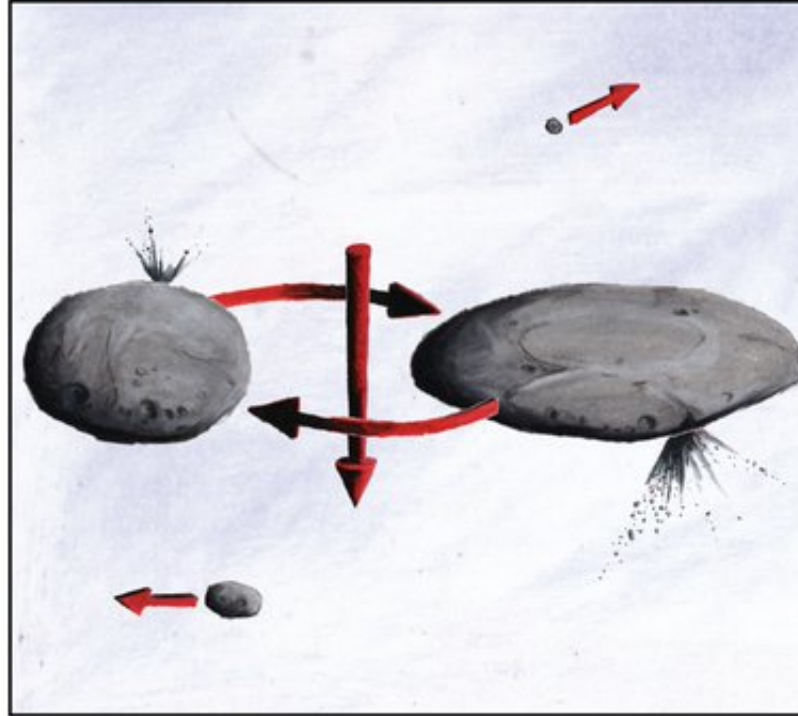
The Formation of 2014 MU69

About 4.5 billion years ago...



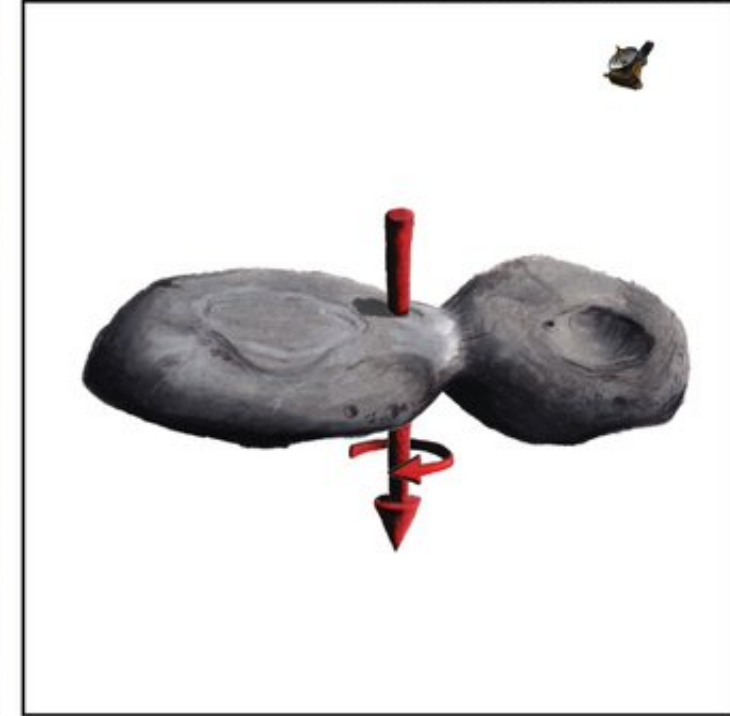
A rotating cloud of small, icy bodies starts to coalesce in the outer solar system.

 New Horizons / NASA / JHUAPL / SwRI / James Tuttle Keane



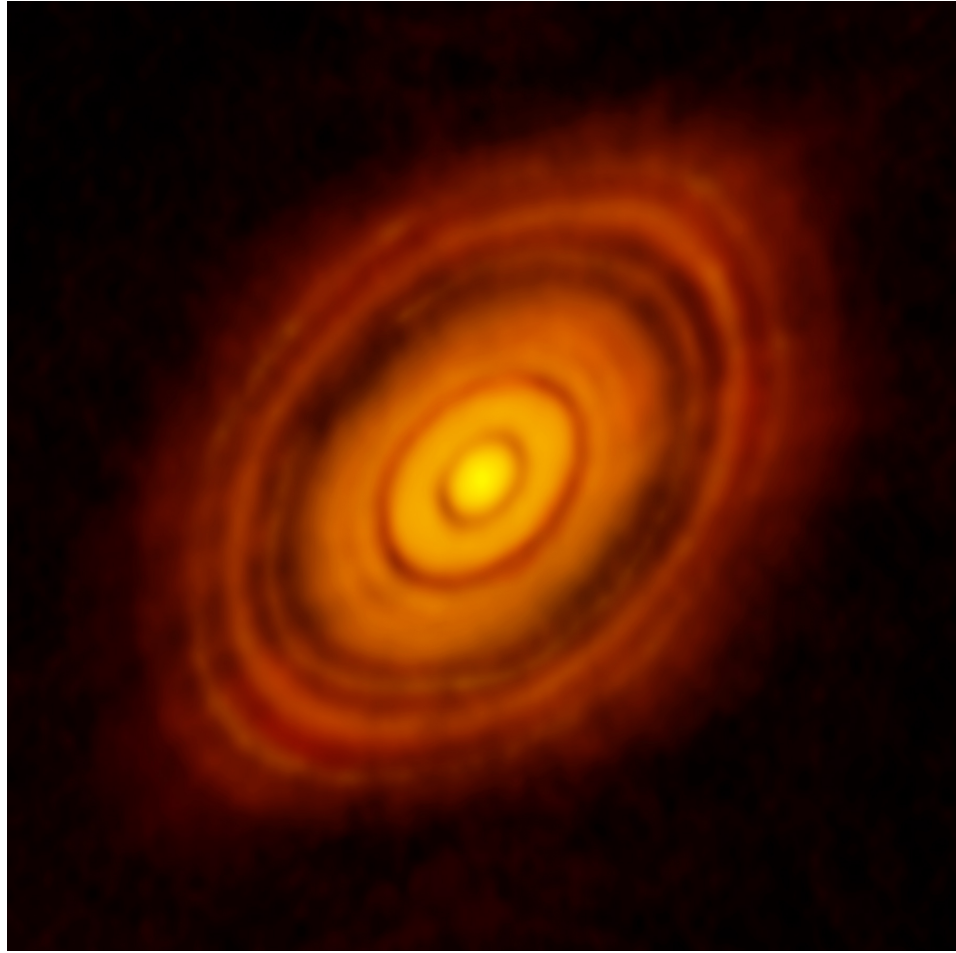
Eventually two larger bodies remain.

...1 January 2019.

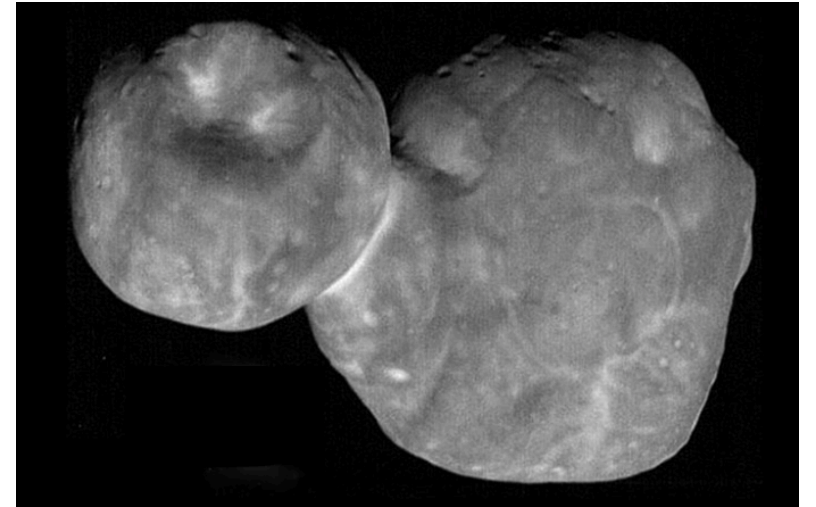


The two bodies slowly spiral closer until they touch, forming the bi-lobed object we see today.

Beyond the cartoon image



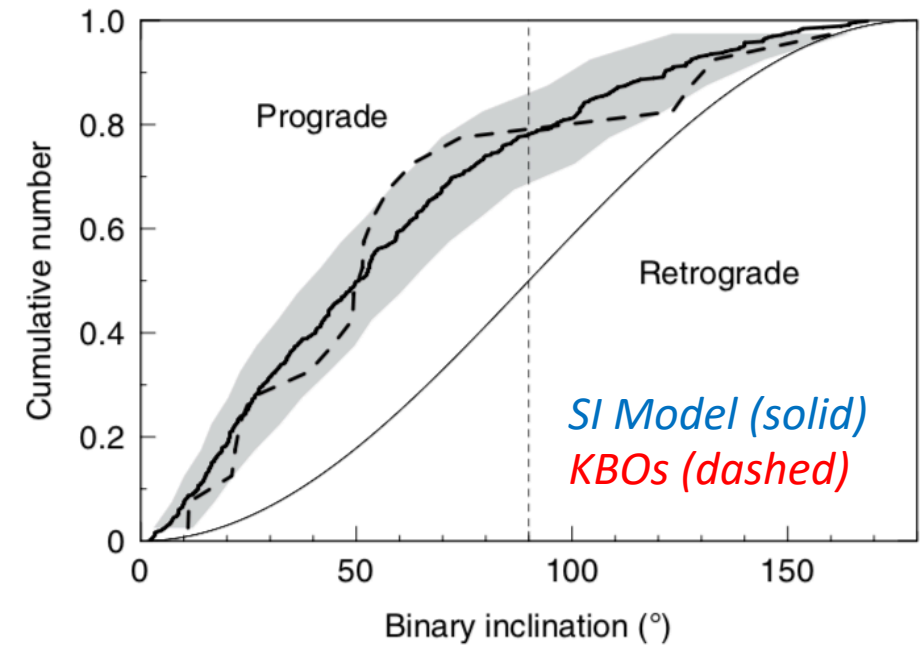
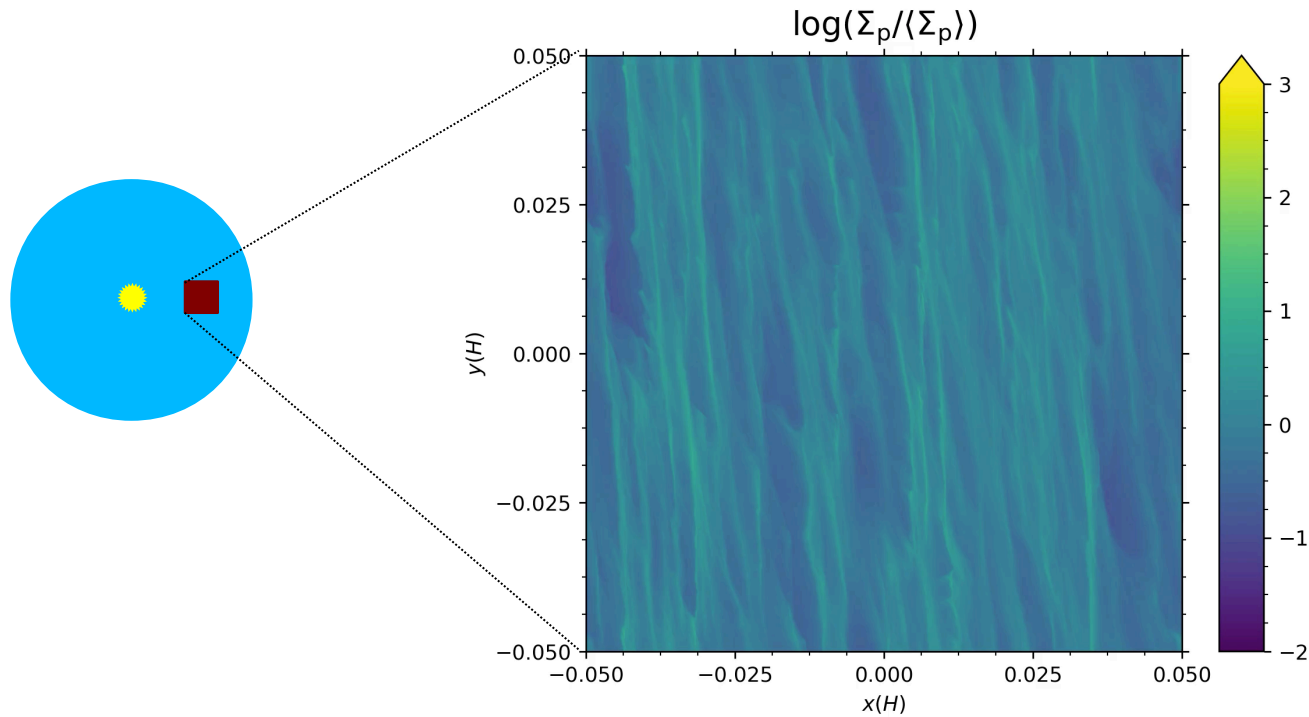
How?



Streaming Instability

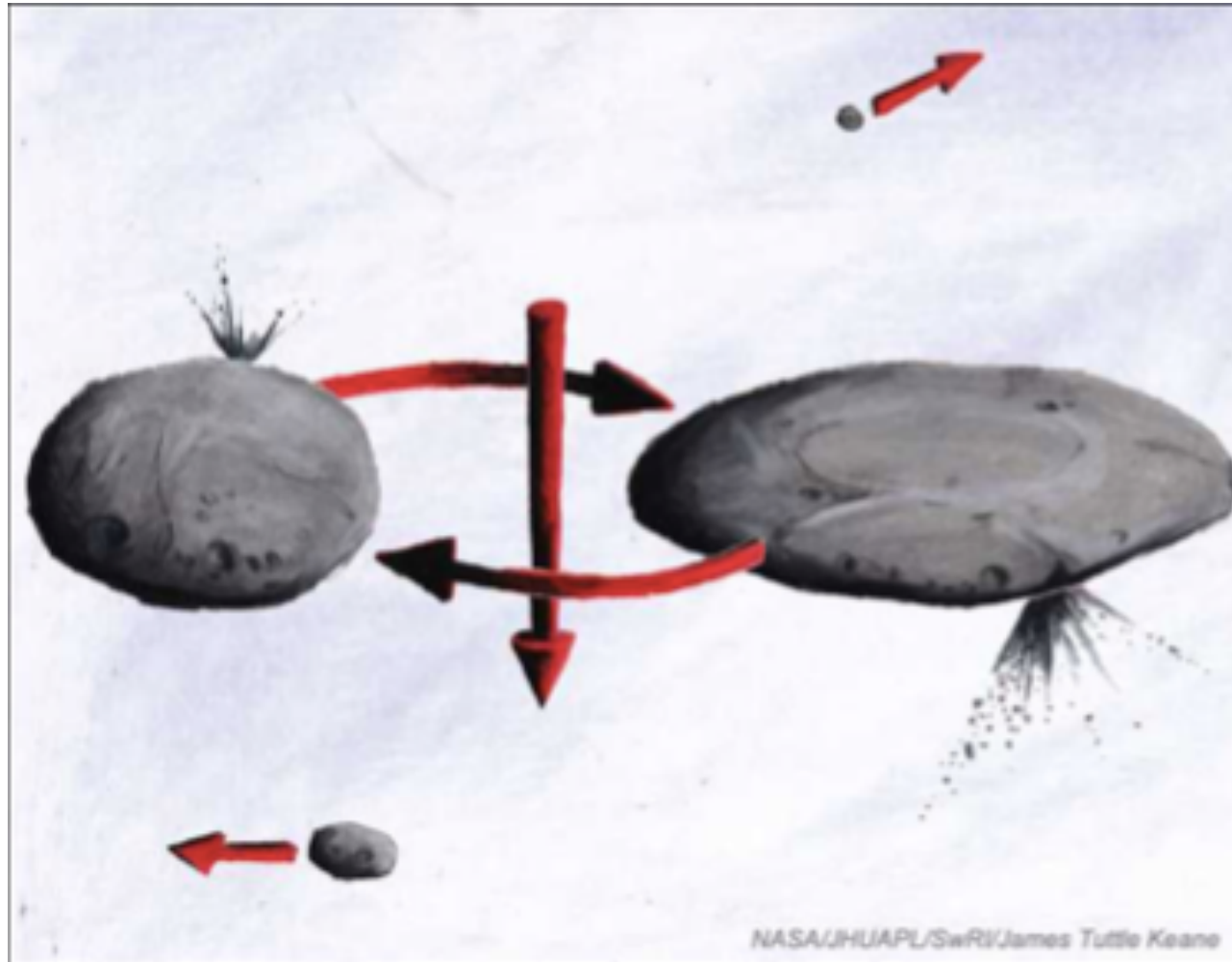
The dust drift is hydrodynamically unstable

Youdin & Goodman (2005), Johansen & Youdin (2007)



Streaming Instability reproduces the
prograde/retrograde distribution of KBO binaries

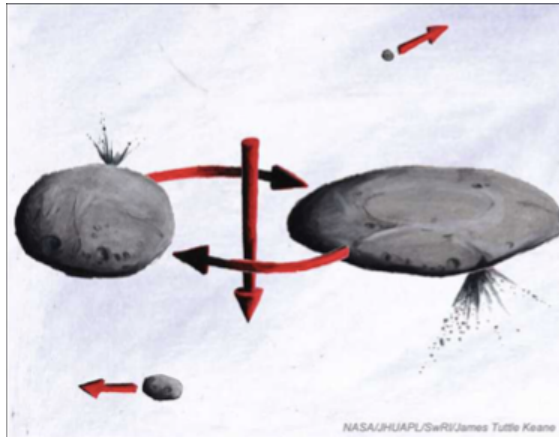
Hardening



Sketch by J.T. Keane

How was angular momentum lost?

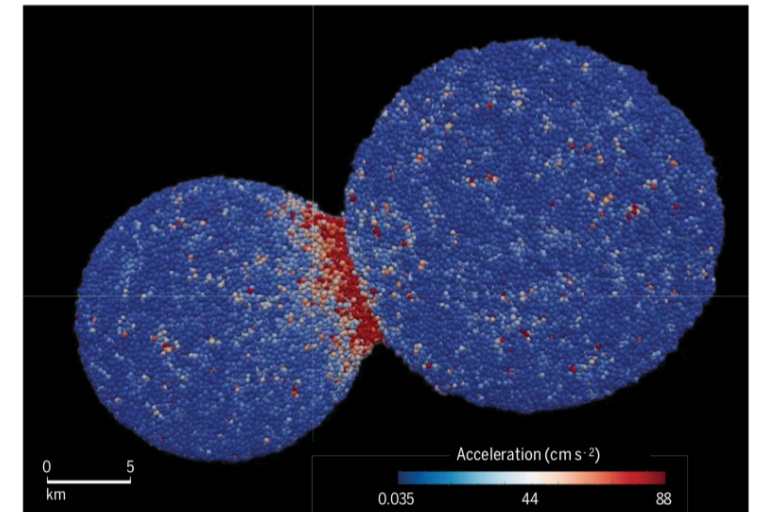
Mutual orbit
(i.e., not captured)



Inferred from:
Alignment of components' axes;
Similar colors.

Sketch by J.T. Keane

Slow merger
($\sim < 5$ m/s)

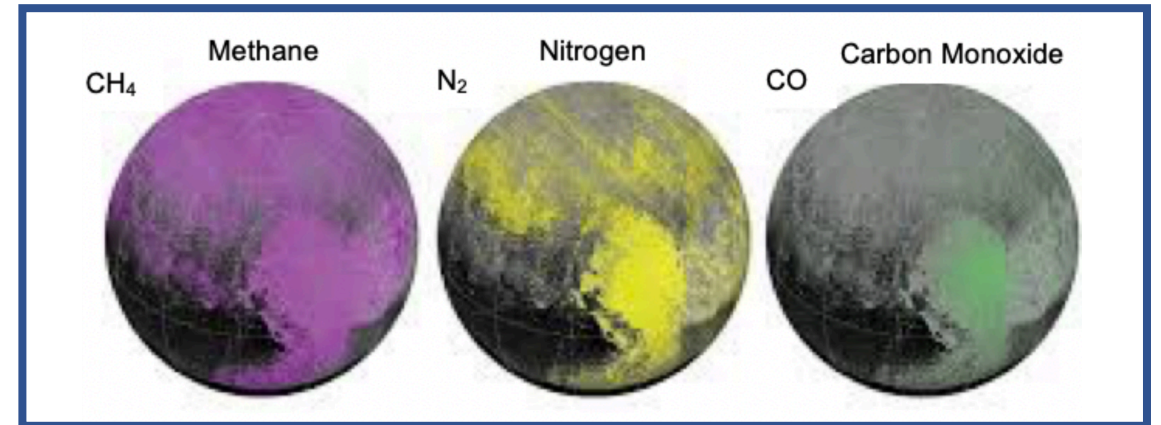
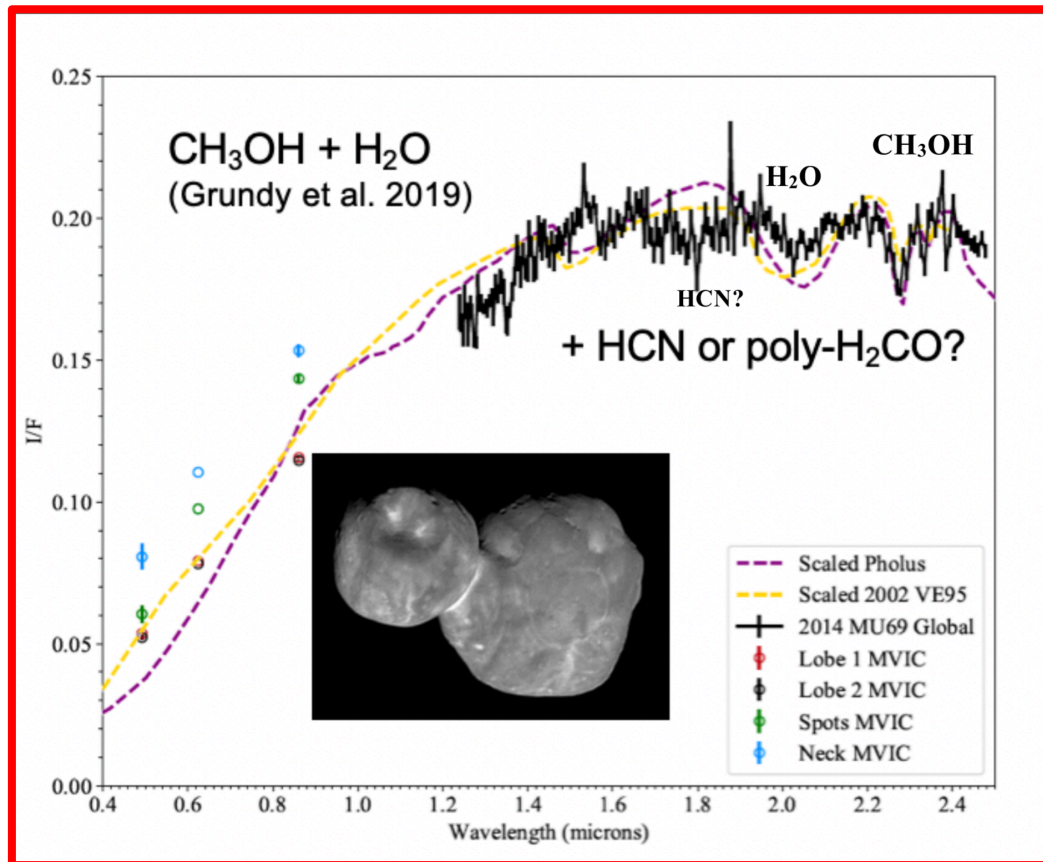


Inferred from:
Negligible evidence for impact damage
SPH simulations

MU69 and Pluto ices are different

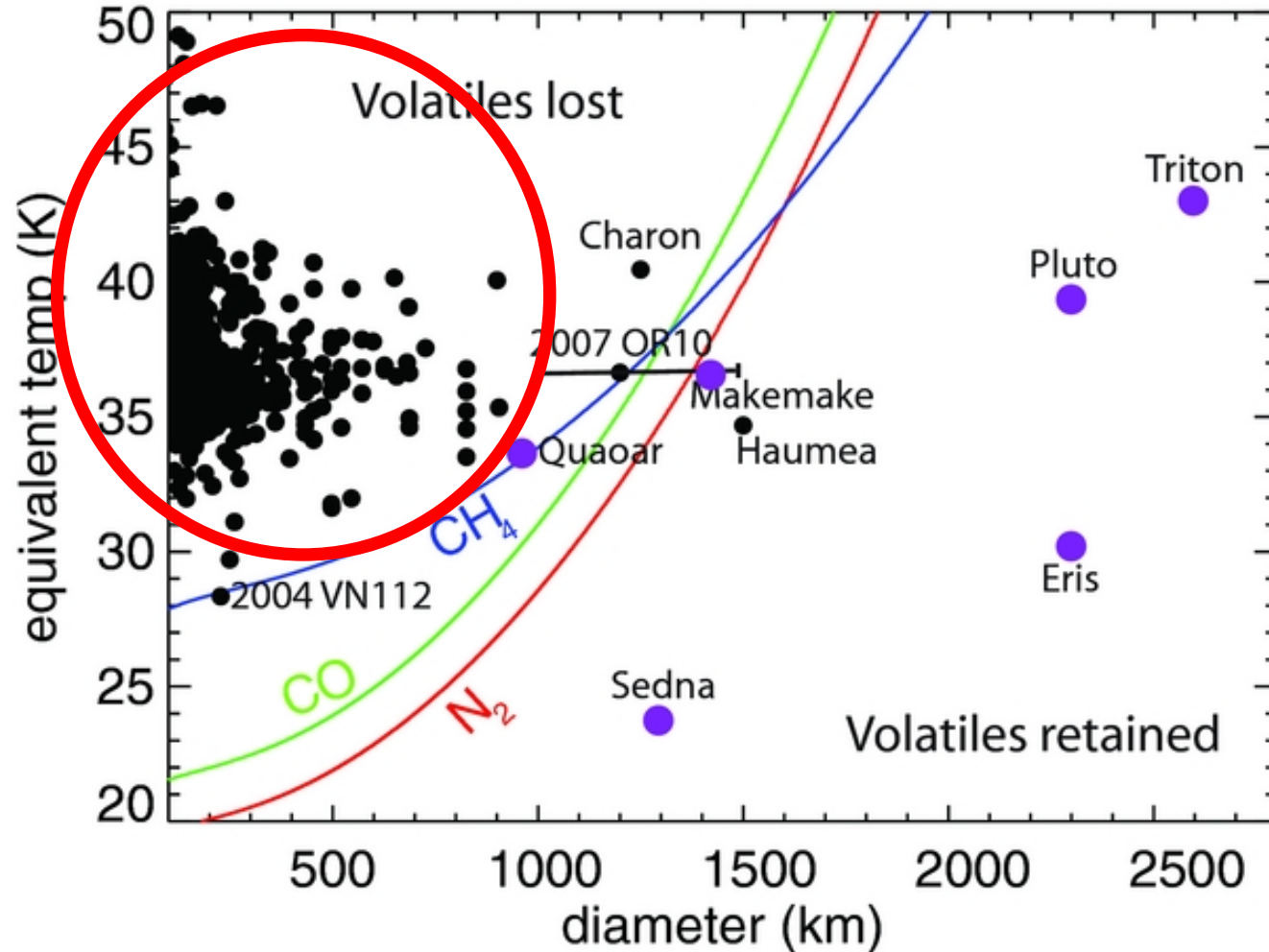
MU69 : Methanol, H₂O, HCN

Pluto : CH₄, N₂, CO



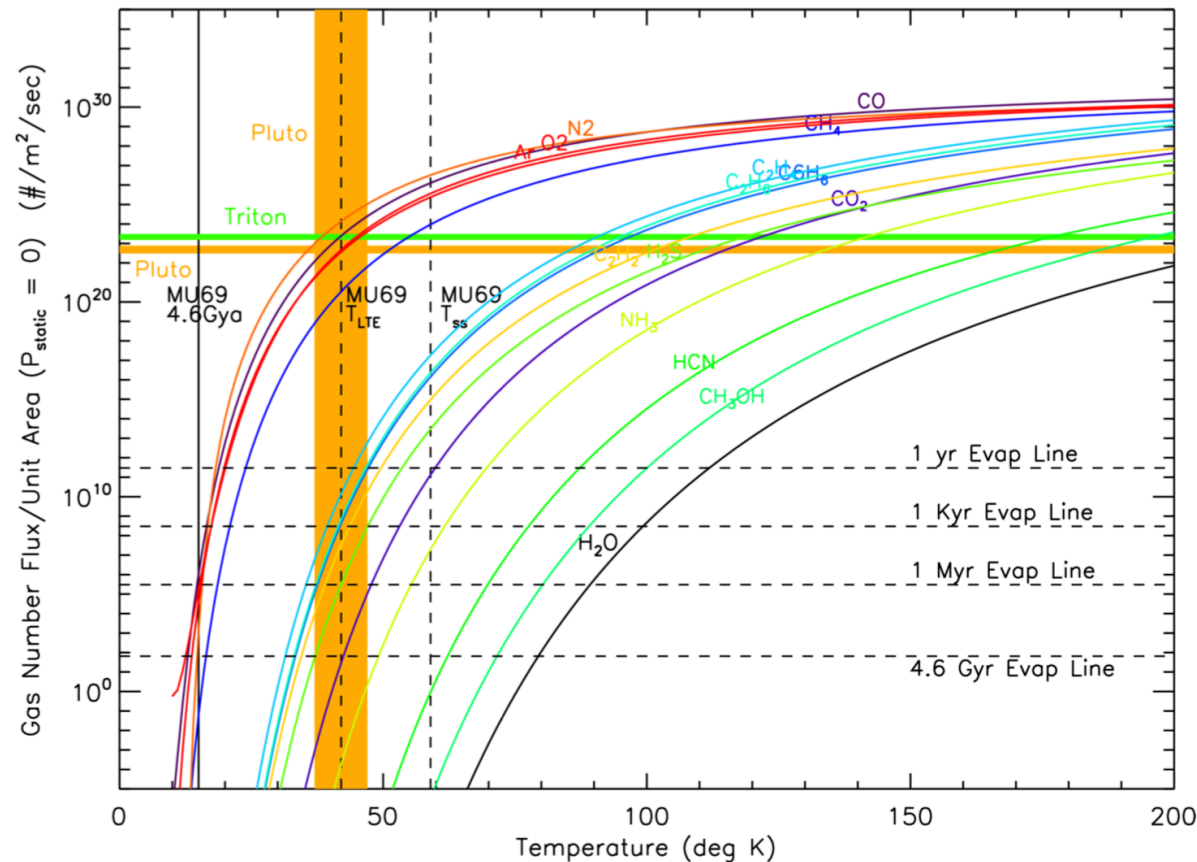
Retention of volatiles

If Pluto is formed from similar bodies to MU69, they must retain N_2



Needs shielding from the sunlight flambé.

Retention of volatiles



Hypervolatiles (CH_4 / CO / N_2)
lost under vacuum pressure and microgravity in ~ 1 Myr
for 40 K

Retained for long times if formed $< 20\text{K}$

Formation of MU69 in an
optically thick disk keeps the
interior cold enough to allow
the volatiles to remain frozen.

Angular momentum loss via nebular drag

$$\begin{aligned}\ddot{\mathbf{r}}_1 &= -Gm_2 \frac{(\mathbf{r}_1 - \mathbf{r}_2)}{|\mathbf{r}_1 - \mathbf{r}_2|^3} - \frac{\dot{\mathbf{r}}_1}{\tau_1} \\ \ddot{\mathbf{r}}_2 &= -Gm_1 \frac{(\mathbf{r}_2 - \mathbf{r}_1)}{|\mathbf{r}_1 - \mathbf{r}_2|^3} - \frac{\dot{\mathbf{r}}_2}{\tau_2}\end{aligned}$$

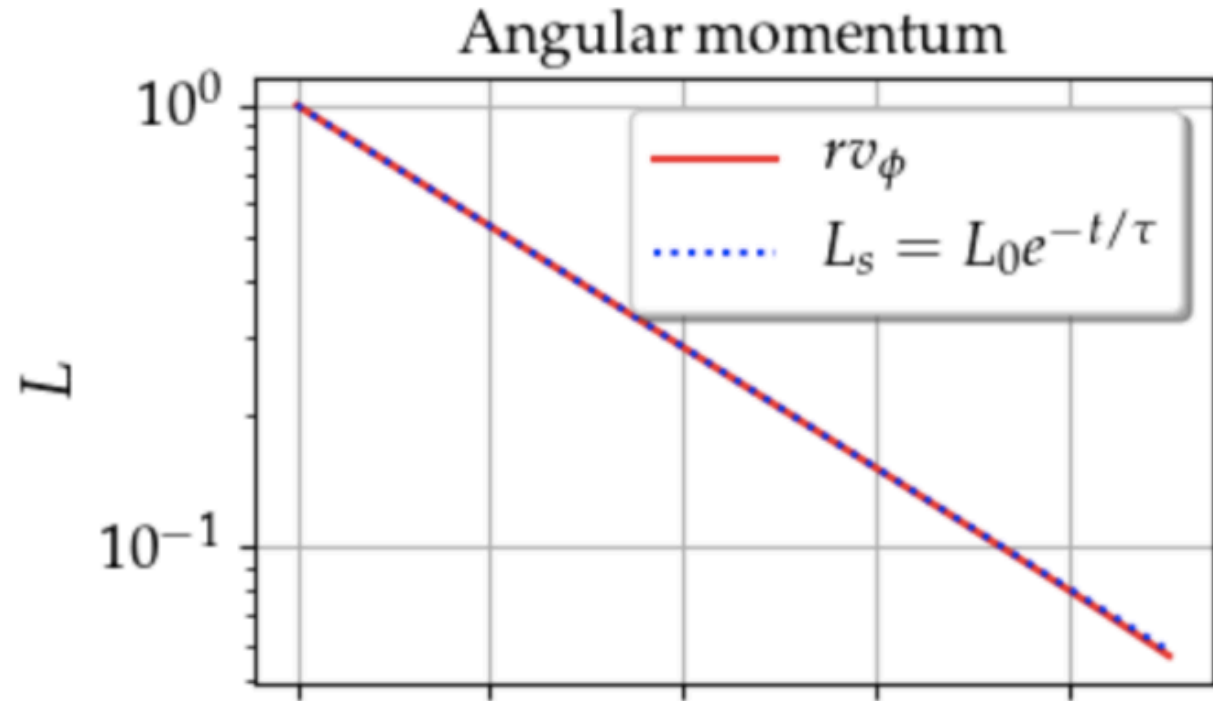
gravity (blue arrow pointing to the first term) and *drag* (red arrow pointing to the second term).

Solve for angular momentum:

$$\begin{aligned}r\ddot{\phi} + 2\dot{r}\dot{\phi} &= -\frac{r\dot{\phi}}{\tau} \\ \frac{dh}{dt} &= -\frac{h}{\tau}\end{aligned}$$

Exponential decay of angular momentum !

$$h = h_0 e^{-t/\tau}$$

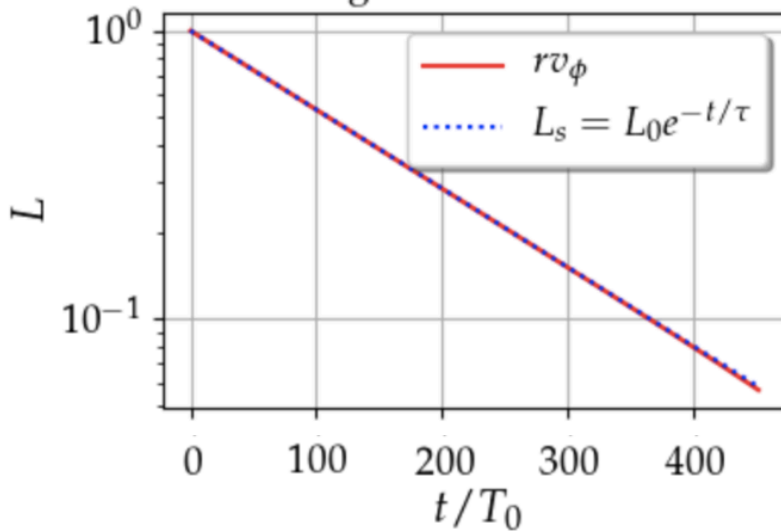


Analytical solution

Exponential decay of angular momentum

$$h = h_0 e^{-t/\tau_{\text{eff}}}$$

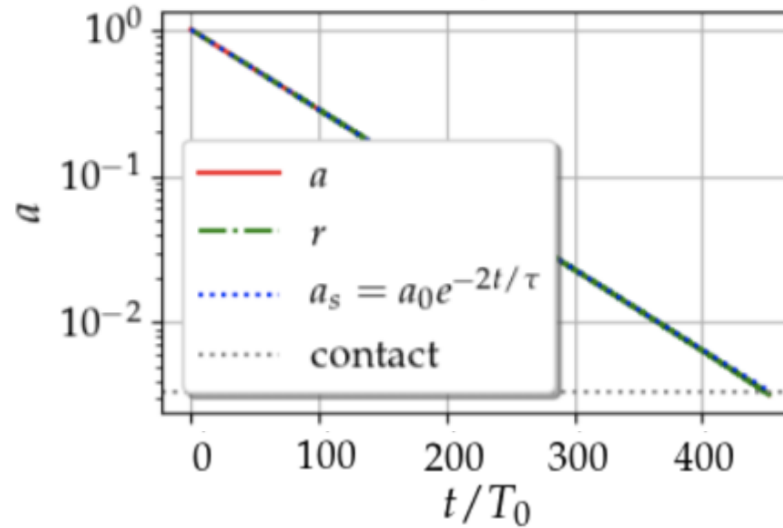
Angular momentum



Exponential decay of energy

$$a = a_0 e^{-2t/\tau_{\text{eff}}}$$

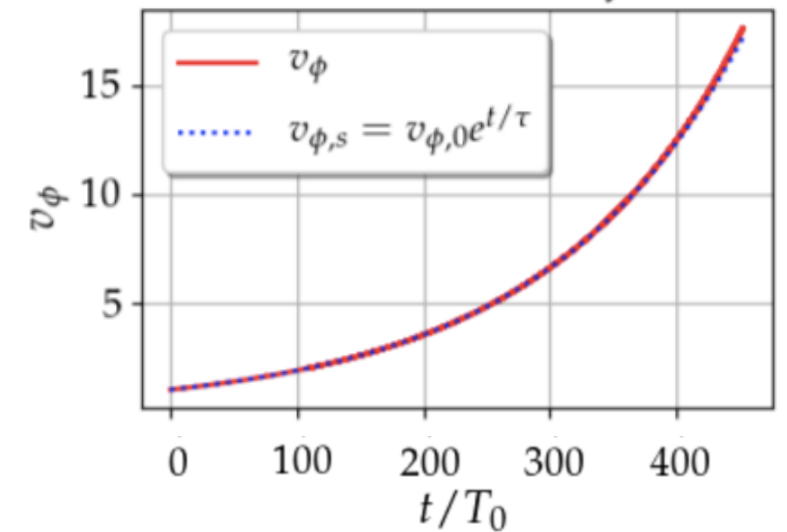
Semimajor axis



Exponential increase of orbital velocity

$$v_\phi = v_{\phi,0} e^{t/\tau_{\text{eff}}}$$

Azimuthal Velocity



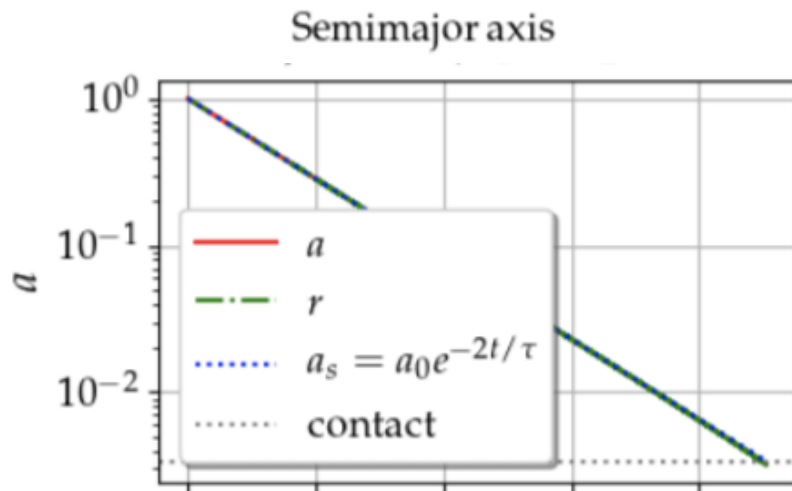
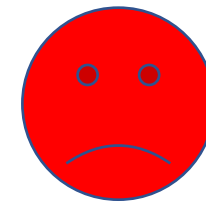
Getting quantitative...

Time until contact

$$t = \frac{\tau}{2} \ln \frac{a_0}{a}$$

For $a = 0.1 r_H$ (4000 km), hardening to $a_0=20\text{km}$ and $\tau\Omega=10^7 \dots$

$t \sim 100 \text{ Myr}$



Wind

At initial separation $a \sim 4000$ km:

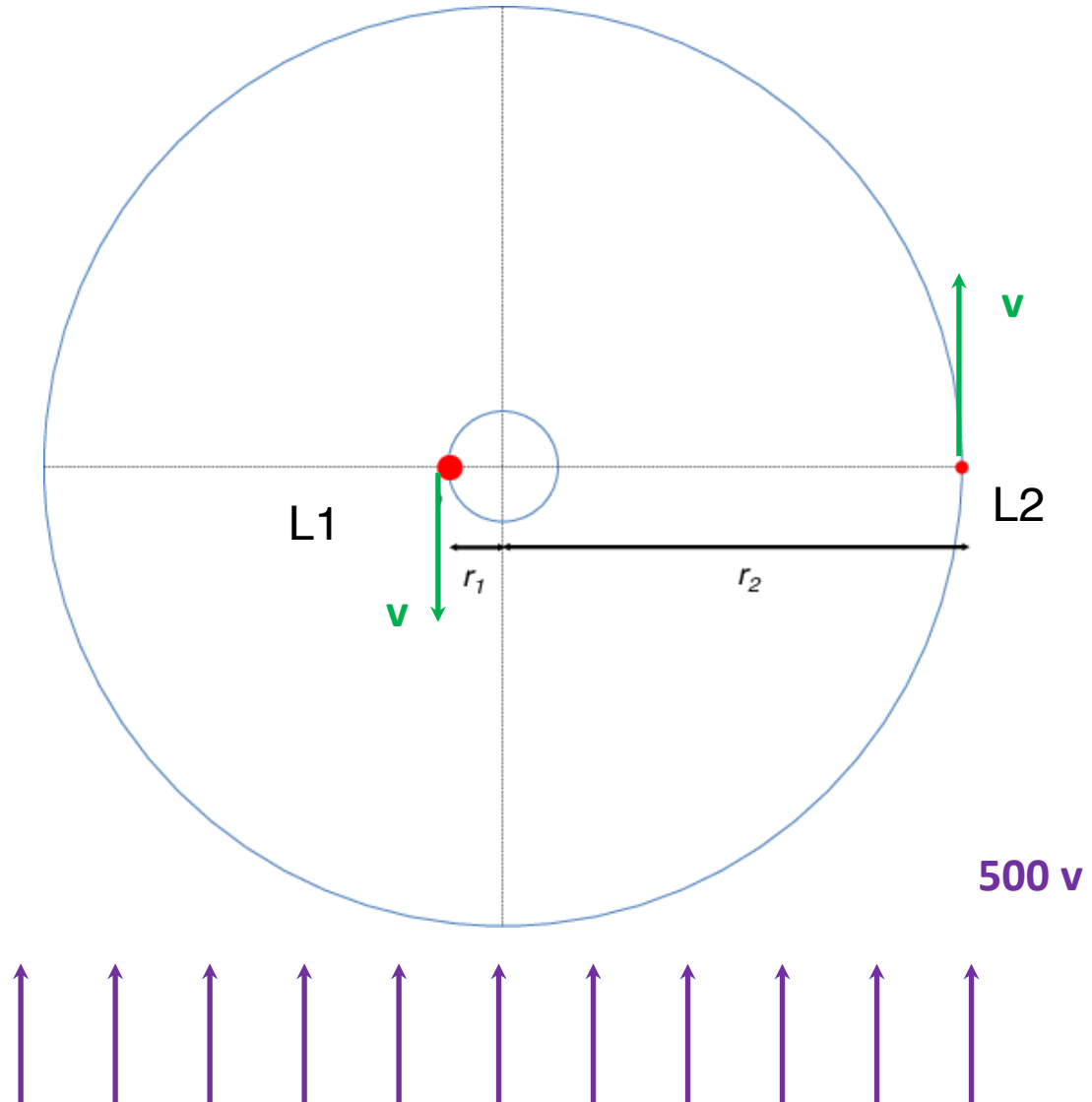
Binary orbital velocity ~ 0.1 m/s

Solar orbit velocity at 45AU
 $v_k \sim 4.5$ km/s

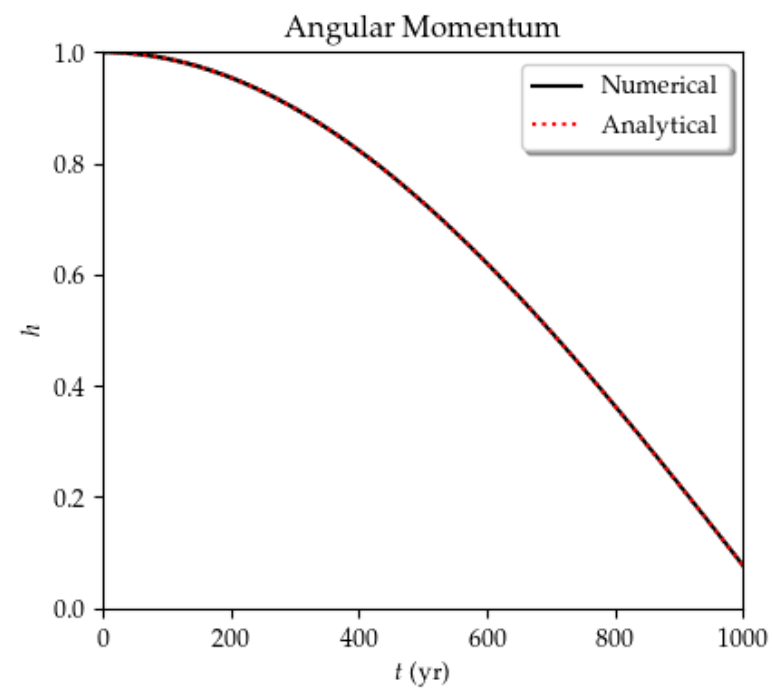
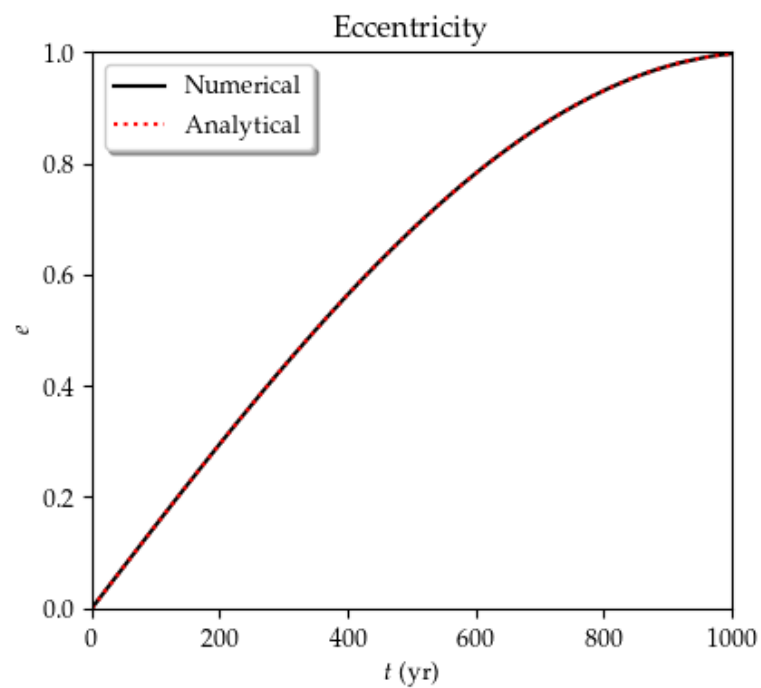
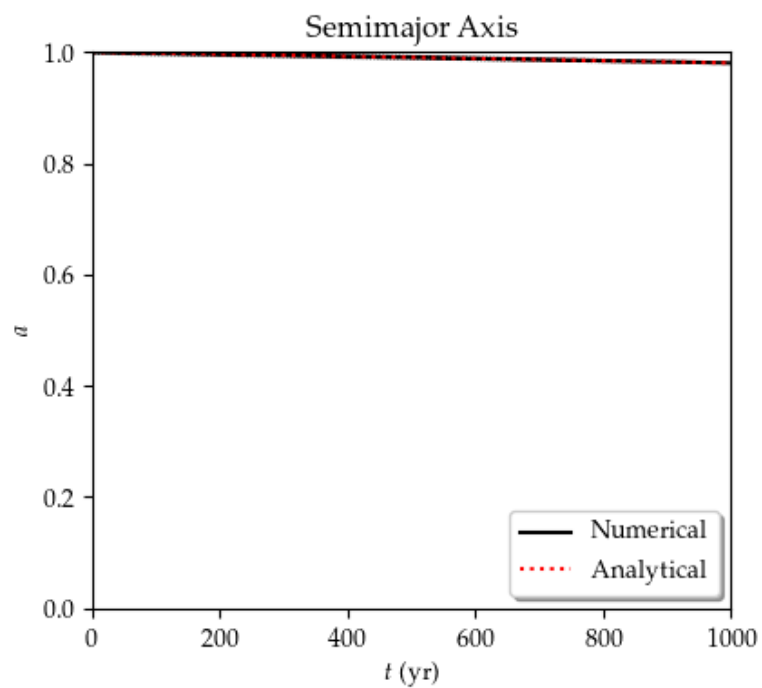
Sub-Keplerian pressure support
 $v = v_k (1 - \eta)$
 $\eta \sim 0.01$

Headwind velocity ($v_k - v$):
 $\eta v \sim 50$ m/s

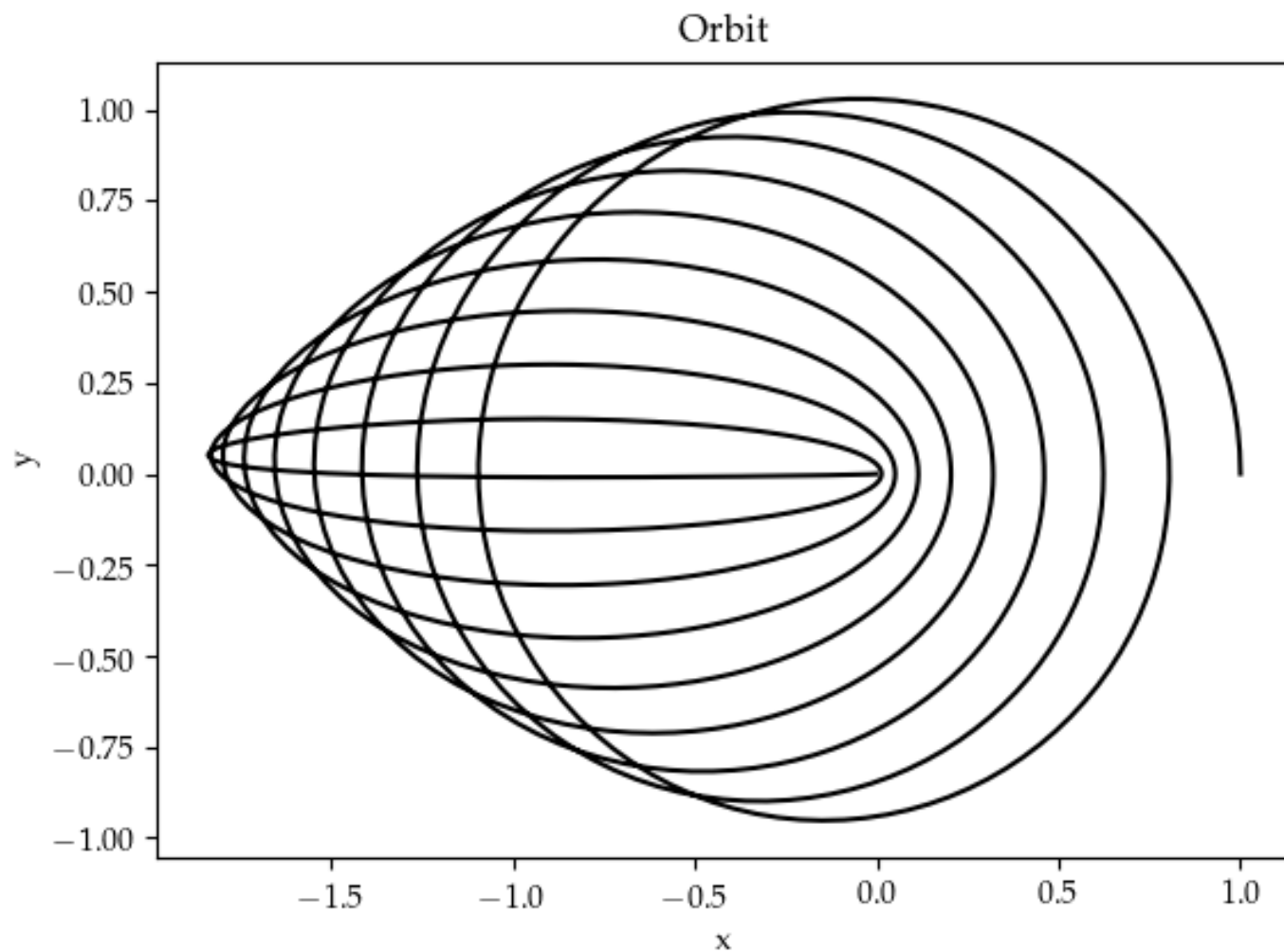
Subkeplerian wind on the binary
= 500 times orbital velocity



Wind solution



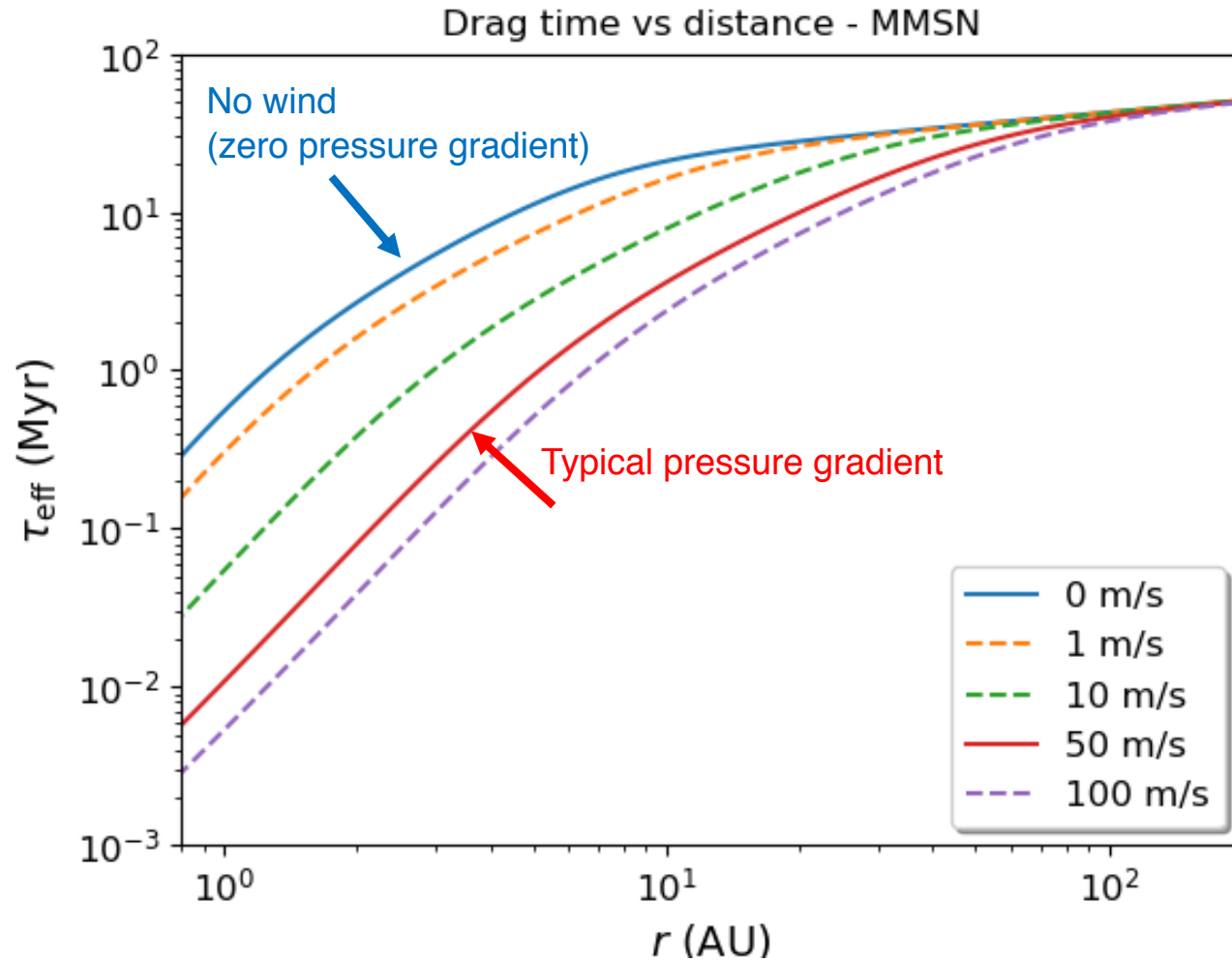
Wind solution



Angular momentum loss at constant energy.

Eccentricity increase at constant semimajor axis

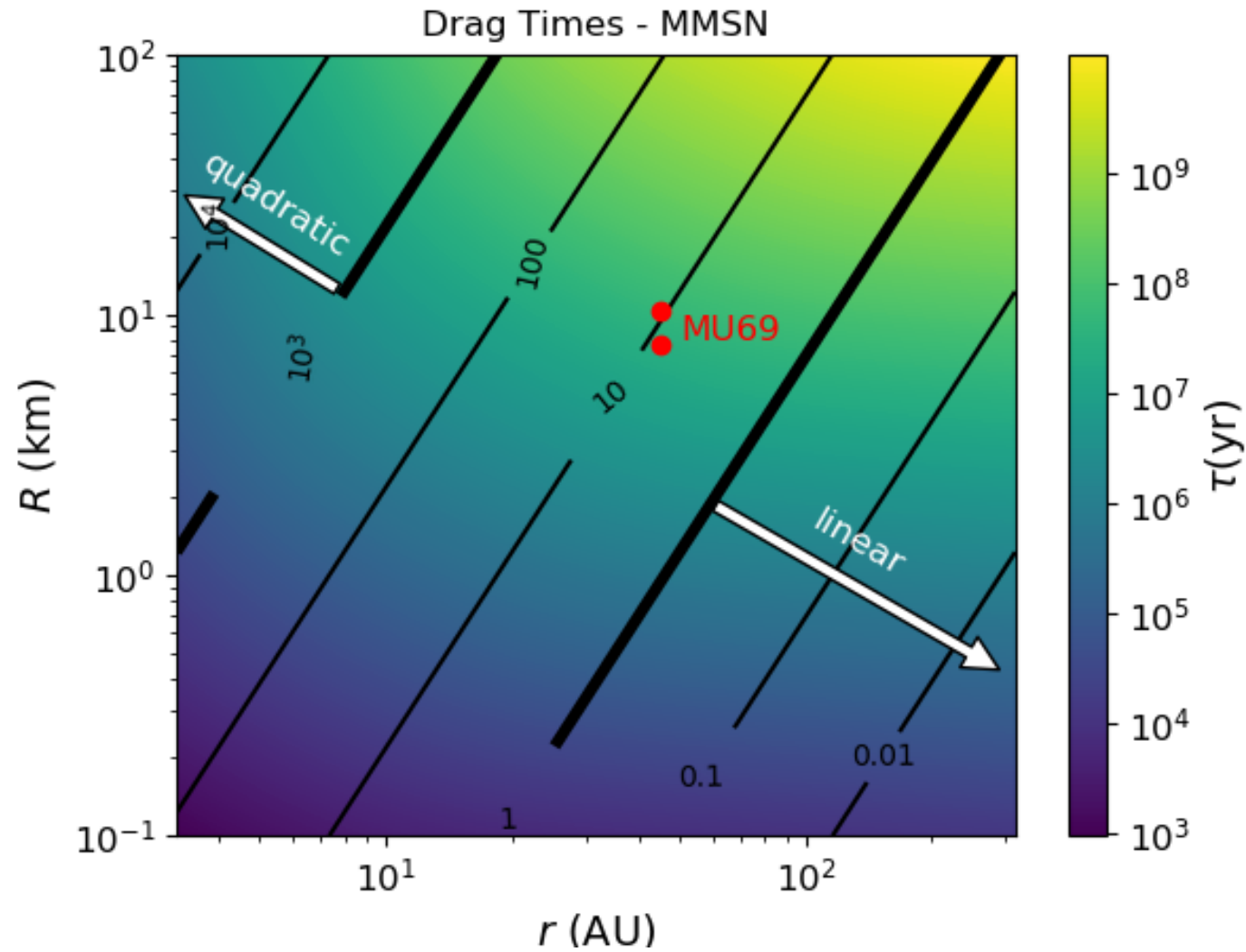
Timescales



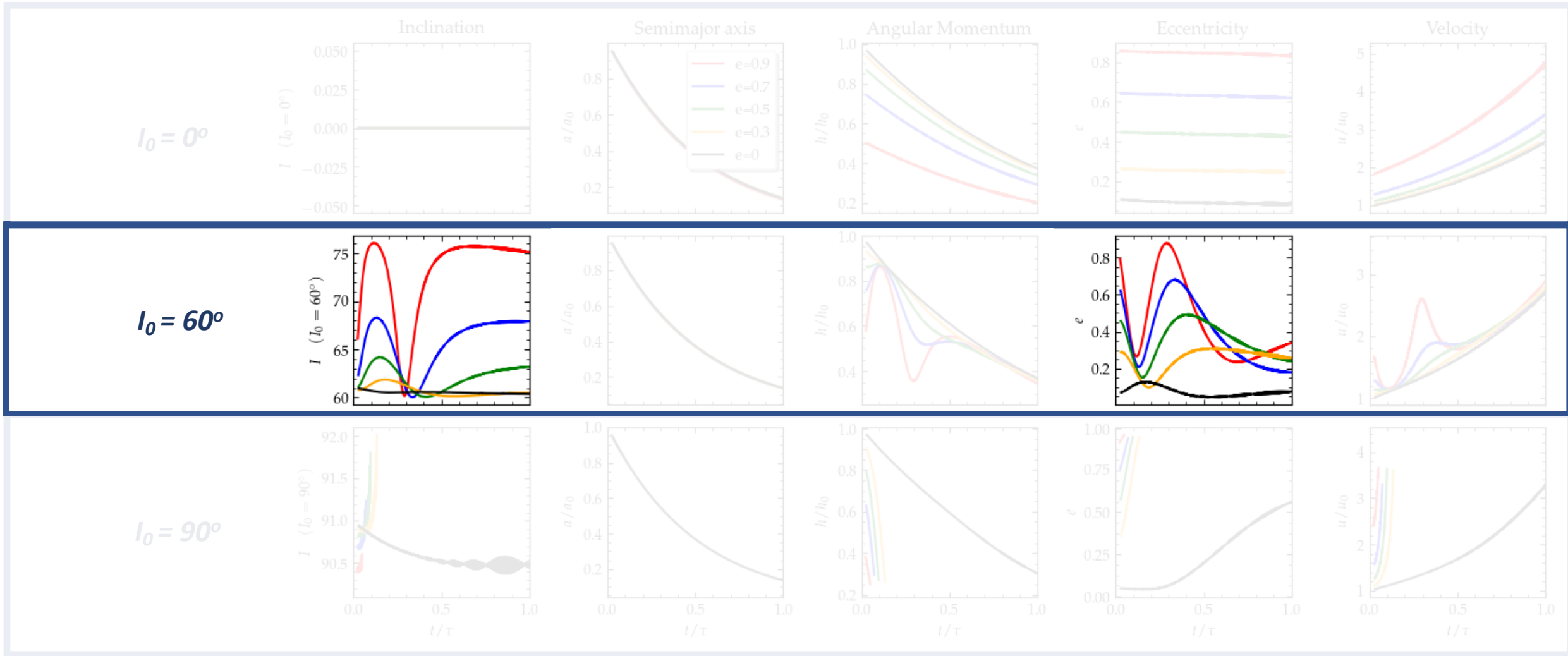
Wind has a strong effect in the distances of the asteroid belt.

Little effect in the Kuiper belt.

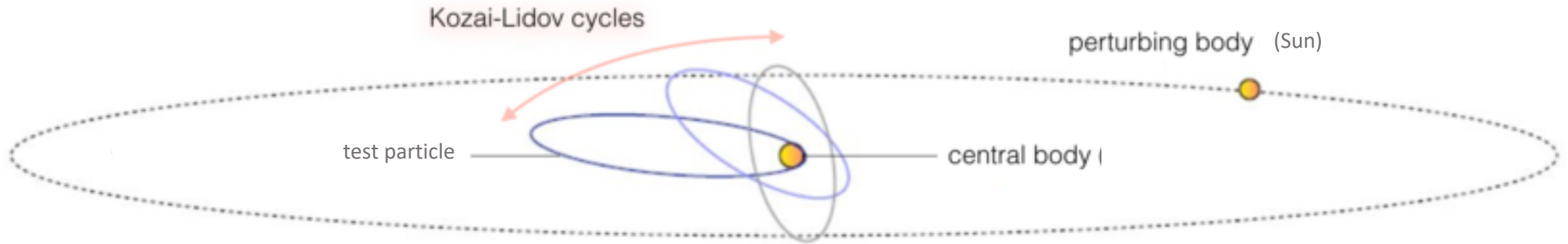
Linear vs quadratic drag



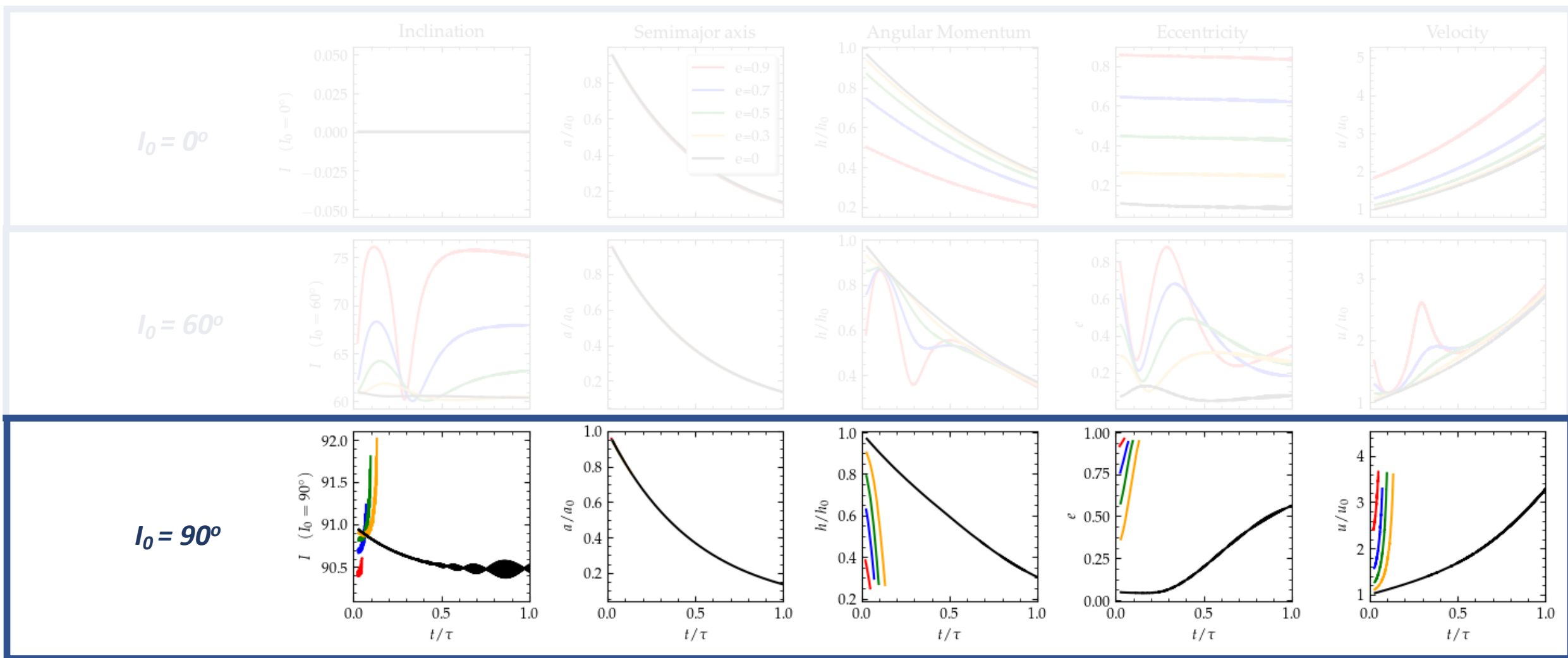
Effect of Inclination



Kozai-Lidov Oscillations

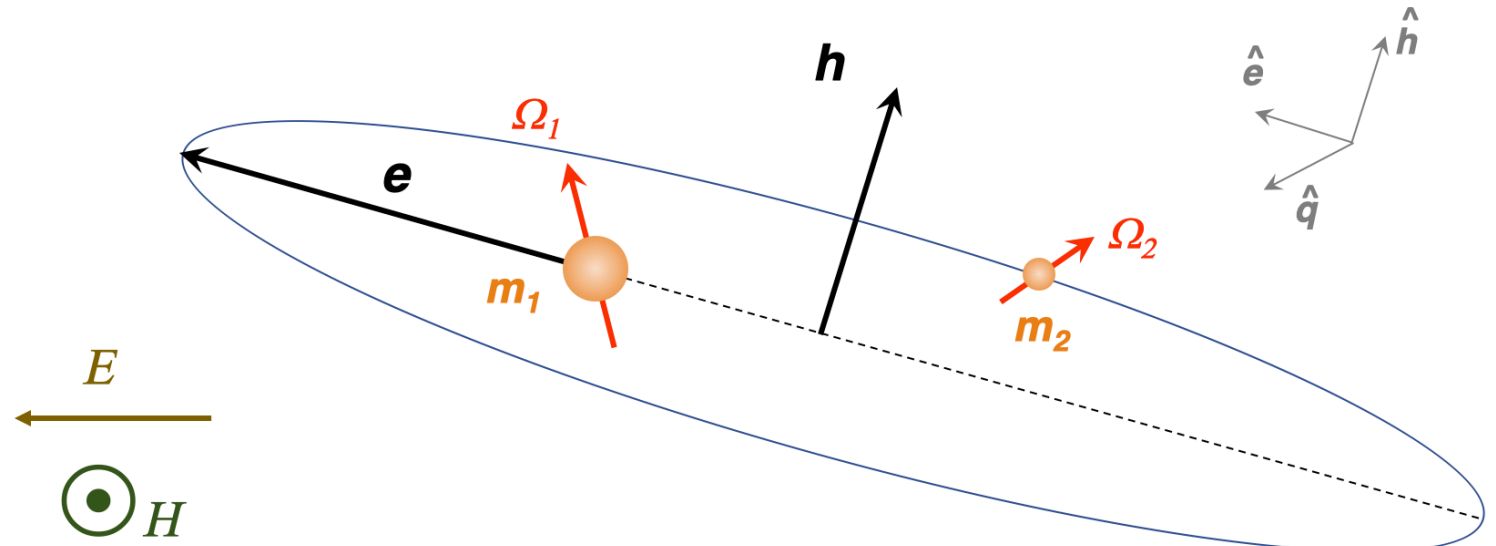


Effect of Inclination

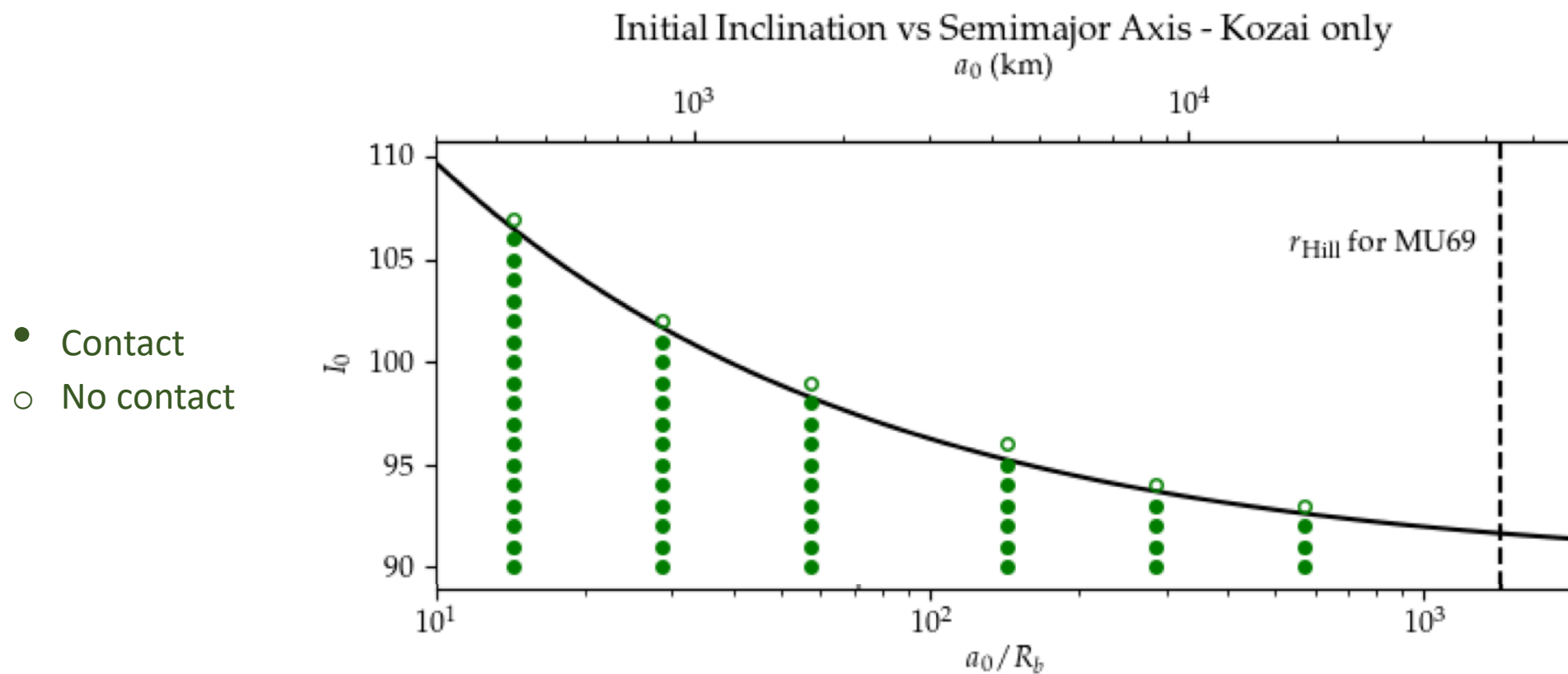


Kozai + Tidal Friction + Drag

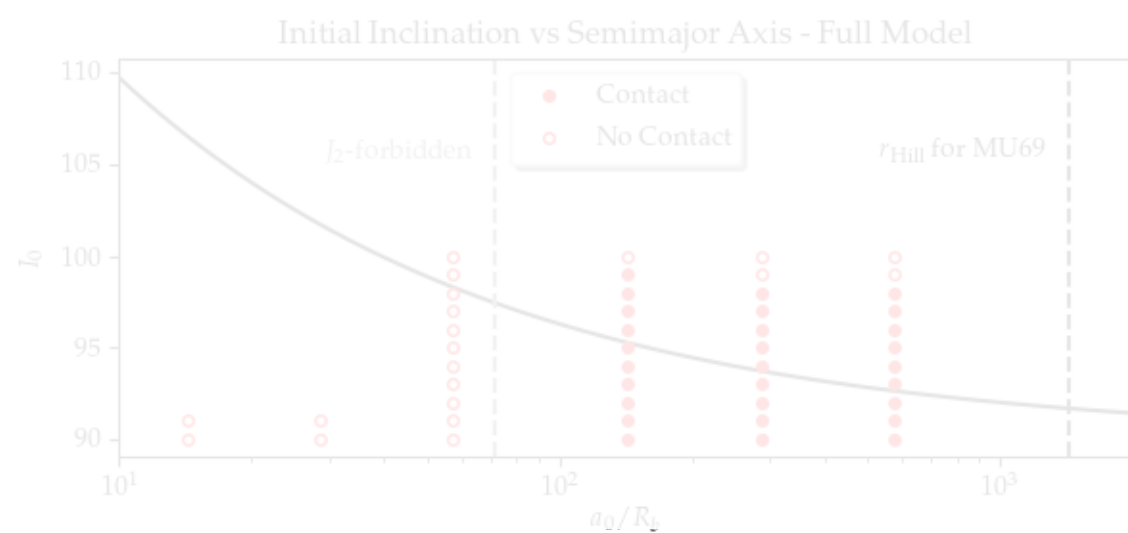
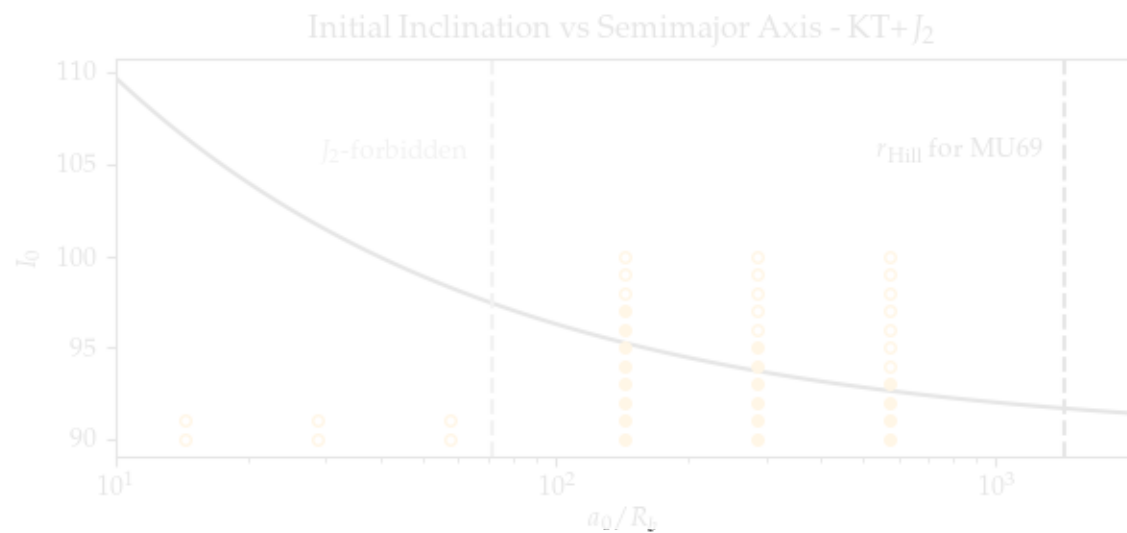
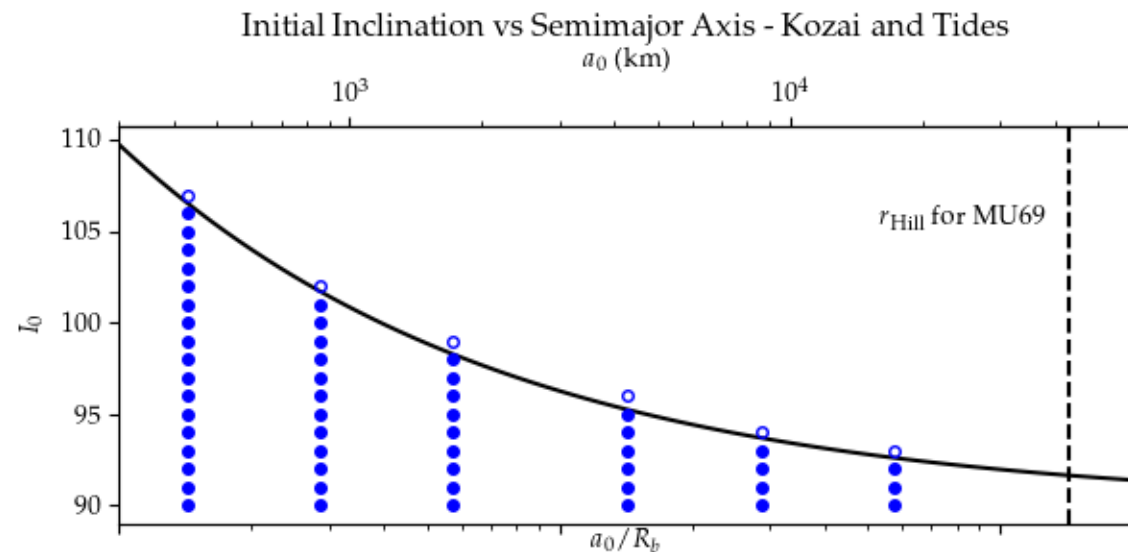
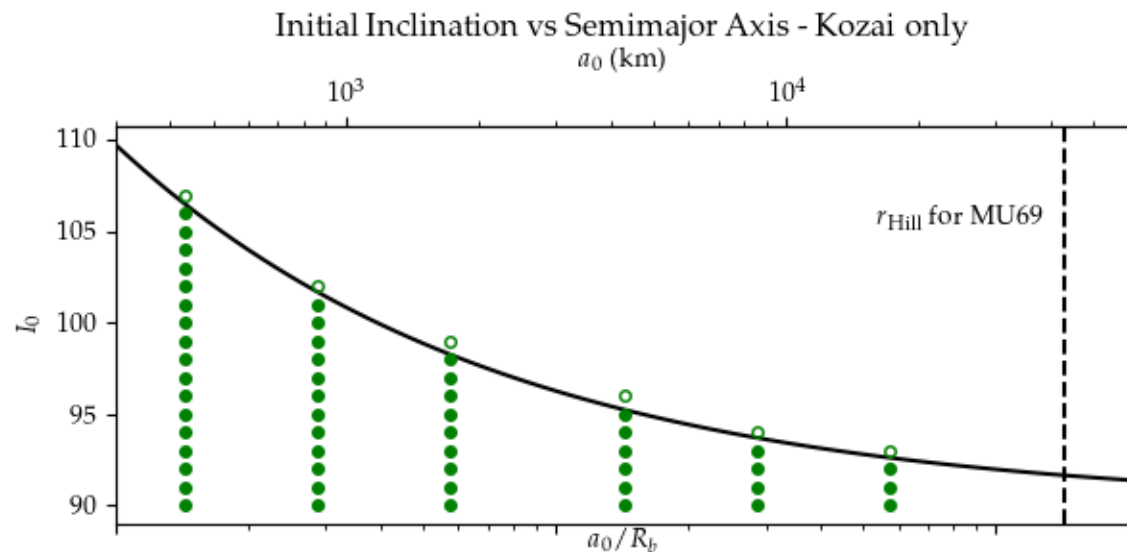
$$\begin{aligned}
 \frac{de}{dt} &= -e \left[V_1 + V_2 + V_d + 5(1 - e^2) S_{eq} \right], \\
 \frac{dh}{dt} &= -h \left(W_1 + W_2 + W_d - 5e^2 S_{eq} \right), \\
 \frac{d\hat{e}}{dt} &= \left[Z_1 + Z_2 + (1 - e^2) (4S_{ee} - S_{qq}) \right] \hat{q} \\
 &\quad - \left[Y_1 + Y_2 + (1 - e^2) S_{qh} \right] \hat{h}, \\
 \frac{d\hat{h}}{dt} &= \left[Y_1 + Y_2 + (1 - e^2) S_{qh} \right] \hat{e} \\
 &\quad - \left[X_1 + X_2 + (4e^2 + 1) S_{eh} \right] \hat{q}, \\
 \frac{d\Omega_1}{dt} &= \frac{\mu_r h}{I_1} \left(-Y_1 \hat{e} + X_1 \hat{q} + W_1 \hat{h} \right), \\
 \frac{d\Omega_2}{dt} &= \frac{\mu_r h}{I_2} \left(-Y_2 \hat{e} + X_2 \hat{q} + W_2 \hat{h} \right).
 \end{aligned}$$



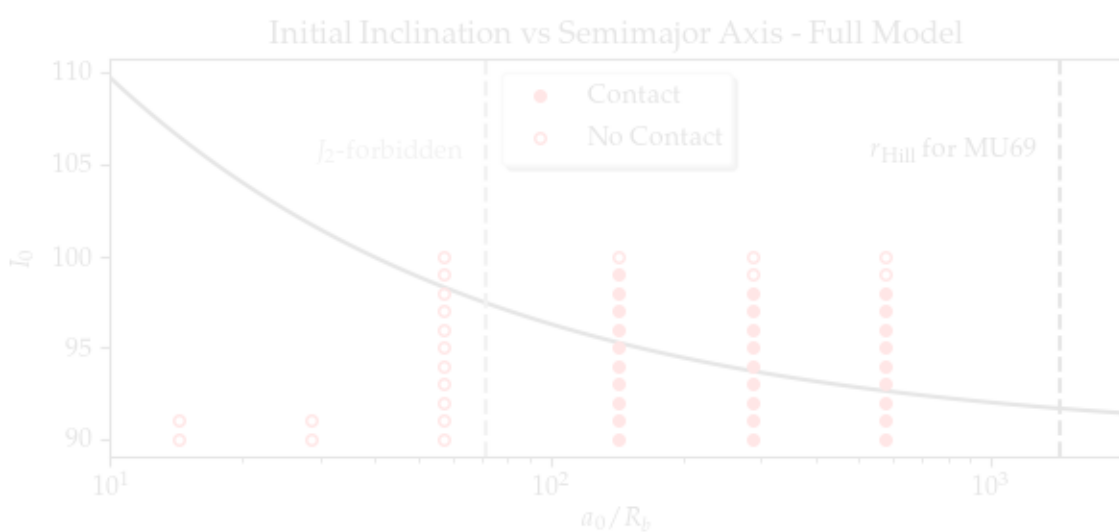
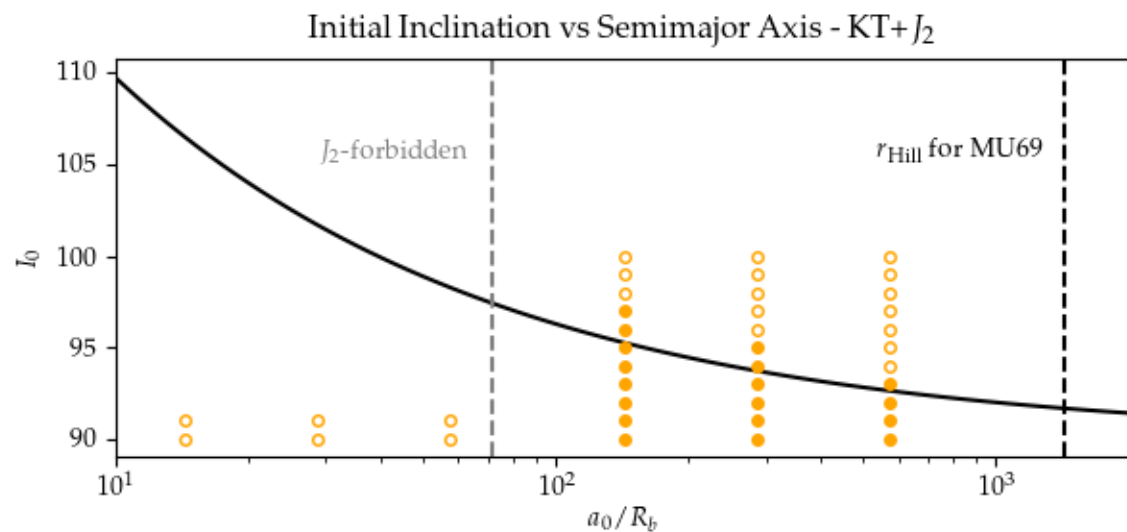
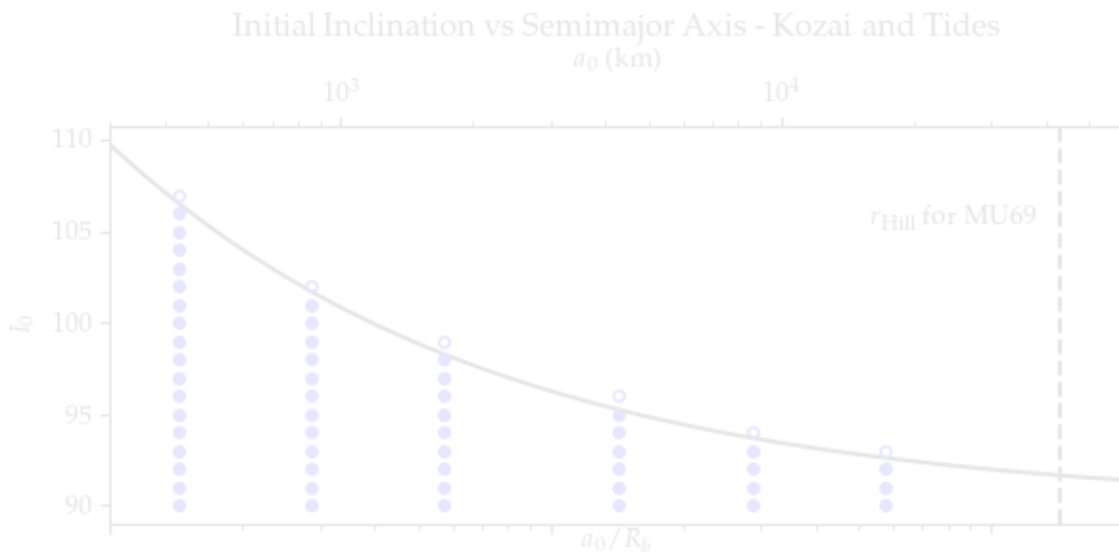
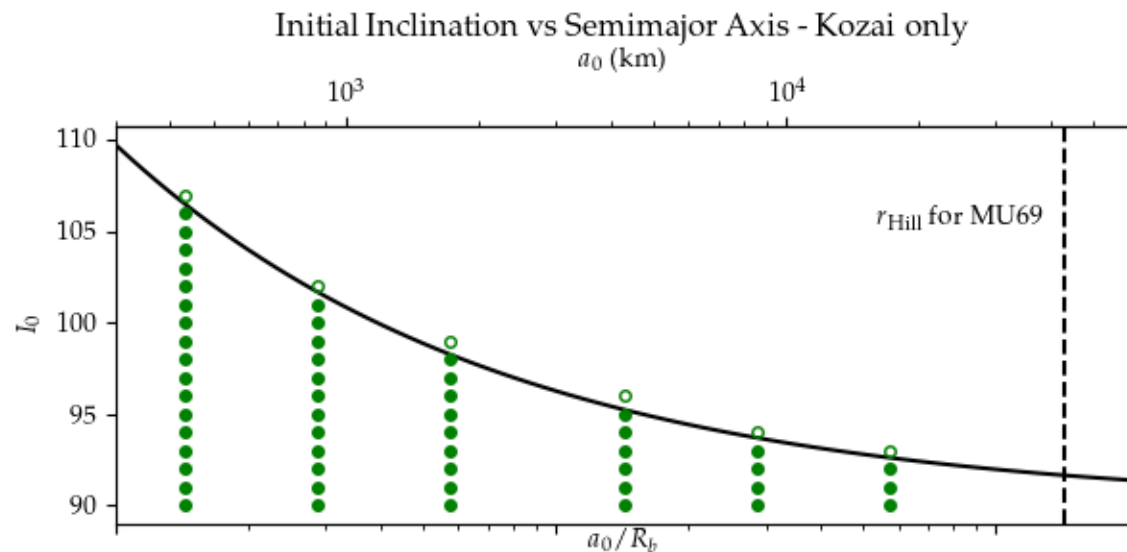
Critical Inclination



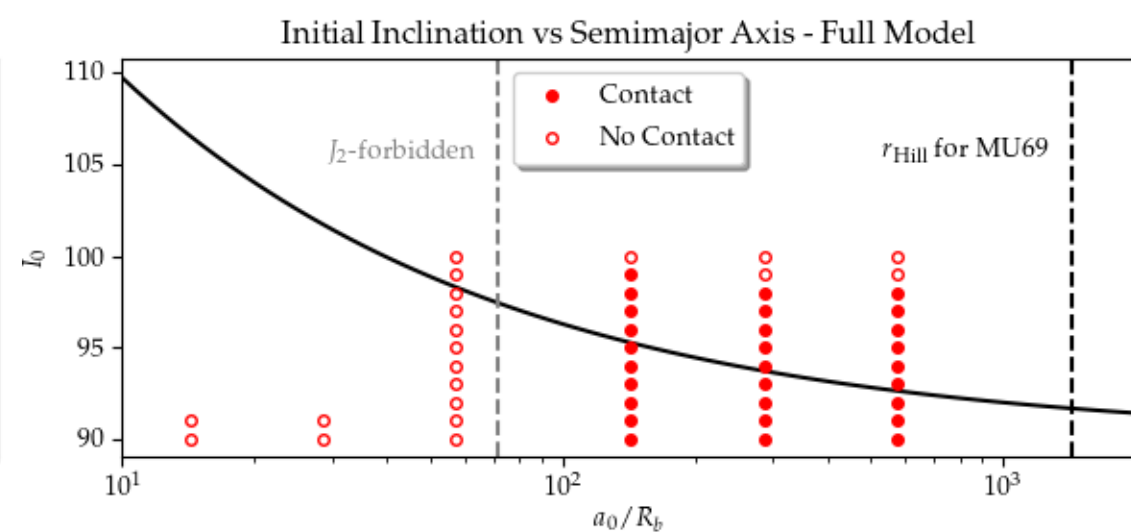
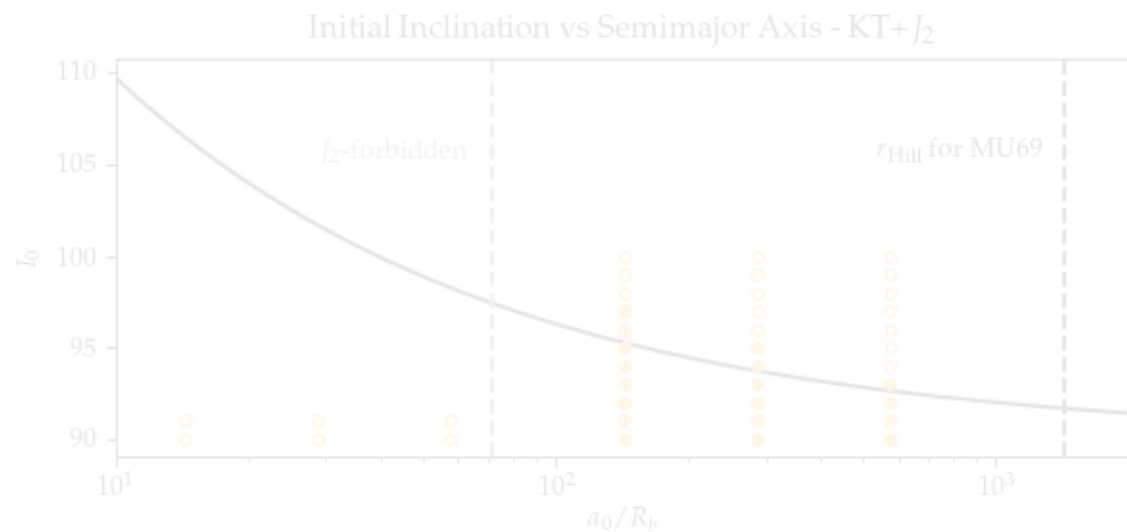
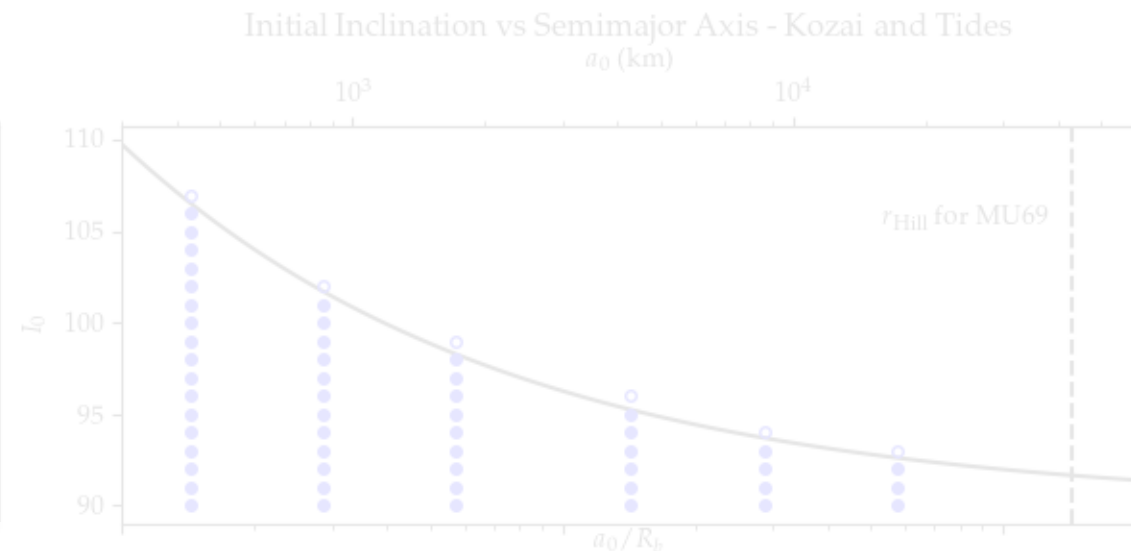
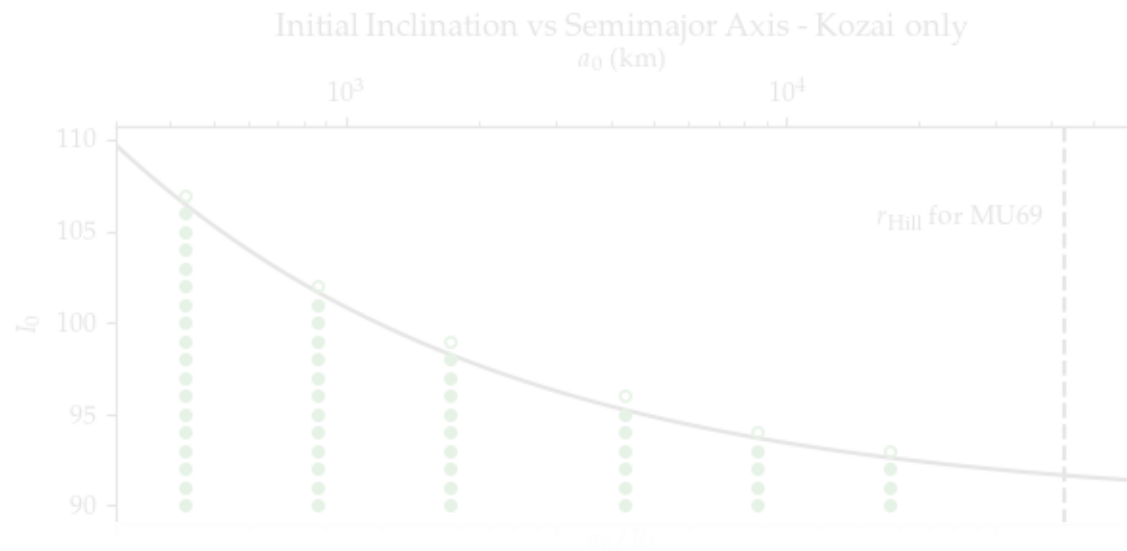
Kozai + Tidal Friction + Drag



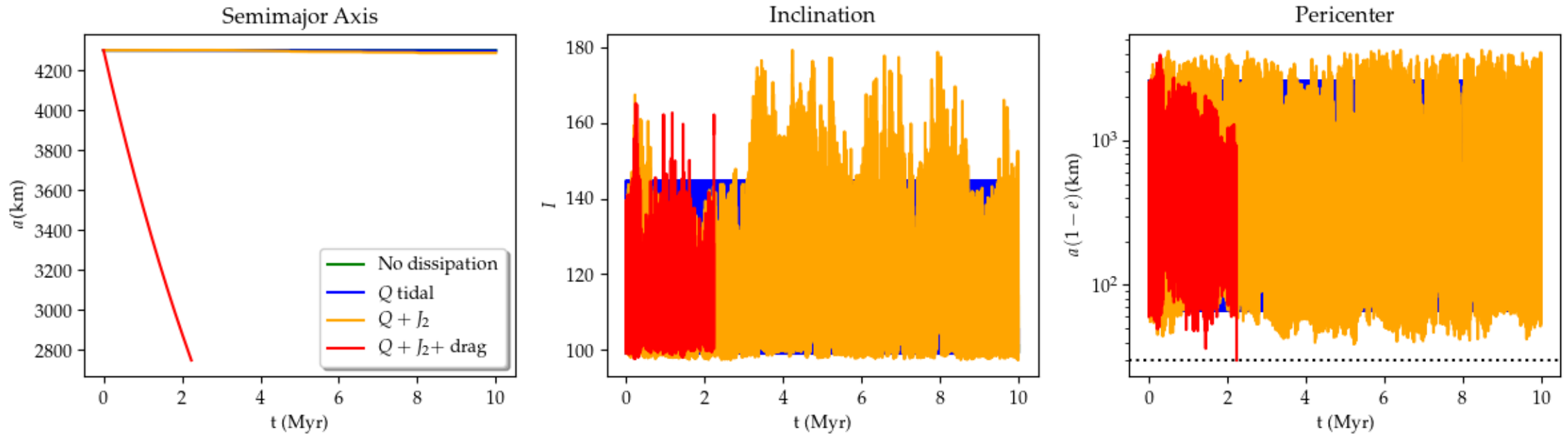
Kozai + Tidal Friction + Drag



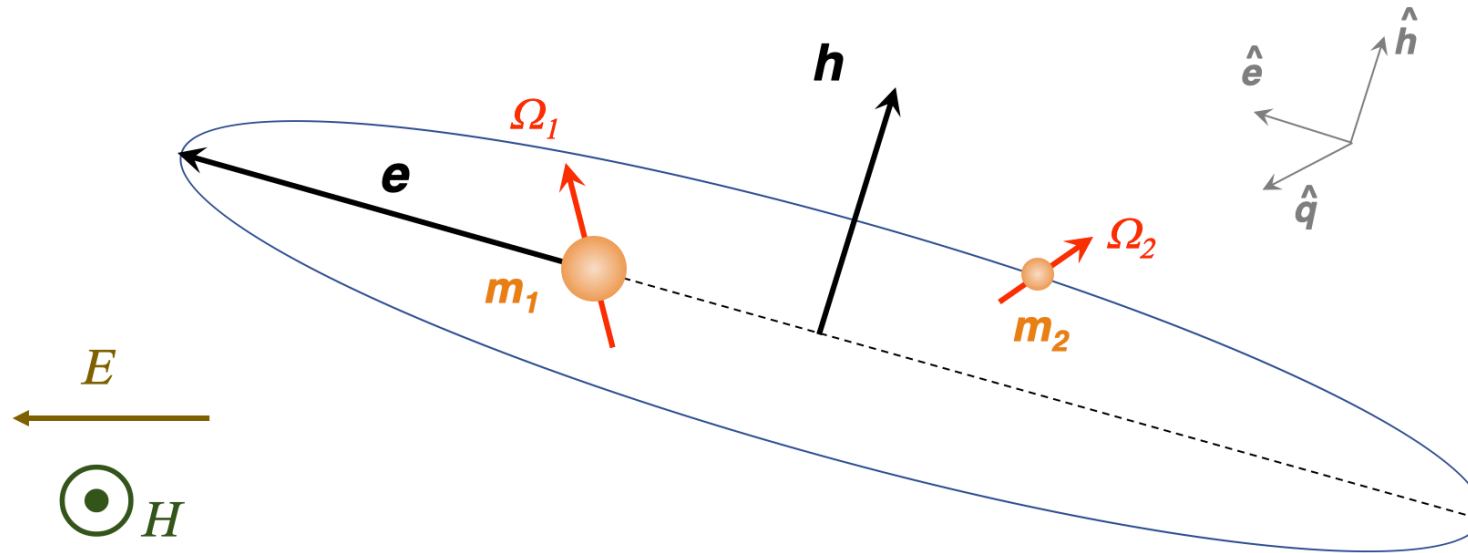
Kozai + Tidal Friction + Drag



Effect of Drag



Alignment of the Spin Vectors



Mainly driven by J_2 (permanent quadrupole)

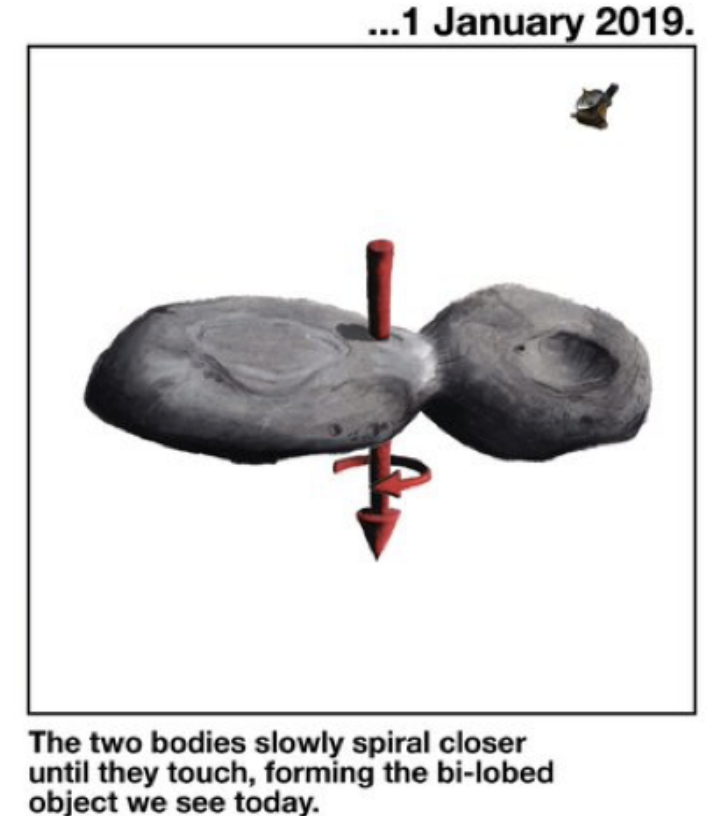
Timescale proportional to a^4 (*4th power of semimajor axis*)

5 Gyr for $a/R \sim 100$

0.5 Myr for $a/R \sim 10$

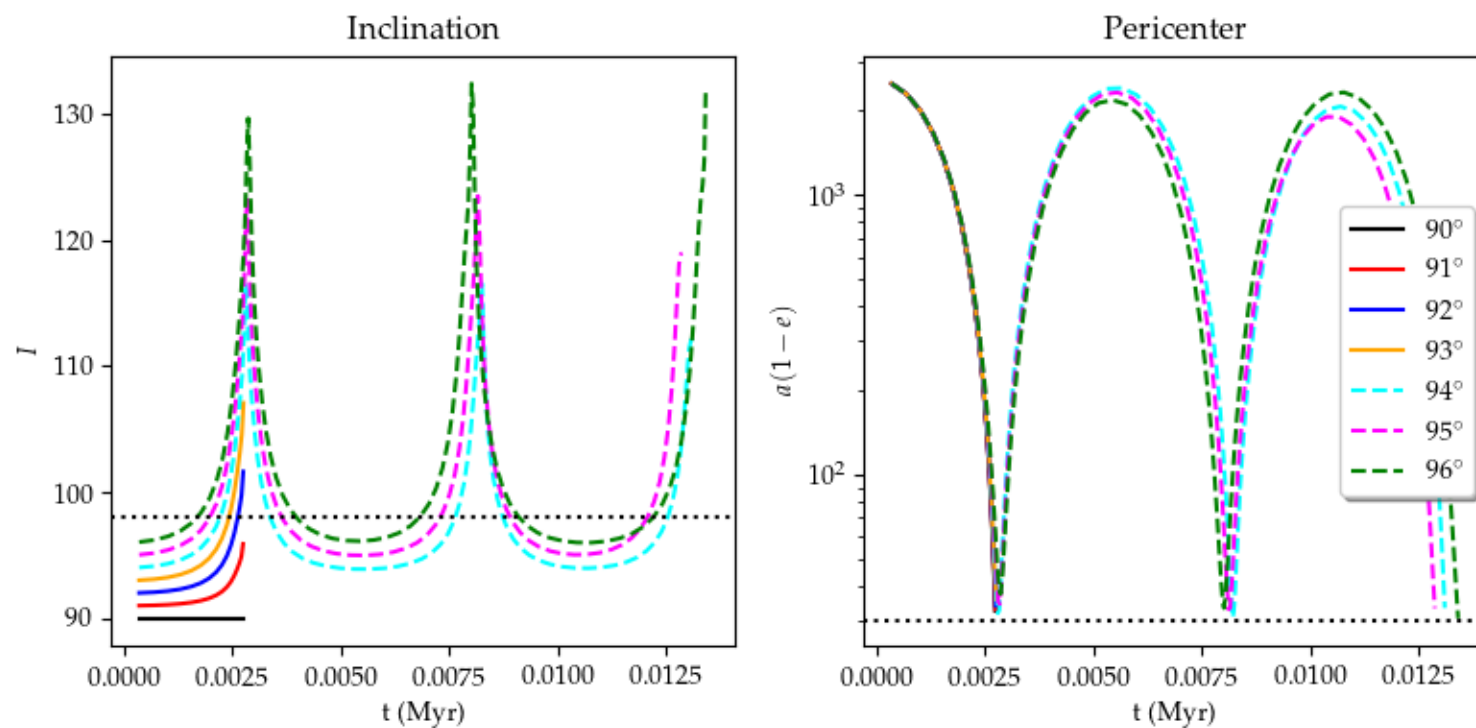
Conclusions

- Solved the binary planetesimal problem with gas drag
- Implemented the solution into a Kozai plus tidal friction code
- Contact possible in the asteroid belt within 0.1 Myr (depleted of binaries)
- Contact via Kozai cycles in the Kuiper belt, orbits become grazing
- Window of contact increased by J_2 and drag
- Enough time for the bodies to come to alignment
- Model predictions:
 - ~ 10% of KBCC binaries should be contact binaries
 - Velocities at contact should be about 3-4 m/s
- Open questions:
 - Single-averaged (or N-body) needed to reproduce final inclinations
 - Combine our model with single-averaged Kozai (or N-body)

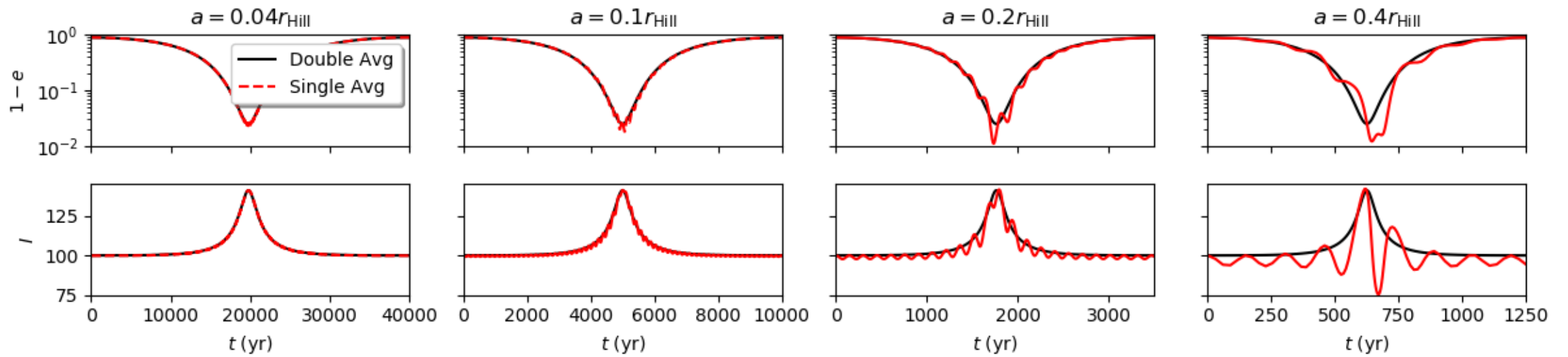


Sketch by J.T. Keane

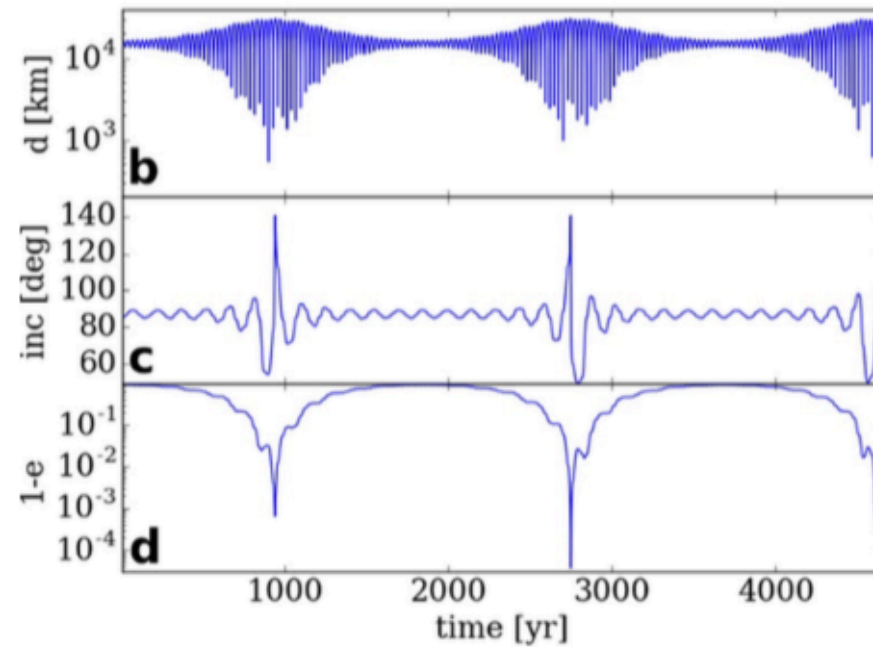
Fine Tuning of Initial Inclination



Double-Averaged vs Single-Averaged

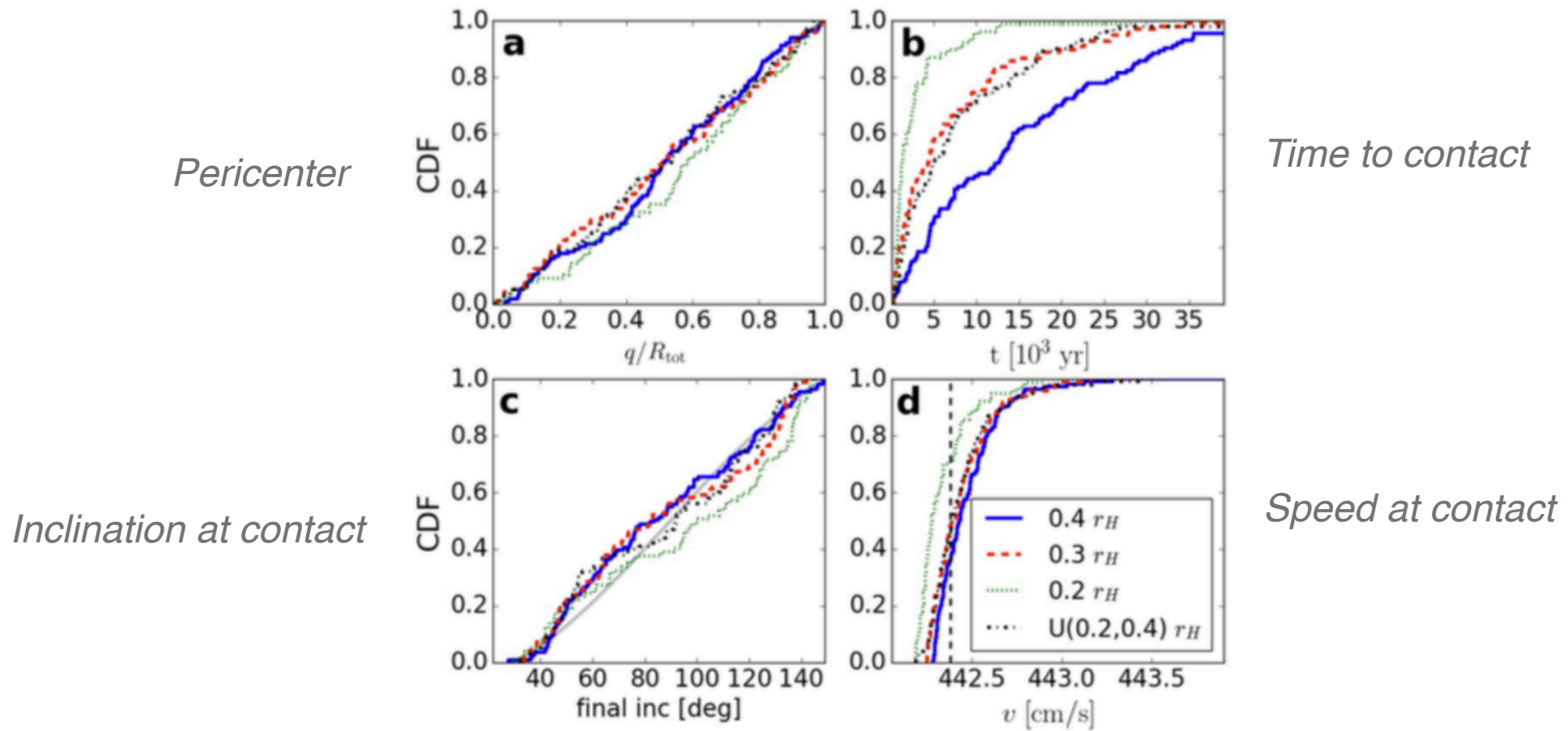


N-body simulations (no tides, J2, or drag)

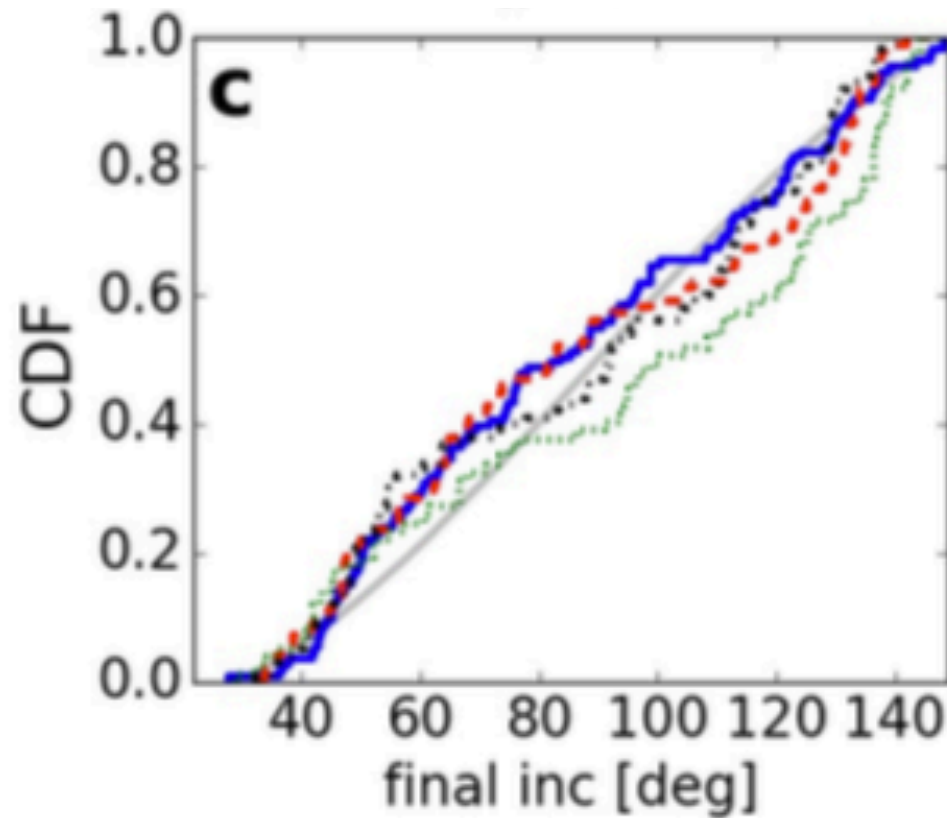


Inclination not limited to the double-averaged constraint.
Cycles lead to lower inclination than initial.
Prograde/retrograde flipping possible.

N-body simulations (no tides, J2, or drag)



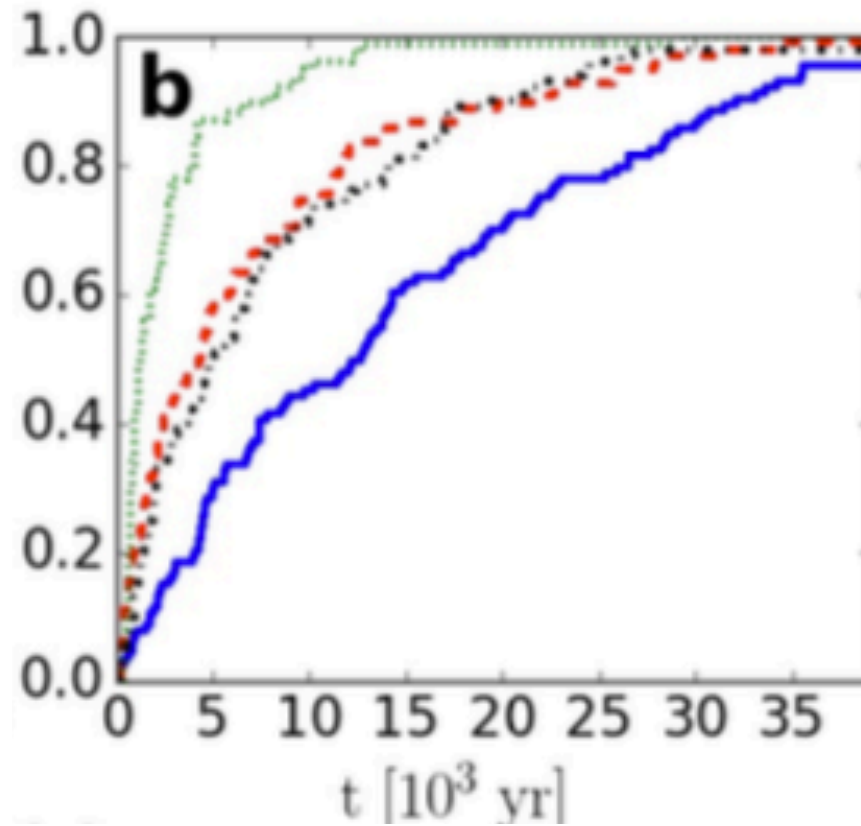
N-body simulations (no tides, J2, or drag)



Inclination at contact

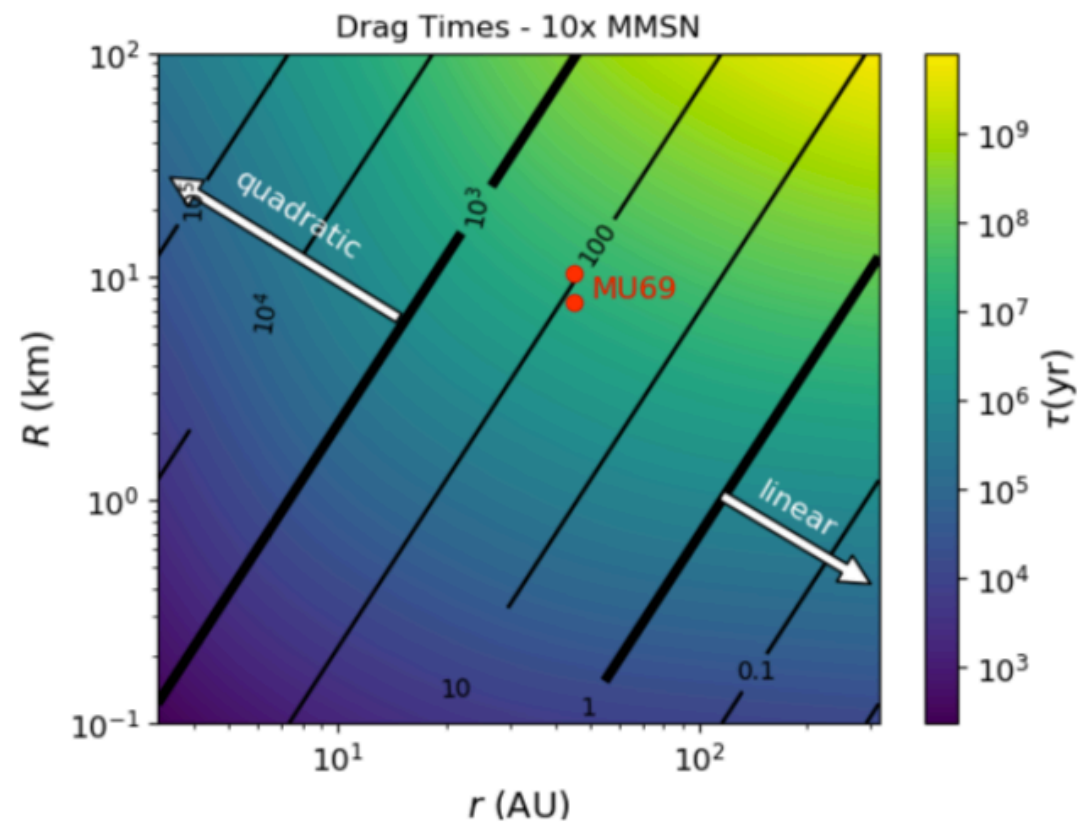
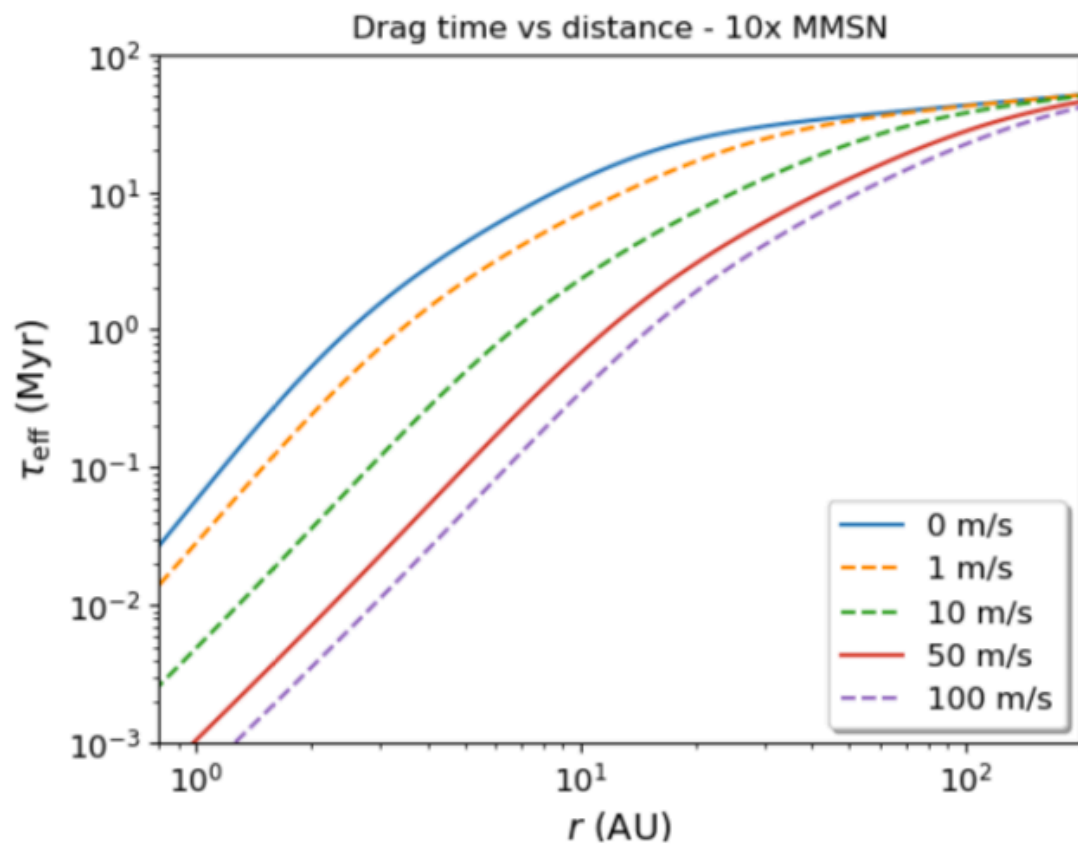
Uniform
any inclination (from 40° to 140°) equally likely

N-body simulations (no tides, J2, or drag)



Time to contact

Too short to allow for alignment



Hardening during disk lifetime

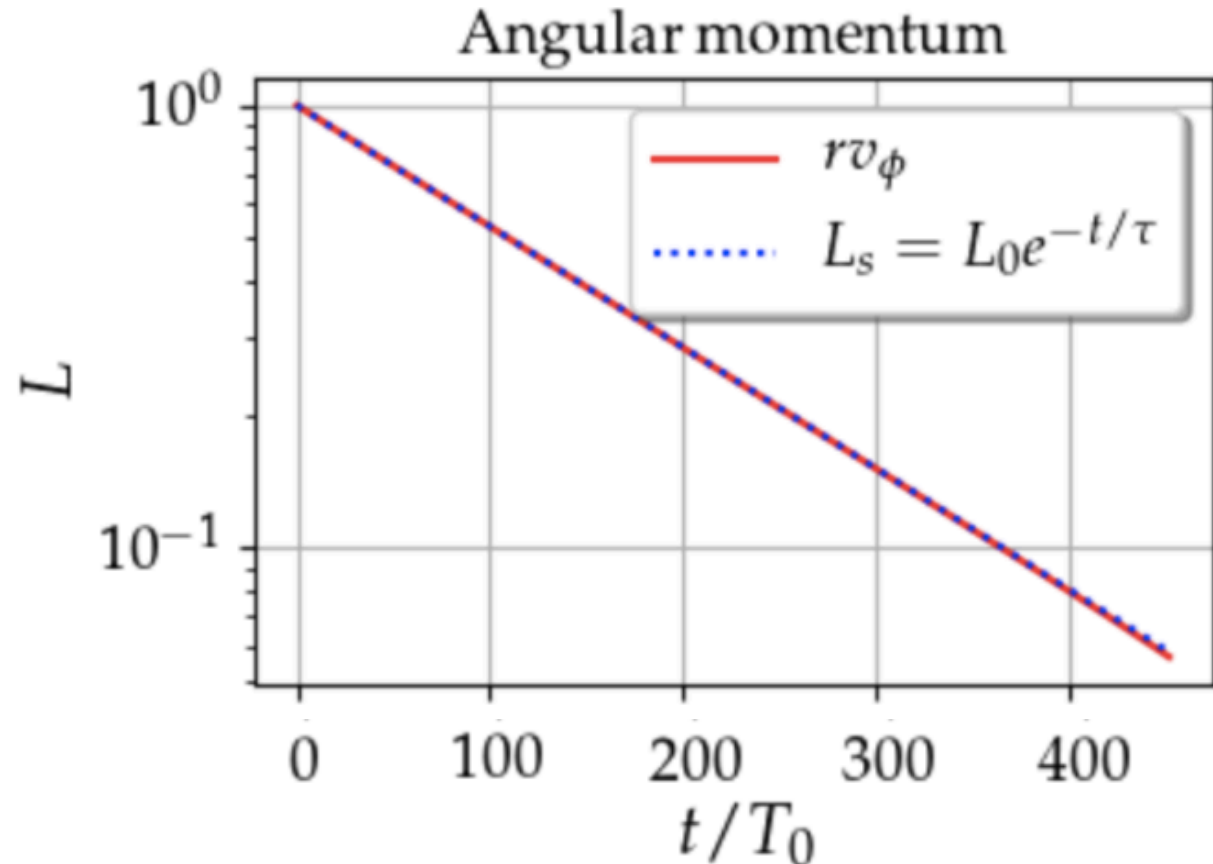
For unequal mass the physics is similar, the drag time is just replaced by an effective drag time:

Effective drag time

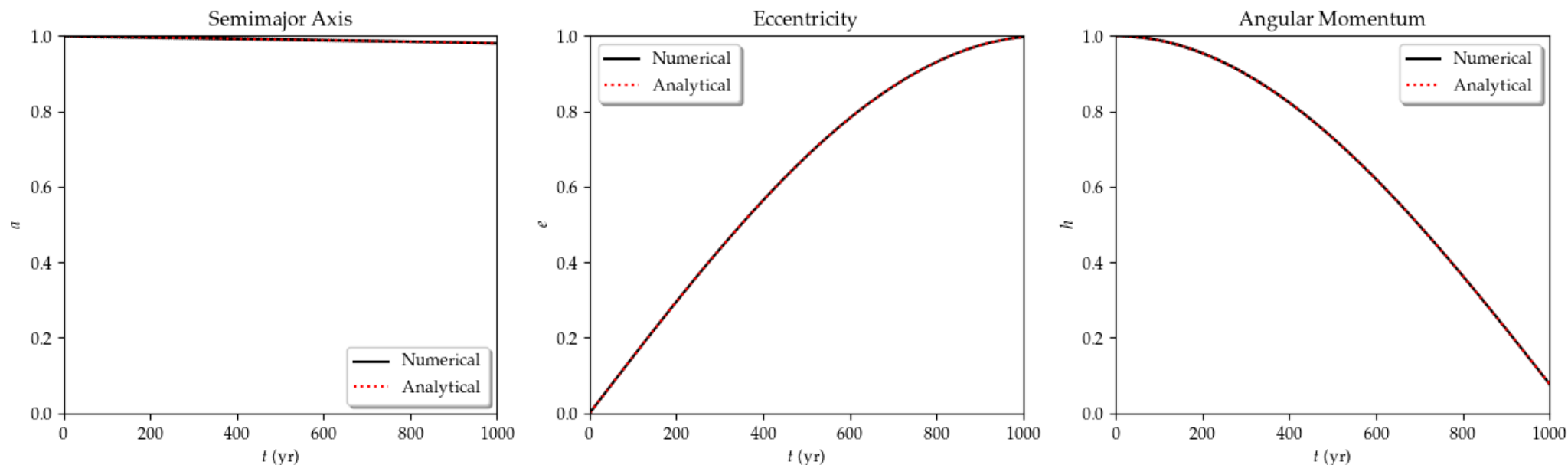
$$\tau_{\text{eff}} = (m_1 + m_2) \frac{\tau_1 \tau_2}{\tau_2 m_2 + \tau_1 m_1}.$$

Exponential decay of angular momentum

$$h = h_0 e^{-t/\tau_{\text{eff}}}.$$



Wind solution

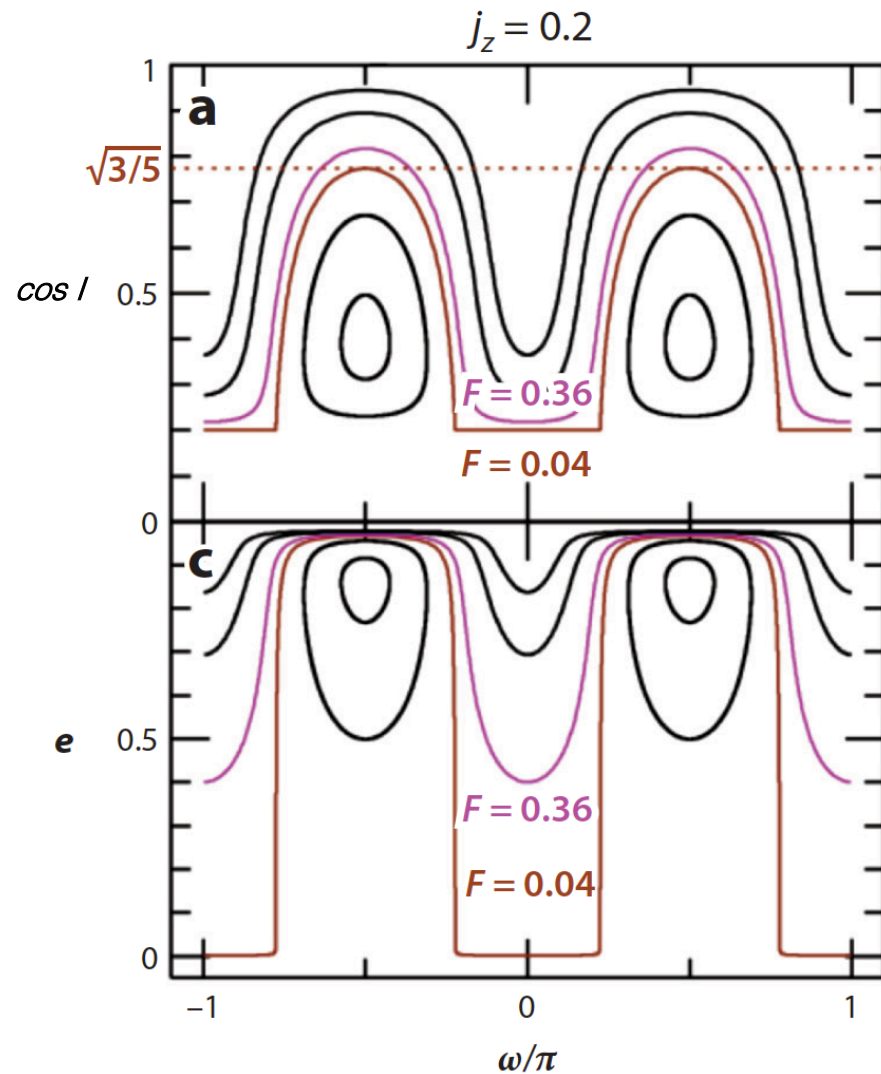


$$\langle a(t) \rangle = a_0 e^{-2t/\tau}$$

$$\langle e(t) \rangle = \cos \left[\cos^{-1} e_0 + \frac{3u}{2} \sqrt{\frac{a_0}{\mu}} \left(1 - e^{-t/\tau} \right) \right]$$

$$\langle h(t) \rangle = e^{-t/\tau} \left\{ h_0 - 1 + \cos \left[\frac{3}{2} a_0 u \left(1 - e^{-t/\tau} \right) \right] \right\}$$

Kozai-Lidov Oscillations

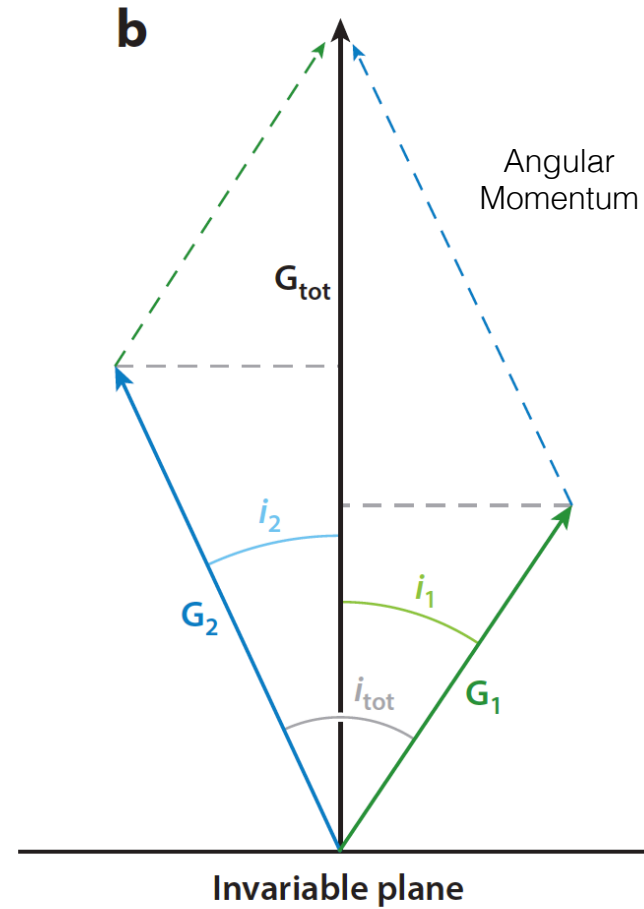
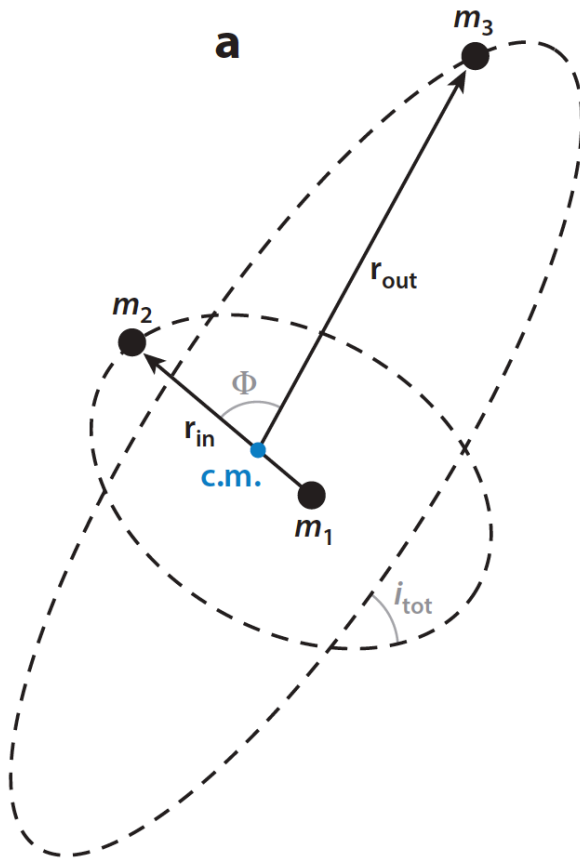


Conserved quantity is not angular momentum, but vertical angular momentum

$$j_z = (1-e^2)^{1/2} \cos i$$

Cycles of inclination and eccentricity.

Kozai-Lidov Oscillations



Conserved quantity is not angular momentum,
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Public code for Kozai-Lidov oscillations with tidal friction, permanent quadrupole, and gas drag.

