

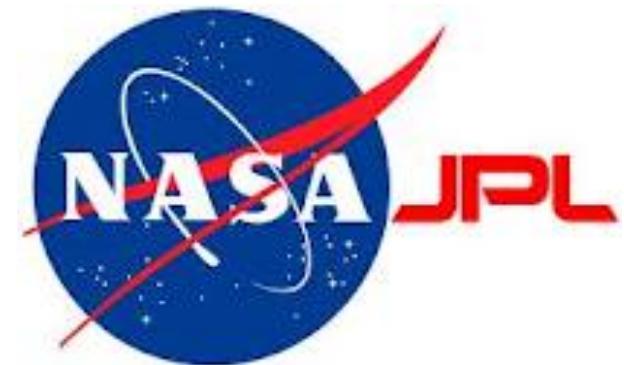
# Evolution of circumstellar disks and planet formation

**Wladimir (Wlad) Lyra**

**Sagan Postdoctoral Fellow**



**Caltech - JPL**



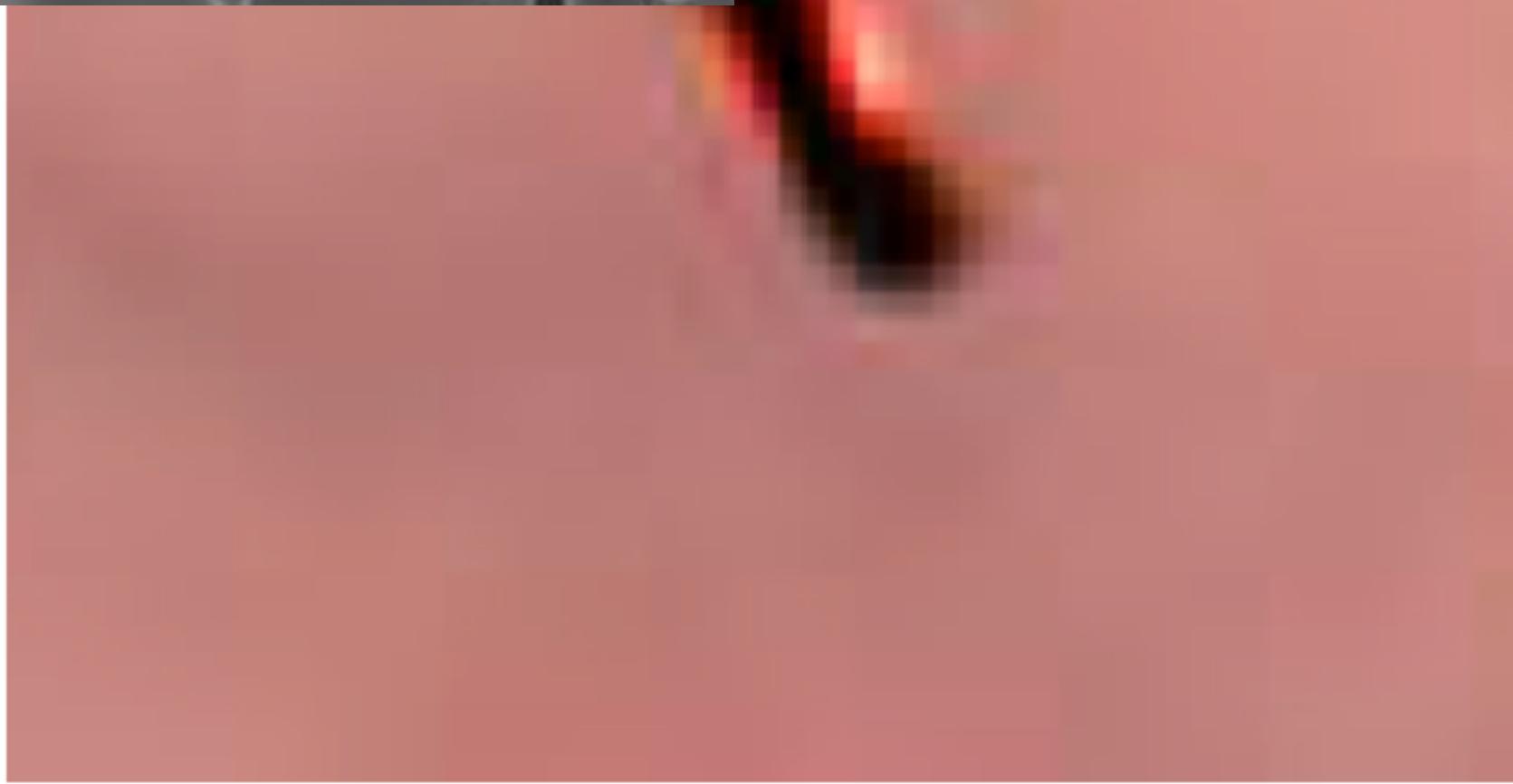
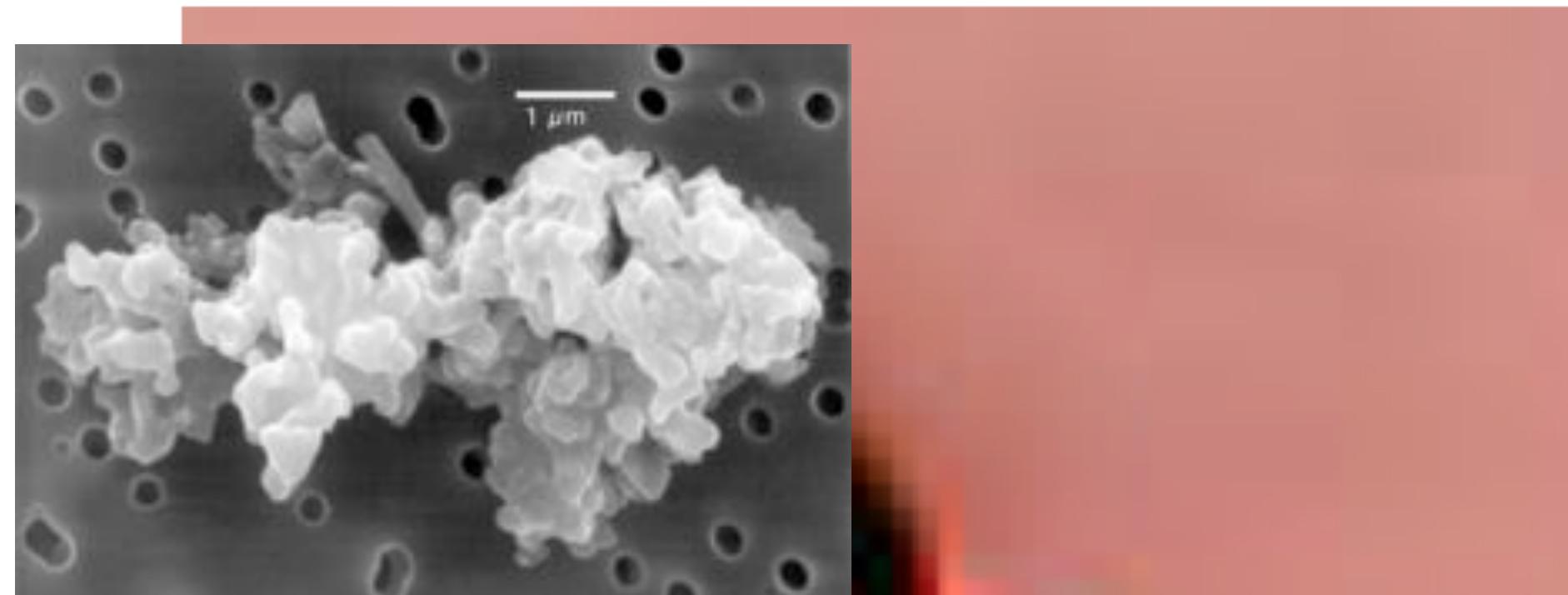
Aaron Boley (Vancouver), Axel Brandenburg (Stockholm), Kees Dullemond (Heidelberg),  
Anders Johansen (Lund), Tobias Heinemann (KITP), Hubert Klahr (Heidelberg),  
Min-Kai Lin (ASU), Mordecai-Mark Mac Low (AMNH), Colin McNally (NBI),  
Krzysztof Mizerski (Warsaw), Sijme-Jan Paardekooper (QMUL), Nikolai Piskunov (Uppsala),  
Natalie Raettig (Heidelberg), Alex Richert (PSU), Neal Turner (JPL),  
Miguel de Val-Borro (Princeton), Andras Zsom (MIT).

Amsterdam, The Netherlands

March 11<sup>th</sup>, 2015

# Outline

- Turbulence
  - Active and dead zones
  - Magneto-rotational and baroclinic instability
  - Vortices and elliptic instability
- Active/dead boundary
  - Rossby wave instability
- Vortex-mode of planet formation
- Observational constraints



# Protoplanetary Disks



## PP disk fact sheet

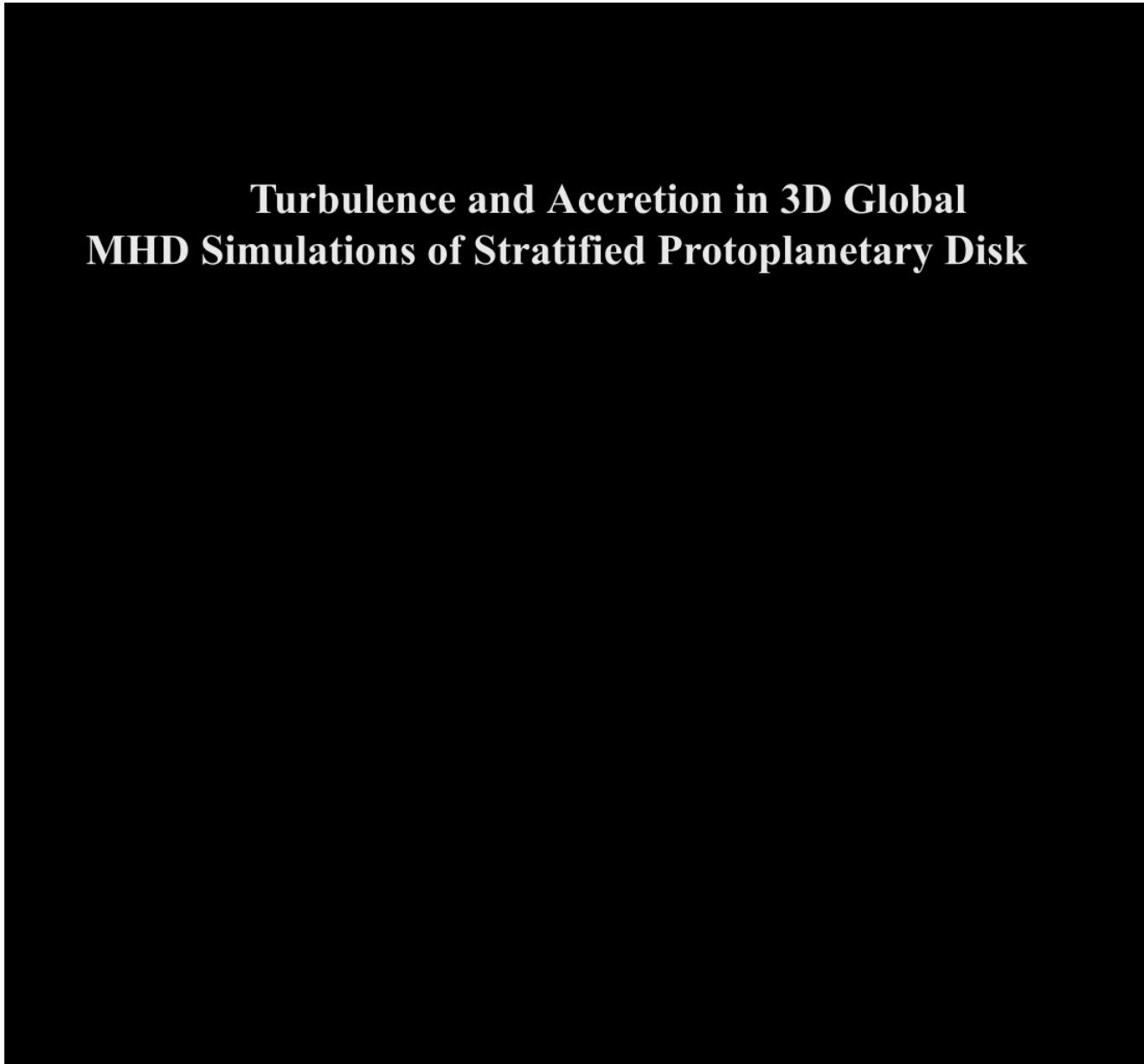
Density:  $10^{13} - 10^{15} \text{ cm}^{-3}$   
(Air:  $10^{21} \text{ cm}^{-3}$ )

Temperature: 10-1000 K

Scale: 0.1-100AU  
(1 AU =  $1.49 \times 10^{13} \text{ cm}$ )

Mass:  $10^{-3} - 10^{-1} M_{\text{sun}}$   
( $1 M_{\text{sun}} = 2 \times 10^{33} \text{ g}$ )

# Magneto-Rotational Instability



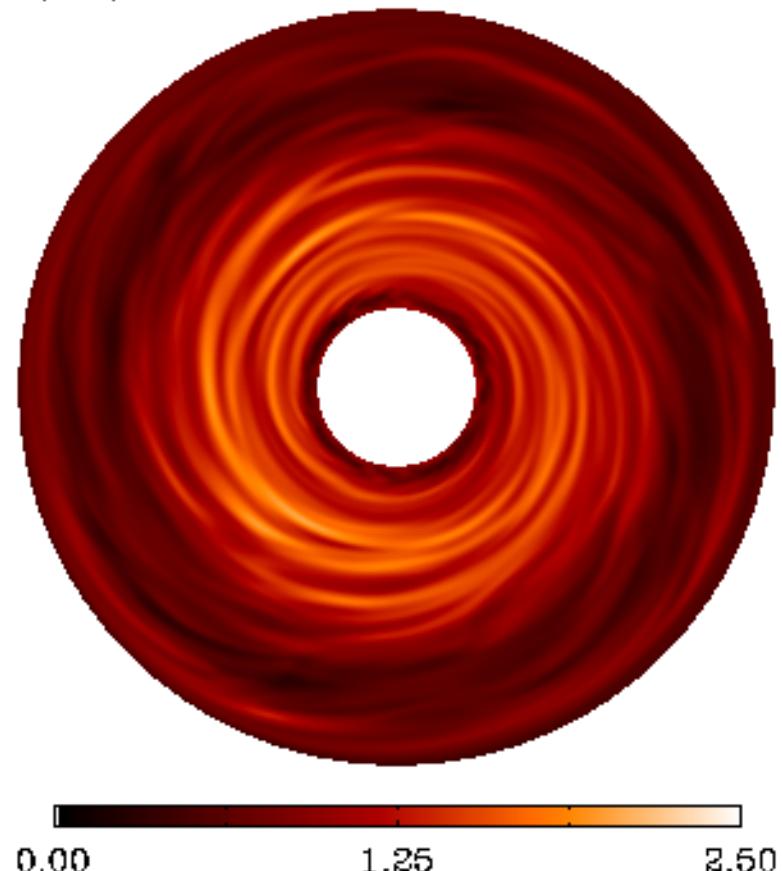
**Turbulence and Accretion in 3D Global  
MHD Simulations of Stratified Protoplanetary Disk**

Video credit: Mario Flock (MPIA/CEA)

# Accretion in disks occurs via turbulent viscosity

Turbulence in disks is enabled by  
the Magneto-Rotational Instability

$t=46.3/88\text{yr}$



Slower  
Rotation

Stretching  
amplifies  
B-field

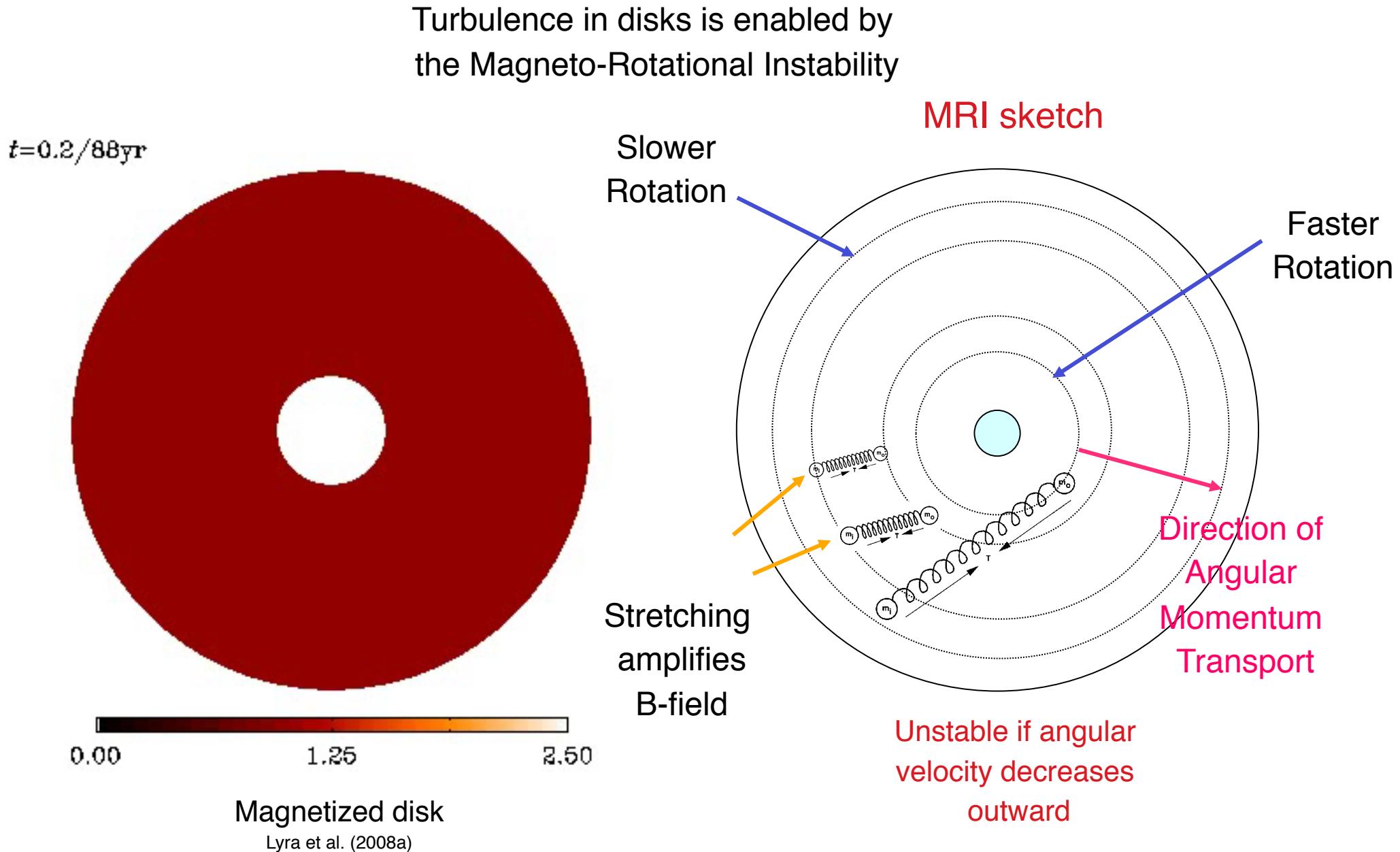
**MRI sketch**

Unstable if angular  
velocity decreases  
outward

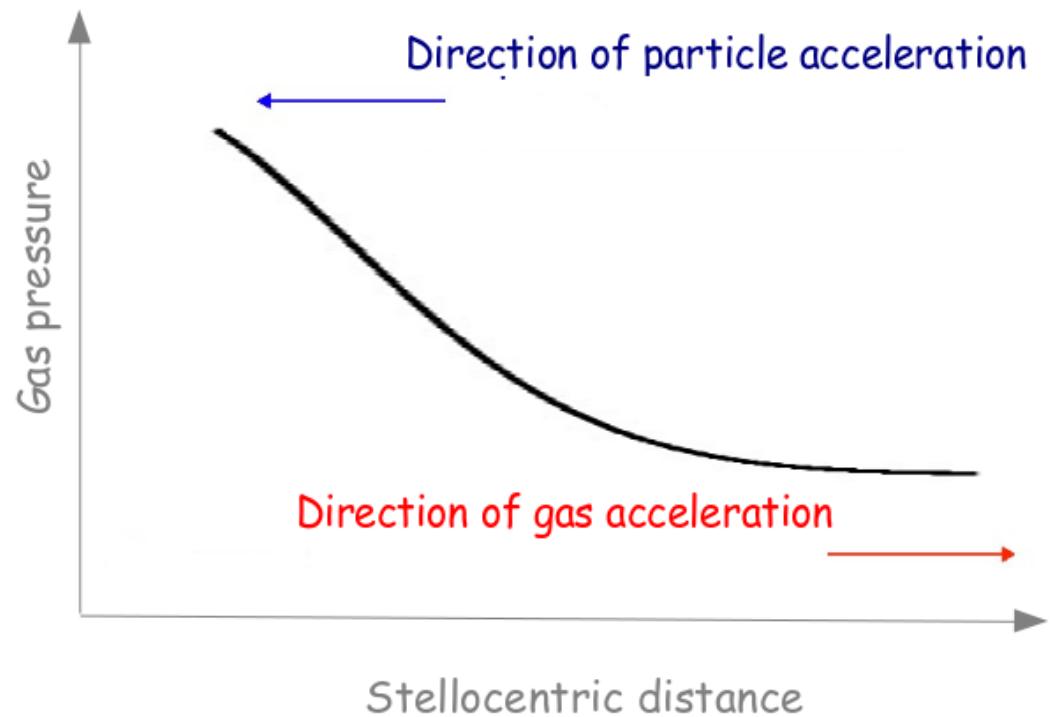
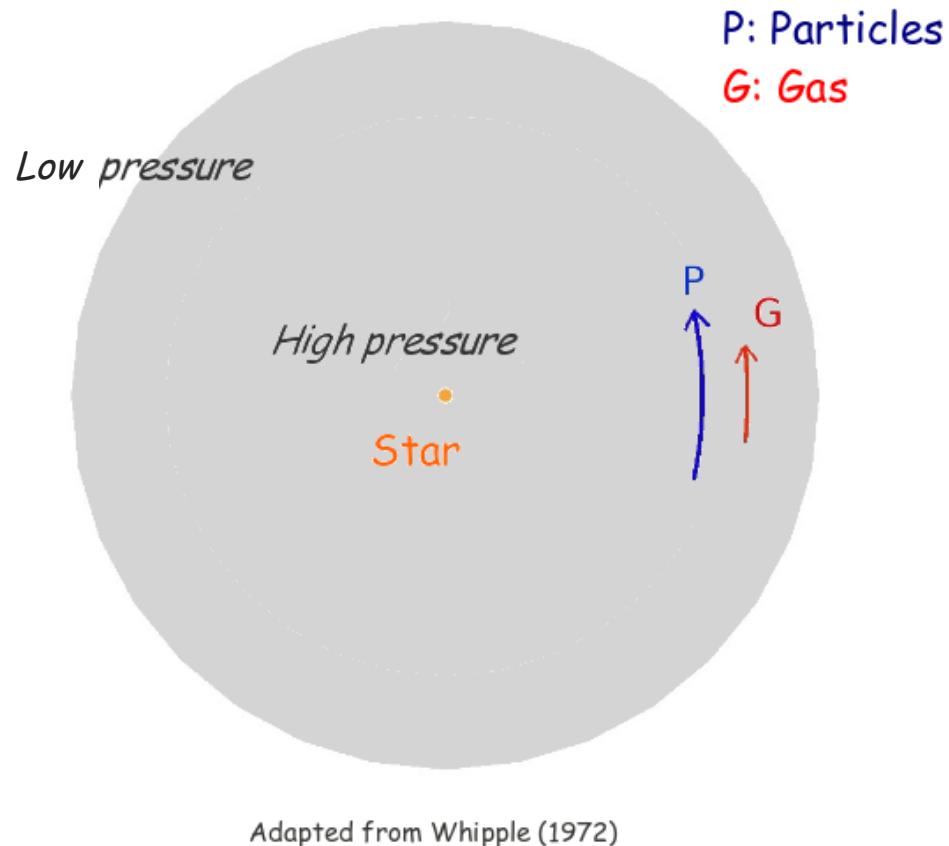
Faster  
Rotation

Direction of  
Angular  
Momentum  
Transport

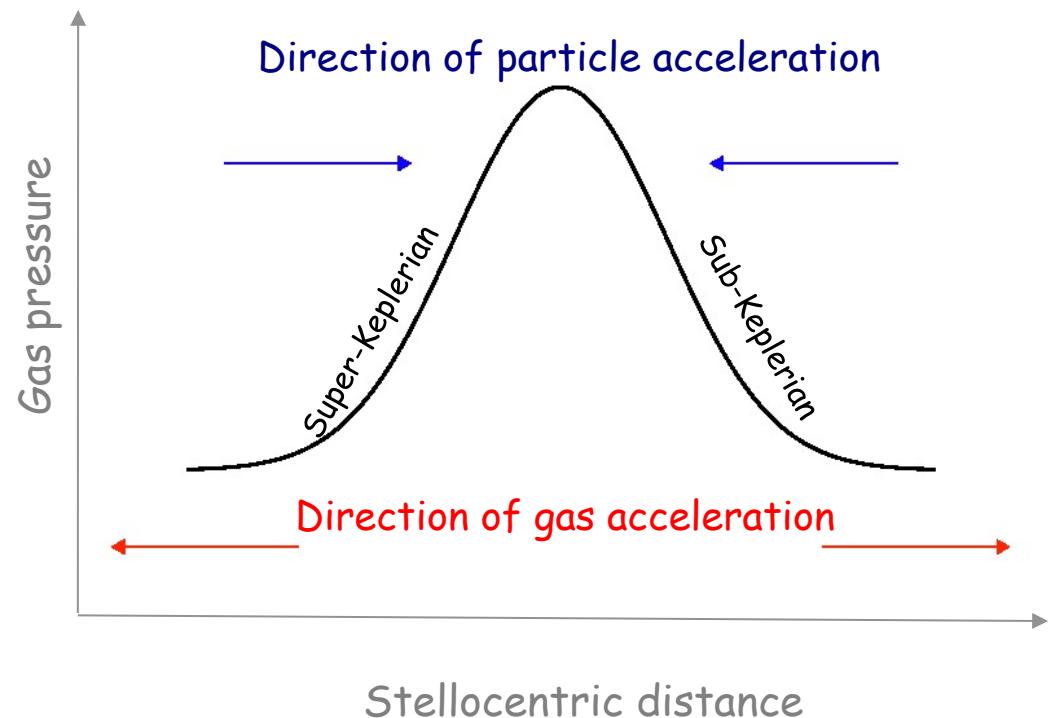
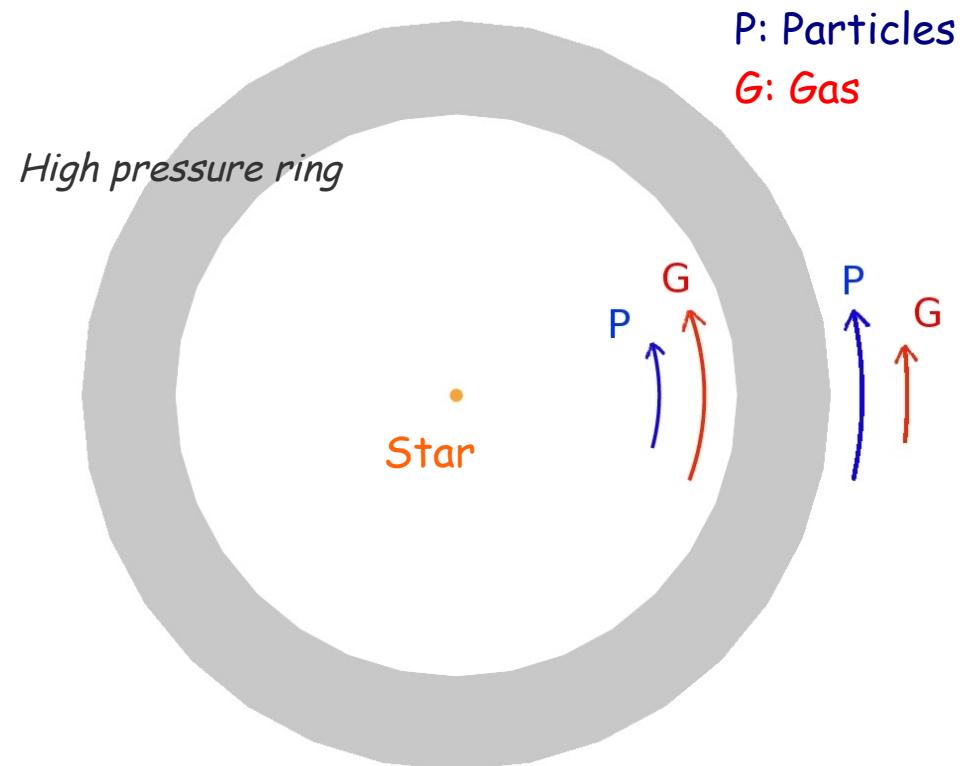
# Accretion in disks occurs via turbulent viscosity



# Particle drift

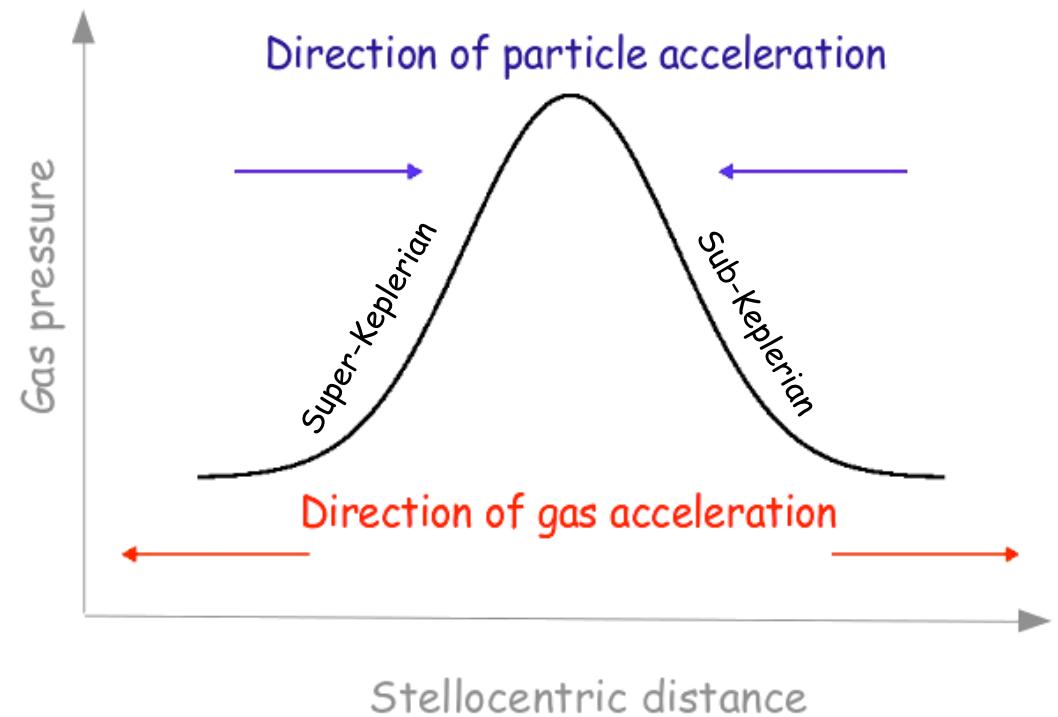
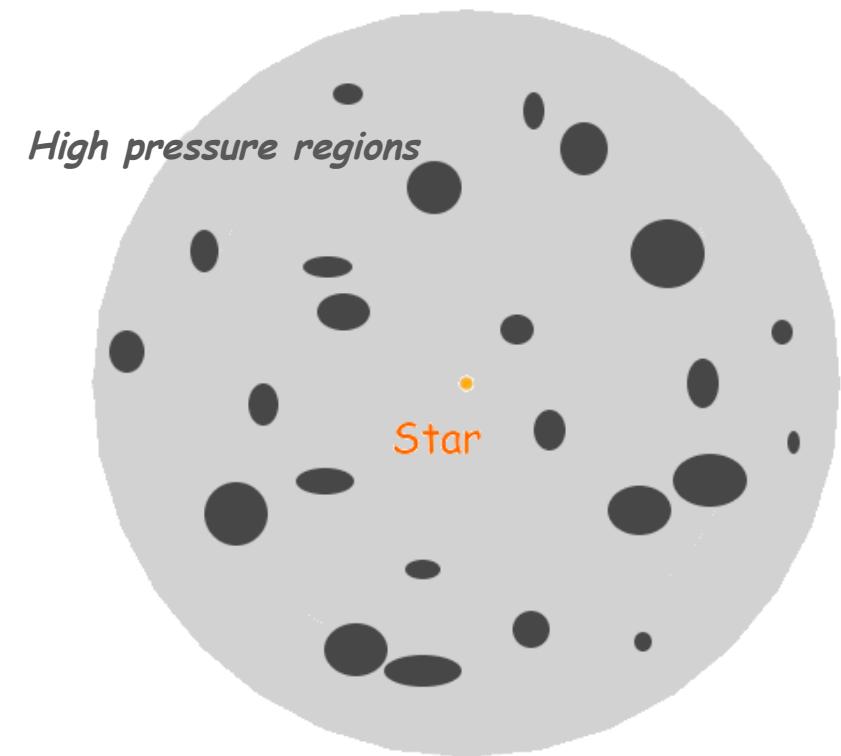


# Pressure Trap

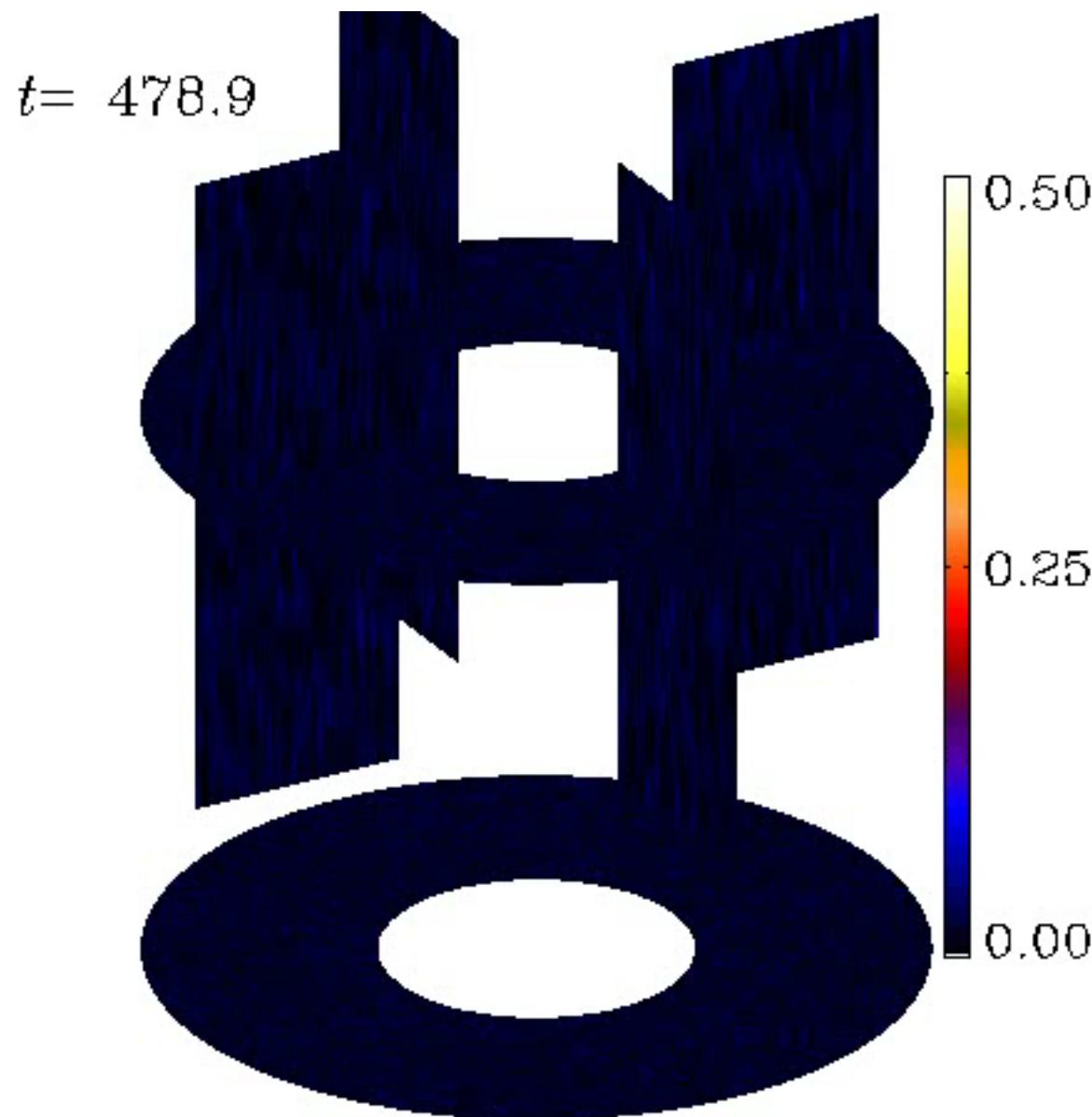


Adapted from Whipple (1972)

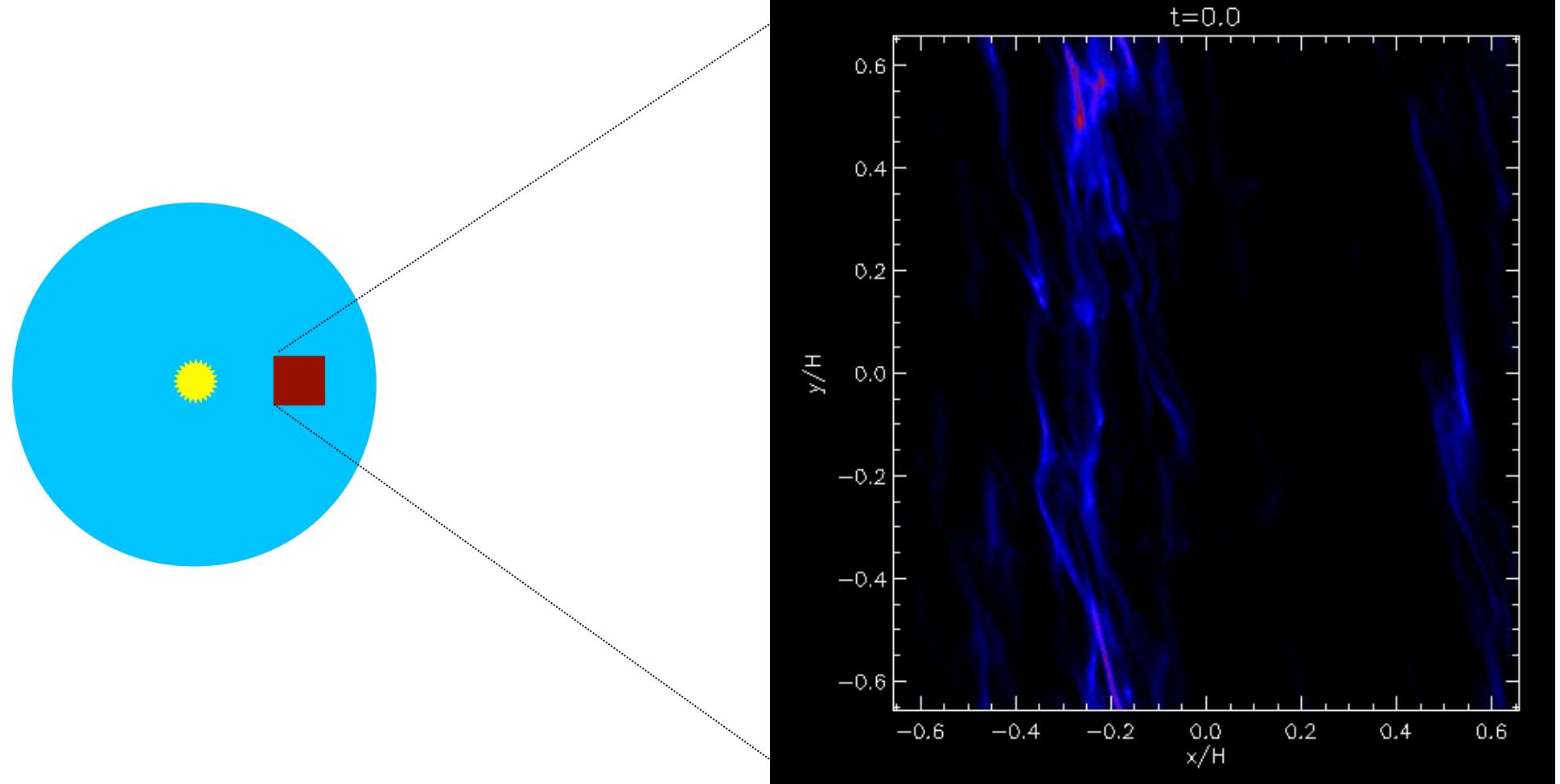
# Pressure Trap



# Turbulence concentrates solids mechanically in pressure maxima

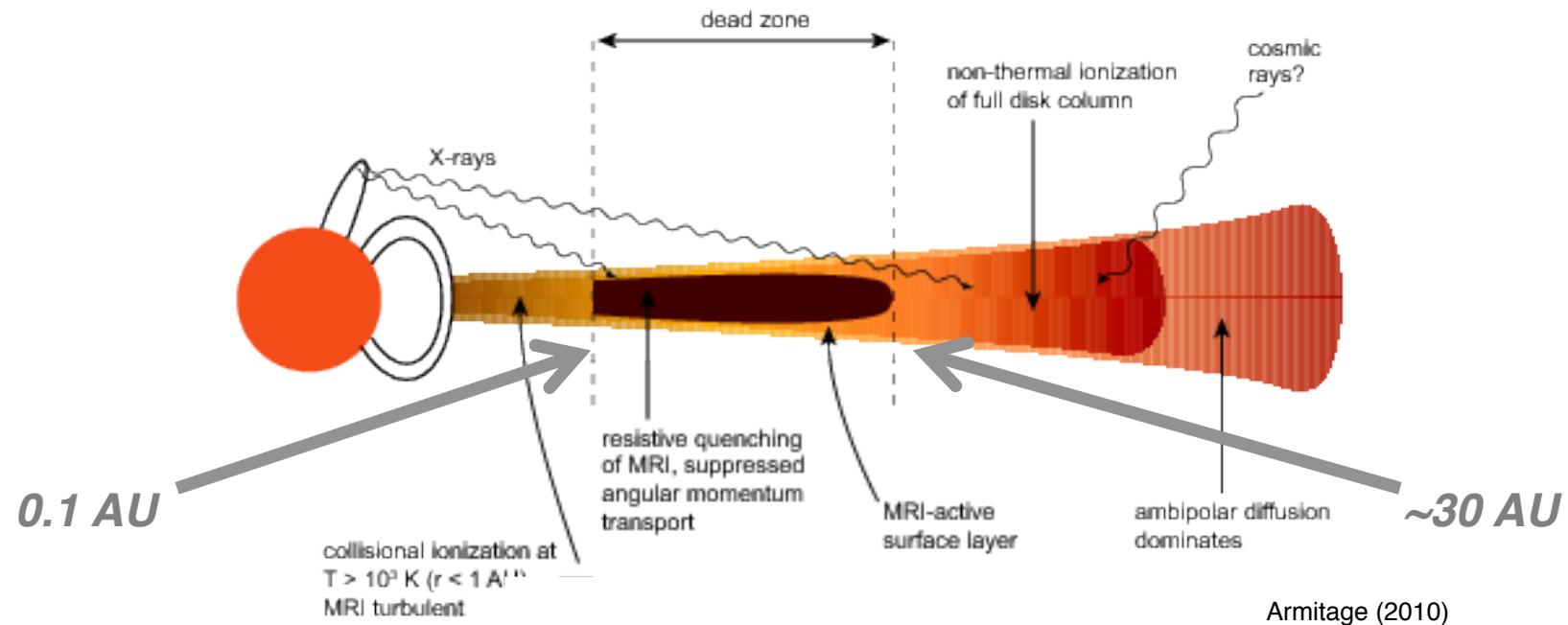


# Gravitational collapse into planetesimals



Johansen et al. (2007)

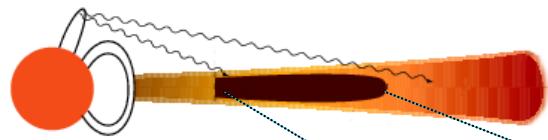
# Dead zones are robust features of protoplanetary disks



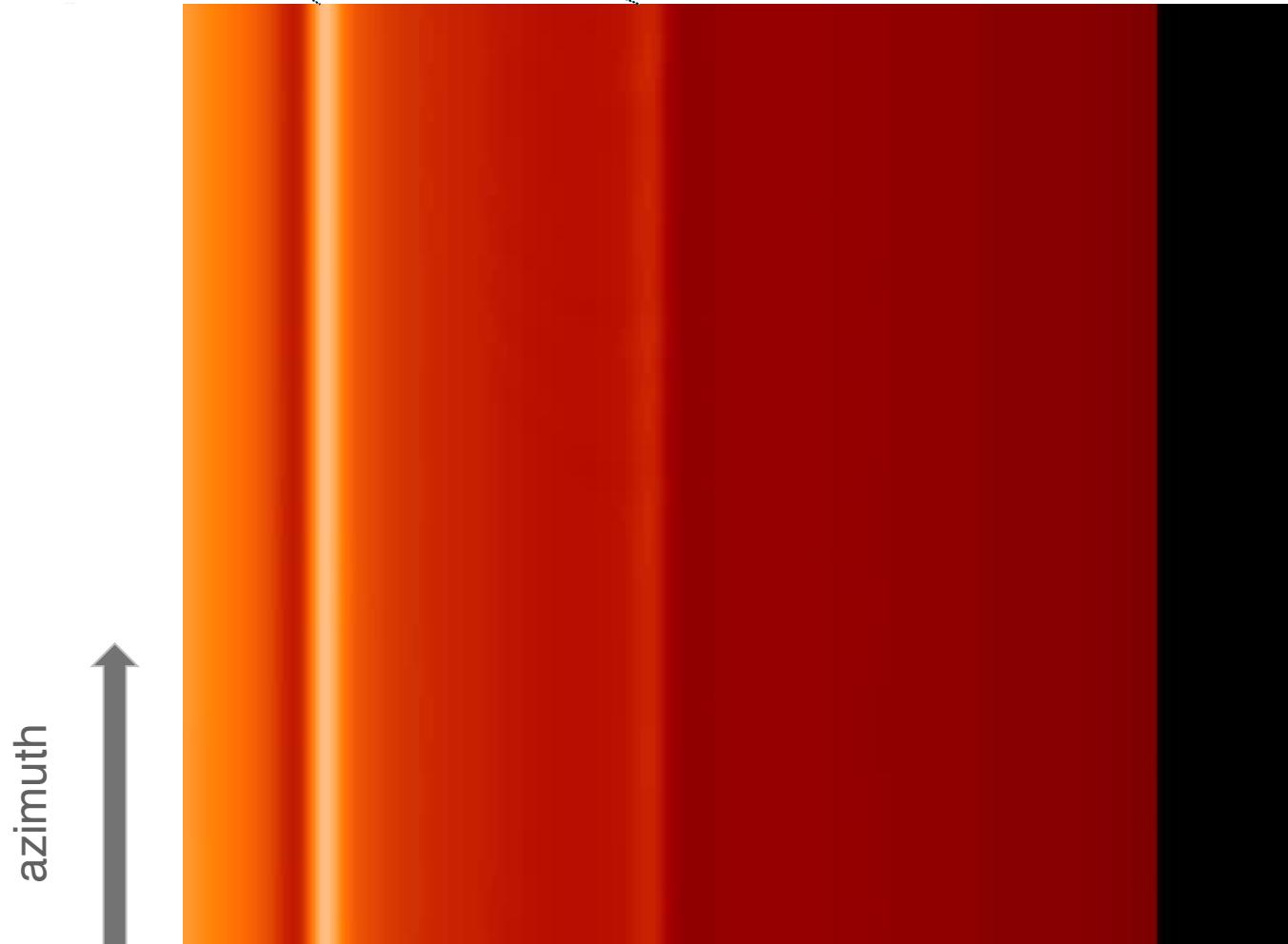
Disks are cold and thus poorly ionized  
(Blaes & Balbus 1994)

Therefore, accretion is **layered**  
(Gammie 1996)

There should be a **magnetized, active zone**,  
and a **non-magnetic, dead zone**.



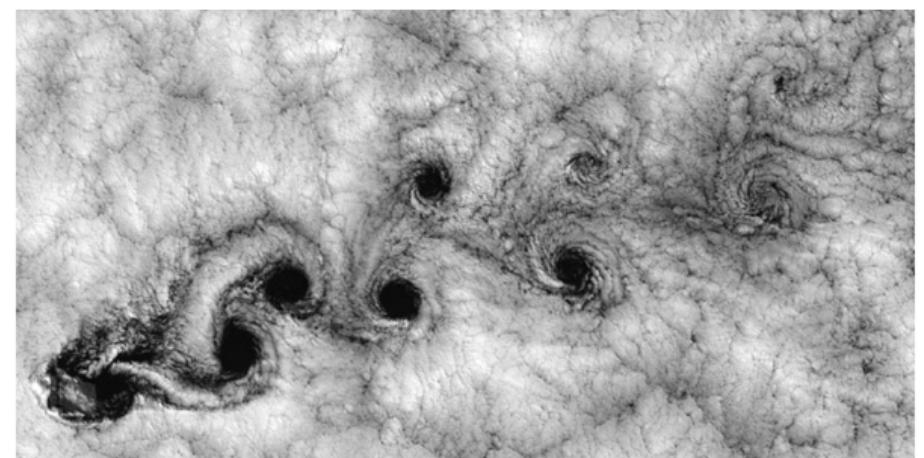
## A simple dead zone model



radius

Lyra et al. (2008b, 2009a);  
See also Varniere & Tagger (2006)

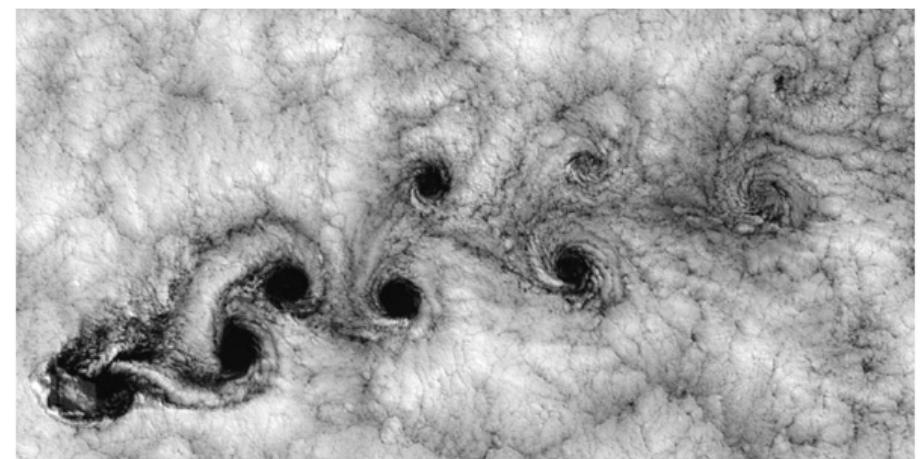
# Vortices – an ubiquitous fluid mechanics phenomenon



# Vortices – an ubiquitous fluid mechanics phenomenon

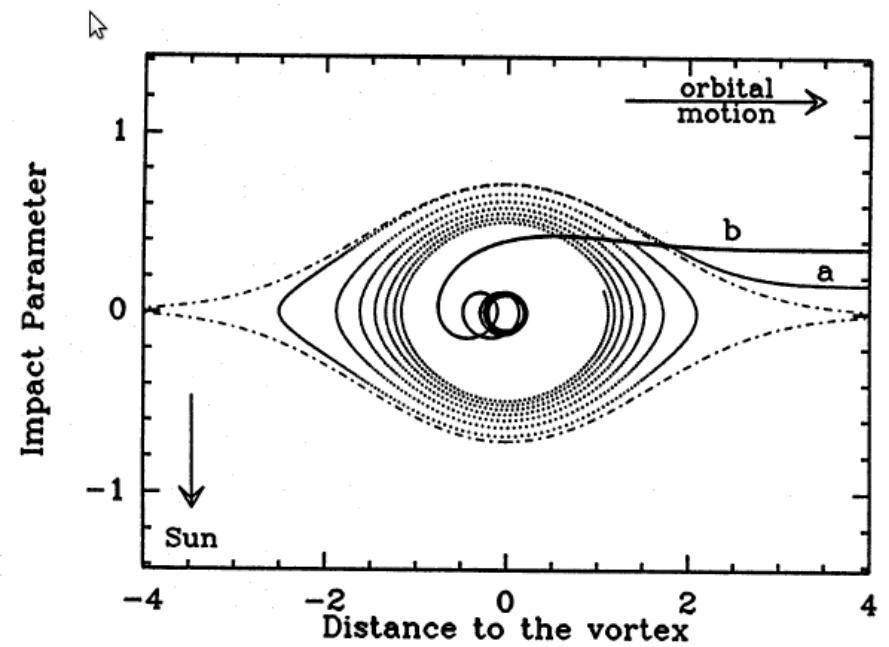
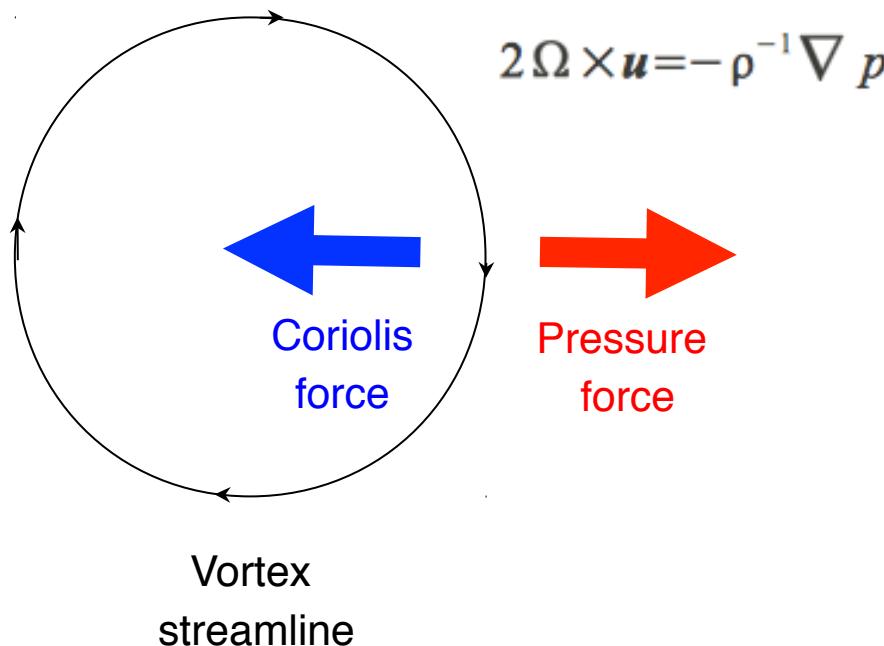


## Von Kármán *vortex street*



# The Tea-Leaf effect

Geostrophic balance:



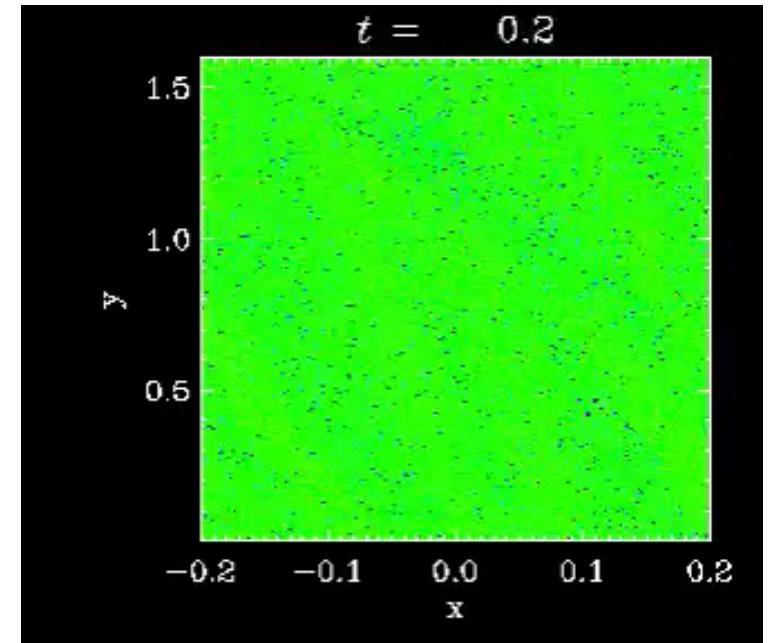
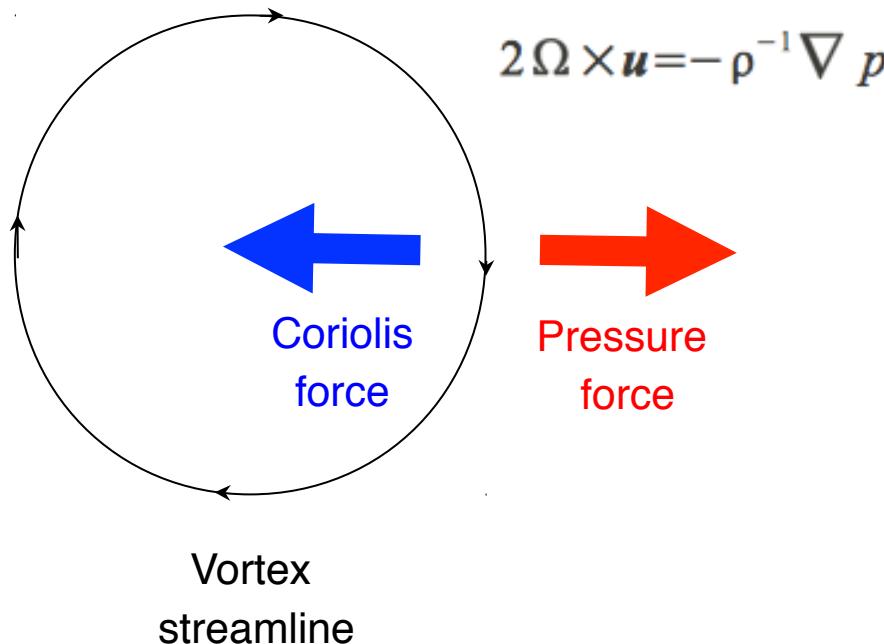
Particles do not feel the pressure gradient.  
They sink towards the center, where they accumulate.

Aid to planet formation  
(Barge & Sommeria 1995, Adams & Watkins 1996, Tanga et al. 1996)

Speed up planet formation enormously  
(Lyra et al. 2008b, 2009ab, Raettig et al. 2012)

# The Tea-Leaf effect

Geostrophic balance:



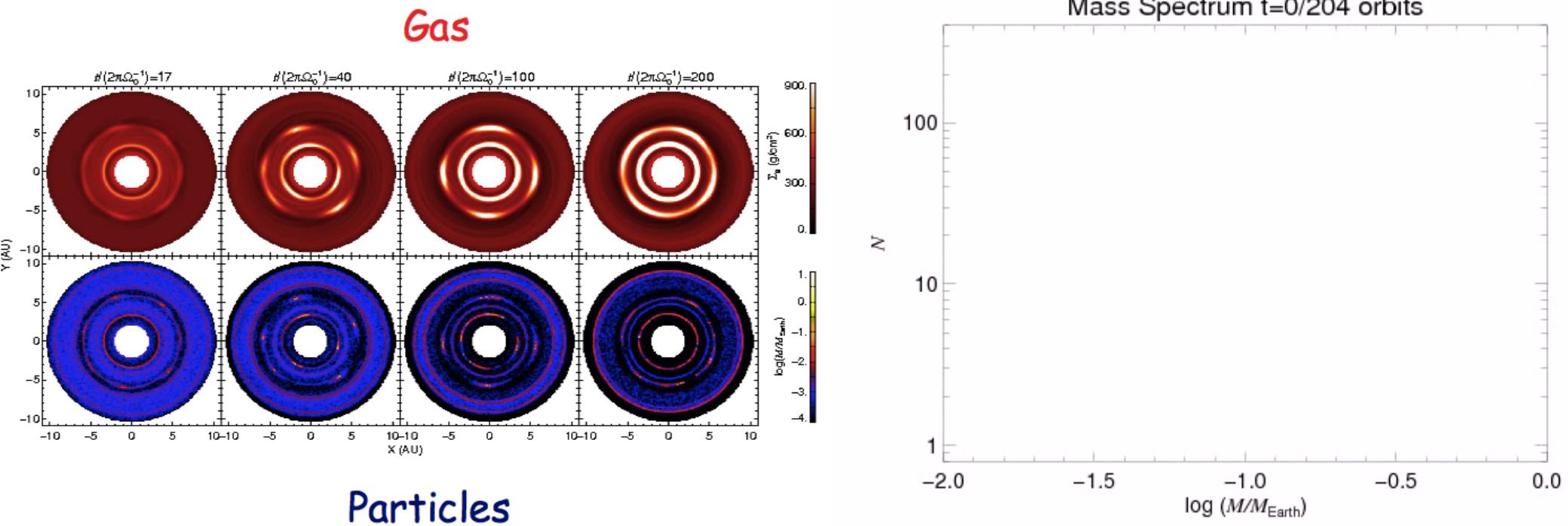
Raettig et al. (2012)

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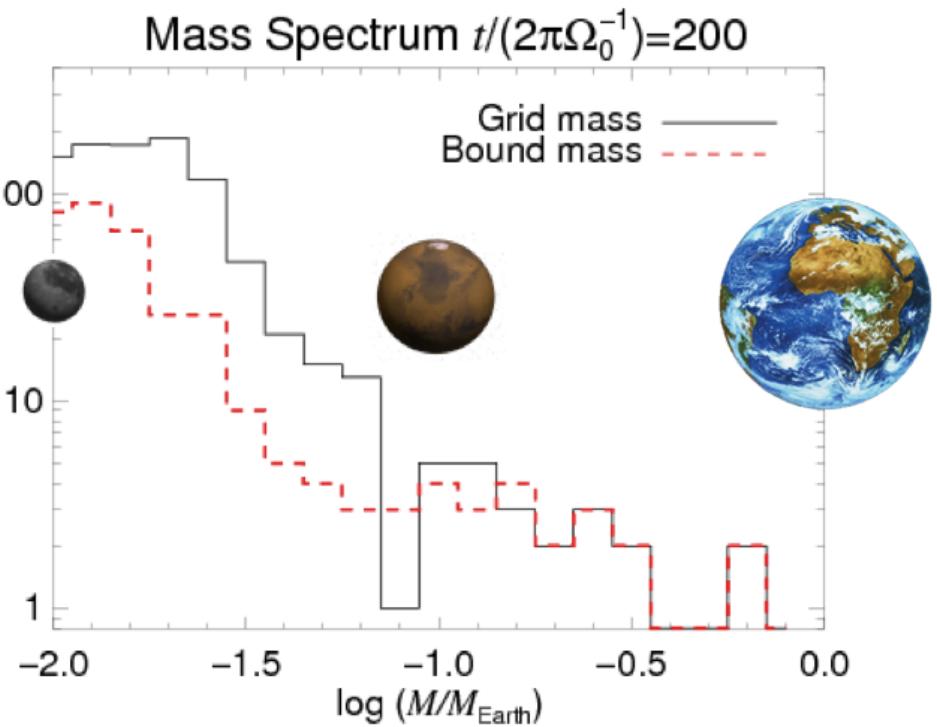
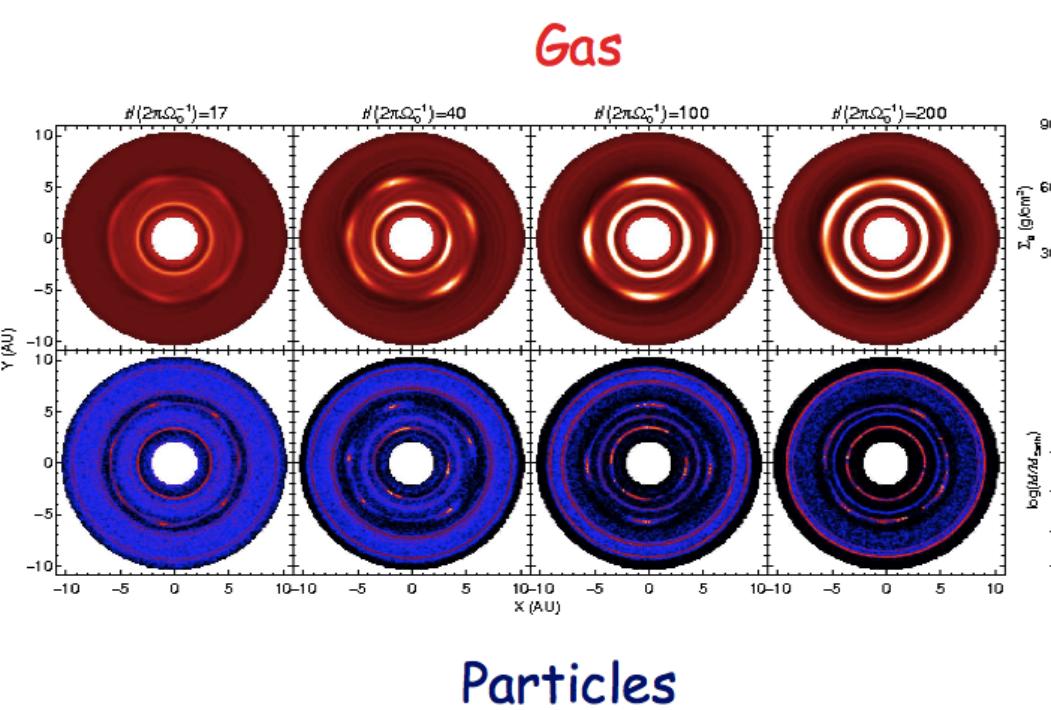
# Vortices and Planet Formation



Collapse into Mars mass objects

(Lyra et al. 2008b, 2009a,  
see also Lambrechts & Johansen 2012)

# Vortices and Planet Formation

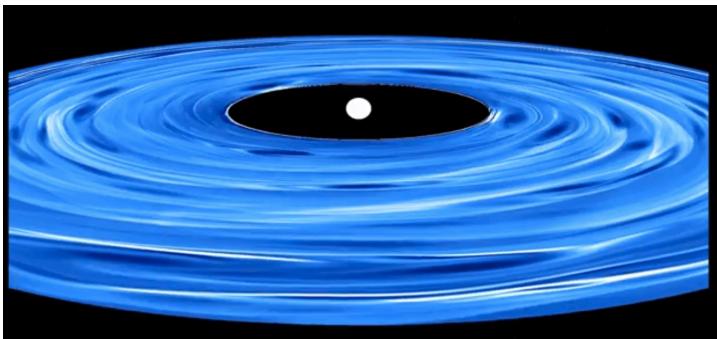


Collapse into Mars mass objects

(Lyra et al. 2008b, 2009a,  
see also Lambrechts & Johansen 2012)

# Sustaining vortices in disks

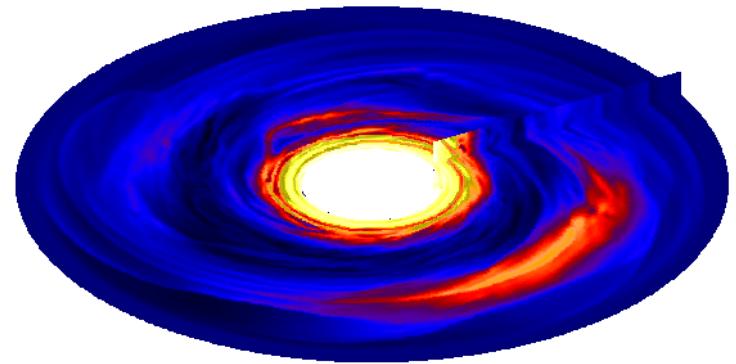
## Baroclinic instability (*Convective overstability*)



Klahr & Bodenheimer (2003), Klahr (2004),  
Johnson & Gammie (2005), Petersen et al. (2007ab),  
Lesur & Papaloizou (2010), Lyra & Klahr (2011), Raettig et al. (2013)  
Klahr & Hubbard (2014), Lyra (2014)

Powered by:  
Buoyancy, thermal diffusion  
(baroclinic source term)

## Rossby wave instability

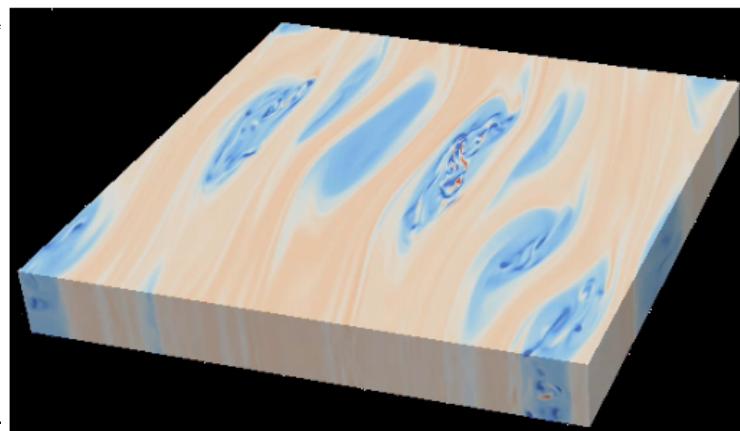
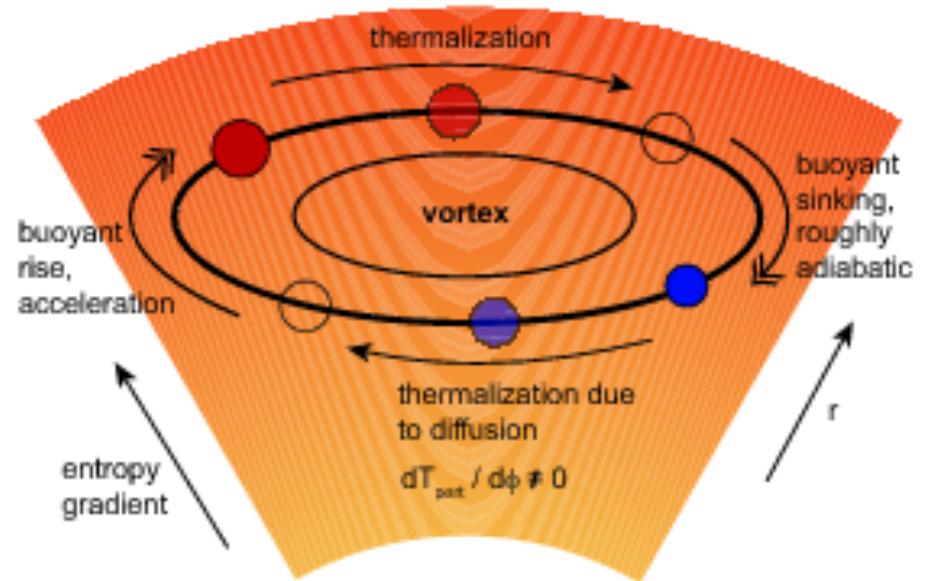


Lovelace & Hohlfield (1978), Toomre (1981), Papaloizou & Pringle (1984, 1985), Hawley et al. (1987), Lovelace et al. (1999), Li et al. (2000, 2011), Tagger (2001), Varniere & Tagger (2006), de Val-Borro et al. (2007), Lyra et al. (2008b, 2009ab), Mehuet et al. (2010, 2012abc), Lin & Papaloizou (2011ab, 2012), Lyra & Mac Low (2012), Regaly et al. (2012, 2013), Lin (2012ab, 2013), Ataiee et al. (2013, 2014), Lyra et al. (2014)

Powered by:  
Modification of shear profile  
**(external vorticity reservoir)**

# Baroclinic Instability – Excitation and self-sustenance of vortices

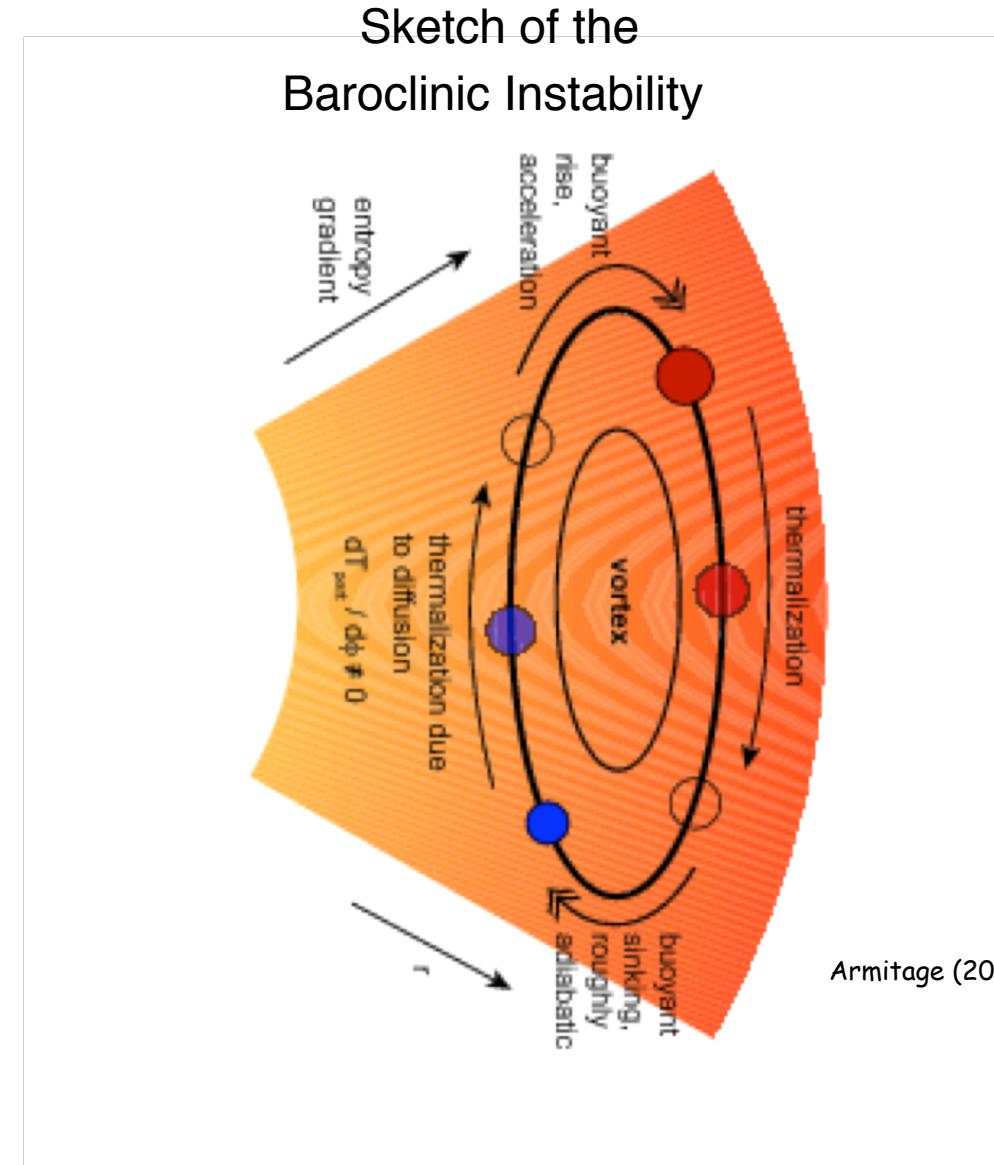
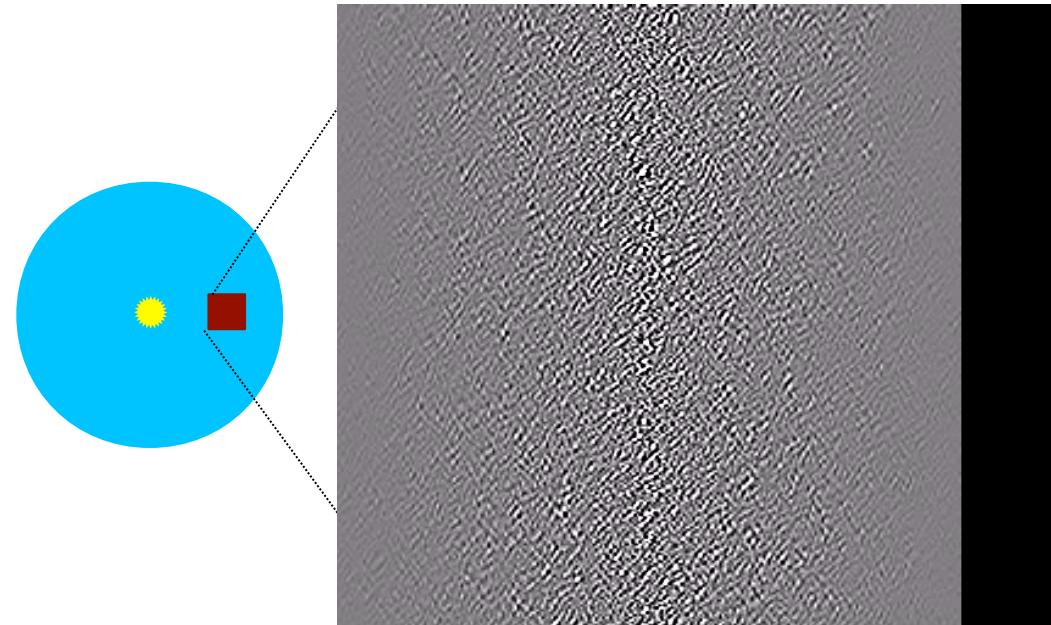
Sketch of the  
Baroclinic Instability



Lesur & Papaloizou (2010)

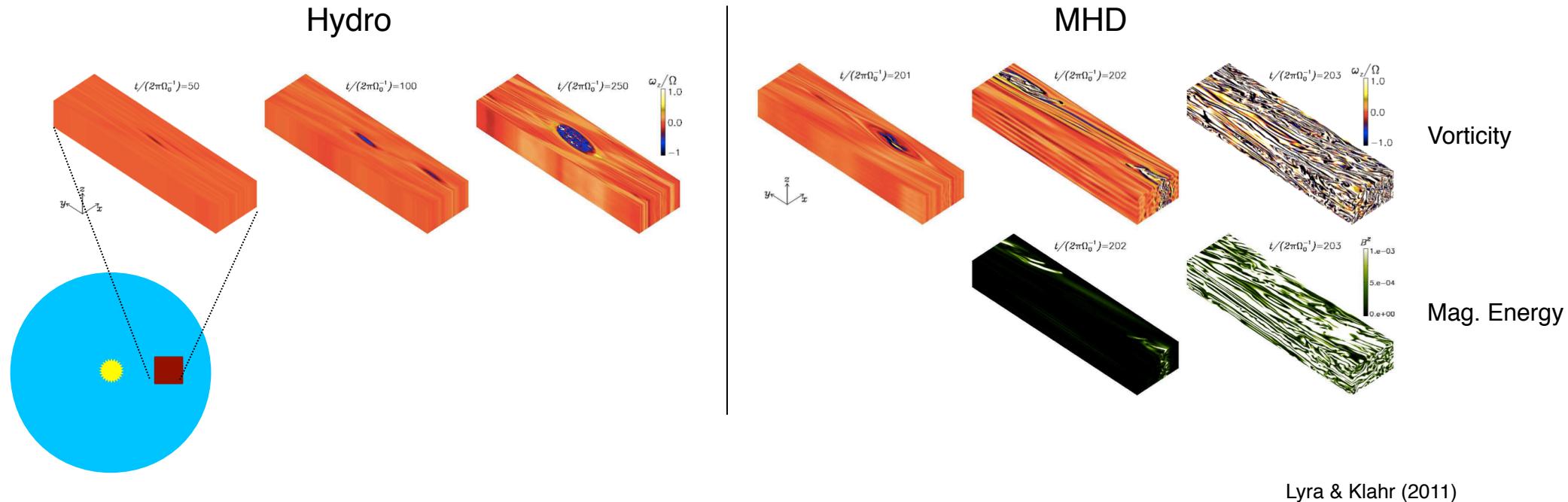
Armitage (2010)

# Baroclinic Instability – Excitation and self-sustenance of vortices



# Baroclinic instability and layered accretion

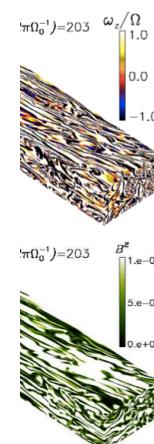
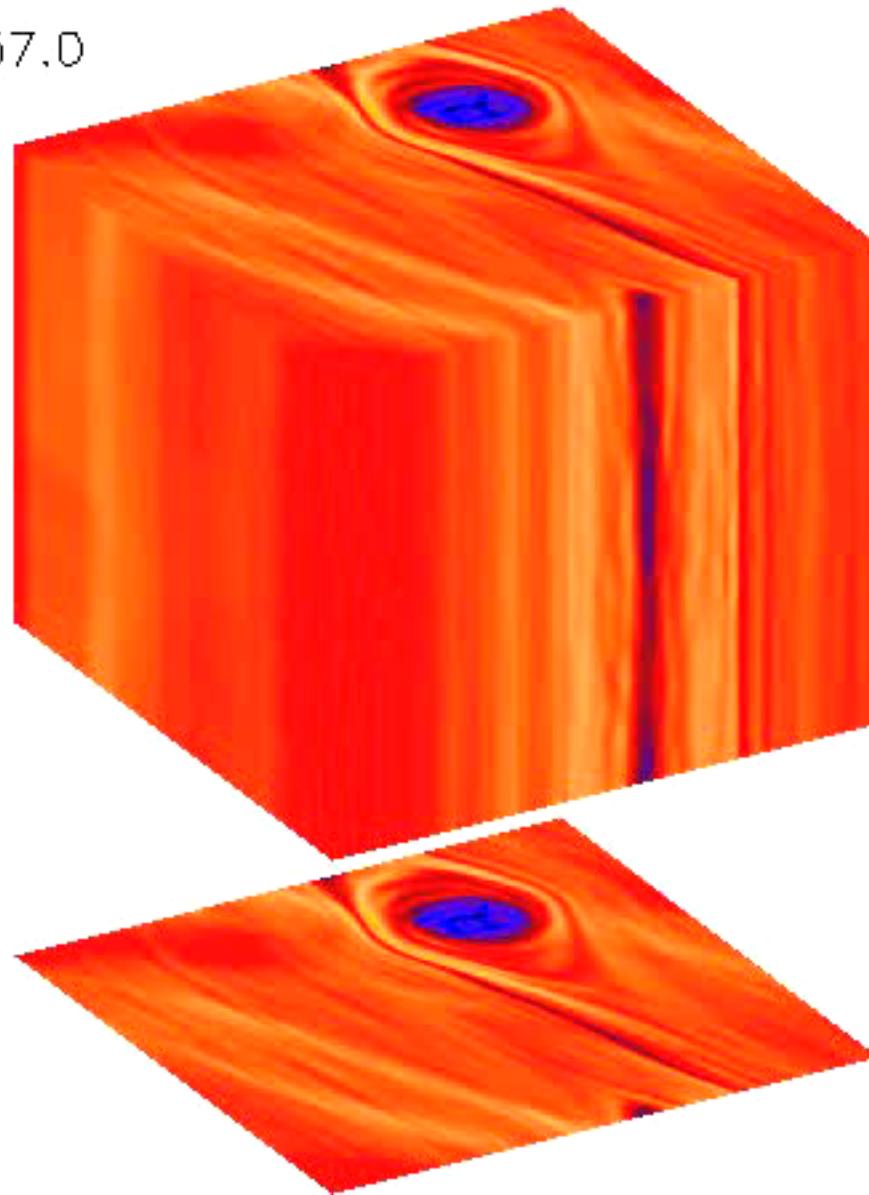
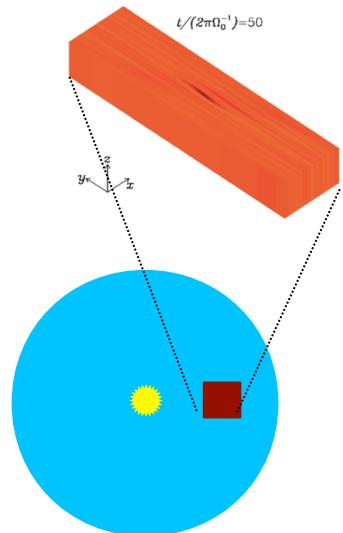
What happens when the vortex is magnetized?



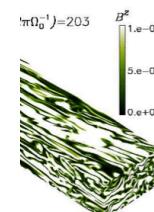
Lyra & Klahr (2011)

# Baroclinic instability and layered accretion

$t=1257.0$



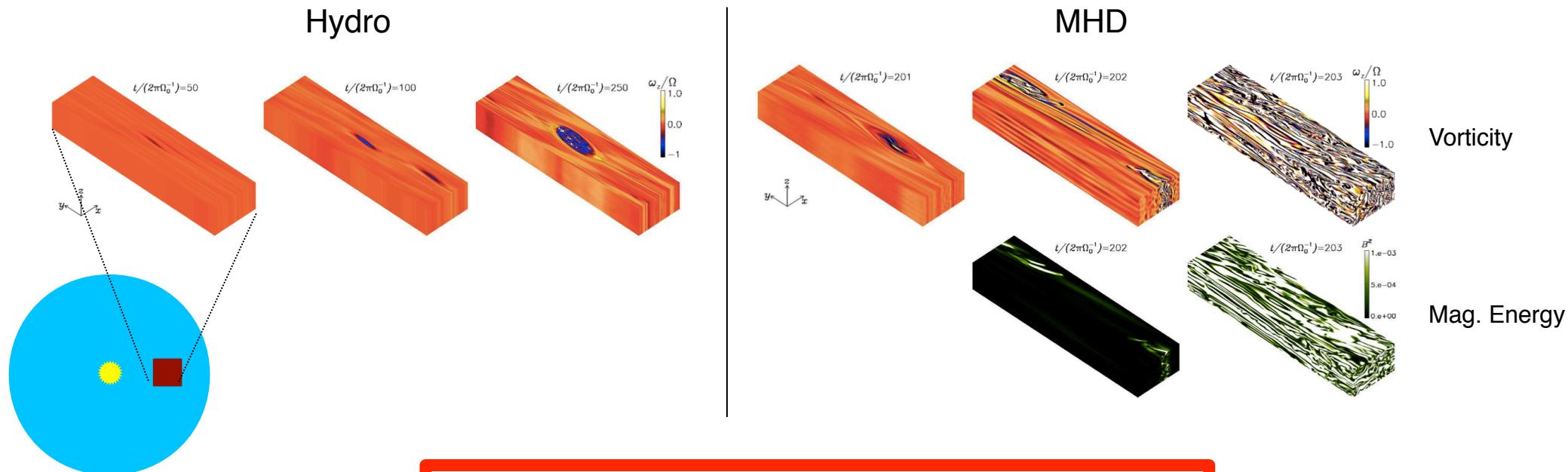
Vorticity



Mag. Energy

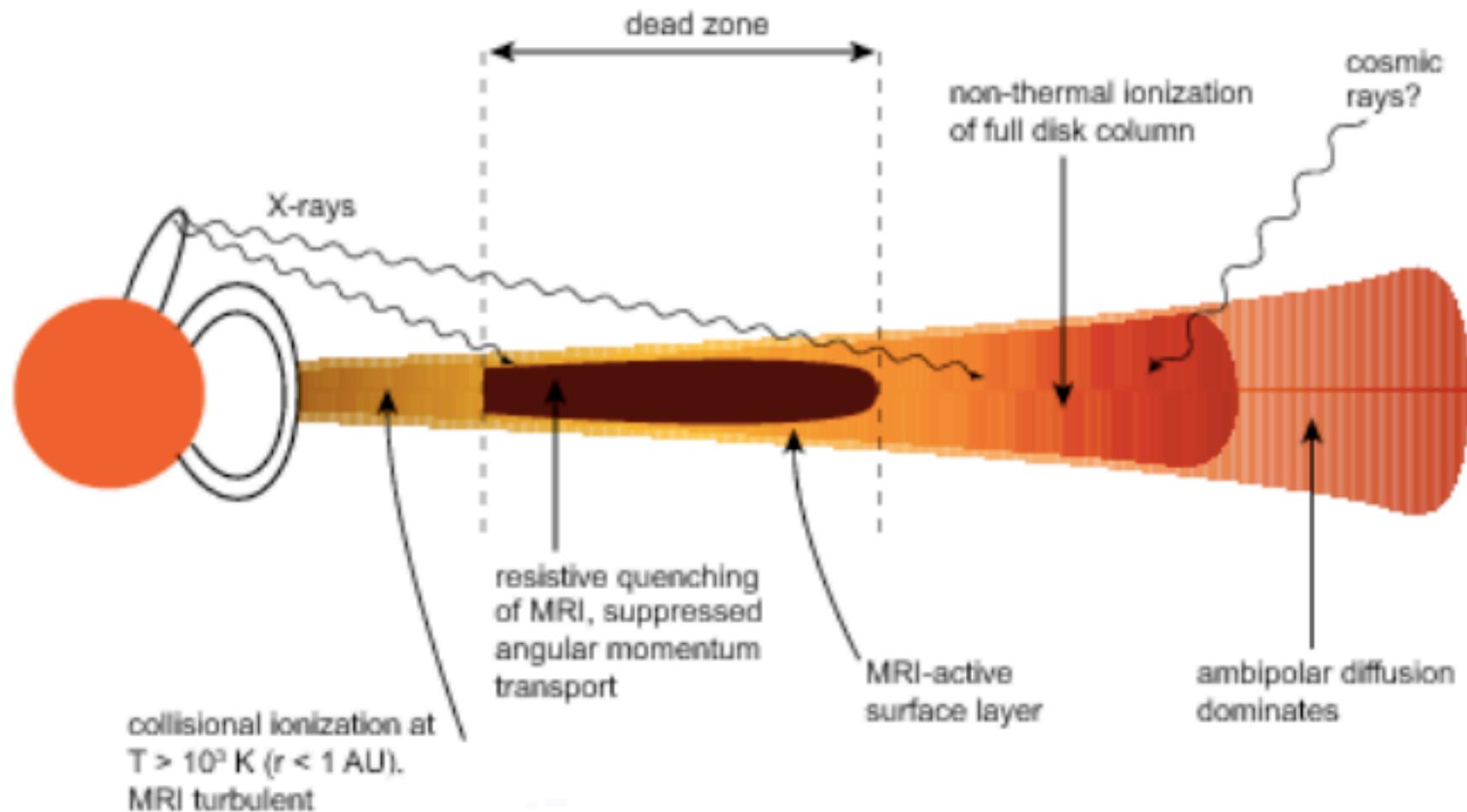
# Baroclinic instability and layered accretion

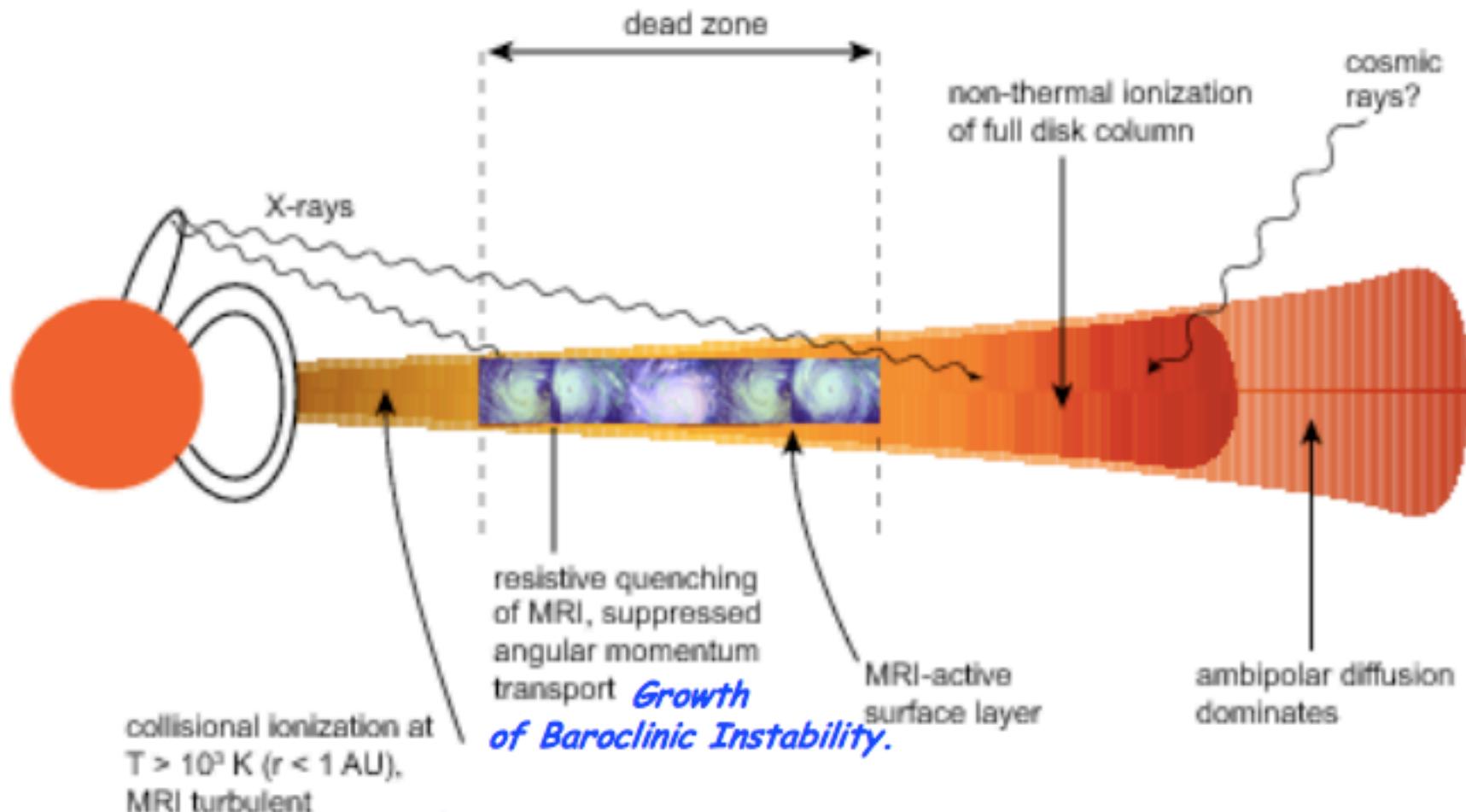
What happens when the vortex is magnetized?



Baroclinic vortices  
do **not** survive magnetization

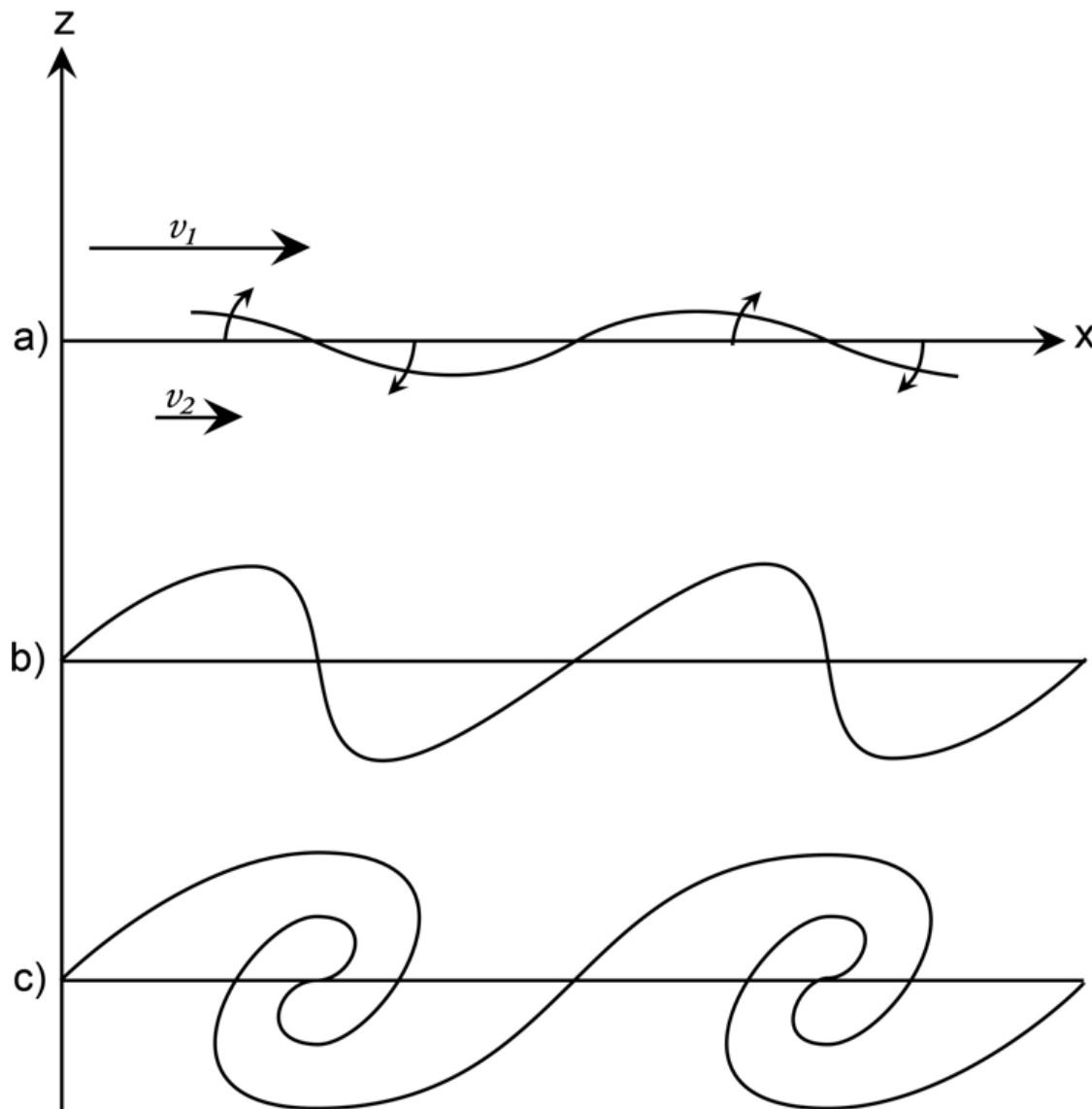
Lyra & Klahr (2011)





# Rossby Wave Instability

(or... Kelvin-Helmholtz in rotating disks)

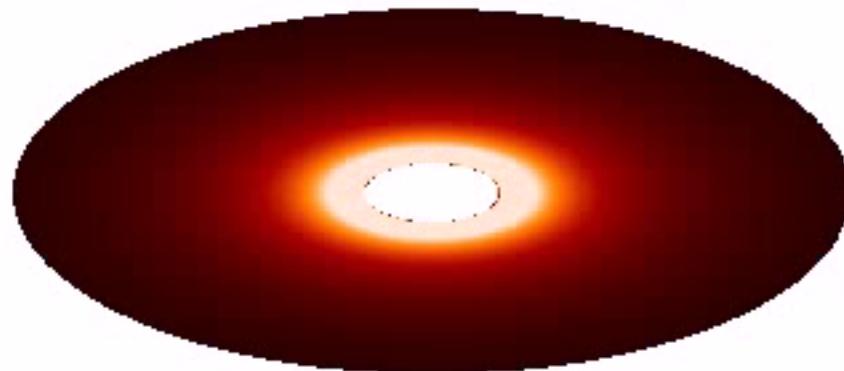
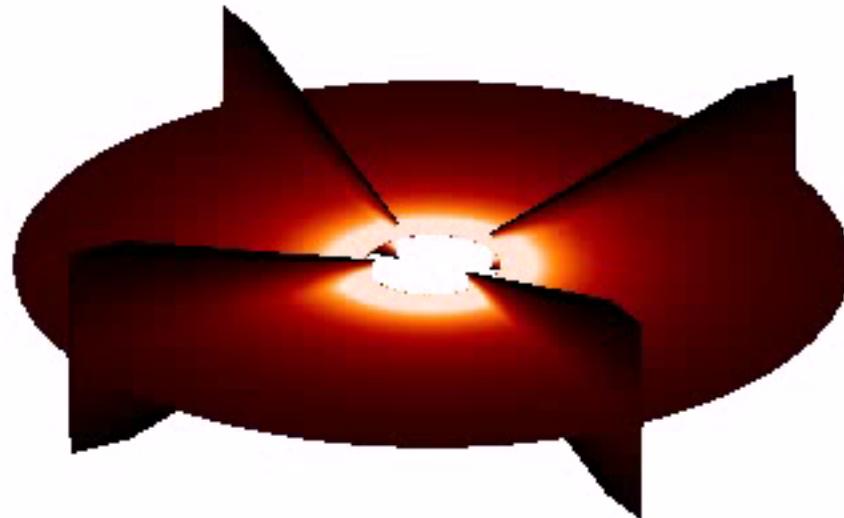


© Brooks Martner

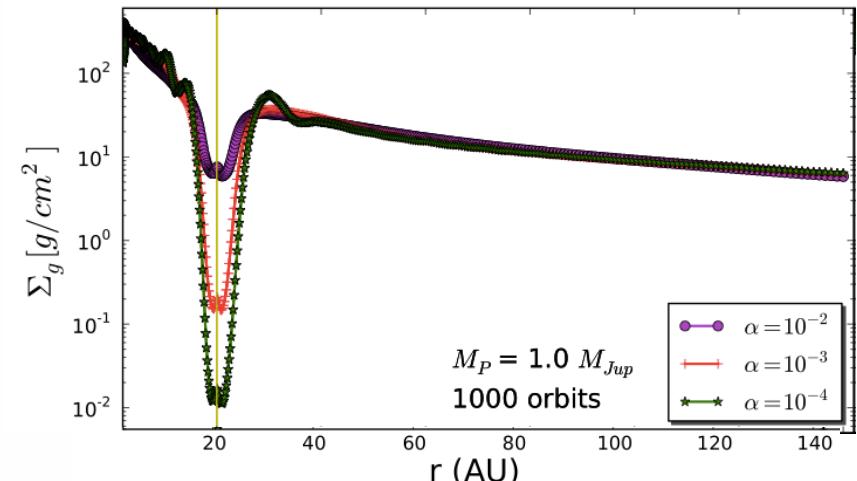
# Planetary gap RWI

(de Val-Borro et al. 2006, 2007)

$t = 0.1$



Lyra (2009)



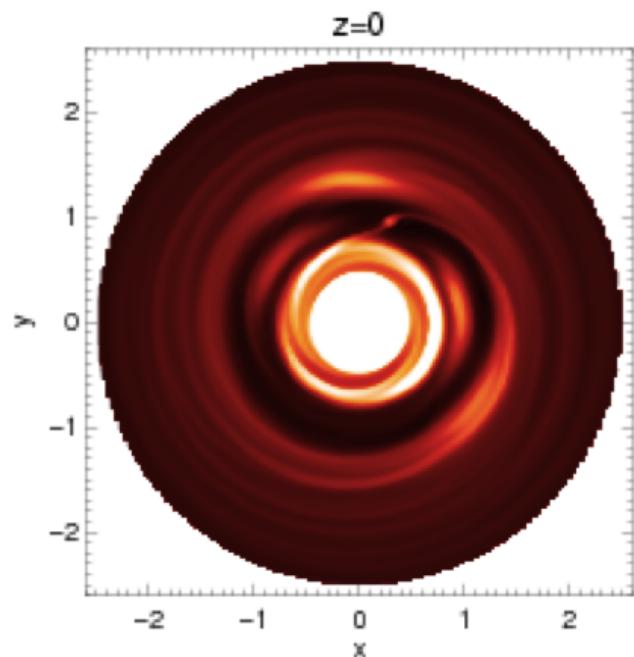
Pinilla et al. (2012)

Planet tides carve gap

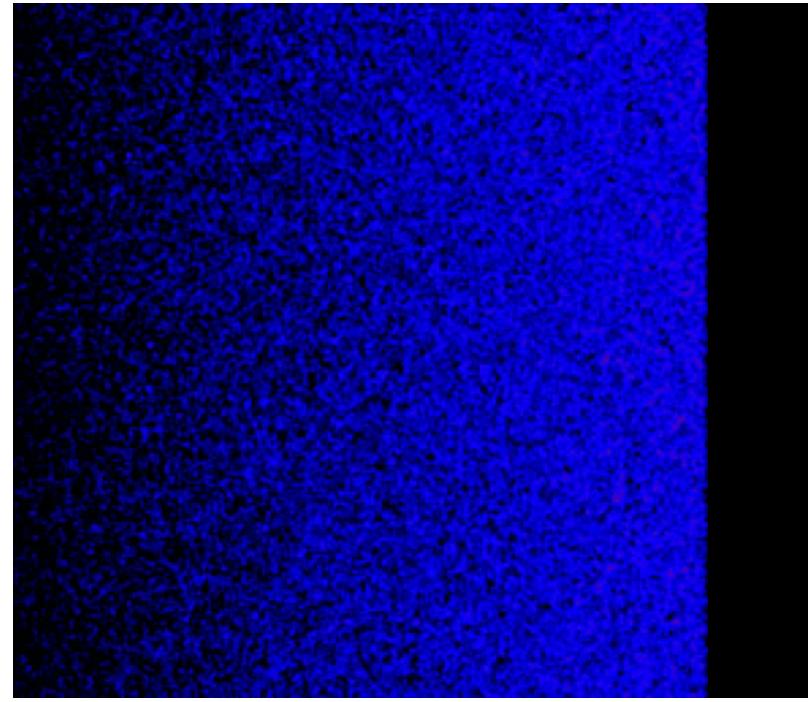
Gap walls are unstable to  
Kelvin-Helmholtz instability

# Planetary gap RWI

Lyra et al. (2009b),  
see also de Val-Borro et al. (2007)



azimuth  
↑

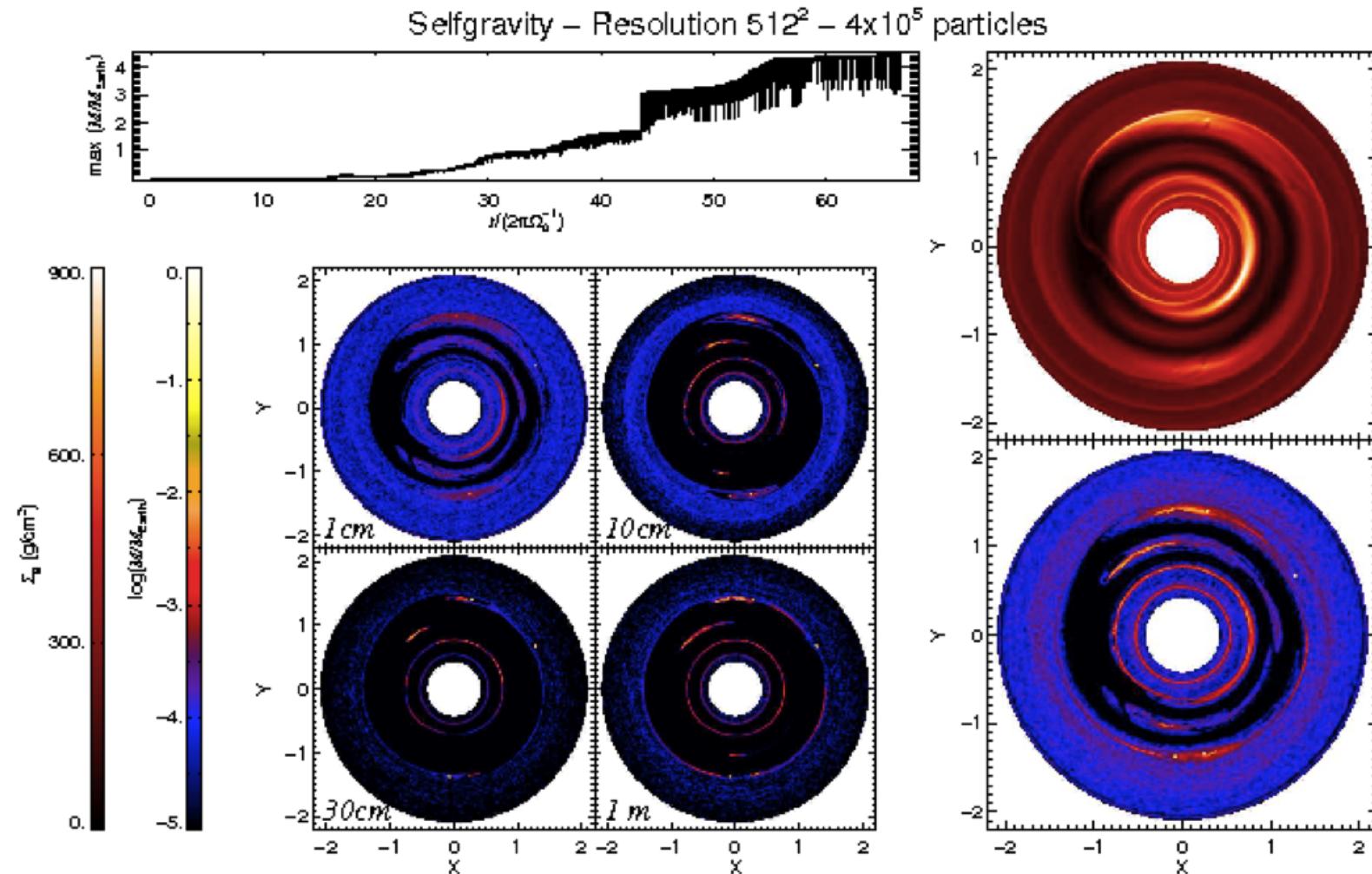


radius  
→

Burst of formation in gap vortices

Plus Trojan planets in Lagrangian clouds

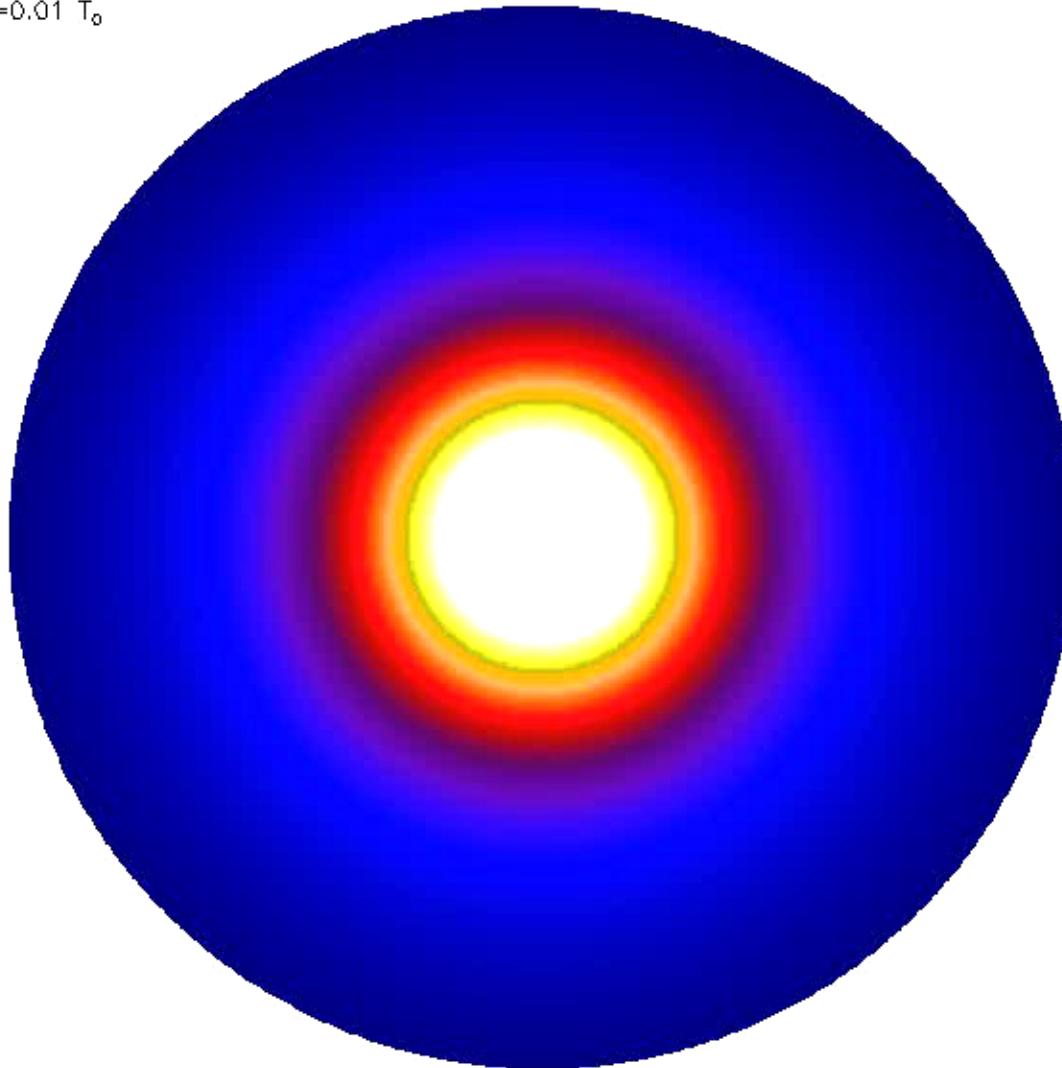
## Vortex trapping



**3 Super-Earths formed + Mars mass Trojans**

## Active/dead zone boundary

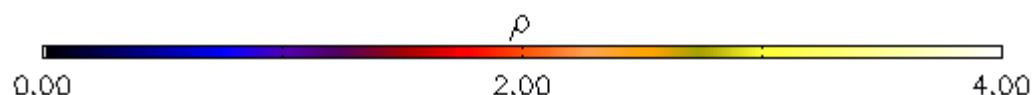
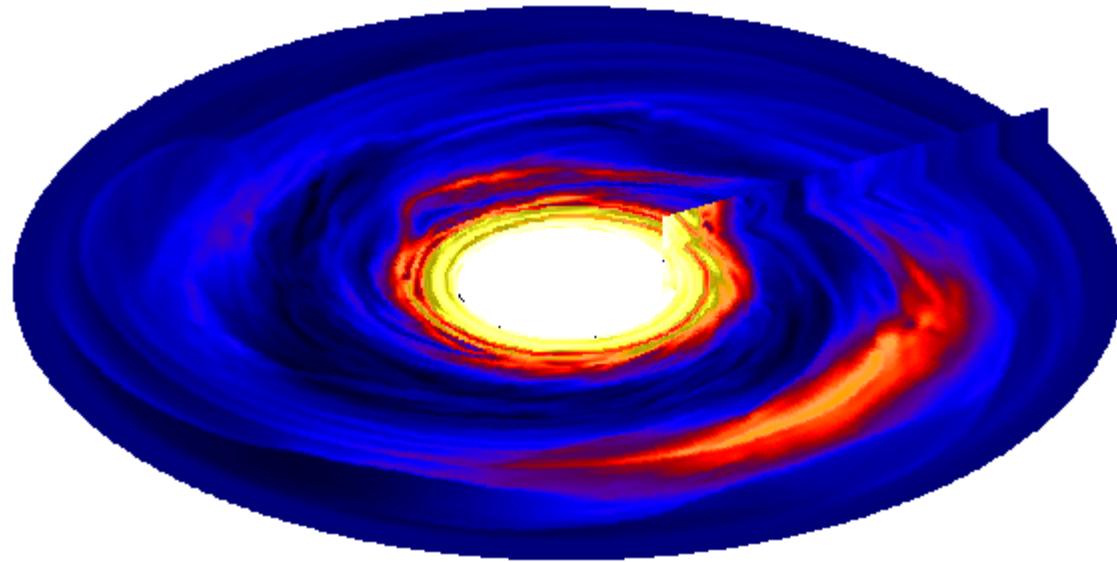
$t=0.01 T_0$



Magnetized inner disk + resistive outer disk  
Lyra & Mac Low (2012)

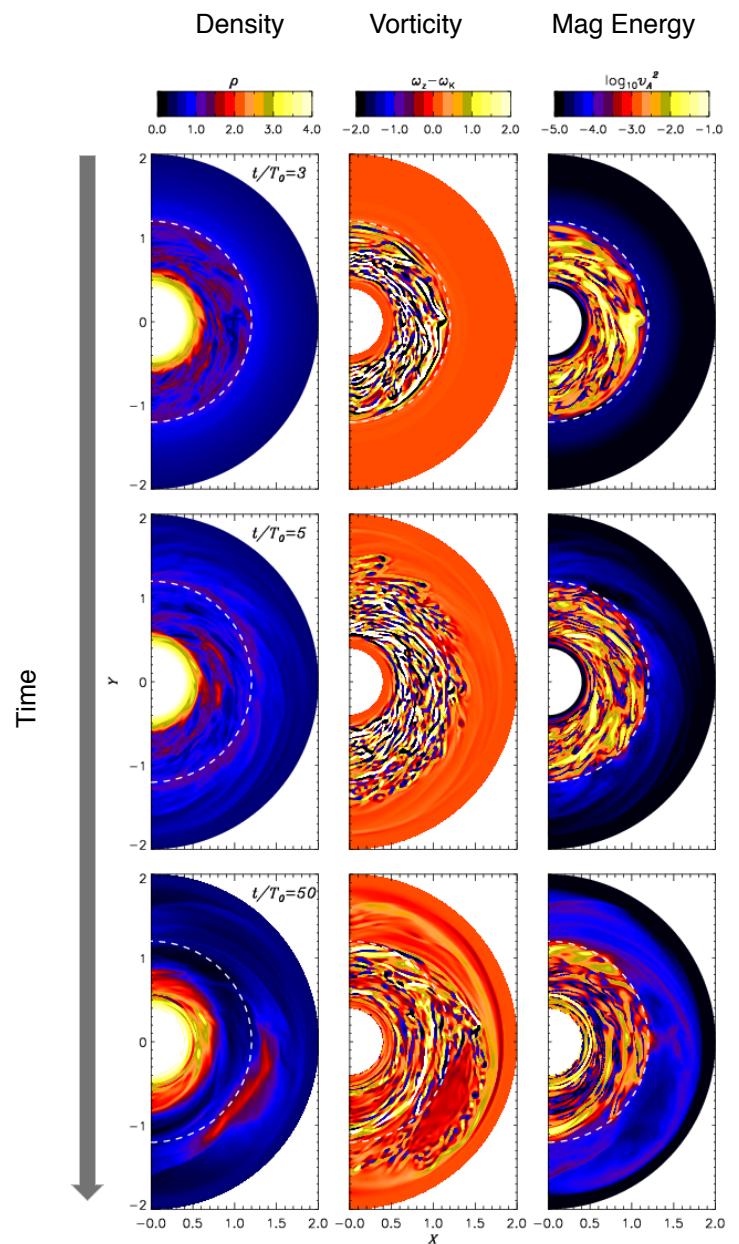
# Active/dead zone boundary

$t=22.28 T_0$



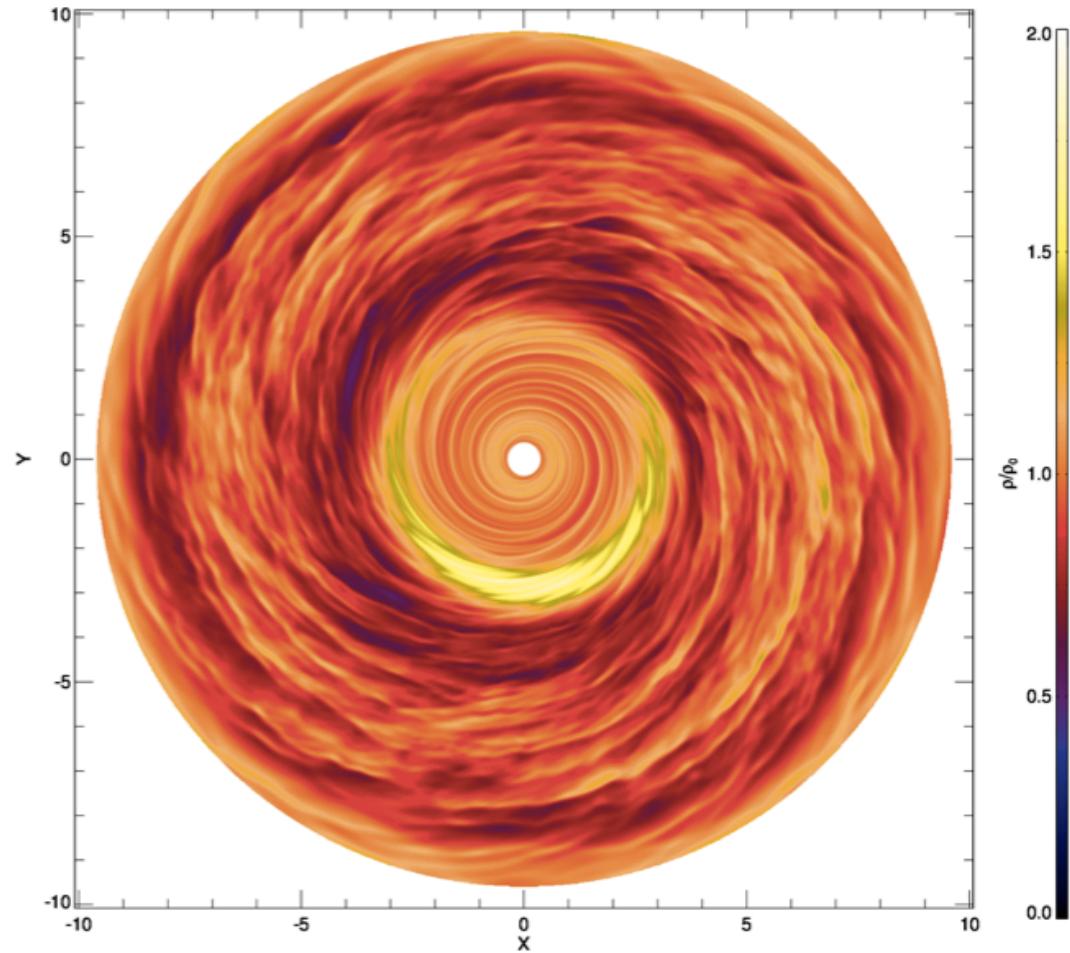
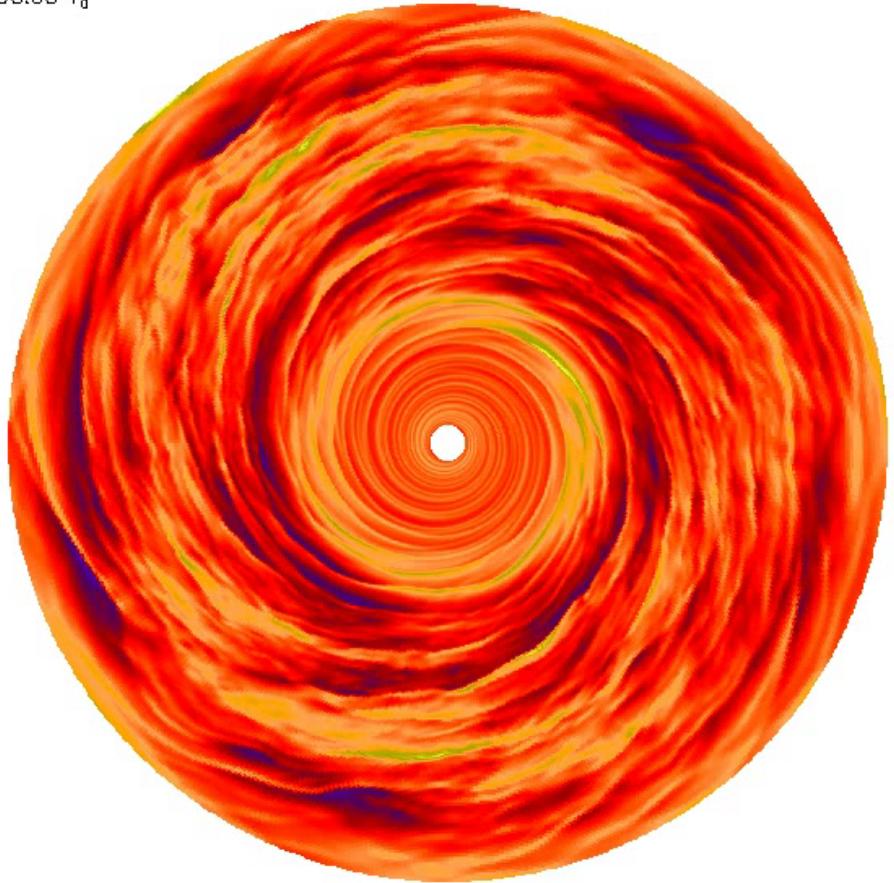
Magnetized inner disk + resistive outer disk

Lyra & Mac Low (2012)



# Outer Dead/Active zone transition RWI

$t=95.58 T_0$



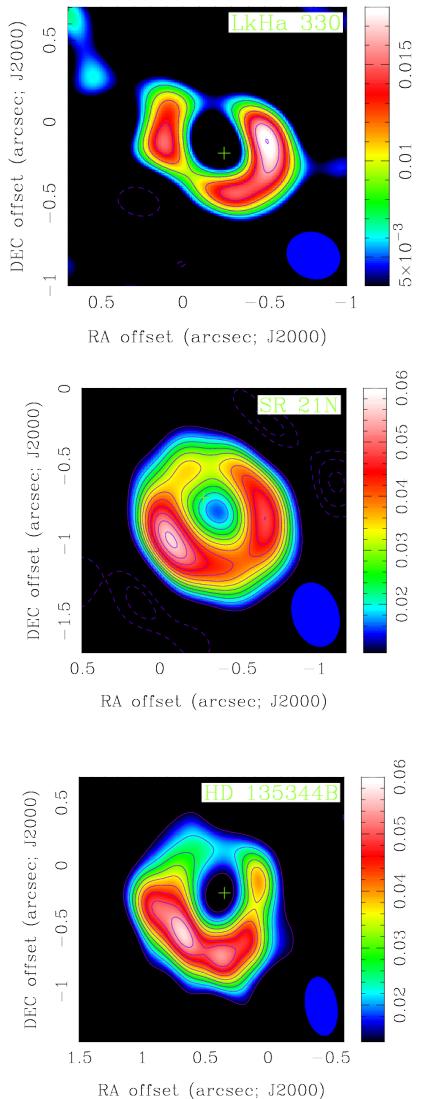
Resistive inner disk + magnetized outer disk

Lyra, Turner, & McNally (2015)

# A possible detection of vortices in disks?

## Observations

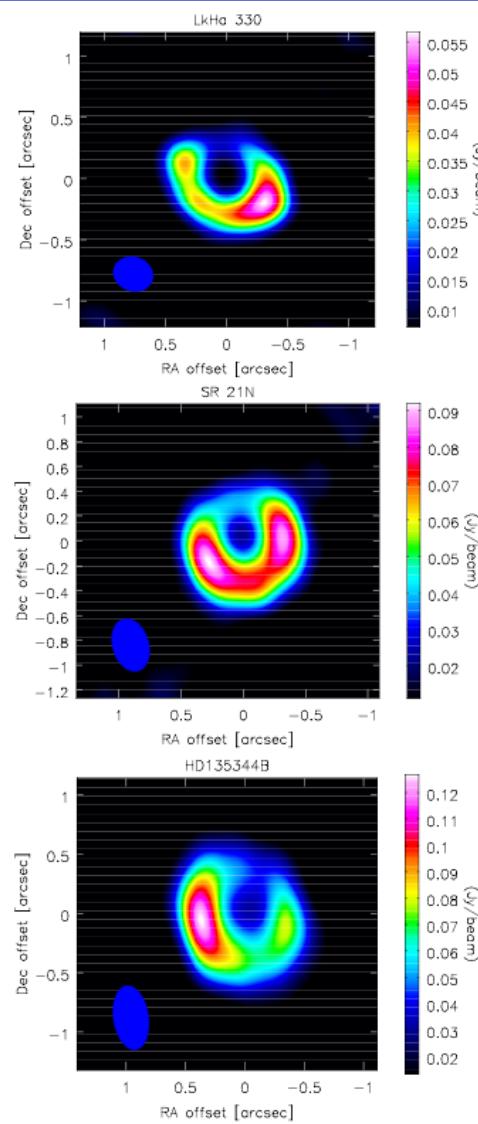
Brown et al. (2009)



## Models

Simulated observations  
of Rossby vortices

Regaly, Sándor  
et al. (2012)



# Oph IRS 48

Down



## A Major Asymmetric Dust Trap in a Transition Disk

Nienke van der Marel,<sup>1,\*</sup> Ewine F. van Dishoeck,<sup>1,2</sup> Simon Bruderer,<sup>2</sup> Til Birnstiel,<sup>3</sup> Paola Pinilla,<sup>4</sup> Cornelis P. Dullemond,<sup>4</sup> Tim A. van Kempen,<sup>1,5</sup> Markus Schmalzl,<sup>1</sup> Joanna M. Brown,<sup>3</sup> Gregory J. Herczeg,<sup>6</sup> Geoffrey S. Mathews,<sup>1</sup> Vincent Geers<sup>7</sup>

The statistics of discovered exoplanets suggest that planets form efficiently. However, there are fundamental unsolved problems, such as excessive inward drift of particles in protoplanetary disks during planet formation. Recent theories invoke dust traps to overcome this problem. We report the detection of a dust trap in the disk around the star Oph IRS 48 using observations from the Atacama Large Millimeter/submillimeter Array (ALMA). The 0.44-millimeter-wavelength continuum map shows high-contrast crescent-shaped emission on one side of the star, originating from millimeter-sized grains, whereas both the mid-infrared image (micrometer-sized dust) and the gas traced by the carbon monoxide 6-5 rotational line suggest rings centered on the star. The difference in distribution of big grains versus small grains/gas can be modeled with a vortex-shaped dust trap triggered by a companion.

Although the ubiquity of planets is confirmed almost daily by detections of new exoplanets (*1*), the exact forma-

tion mechanism of planetary systems in disks of gas and dust around young stars remains a long-standing problem in astrophysics (*2*). In

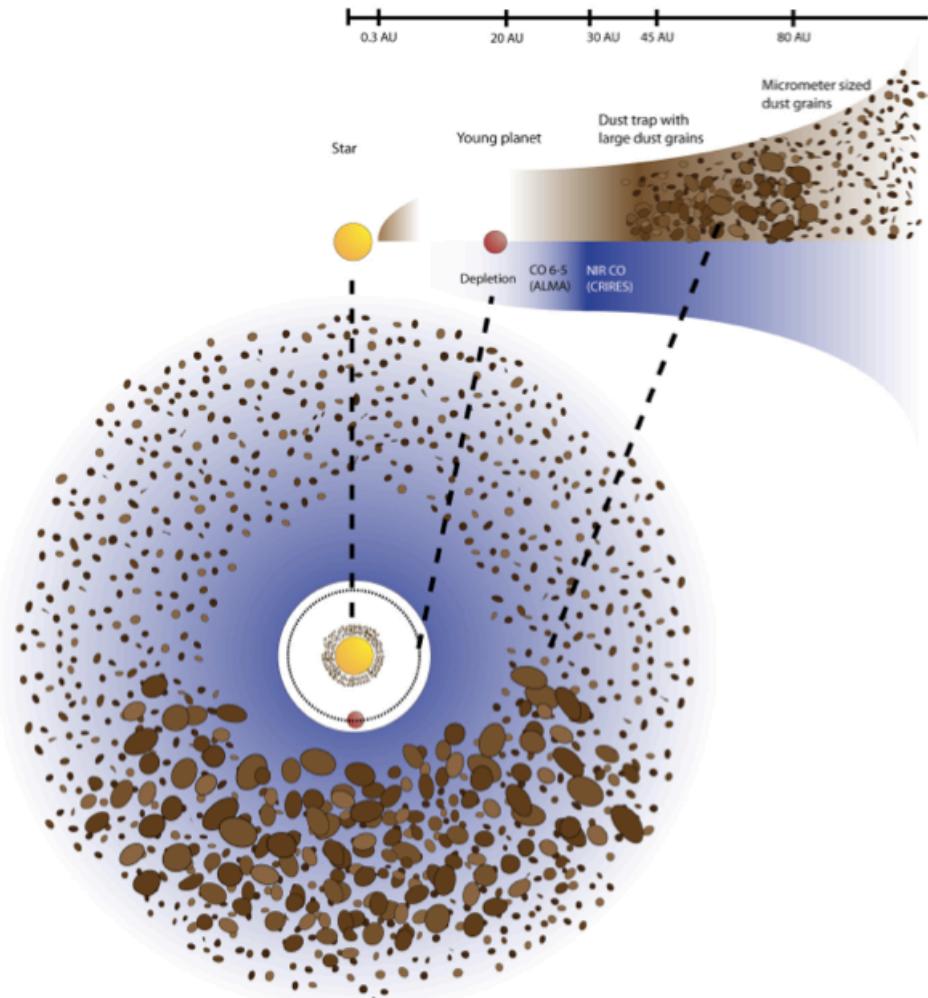
iencemag.org SCIENCE VOL 340 7 JUNE 2013

1199

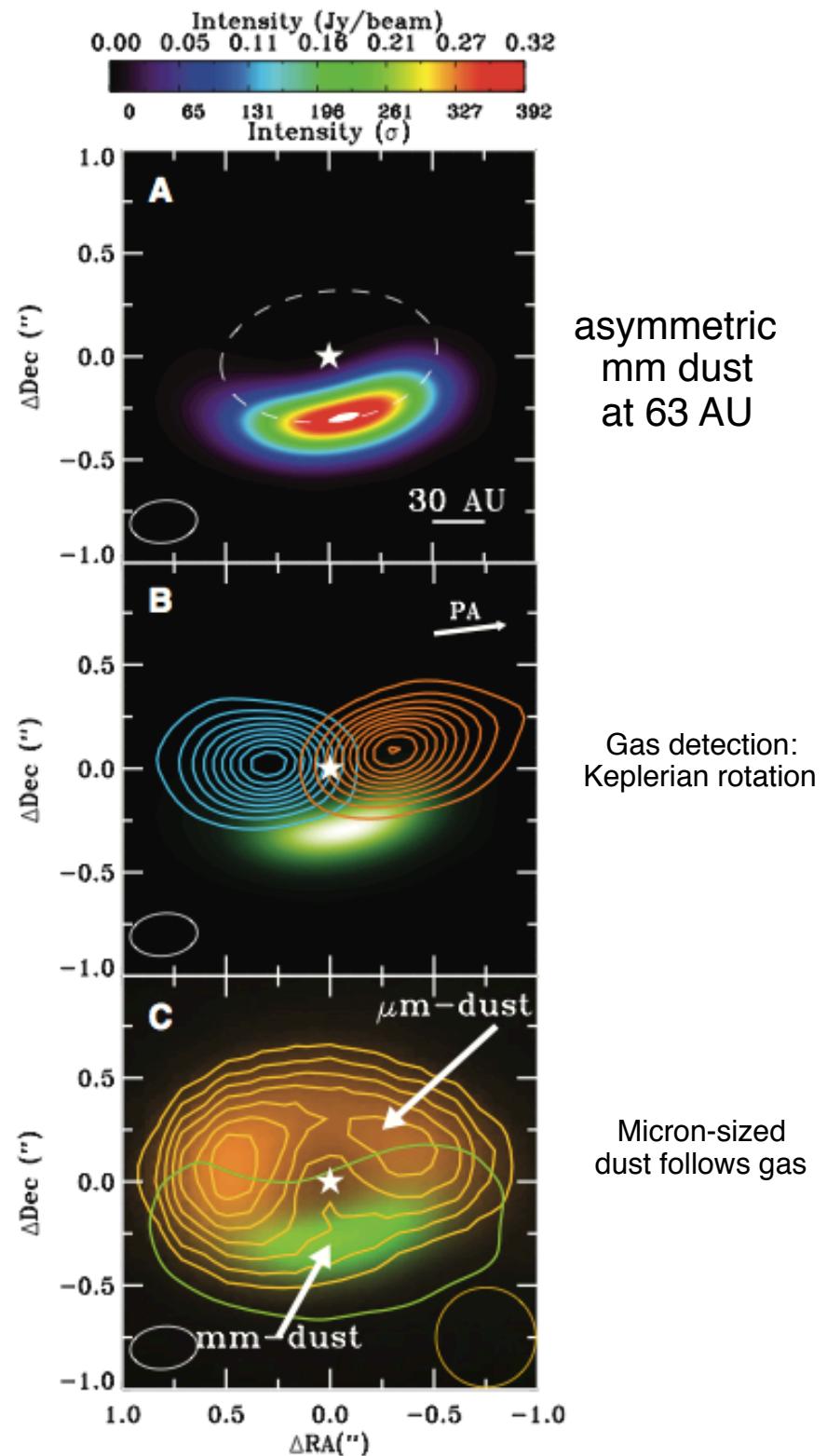
van der Marel et al. 2013

A possible huge vortex observed with ALMA

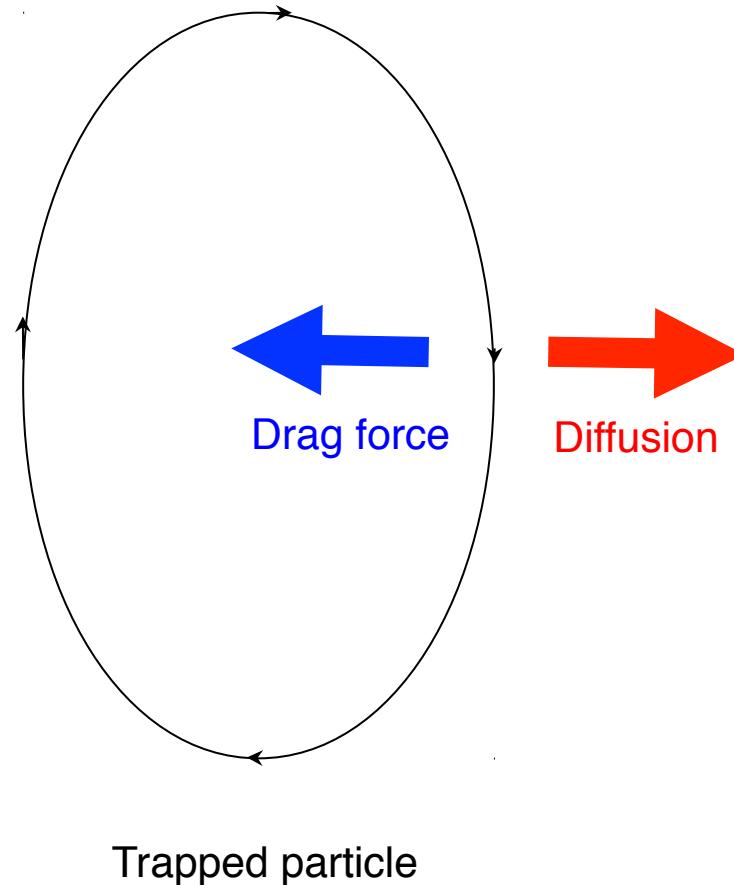
## The Oph IRS 48 “dust trap”



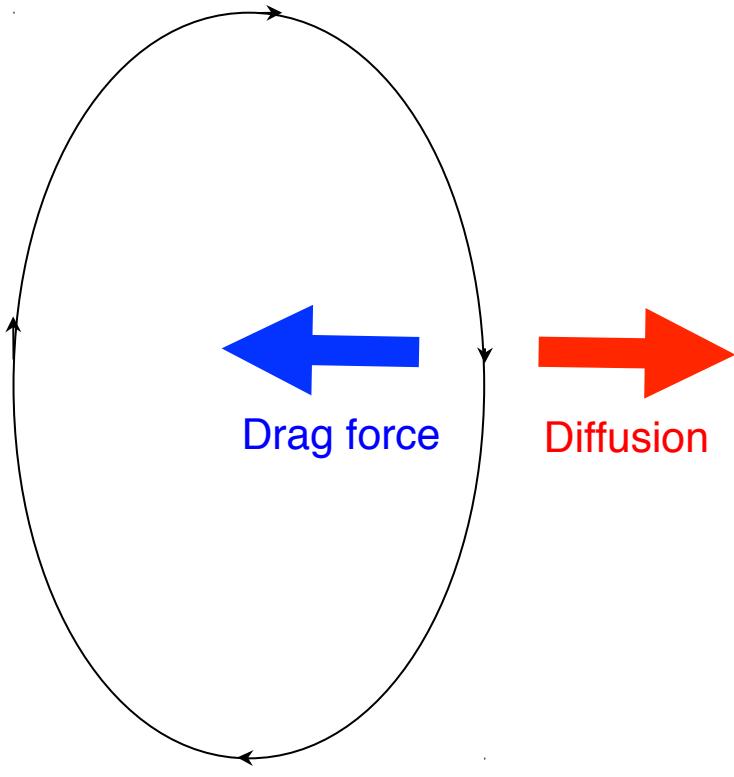
van der Marel et al. (2013)



# Drag-Diffusion Equilibrium



# Drag-Diffusion Equilibrium



Trapped particle

Dust continuity equation

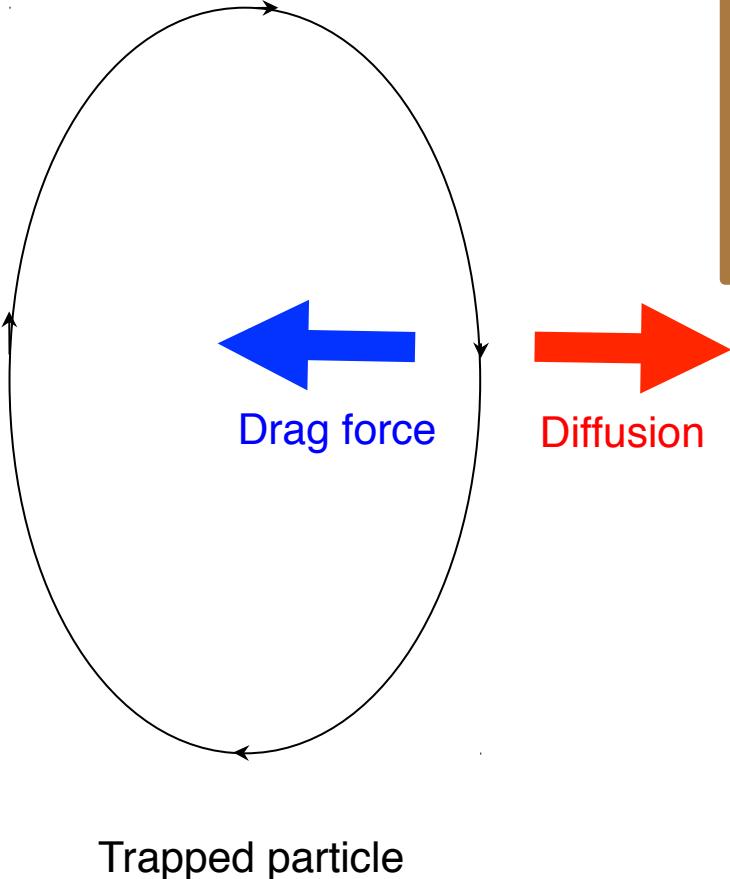
$$\frac{\partial \rho_d}{\partial t} = -(\mathbf{v} \cdot \nabla) \rho_d - \rho_d \nabla \cdot \mathbf{v} + D \nabla^2 \rho_d,$$

advection

compression

diffusion

# Drag-Diffusion Equilibrium



Steady-state solution

$$\rho_d(a, z) = \epsilon \rho_0 (S + 1)^{3/2} \exp \left\{ - \frac{[a^2 f^2(\chi) + z^2]}{2H^2} (S + 1) \right\}$$

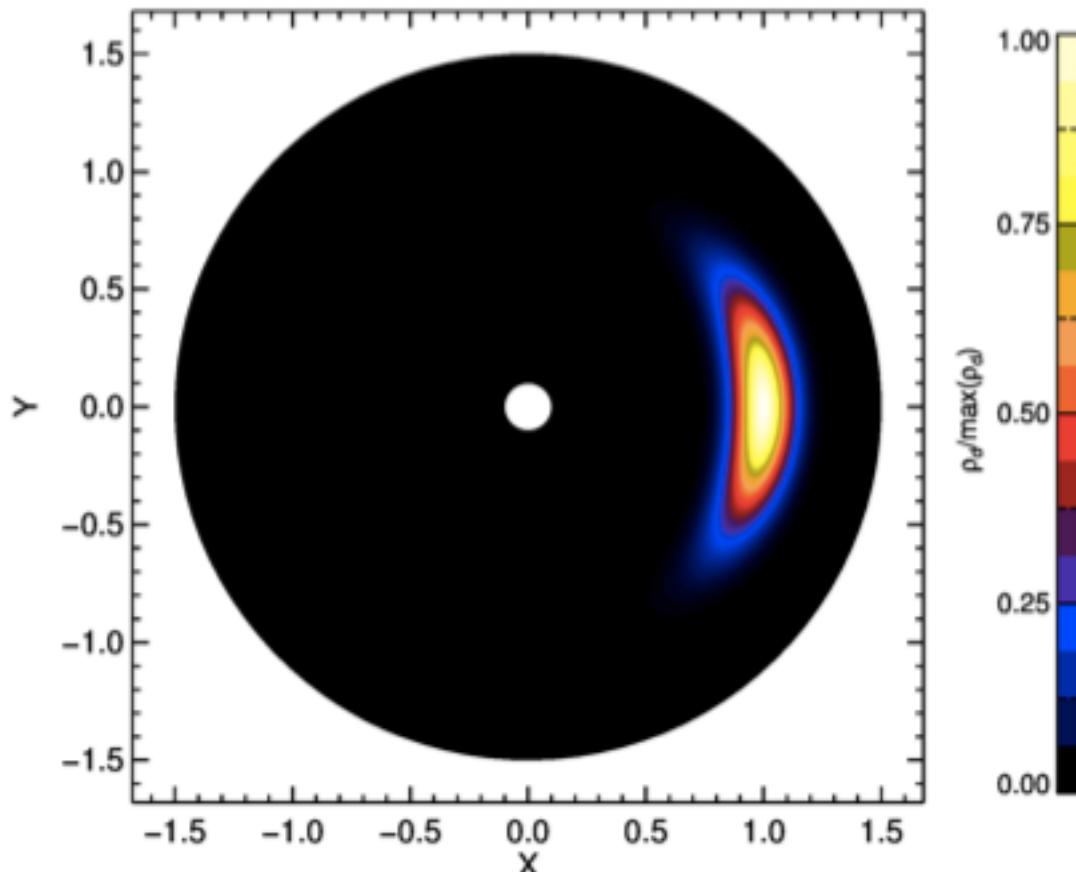
Lyra & Lin (2013)

$$S = \frac{St}{\delta}$$

$$\delta = v_{\text{rms}}^2 / c_s^2,$$

$a$  = vortex semi-minor axis  
 $H$  = disk scale height (temperature)  
 $\chi$  = vortex aspect ratio  
 $\delta$  = diffusion parameter  
 $St$  = Stokes number (particle size)  
 $f(\chi)$  = model-dependent scale function

# Analytical solution for dust trapping



Solution for

$$H/r=0.1 \quad \chi=4 \quad S=1$$

## Solution

$$\rho_d(a) = \rho_{d\max} \exp\left(-\frac{a^2}{2H_V^2}\right),$$

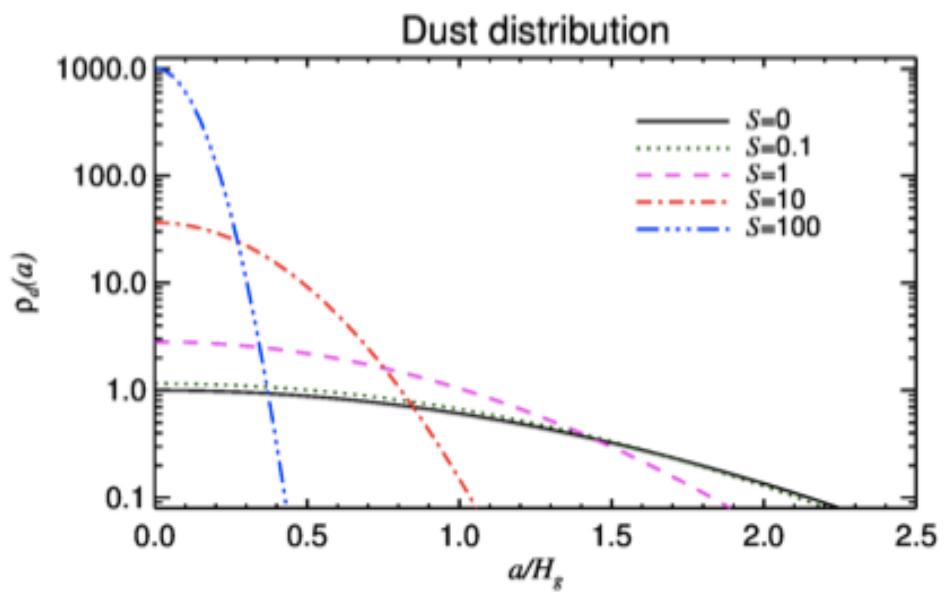
$$H_V = \frac{H}{f(\chi)} \sqrt{\frac{1}{S+1}}$$

$$S = \frac{St}{\delta}$$

$$\delta = v_{\text{rms}}^2 / c_s^2,$$

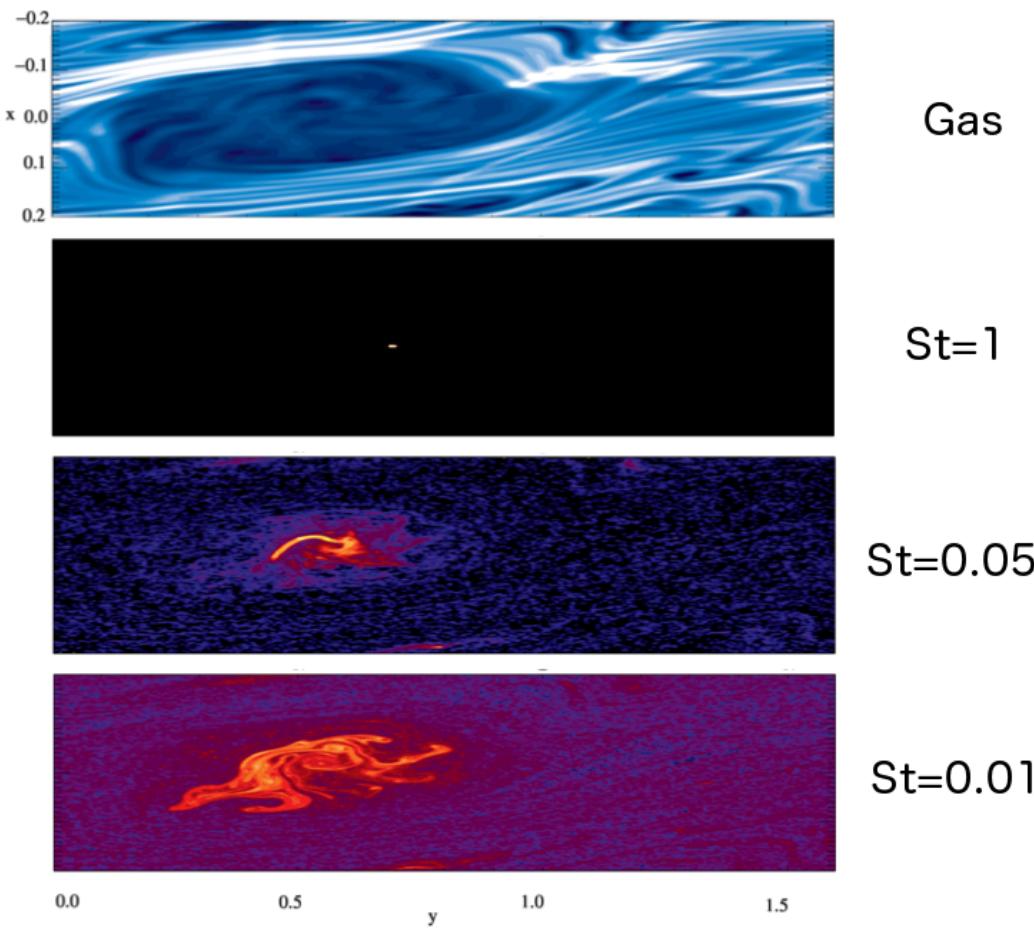
- $a$  = vortex semi-minor axis  
 $H$  = disk scale height (temperature)  
 $\chi$  = vortex aspect ratio  
 $\delta$  = diffusion parameter  
St = Stokes number (particle size)  
 $f(\chi)$  = model-dependent scale function

# Analytical vs Numerical



$$S = \frac{St}{\delta} \quad \delta = v_{\text{rms}}^2 / c_s^2,$$

Lyra & Lin (2013)



Raettig et al (2015)

## Derived quantities

$$\rho_d(a, z) = \epsilon \rho_0 (S + 1)^{3/2} \exp \left\{ - \frac{[a^2 f^2(\chi) + z^2]}{2H^2} (S + 1) \right\}$$

Lyra & Lin (2013)

### Gas distribution

$$\rho_g(a) = \rho_{g\max} \exp \left( - \frac{a^2}{2H_g^2} \right),$$

### Maximum dust density

$$\rho_{d\max} = \epsilon \rho_0 (S + 1)^{3/2}$$

### Gas contrast

$$\frac{\rho_{g\max}}{\rho_{g\min}} = \exp \left[ \frac{f^2(\chi)}{2\chi^2 \omega_V^2} \right],$$

### Dust contrast

$$\frac{\rho_{d\max}}{\rho_{d\min}} = \frac{\rho_{g\max}}{\rho_{g\min}} \exp(S),$$

### Total trapped mass

$$\int \rho_d(a, z) dV = (2\pi)^{3/2} \epsilon \rho_0 \chi H H_g^2$$

### Vortex size

$$a_s = H(\chi \omega_V)^{-1}$$

$H$  = disk scale height (temperature)  
 $\chi$  = vortex aspect ratio  
 $\delta$  = diffusion parameter

St = Stokes number (particle size)  
 $f(\chi)$  = model-dependent scale function  
 $\epsilon$  = dust-to-gas ratio

## Applying the model to Oph IRS 48

### Observed parameters

Aspect ratio: 3.1

Dust contrast: 130

Temperature: 60K

**Trapped mass:  $9 M_{Earth}$**

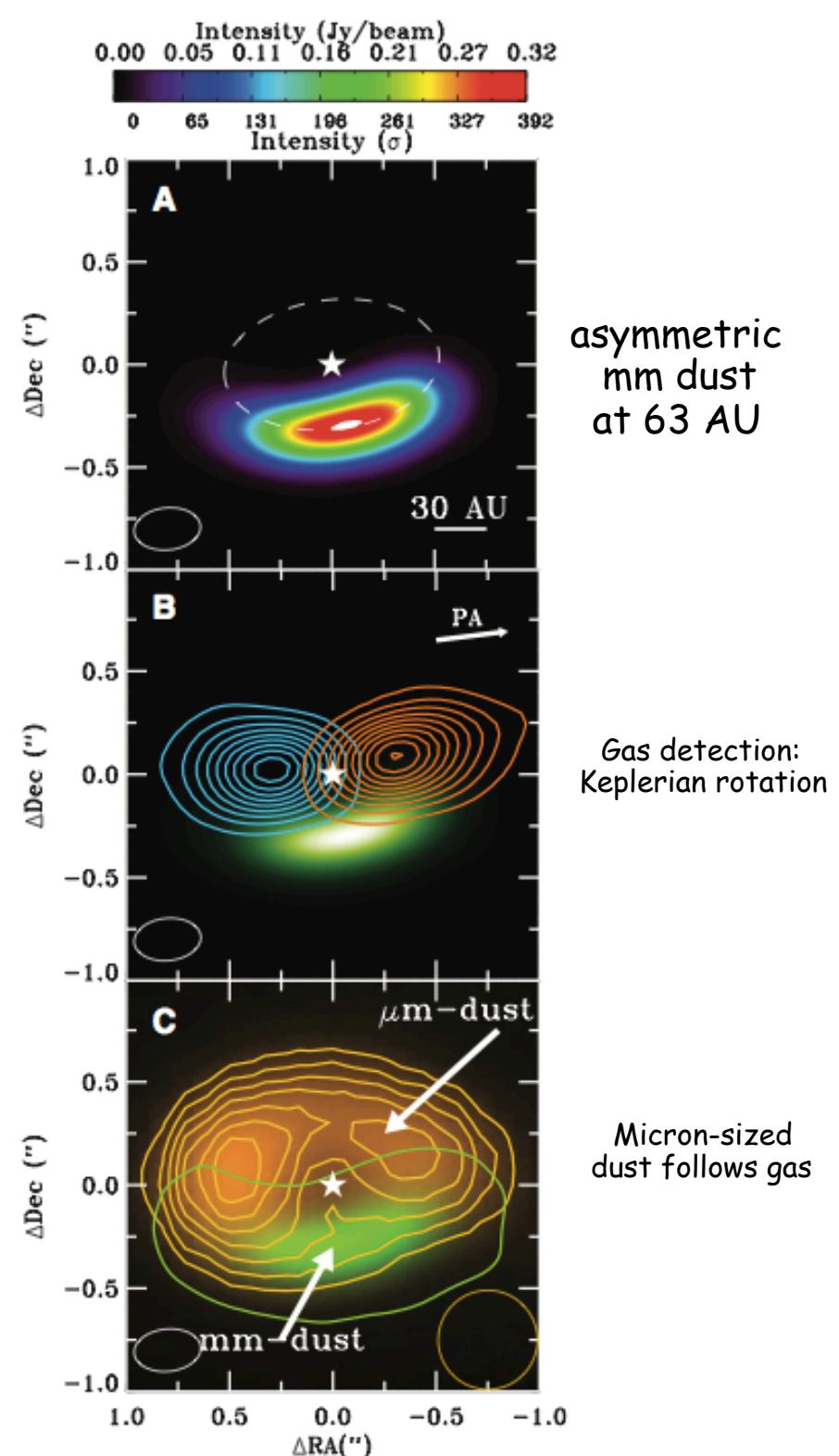
### Derived parameters

S=4.8

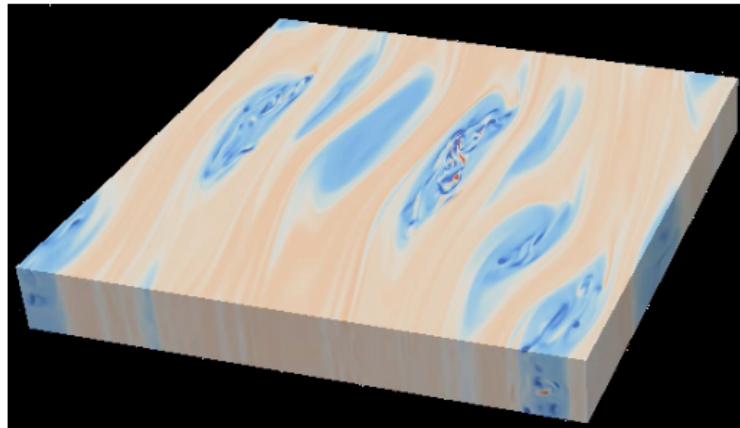
Stokes number, St=0.008

$\delta = 0.005$ ,  $V_{rms} = 4\% C_s$

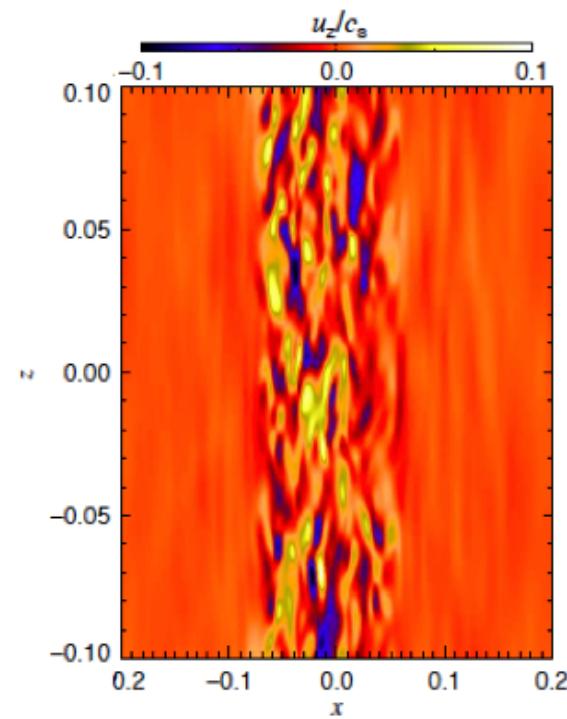
**Trapped mass:  $11 M_{Earth}$**



## Turbulence in vortex cores



Lesur & Papaloizou (2010)



Lyra & Klahr (2011)

Turbulence in vortex cores:

max at ~10% of sound speed  
rms at ~3% of sound speed

# HD 142527

## Observed parameters

Aspect ratio: 10

Dust contrast: 30

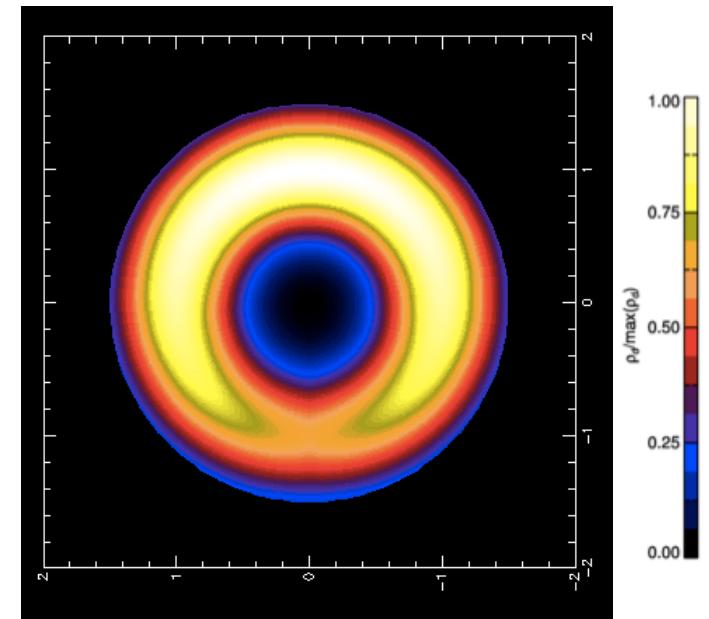
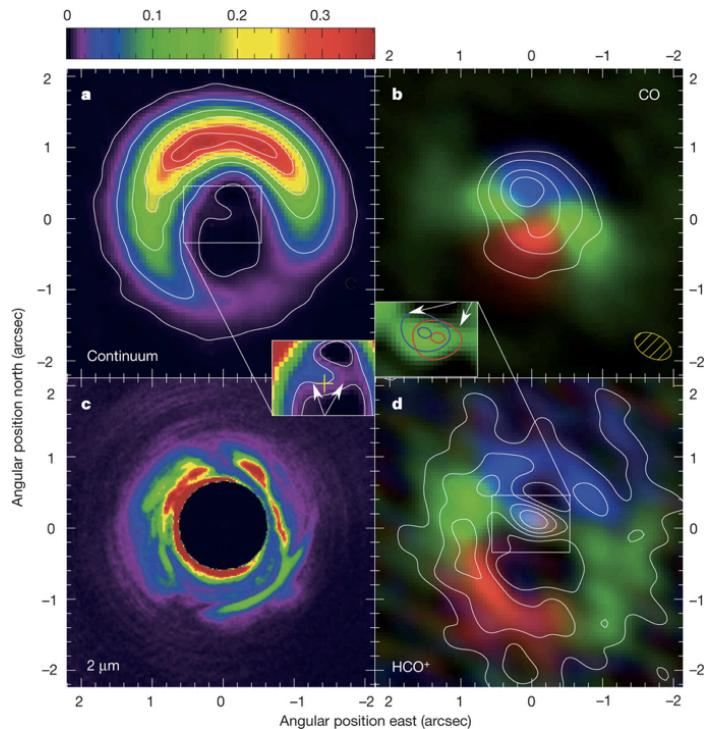
Temperature: 25K

## Derived parameters

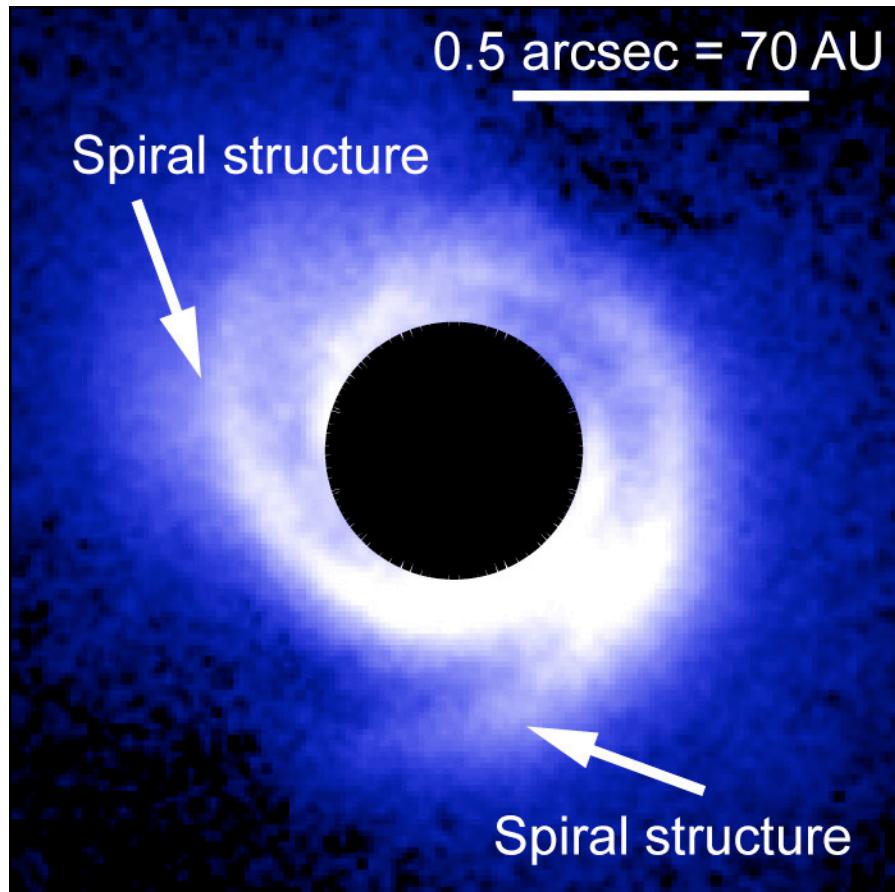
$S=3.5$

Stokes number,  $St=0.004$

$\delta = 0.001$ ,  $v_{rms} = 4\% cs$

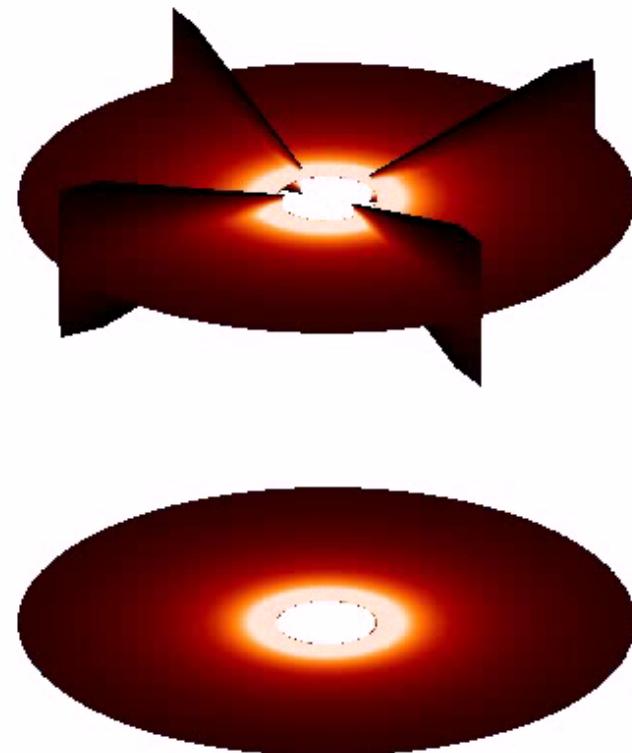


## Spirals in transition disks



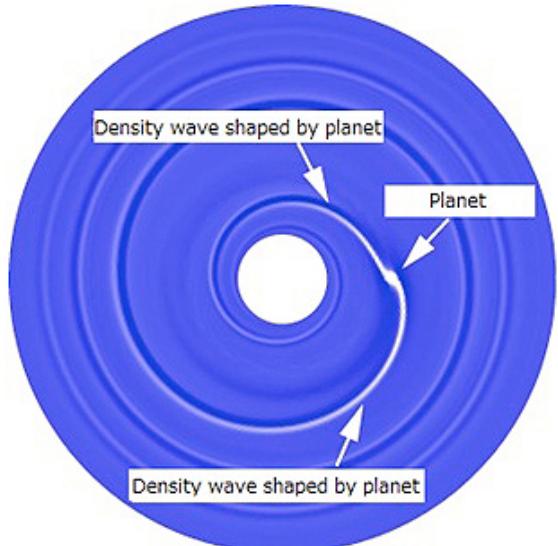
Muto et al. (2012)

$t= 0.1$



# Spiral arm fitting leads to problems

## Analytical spiral fit

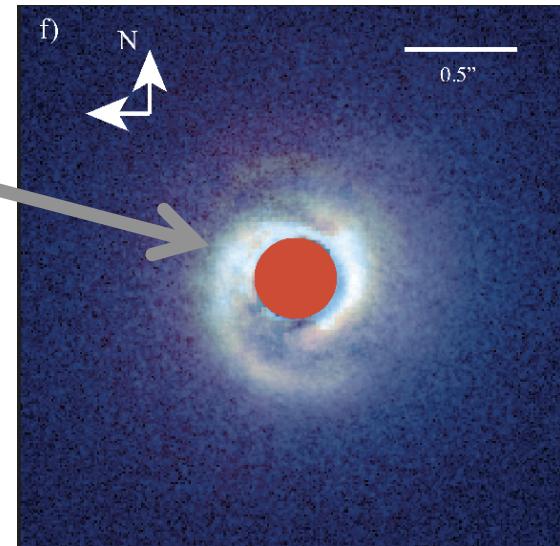


$$\theta(r) = \theta_c + \frac{\text{sgn}(r - r_c)}{h_c} \times \left\{ \left( \frac{r}{r_c} \right)^{1+\beta} \left[ \frac{1}{1+\beta} - \frac{1}{1-\alpha+\beta} \left( \frac{r}{r_c} \right)^{-\alpha} \right] - \left( \frac{1}{1+\beta} - \frac{1}{1-\alpha+\beta} \right) \right\},$$

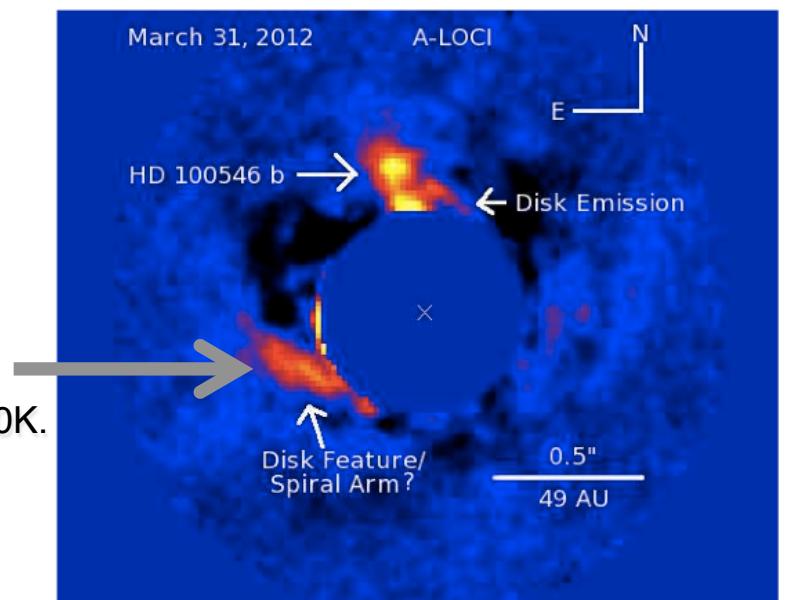
Rafikov (2002)

Muto et al. (2012)

Spiral is too wide,  
hotter (300K) than  
ambient gas (50K).

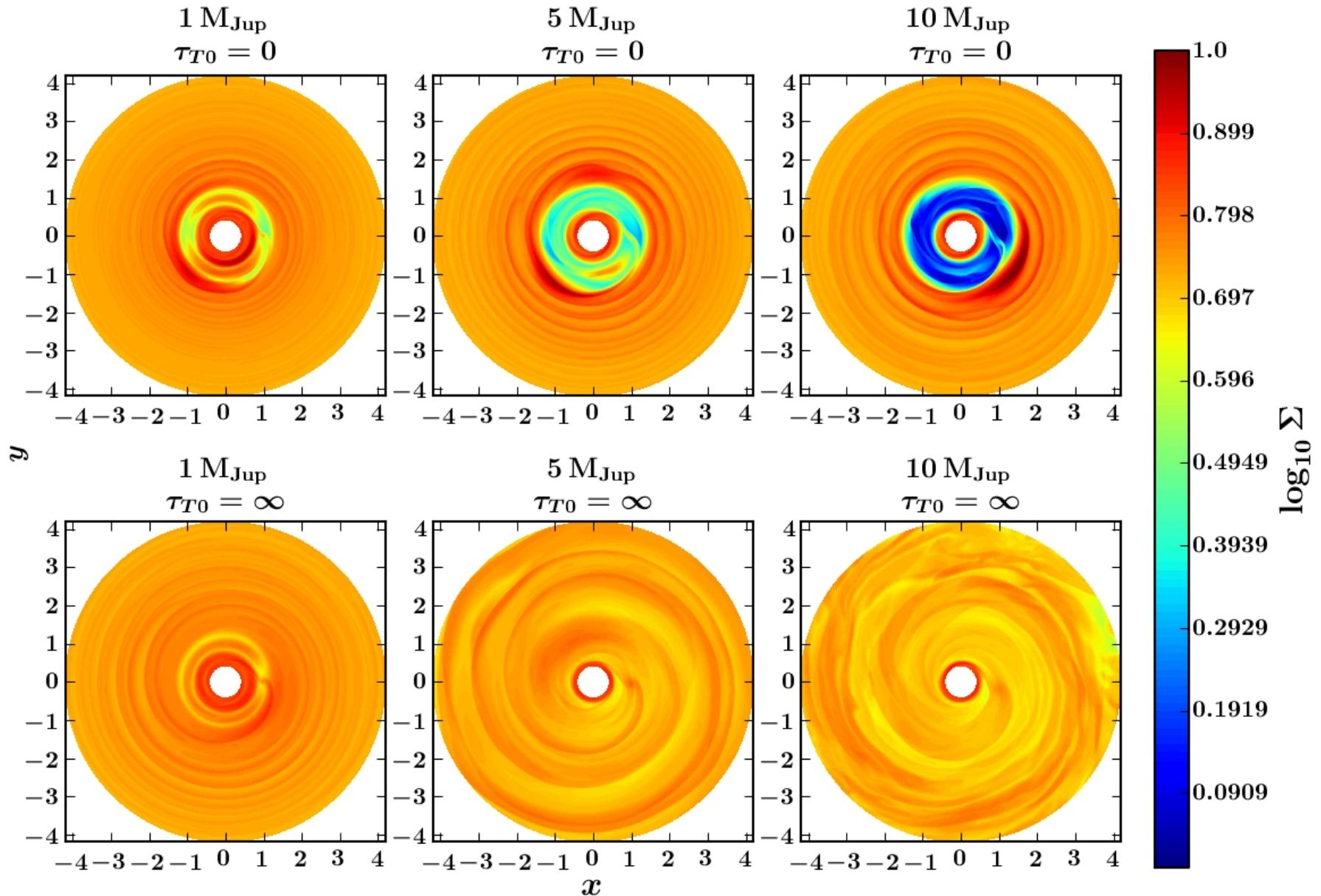


Spiral has little  
polarization. Must be  
thermal emission at 1000K.

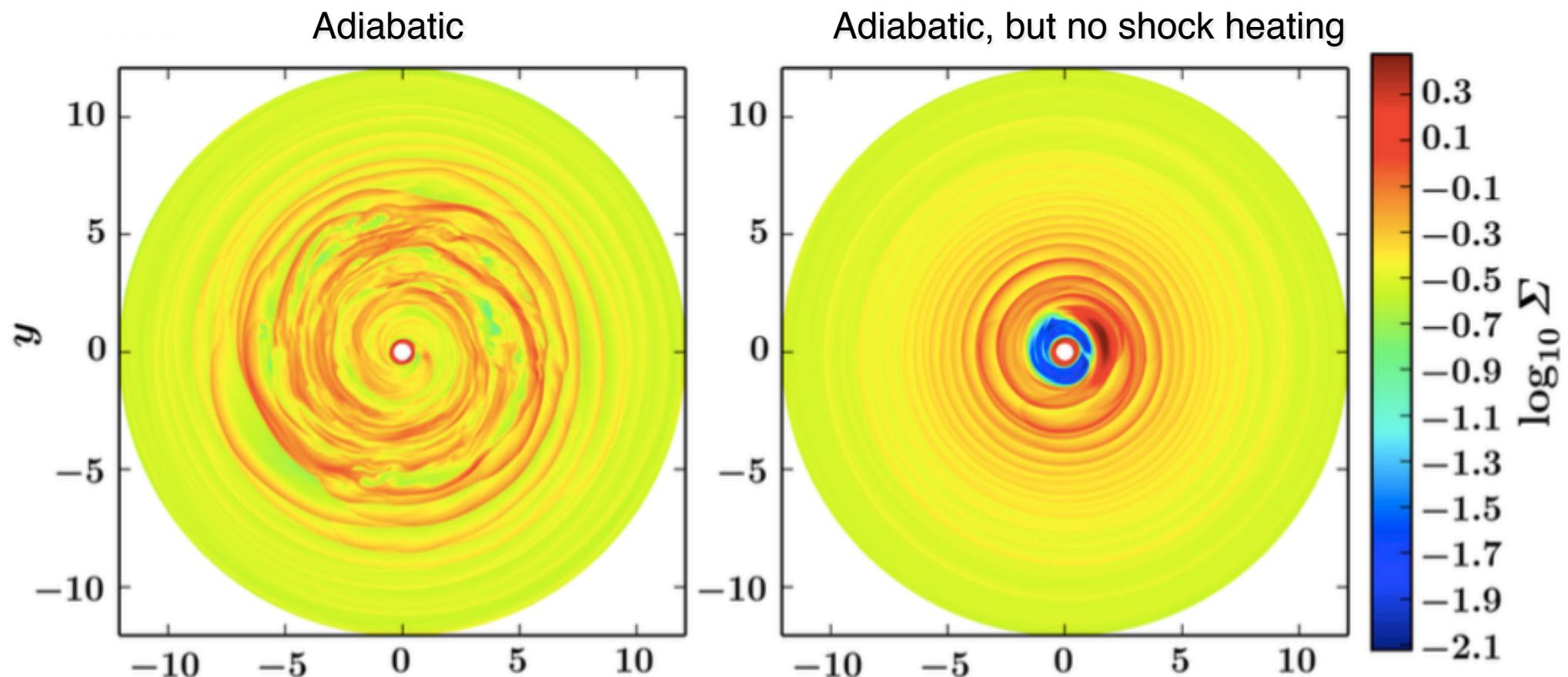


Currie et al. (2014)

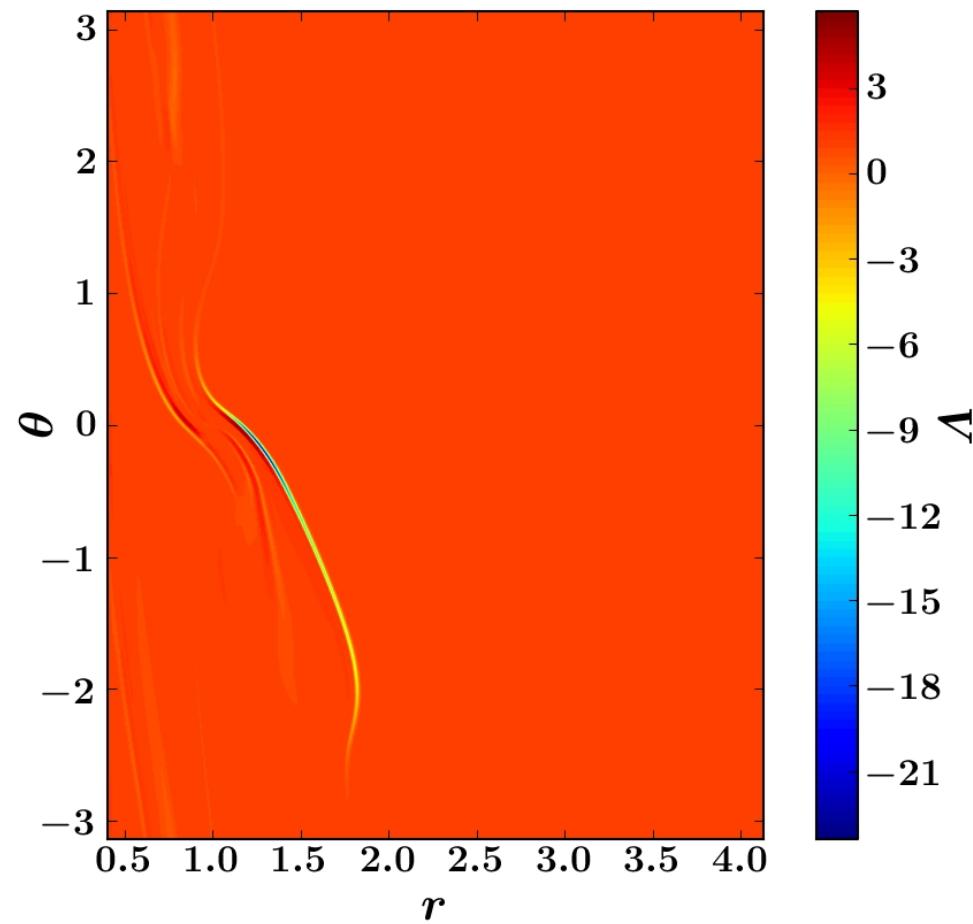
# Isothermal vs Adiabatic



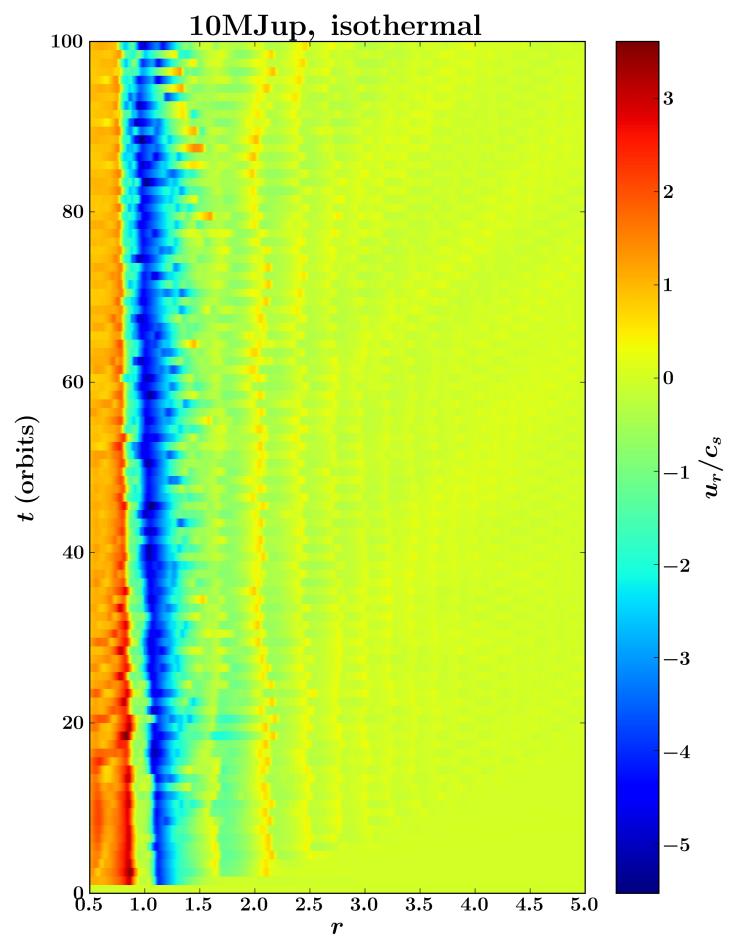
# The energy source: shock heating!



**The spiral is buoyantly unstable**

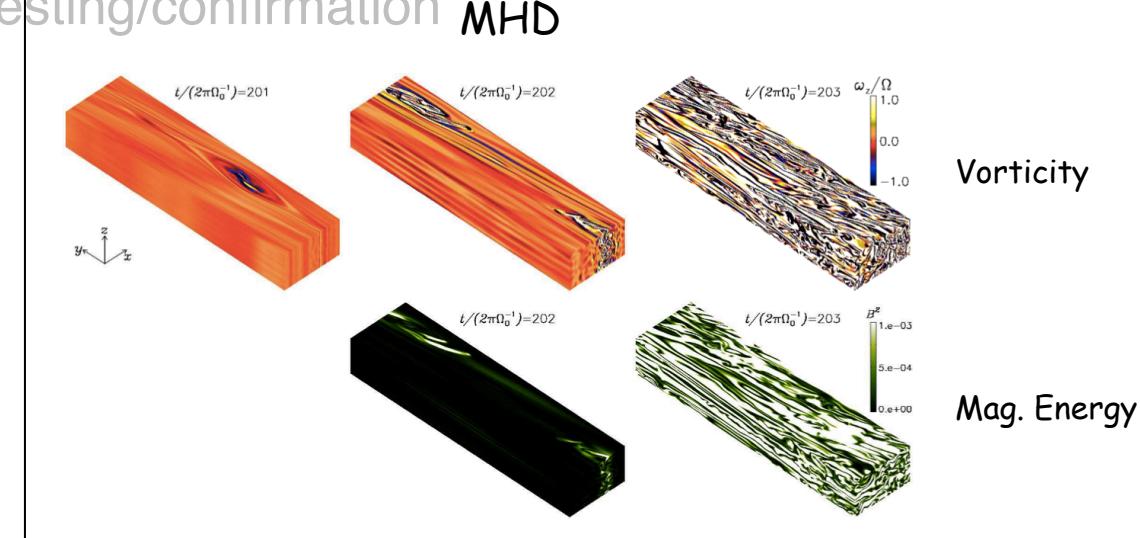
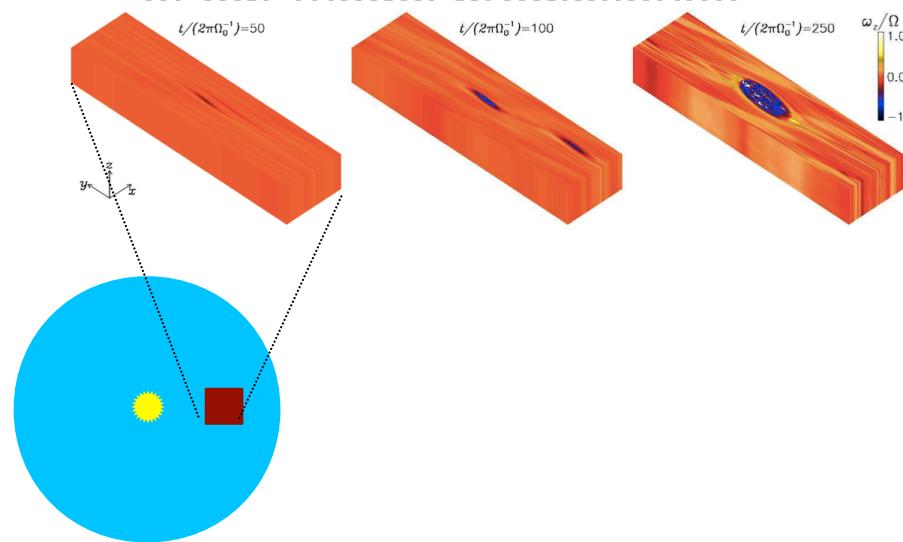


**The spiral has  $\text{Ma} > \sim 1$**



# Conclusions

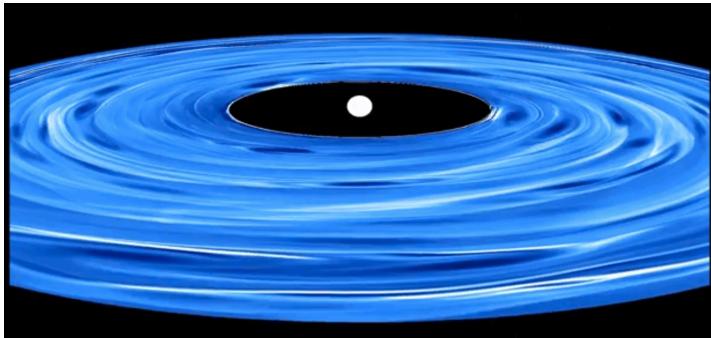
- Vortices exist in the dead zone only
- Two sustenance modes: Rossby Wave Instability and Convective Overstability
- Vortex-assisted and streaming instability are complementary
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Rossby wave instability may be the culprit of these dust traps
- We're in the era of observational testing/confirmation **Hydro MHD** of our model predictions!!



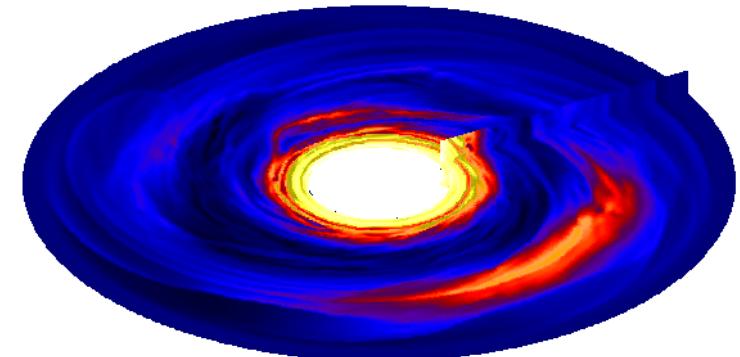
# Conclusions

- Vortices exist in the dead zone only
- Two sustenance modes: Rossby Wave Instability and Convective Overstability
- Vortex-assisted is a complementary formation mode to streaming instability
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Rossby wave instability may be the culprit of these dust traps
- We're in the era of observational testing/cor

## Baroclinic instability



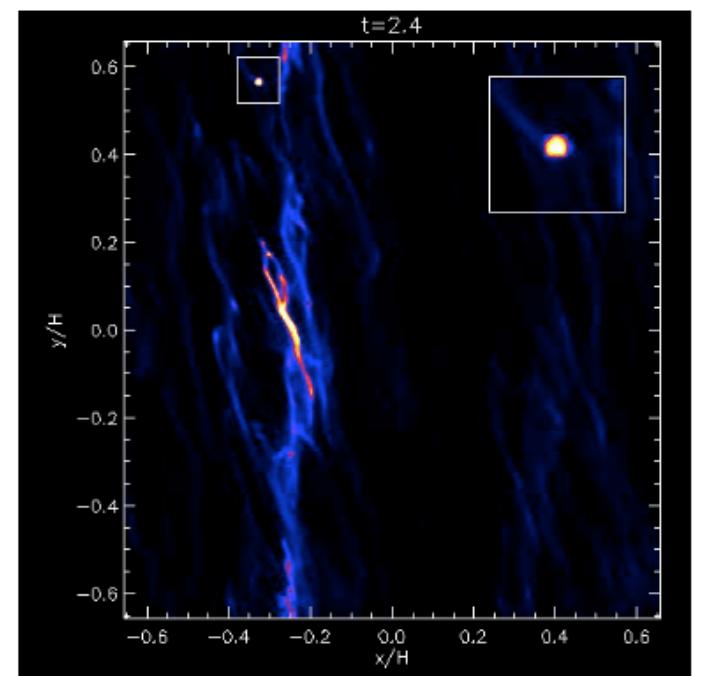
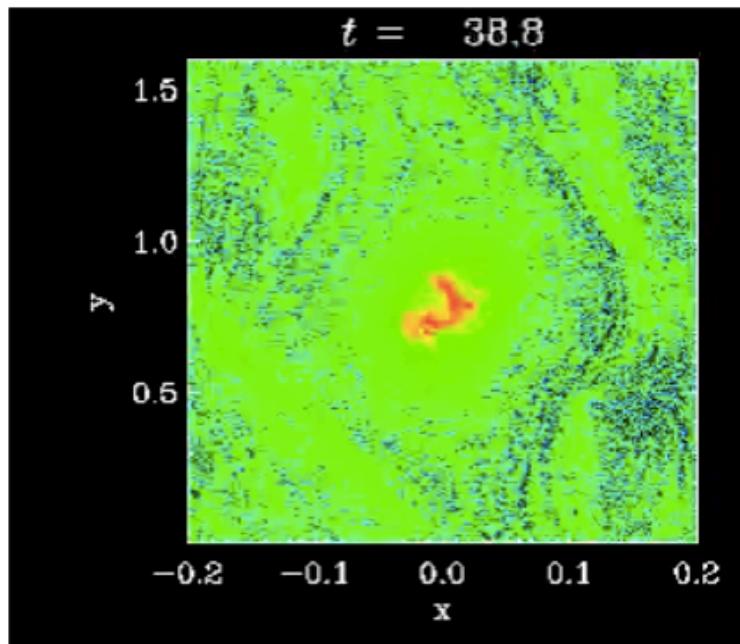
## Rossby wave instability



# Conclusions

- Vortices exist in the dead zone only
- Two sustenance modes: Rossby Wave Instability and Convective Overstability
- Vortex-assisted and streaming instability are complementary
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Rossby wave instability may be the culprit of these dust traps

VI. VORTEX MODELLING PREDICTIONS:

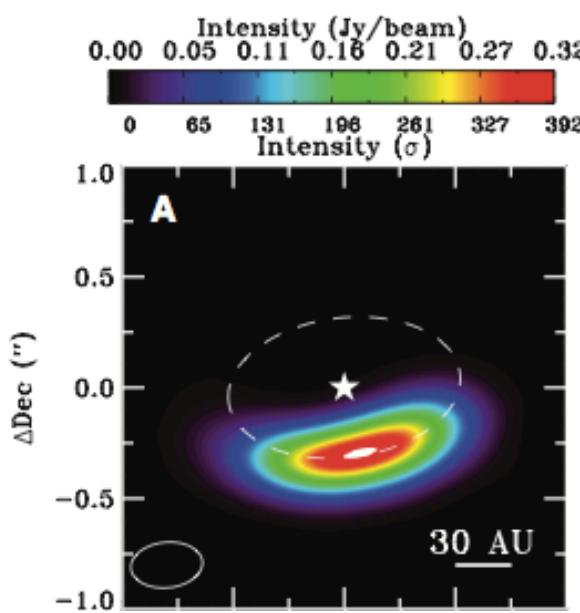
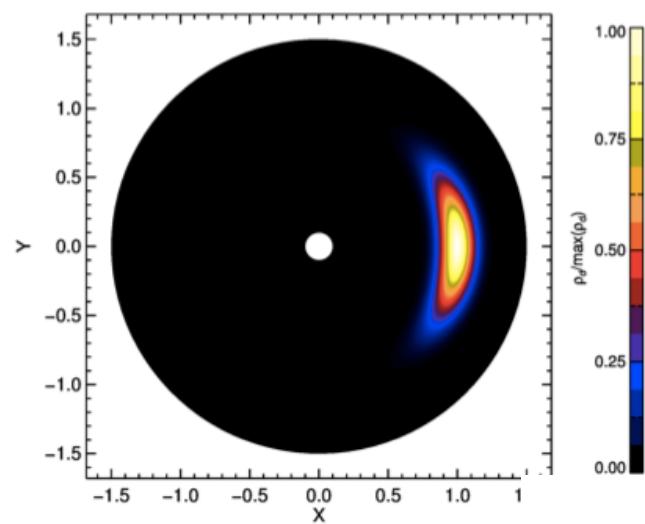


# Conclusions

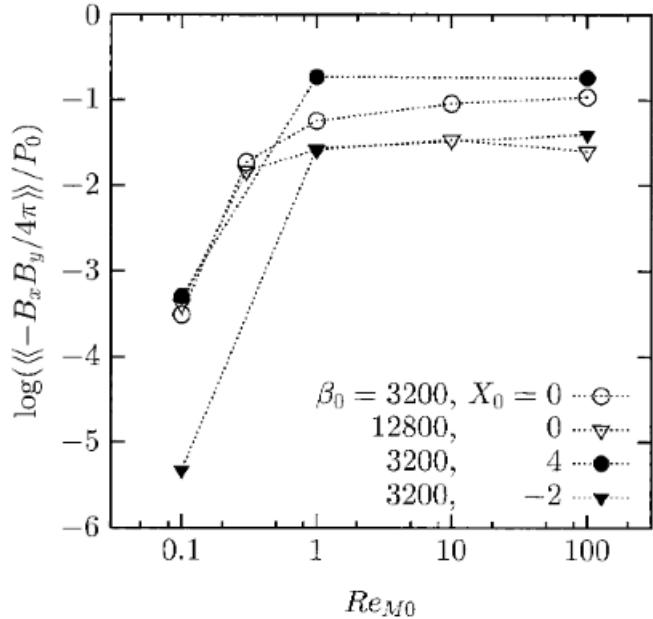
- Vortices exist in the dead zone
- Two sustenance modes: Rossby wave and vortex
- Vortex-assisted and streamwise diffusion
- Vortex-trapped dust in drag-diffusion equilibrium explains the observations
- Rossby wave instability may be the culprit of these dust traps
- We're in the era of observational tests of our model predictions!!

$$\rho_d(a,z) = \epsilon \rho_0 (S+1)^{3/2} \exp \left\{ - \frac{[a^2 f^2(\chi) + z^2]}{2H^2} (S+1) \right\}$$

Lyra & Lin (2013)



## Conclusions



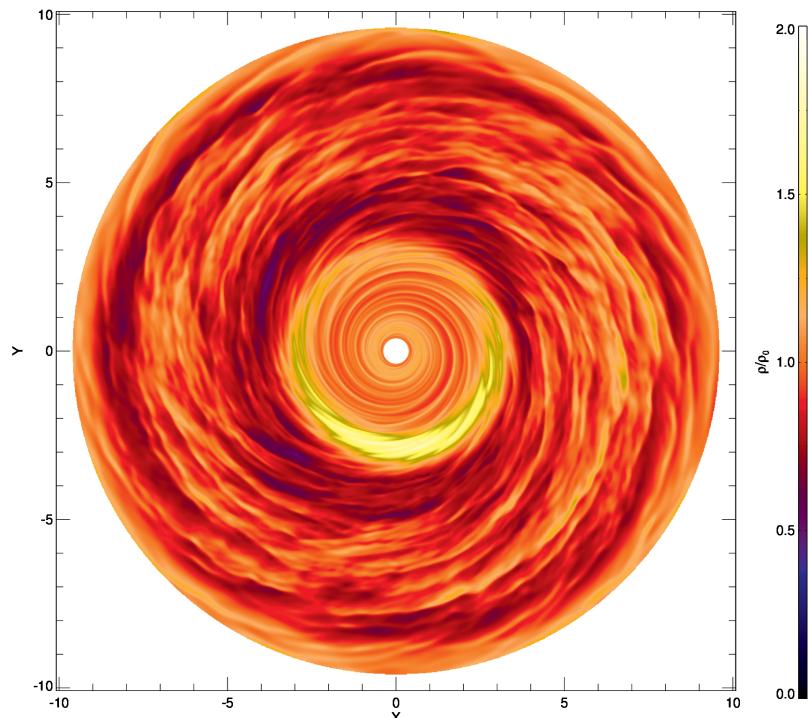
zone only

Rossby Wave Instability and Convective Overstability

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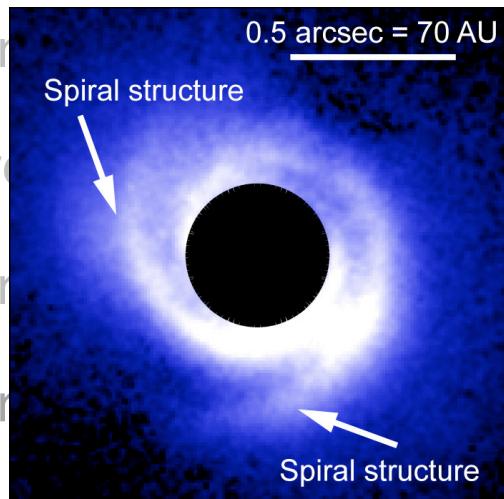
ig-diffusion equilibrium explains the observations

- Rossby wave instability may be the culprit of these dust traps
- We're in the era of observational testing/confirming of our model predictions!!



# Conclusions

- Vorticity is concentrated in the innermost zone only
- Twists are concentrated in the outermost zone
- Vorticity is concentrated in the outermost zone
- Vorticity is concentrated in the outermost zone
- Rossby wave instability may be the culprit of these observations
- We're in the era of observational testing/confirmation of our model predictions!!

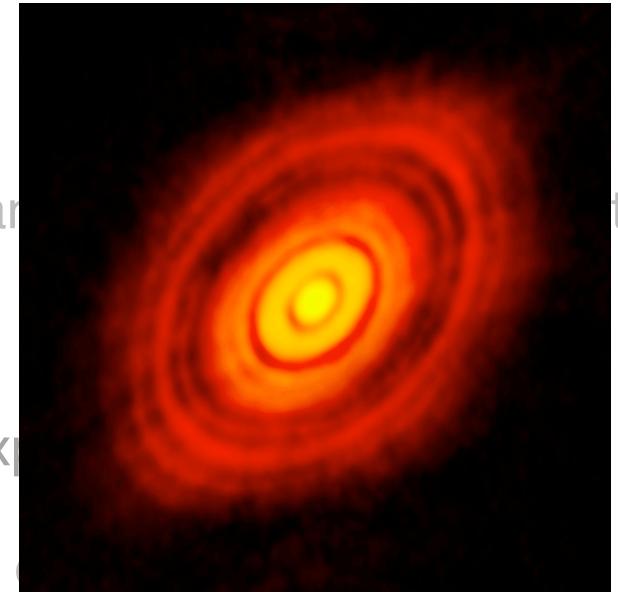


and zone only

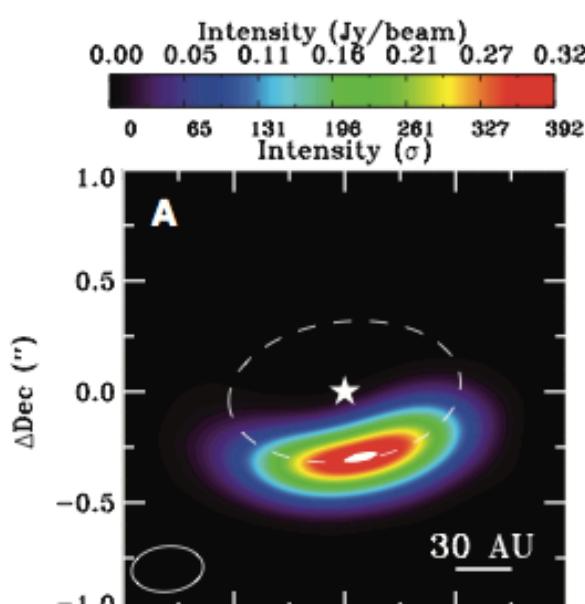
Rossby Wave Instability and

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# Conclusions

- Vortices e
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- Rossby w
- We're in th
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