

Planet Formation – The Evidence from The Kuiper Belt



UPPSALA
UNIVERSITET



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Current Funding



AAG – 2020, 2021



XRP - 2023

EW – 2021, 2022, 2023

TCAN – 2020

Computational Facilities



Circumstellar/Protoplanetary Disks



PP disk fact sheet

Density: $10^{13} - 10^{15} \text{ cm}^{-3}$
(Air: 10^{21} cm^{-3})

Temperature: 10-1000 K

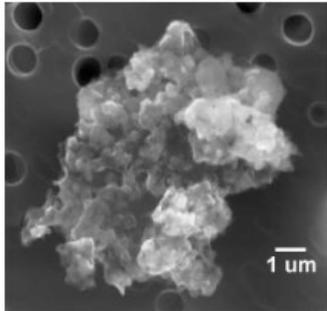
Scale: 0.1-100AU

Mass: $10^{-3} - 10^{-1} M_{\text{sun}}$

Composition: 5:2 H₂-He
mixture. 1% metals.

Planet Formation

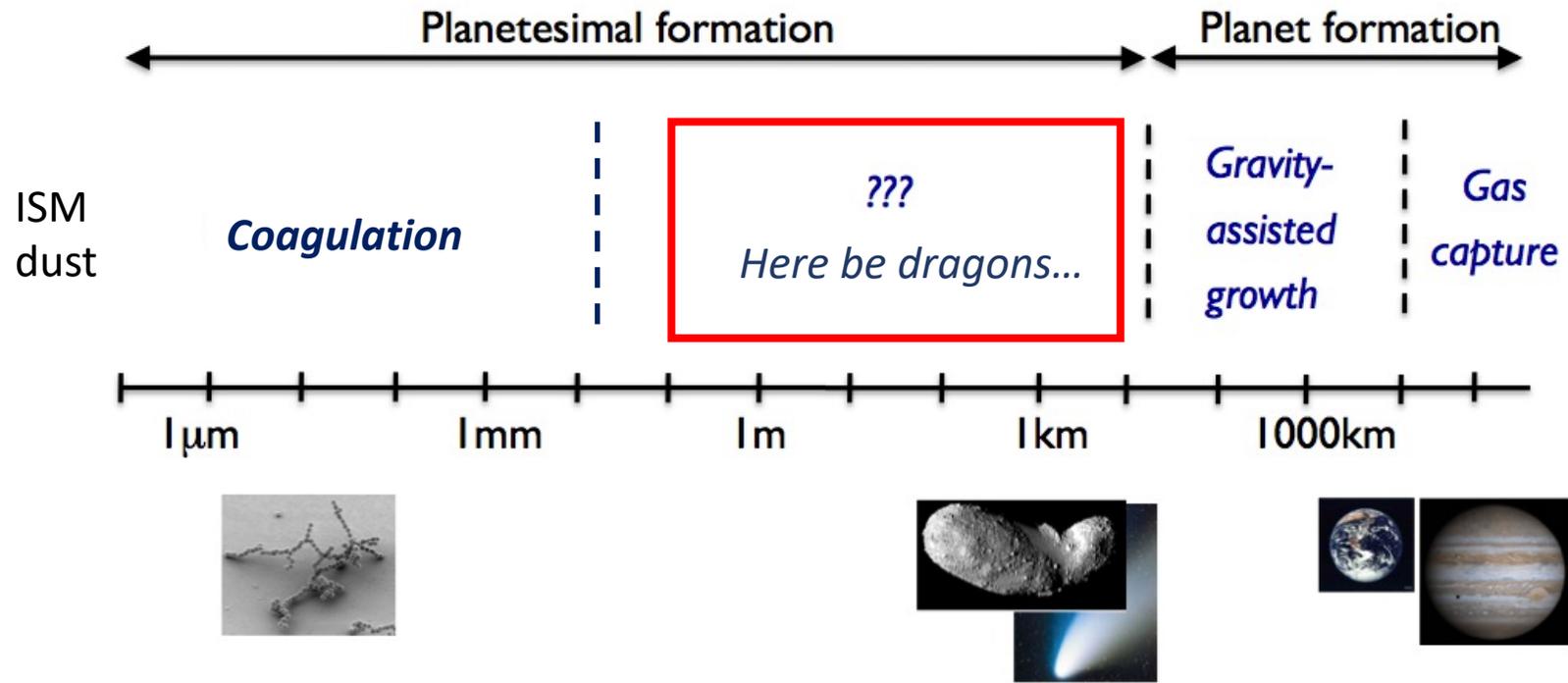
“Planets form in disks of gas and dust”



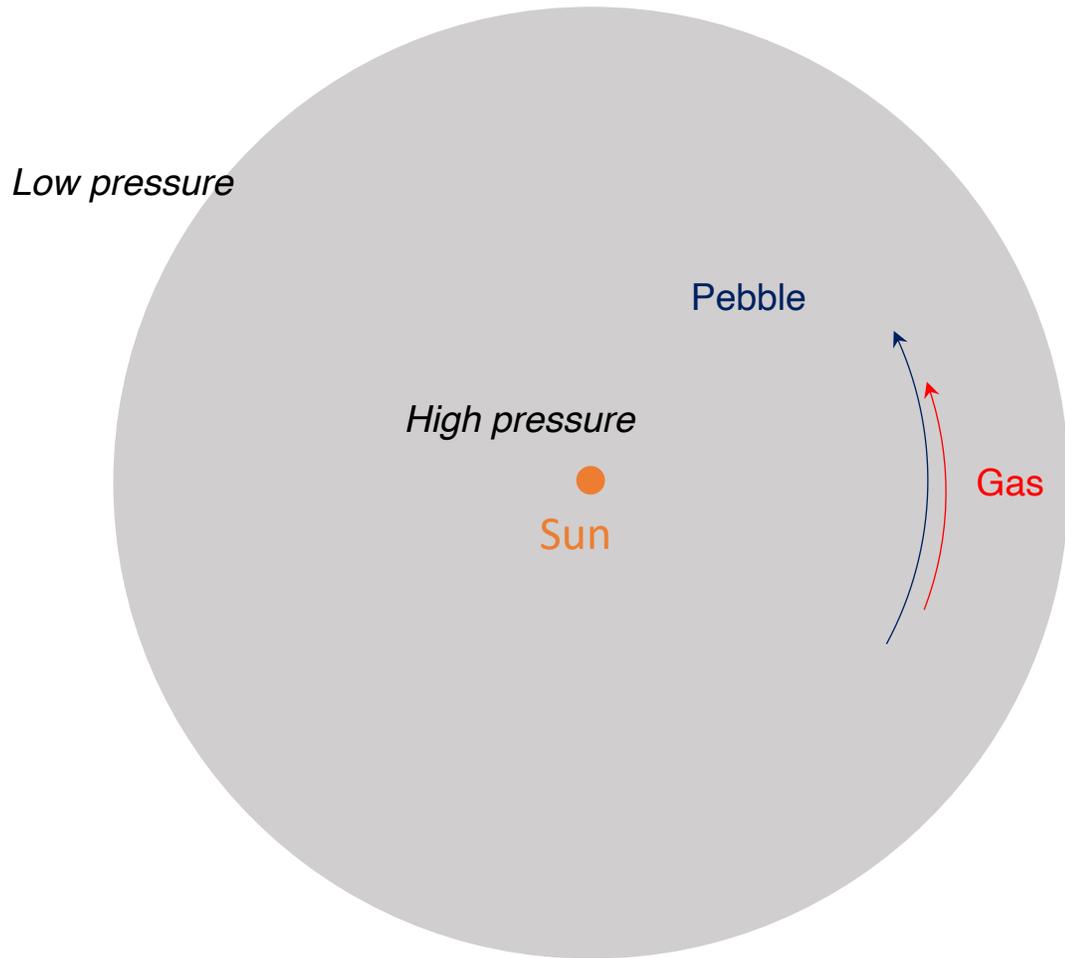
— ***A miracle happens*** —▶



Dust evolution



Headwind and Dust Drift



The **gas** has some pressure support (sub-Keplerian).

The **pebbles** do not feel gas pressure (Keplerian).

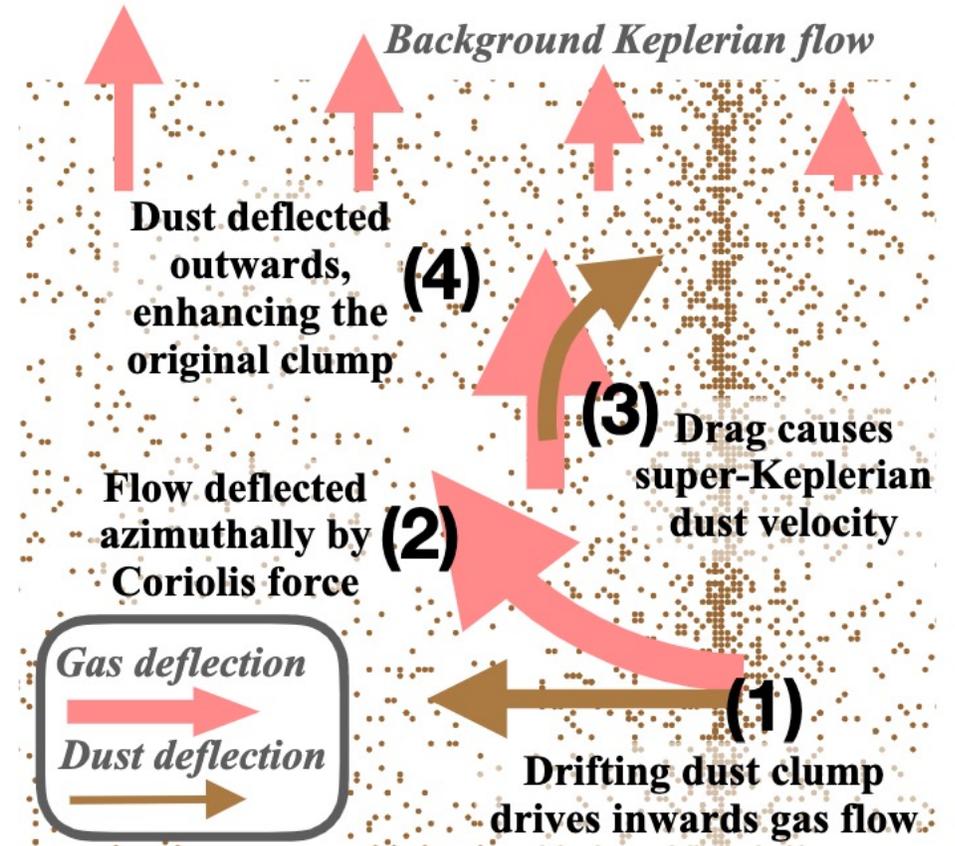
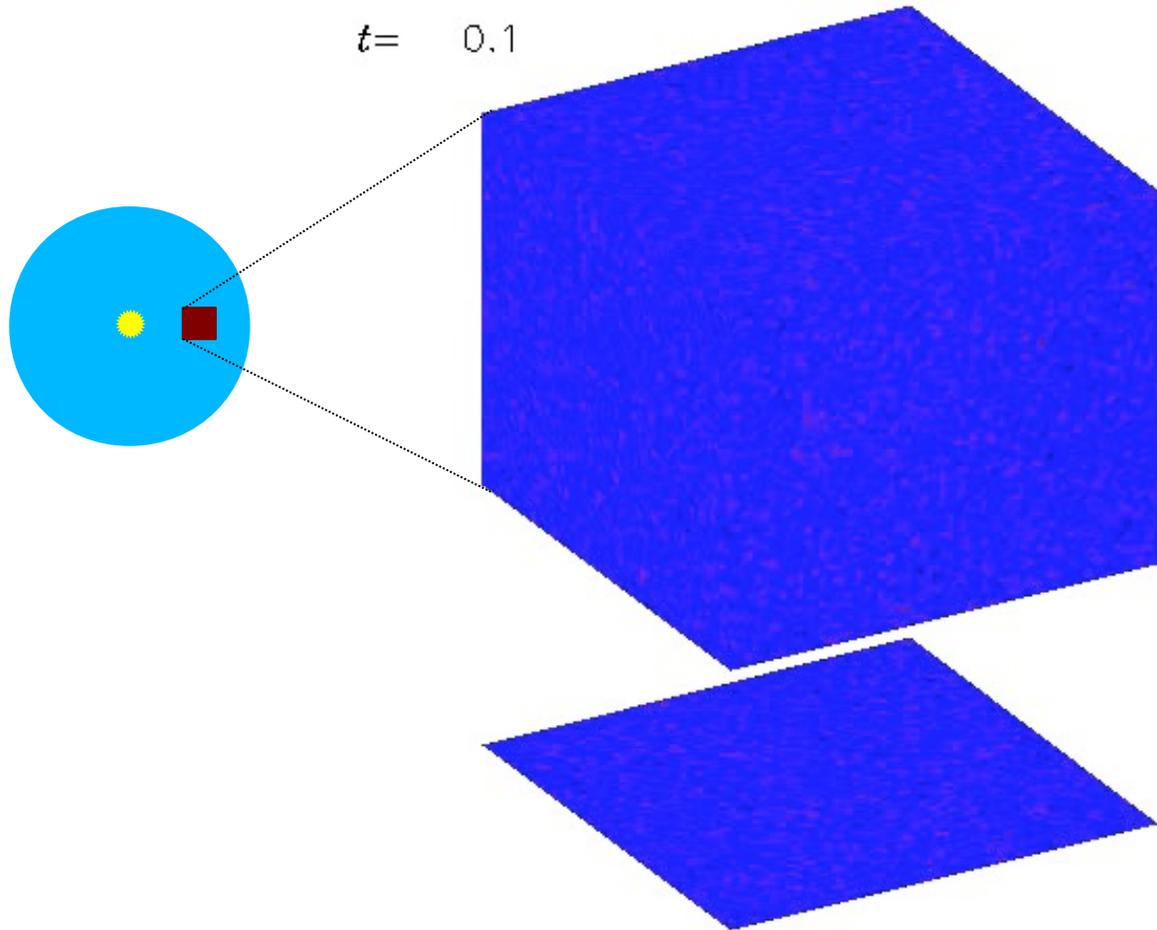
Dust coagulation and drift

Dust particle
coagulation
and radial drift

F. Brauer, C.P. Dullemond
Th. Henning

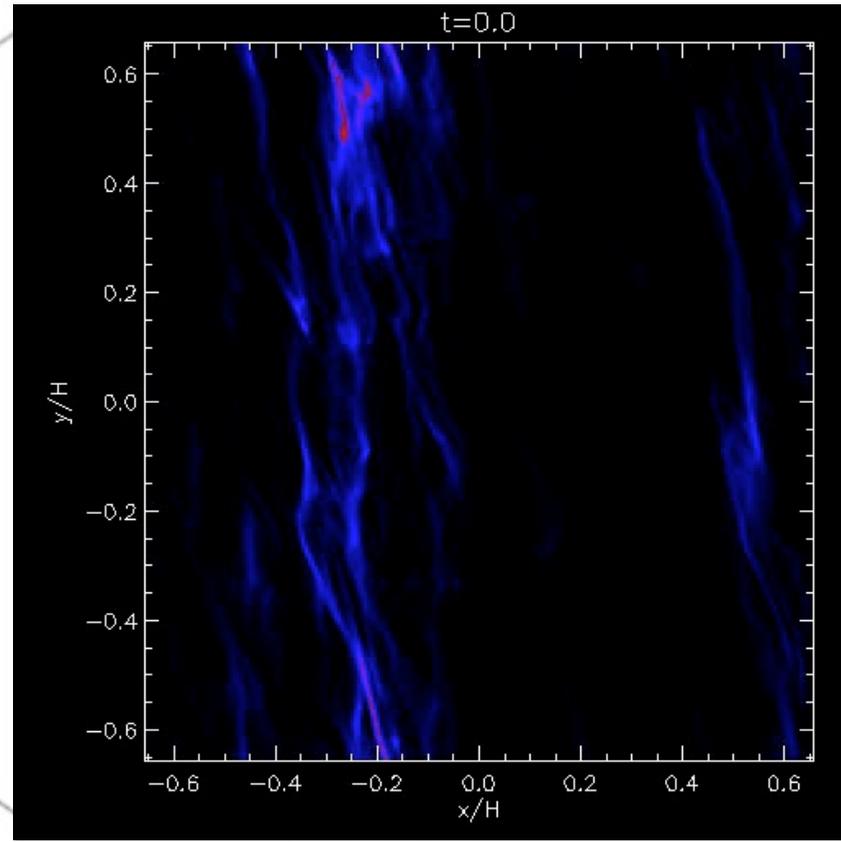
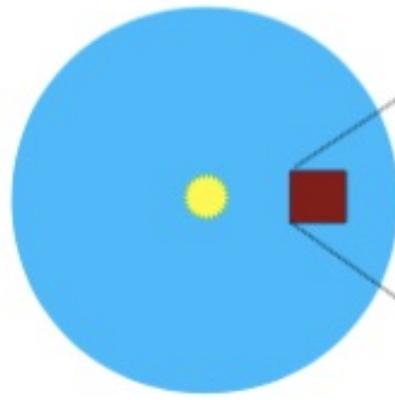
Streaming Instability

The dust drift is hydrodynamically unstable



Lesur et al. (2022)

Gravitational collapse into planetesimals



Johansen et al. (2007)

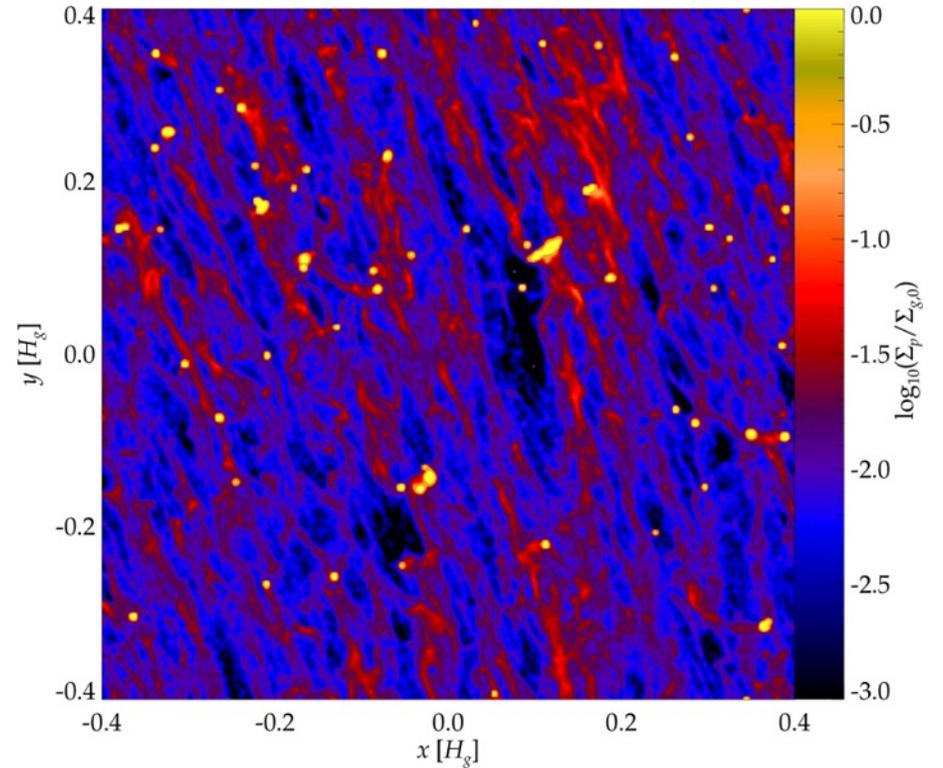
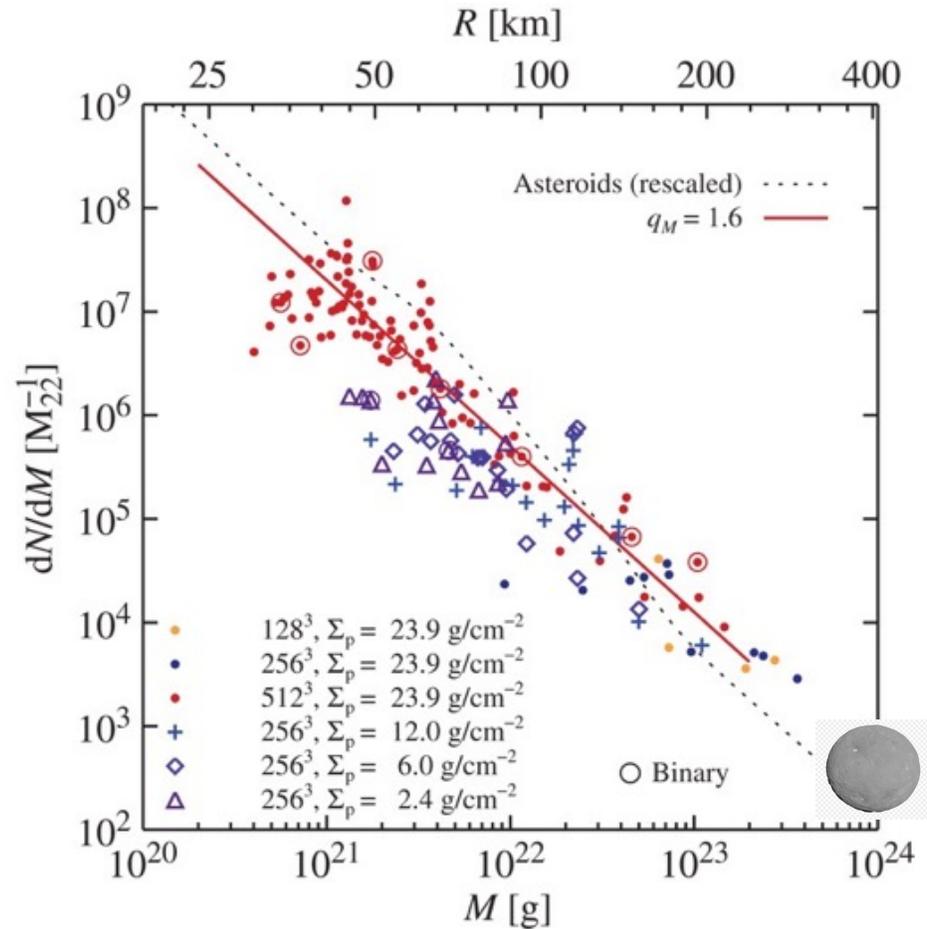


nature
astronomy

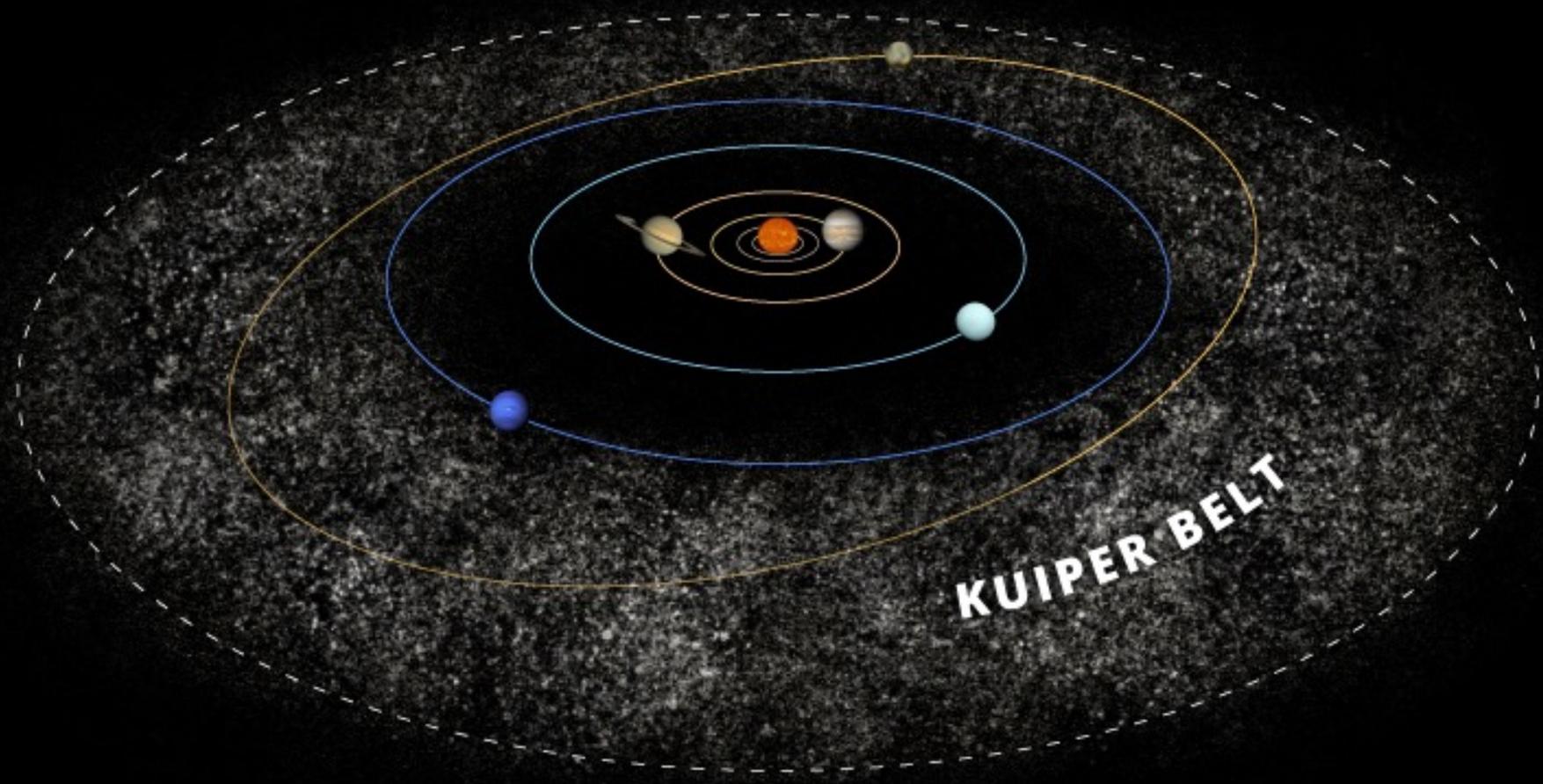
Fingerprints of
streaming instability

**How can we verify the
streaming instability
hypothesis?**

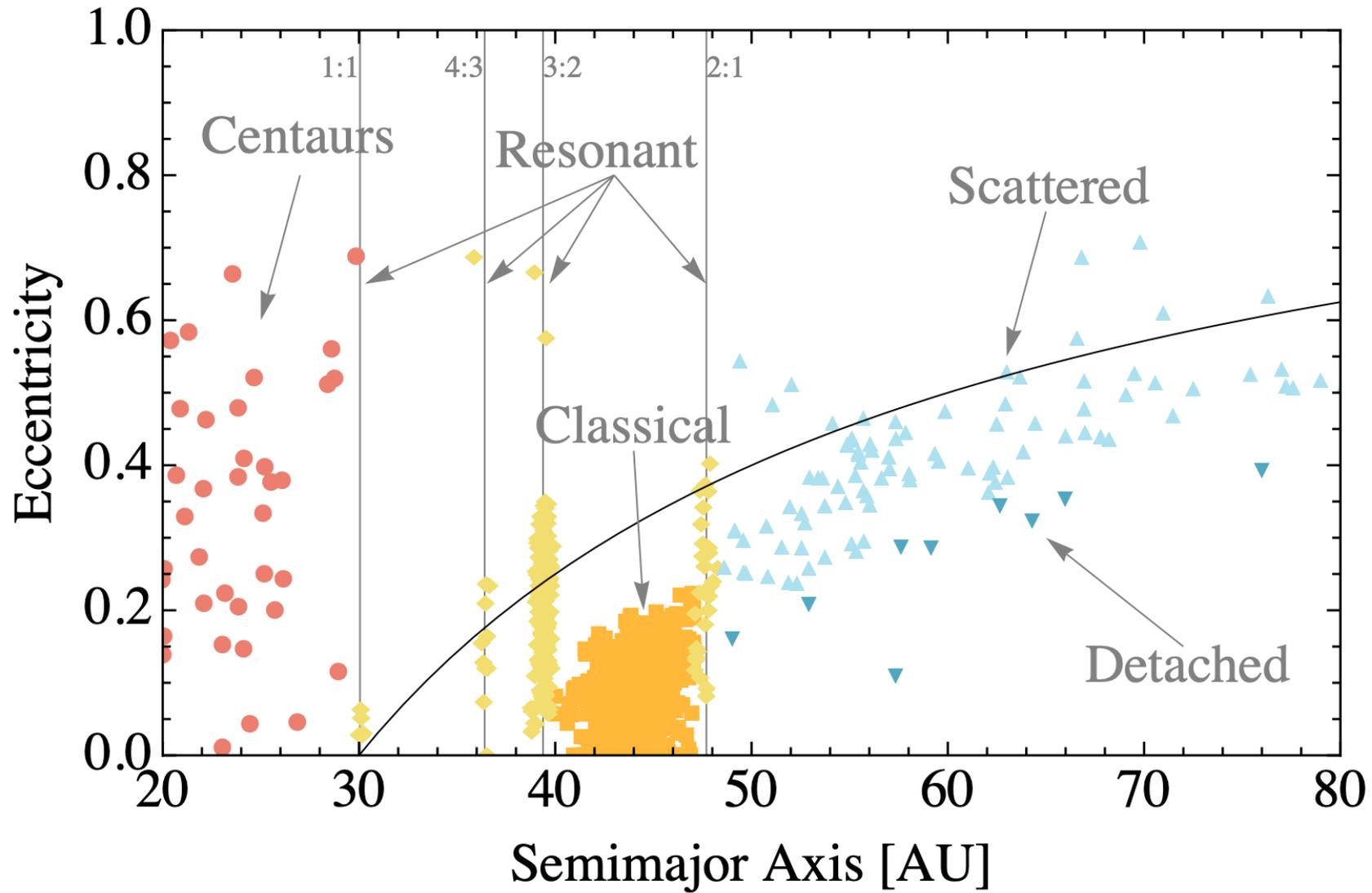
Planetesimal Formation



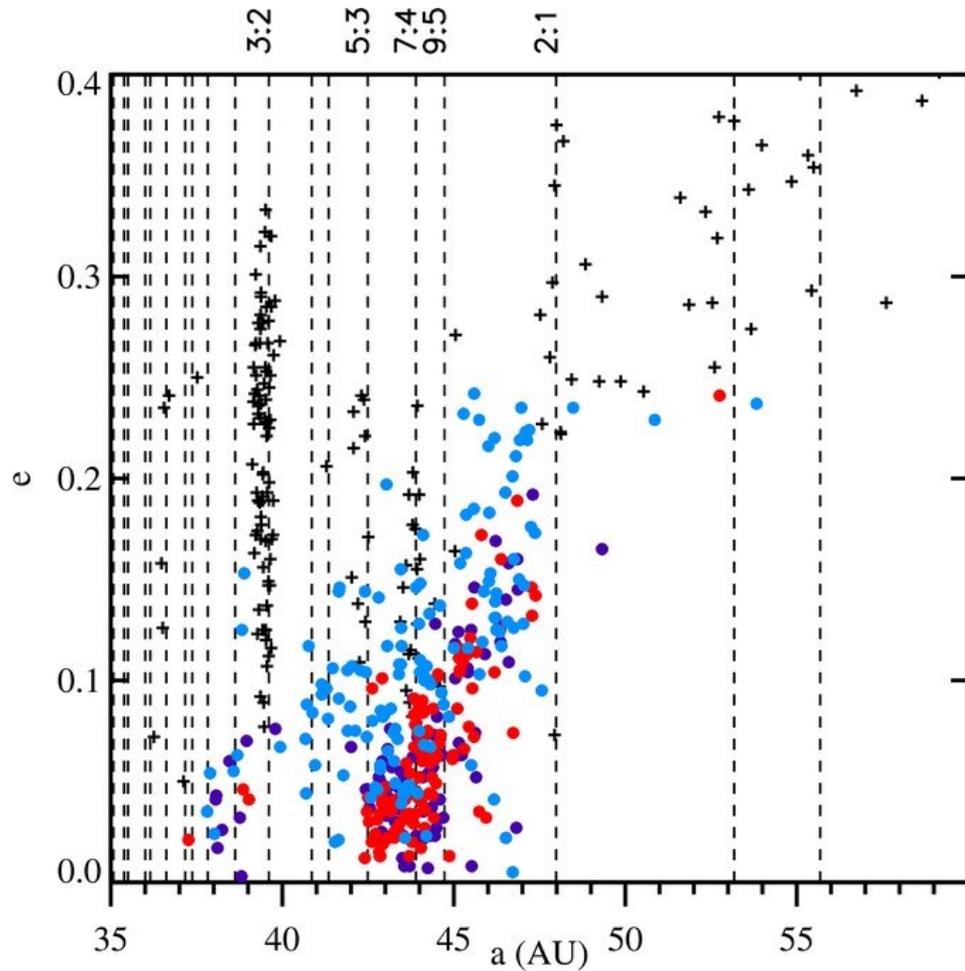
Initial mass function consistent with mass distribution of asteroid belt. Slope 1.6



Structure of the Kuiper Belt



Structure of the Kuiper Belt



+ Resonant and Scattered

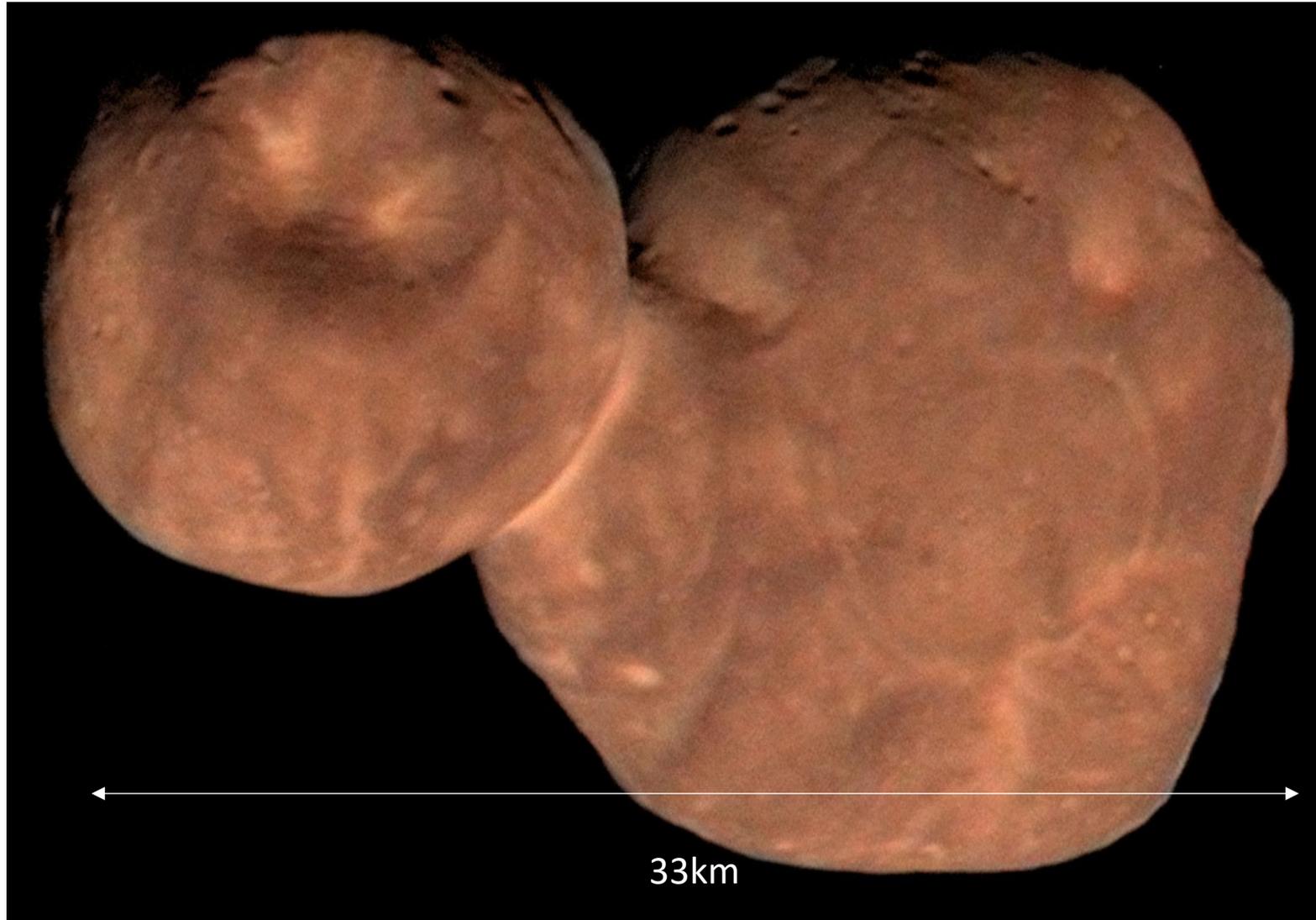
Cold Classical $i < 2^\circ$

"Ambiguous" $2^\circ < i < 6^\circ$

Hot Classicals $i > 6^\circ$

Cold Classicals: Presumably
pristine planetesimals

Arrokoth (MU₆₉)

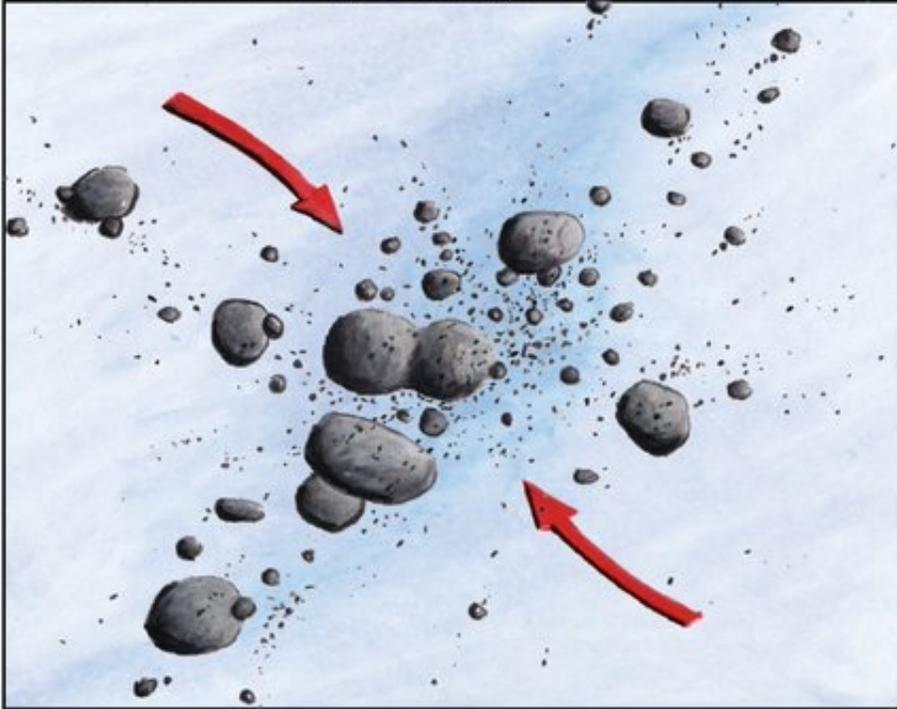


New Horizons Flyby, Jan 2019

The Cartoon Image

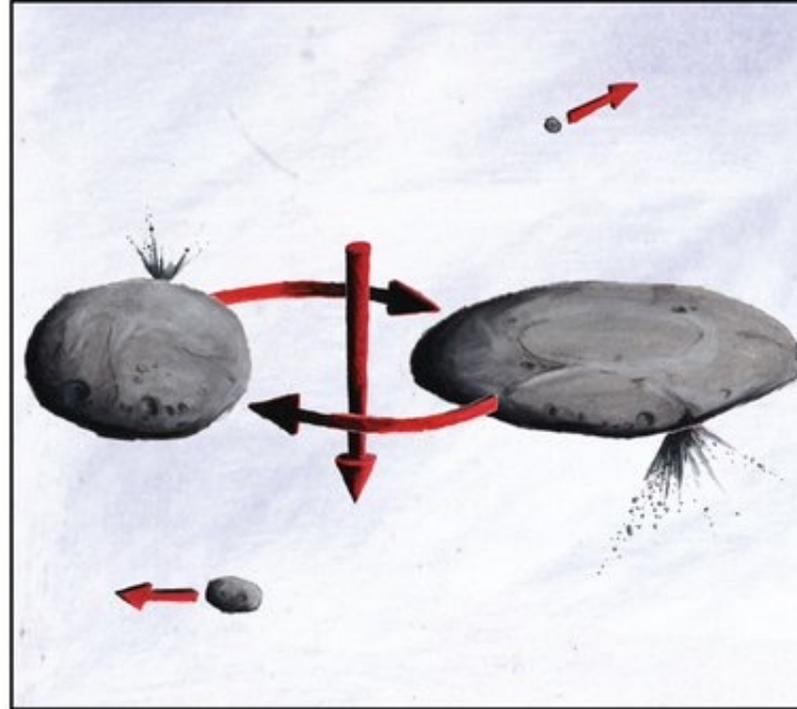
The Formation of 2014 MU69

About 4.5 billion years ago...



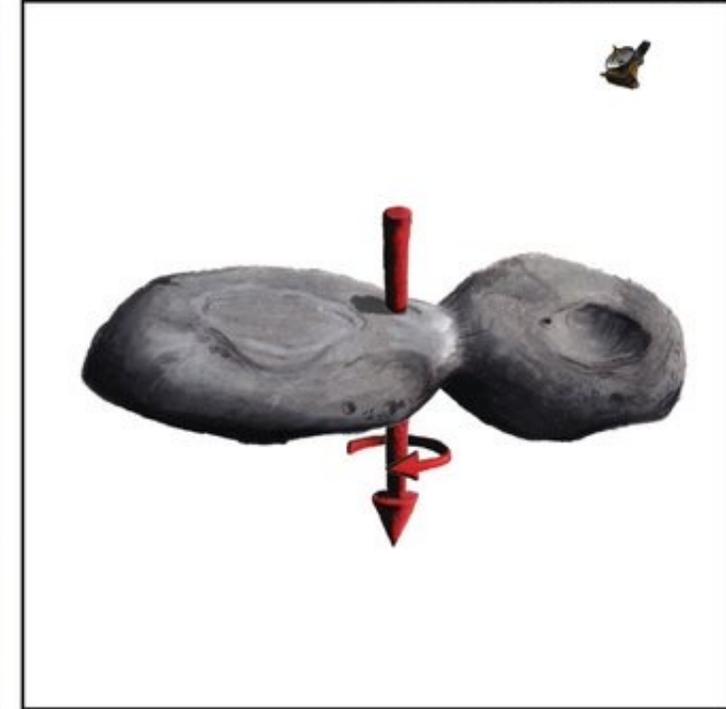
A rotating cloud of small, icy bodies starts to coalesce in the outer solar system.

 New Horizons / NASA / JHUAPL / SwRI / James Tuttle Keane



Eventually two larger bodies remain.

...1 January 2019.

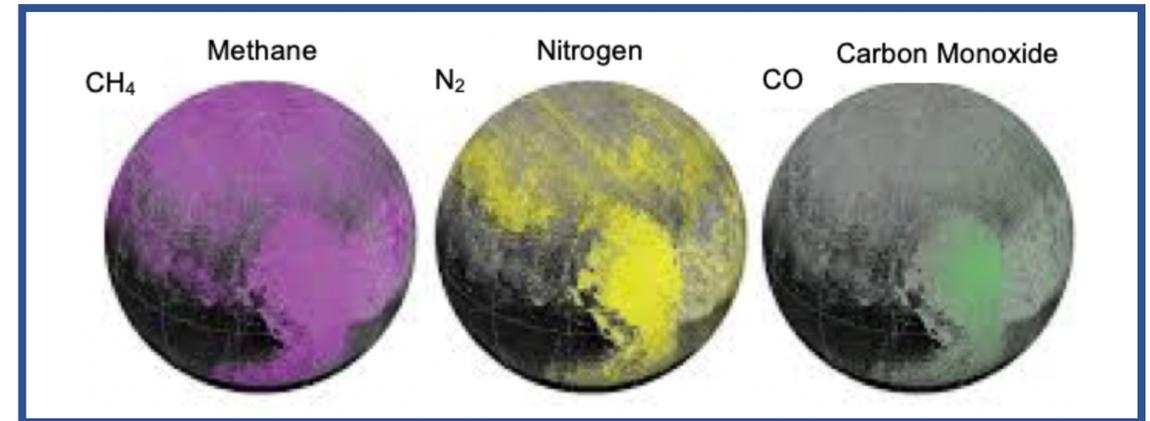
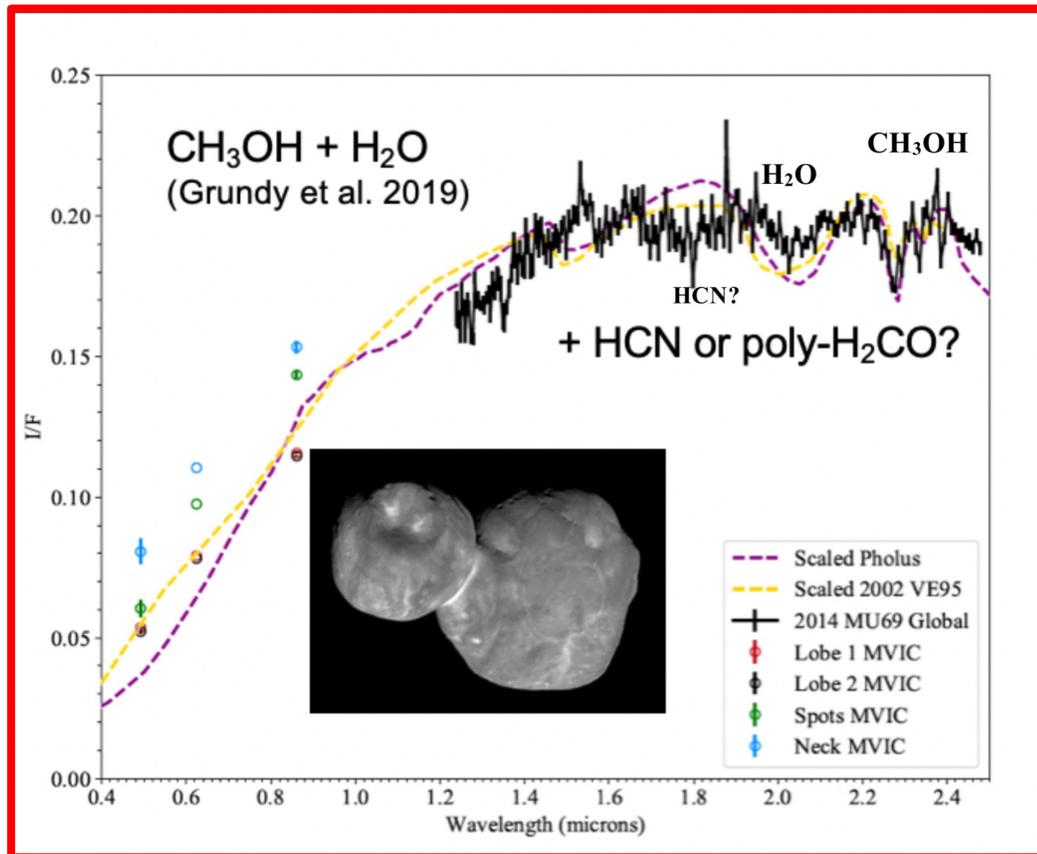


The two bodies slowly spiral closer until they touch, forming the bi-lobed object we see today.

Arrokoth and Pluto ices are different

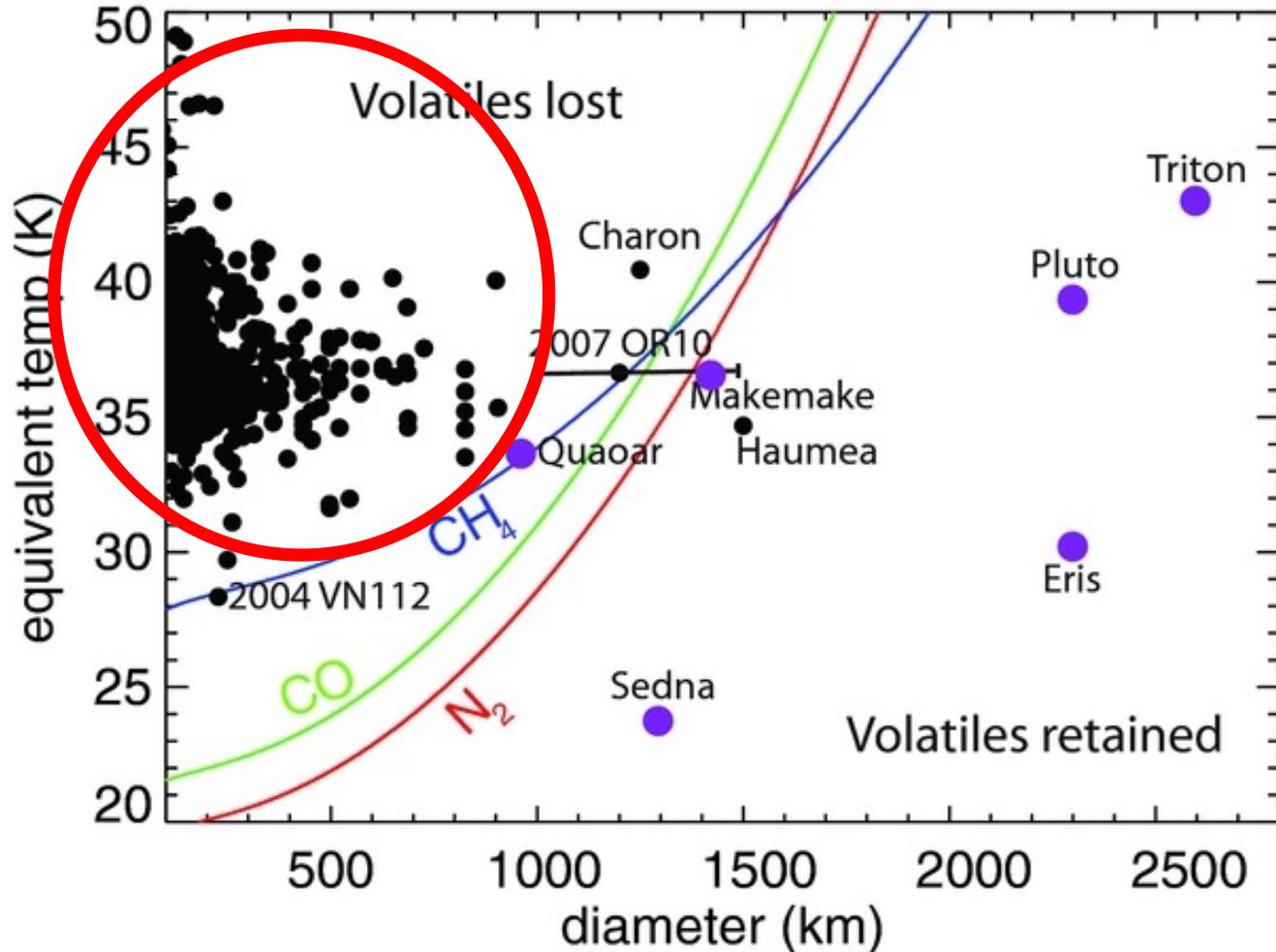
Arrokoth : Methanol, H₂O, HCN

Pluto : CH₄, N₂, CO



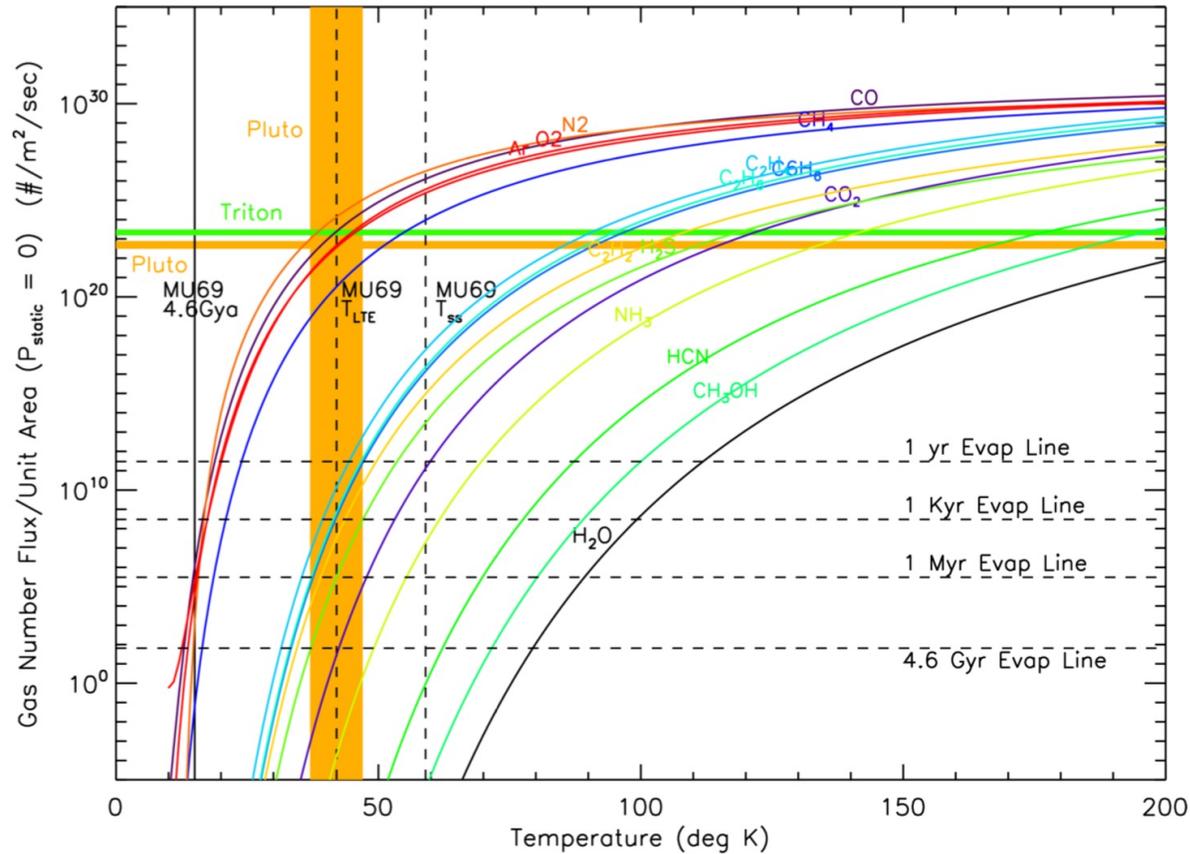
Retention of volatiles

If Pluto is formed from similar bodies to Arrokoth, they must retain volatiles



Needs shielding from sunlight

Retention of volatiles

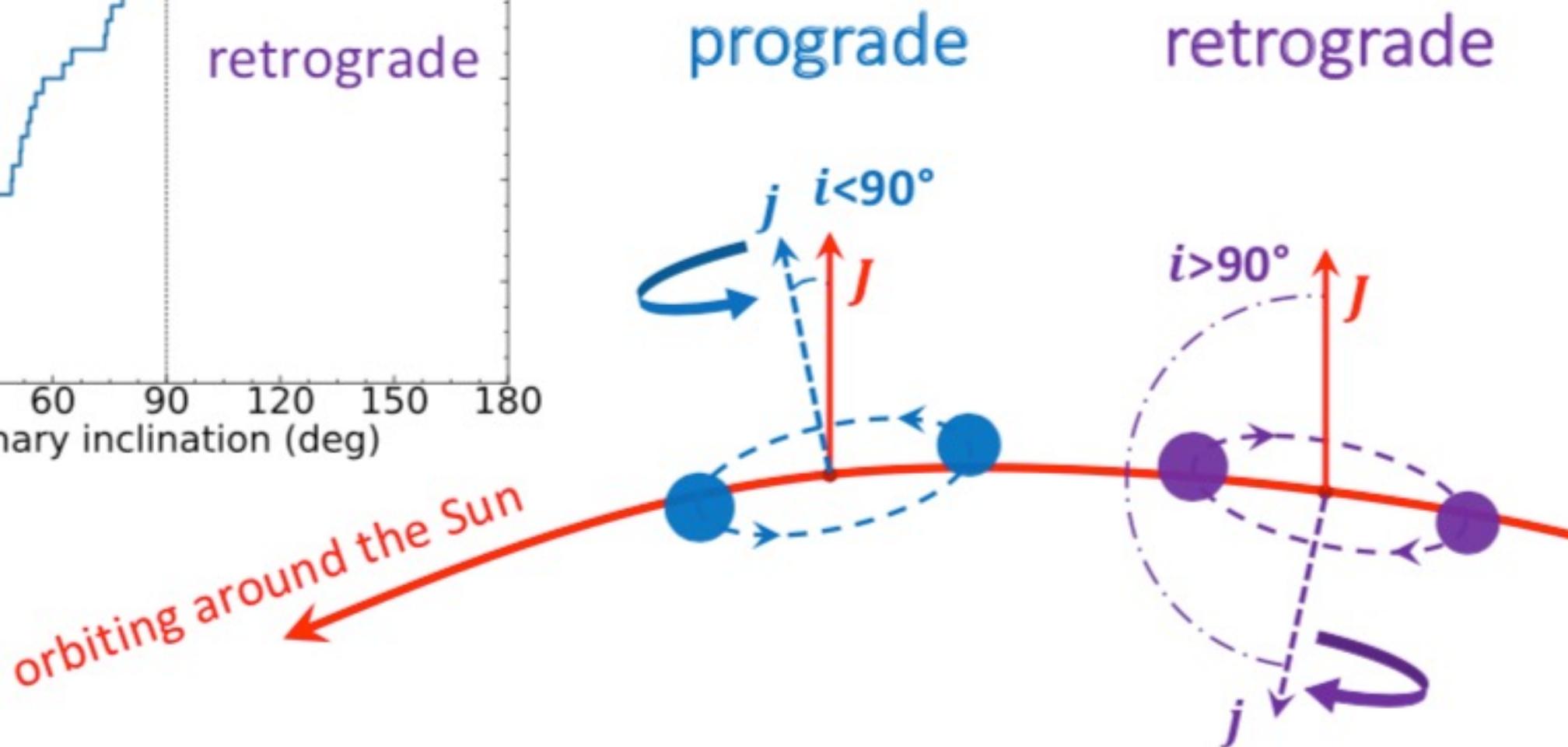
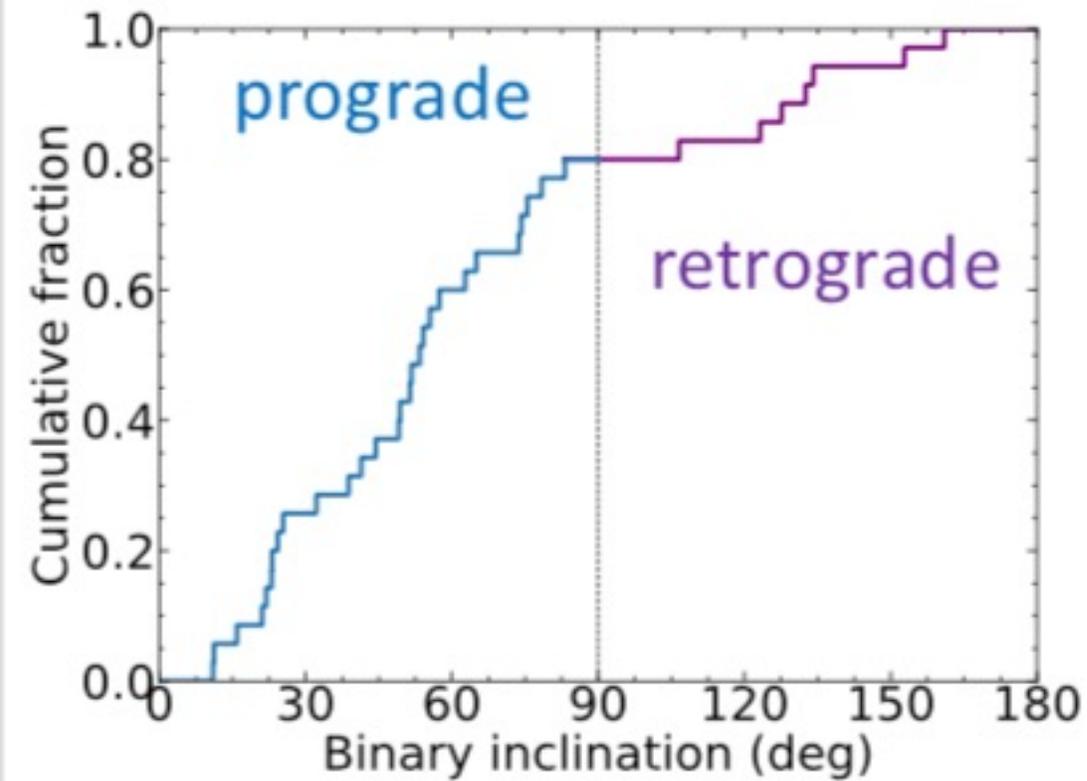


Hypervolatiles ($\text{CH}_4 / \text{CO} / \text{N}_2$)
lost under vacuum pressure and microgravity in ~ 1 Myr
for 40 K

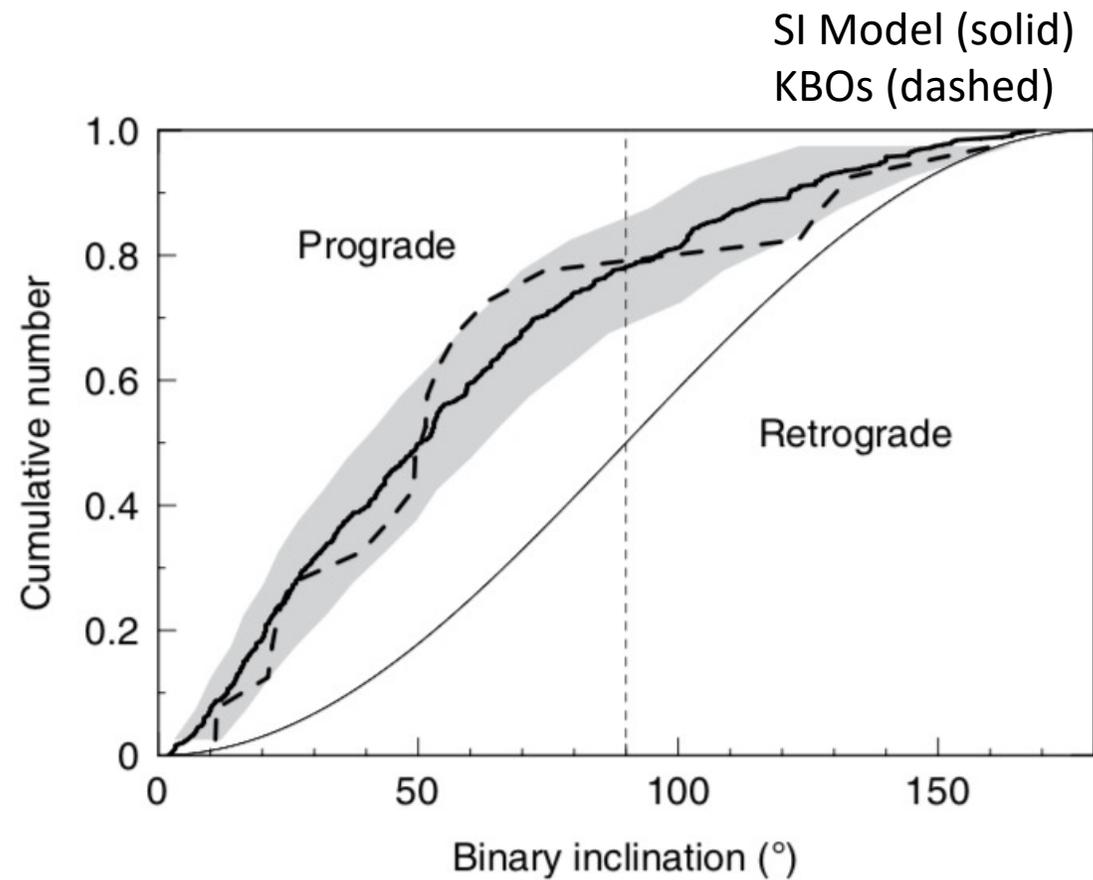
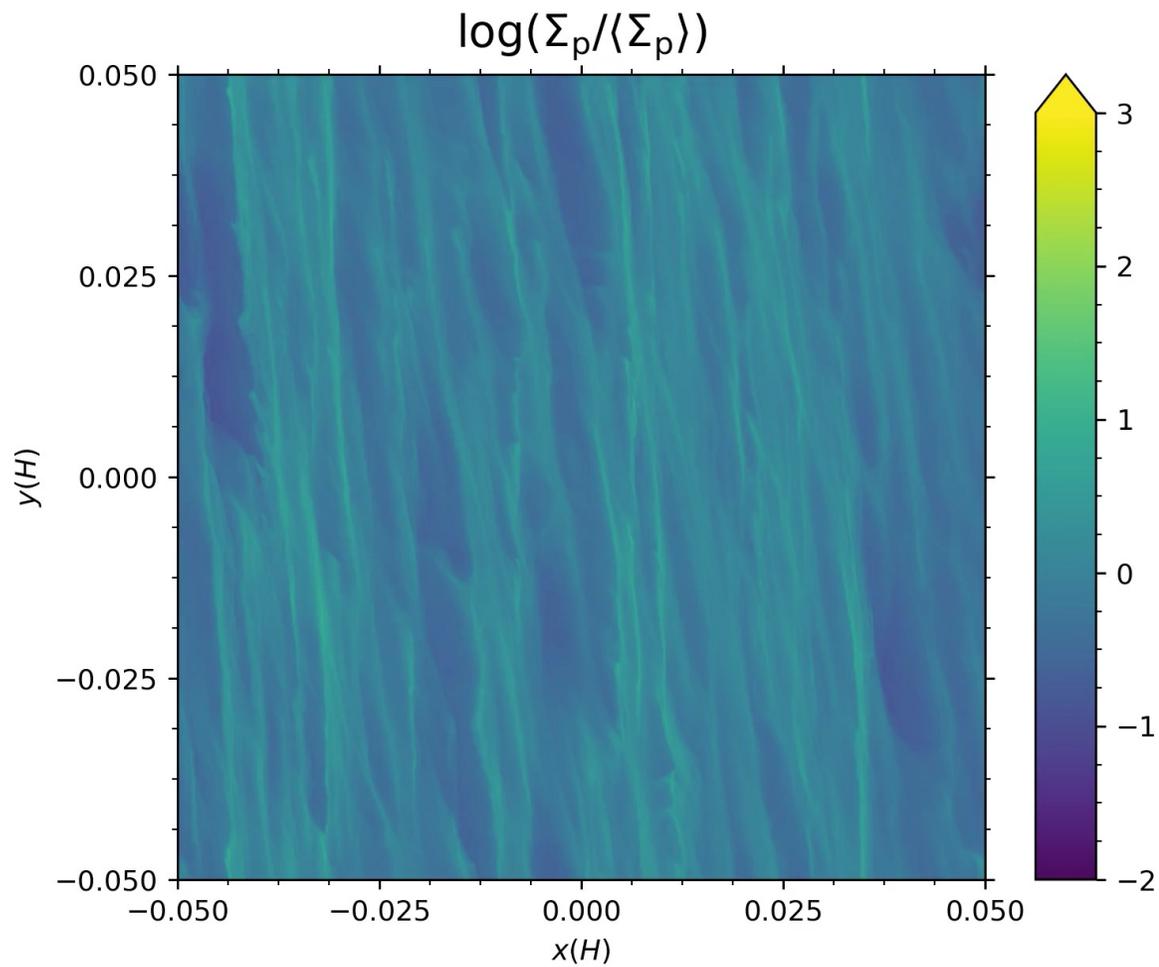
Retained for long times if formed $< 20\text{K}$

Formation of MU69 in an optically thick disk keeps the interior cold enough to allow the volatiles to remain frozen.

Cold Classical KBOs: Preference for Prograde

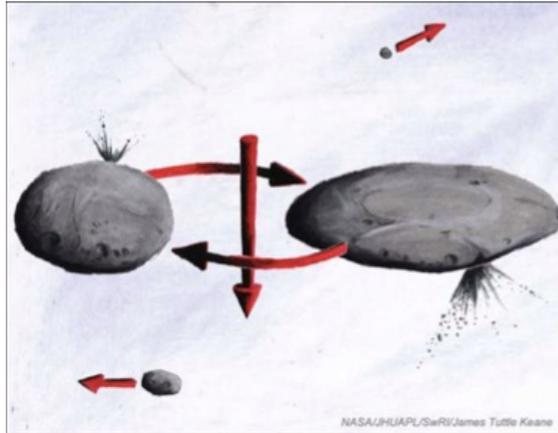


Counting binaries: Preference for Prograde (~80%)



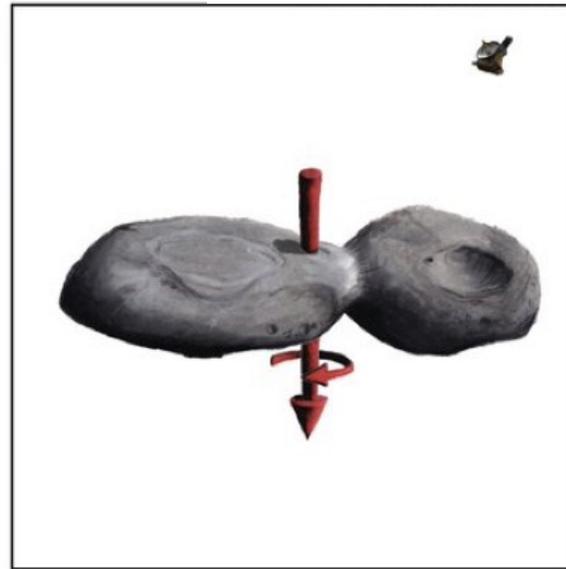
How did contact happen?

Mutual orbit
(i.e., not captured)

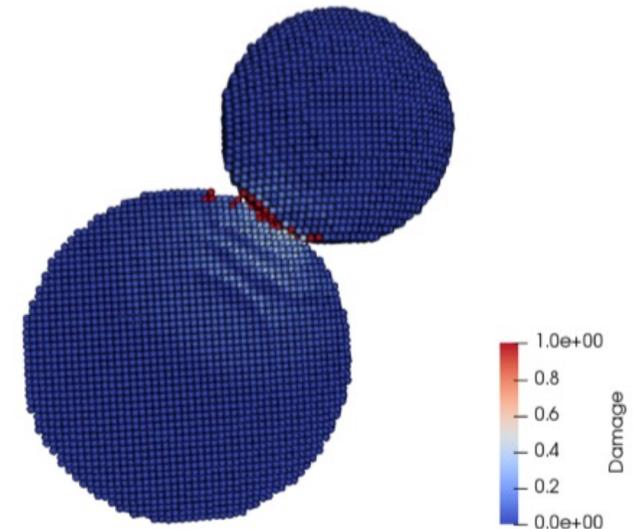


Inferred from:
alignment of component minor axes,
small angular momentum,
similar colors.

Slow merger
(~2 m/s: human walking speed)



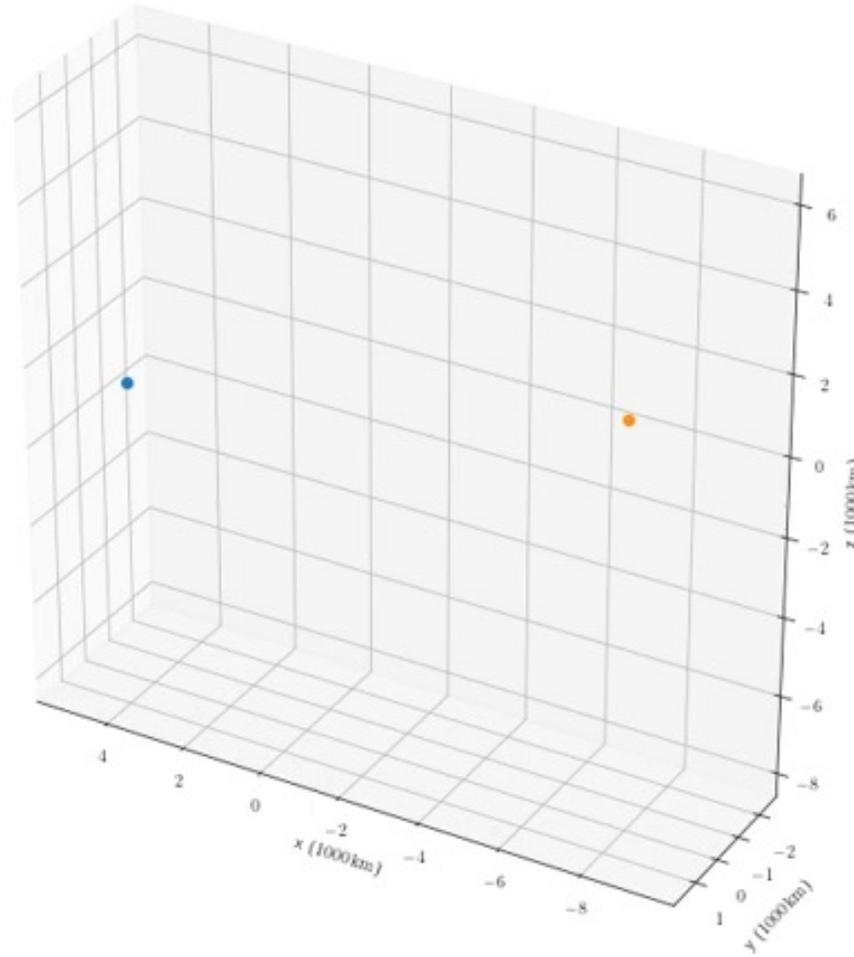
Inferred from:
Negligible evidence for impact damage



Arrokoth (MU₆₉)

time = -1.3 kyr

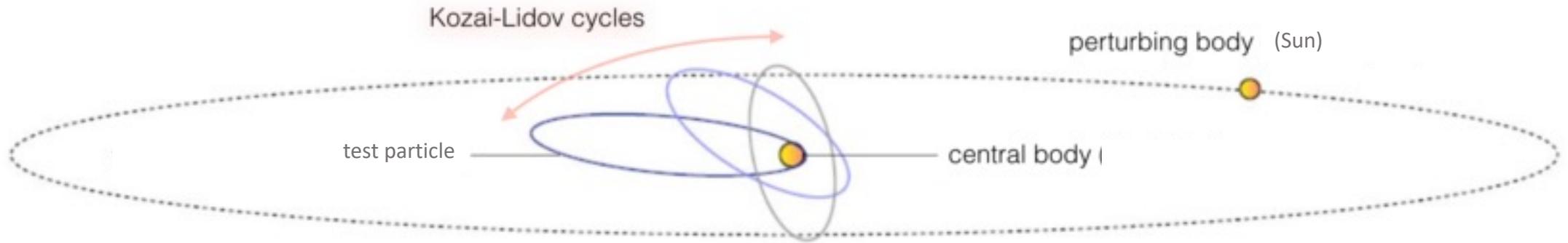
Wenu - Weeyo



© Alexander Heger (2023)

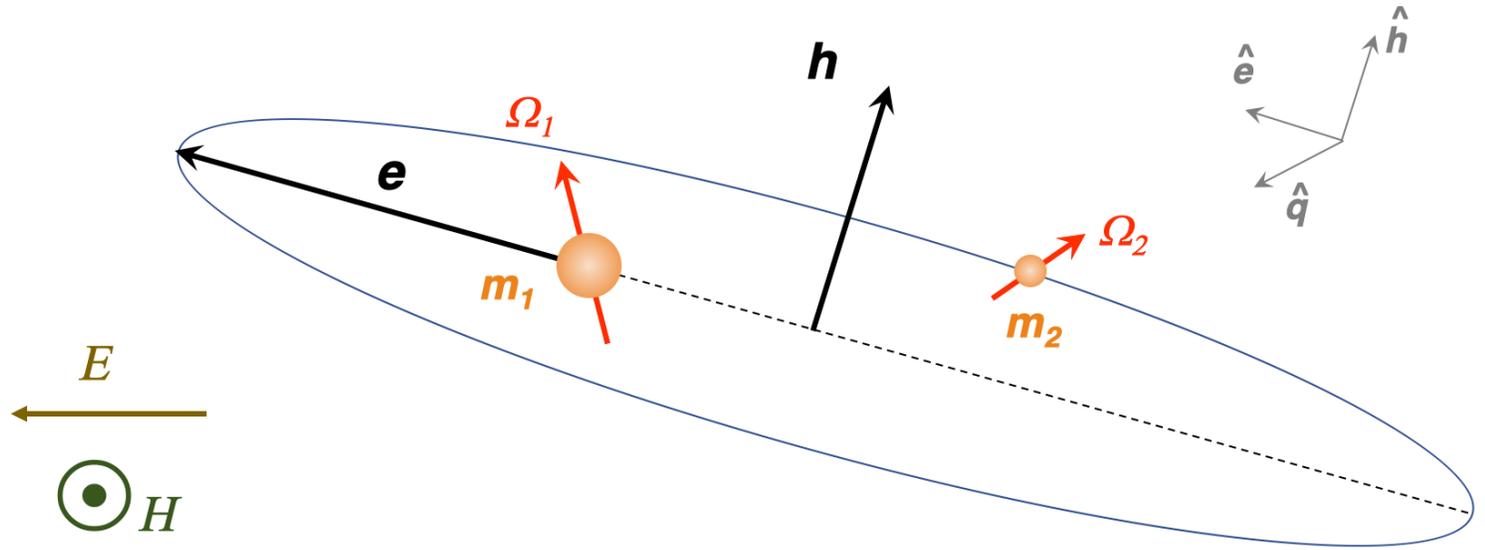


Kozai-Lidov Oscillations



Kozai + Tidal Friction + Permanent Quadrupole + Drag

$$\begin{aligned} \frac{de}{dt} &= -e \left[V_1 + V_2 + V_d + 5(1 - e^2) S_{eq} \right], \\ \frac{dh}{dt} &= -h \left(W_1 + W_2 + W_d - 5e^2 S_{eq} \right), \\ \frac{d\hat{e}}{dt} &= \left[Z_1 + Z_2 + (1 - e^2) (4S_{ee} - S_{qq}) \right] \hat{q} \\ &\quad - \left[Y_1 + Y_2 + (1 - e^2) S_{qh} \right] \hat{h}, \\ \frac{d\hat{h}}{dt} &= \left[Y_1 + Y_2 + (1 - e^2) S_{qh} \right] \hat{e} \\ &\quad - \left[X_1 + X_2 + (4e^2 + 1) S_{eh} \right] \hat{q}, \\ \frac{d\Omega_1}{dt} &= \frac{\mu_r h}{I_1} \left(-Y_1 \hat{e} + X_1 \hat{q} + W_1 \hat{h} \right), \\ \frac{d\Omega_2}{dt} &= \frac{\mu_r h}{I_2} \left(-Y_2 \hat{e} + X_2 \hat{q} + W_2 \hat{h} \right). \end{aligned}$$



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Public code for Kozai-Lidov oscillations with tidal friction, permanent quadrupole, and gas drag.

2 commits 1 branch 0 releases 1 contributor

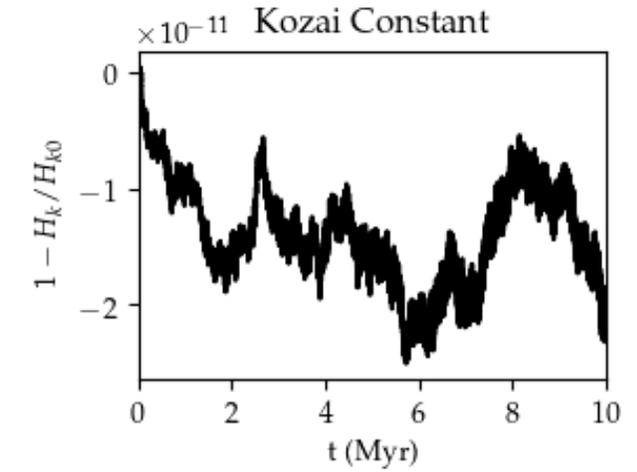
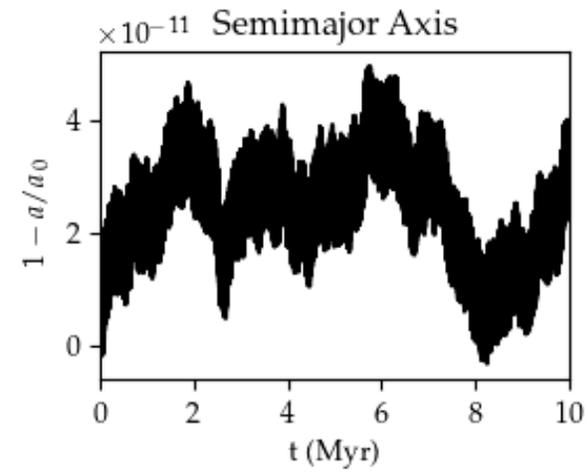
Branch: master - New pull request Find file Clone or download -

wlyra	The Kozai code for KTJD (Kozai, Tides, J2, and Drag).	Latest commit 5d9b547 7 days ago
Makefile	The Kozai code for KTJD (Kozai, Tides, J2, and Drag).	7 days ago
README.md	Initial commit	7 days ago
input.in	The Kozai code for KTJD (Kozai, Tides, J2, and Drag).	7 days ago
yoshikozai.f90	The Kozai code for KTJD (Kozai, Tides, J2, and Drag).	7 days ago

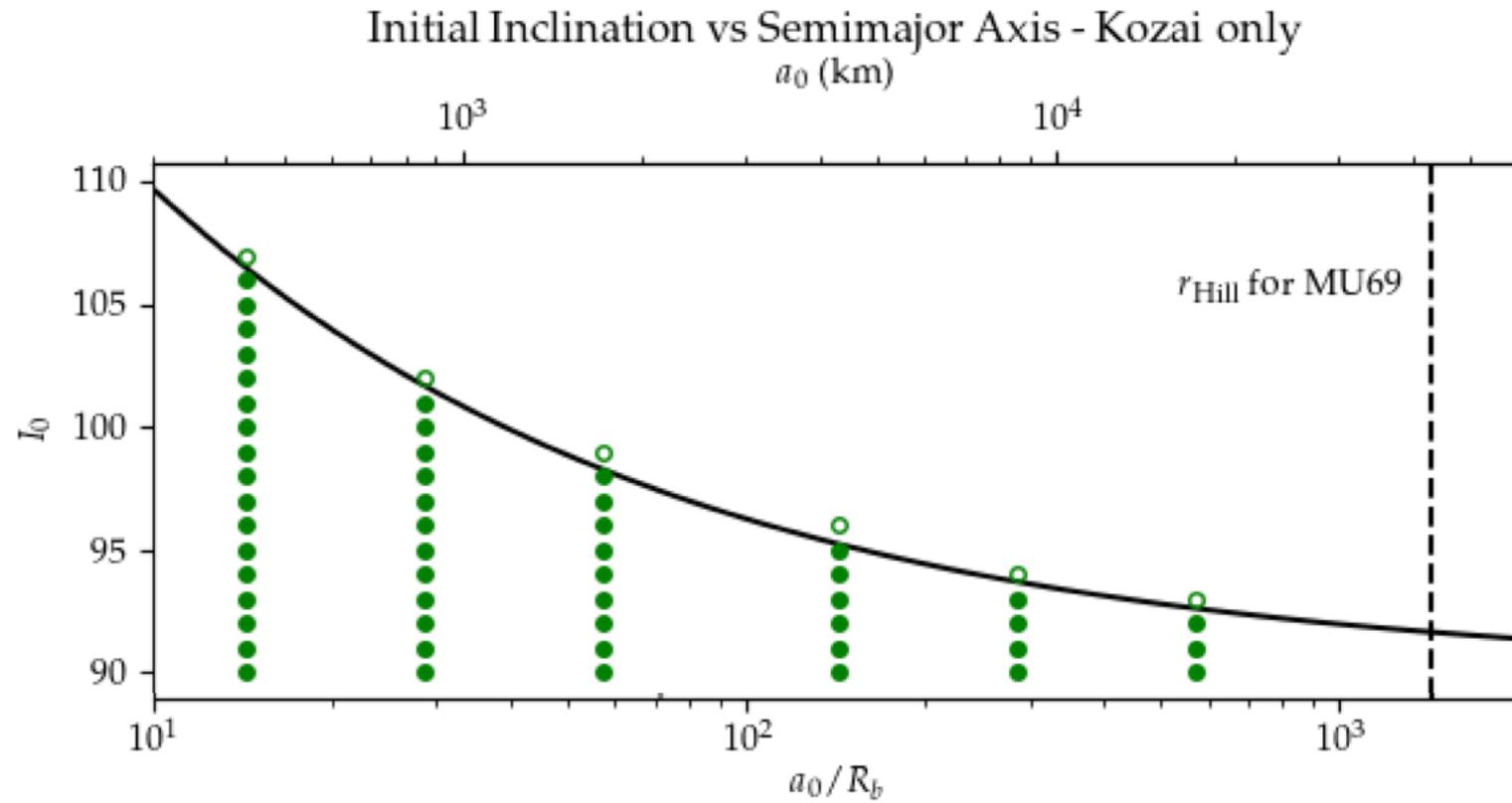
README.md

yoshikozai

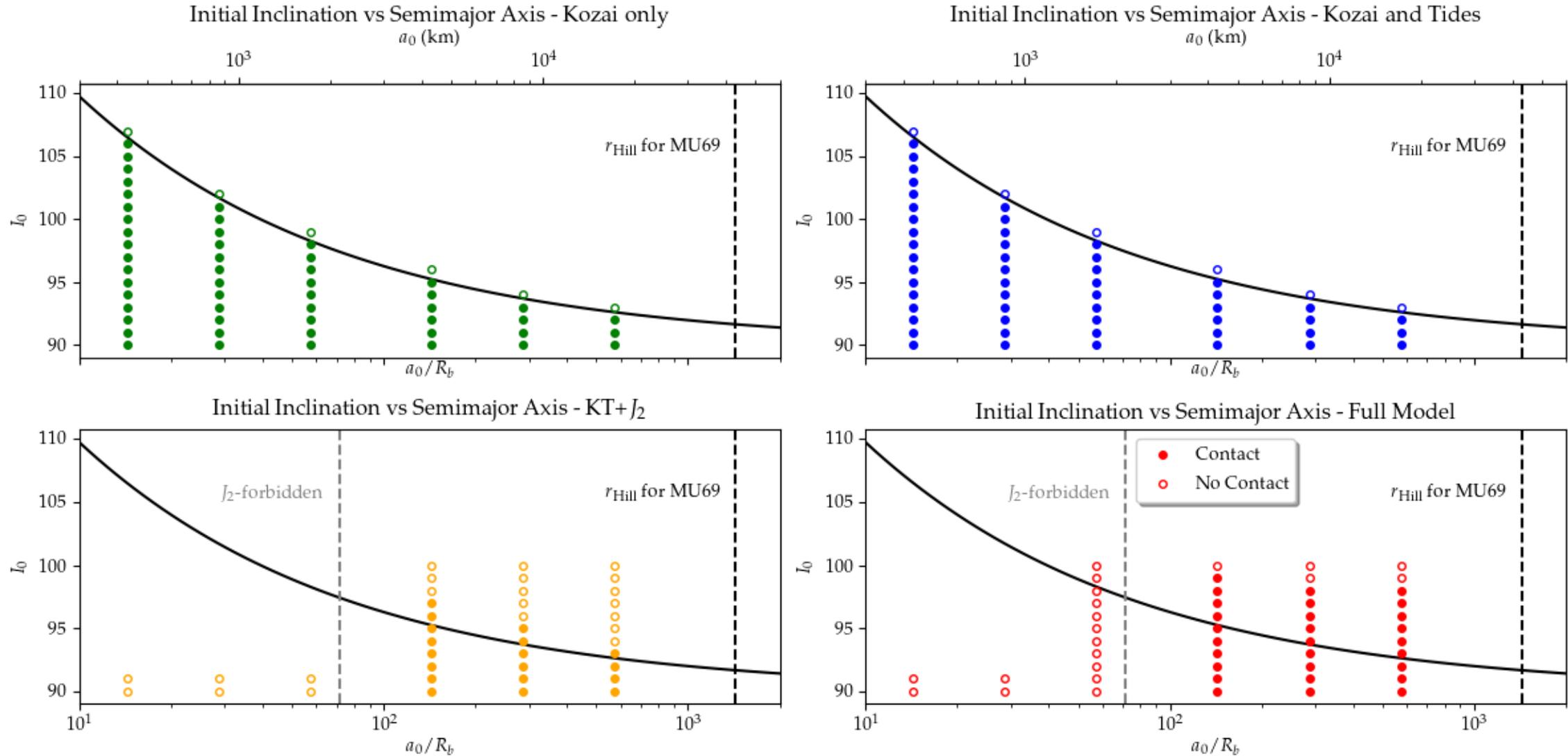
Public code for Kozai-Lidov oscillations with tidal friction, permanent quadrupole, and gas drag.



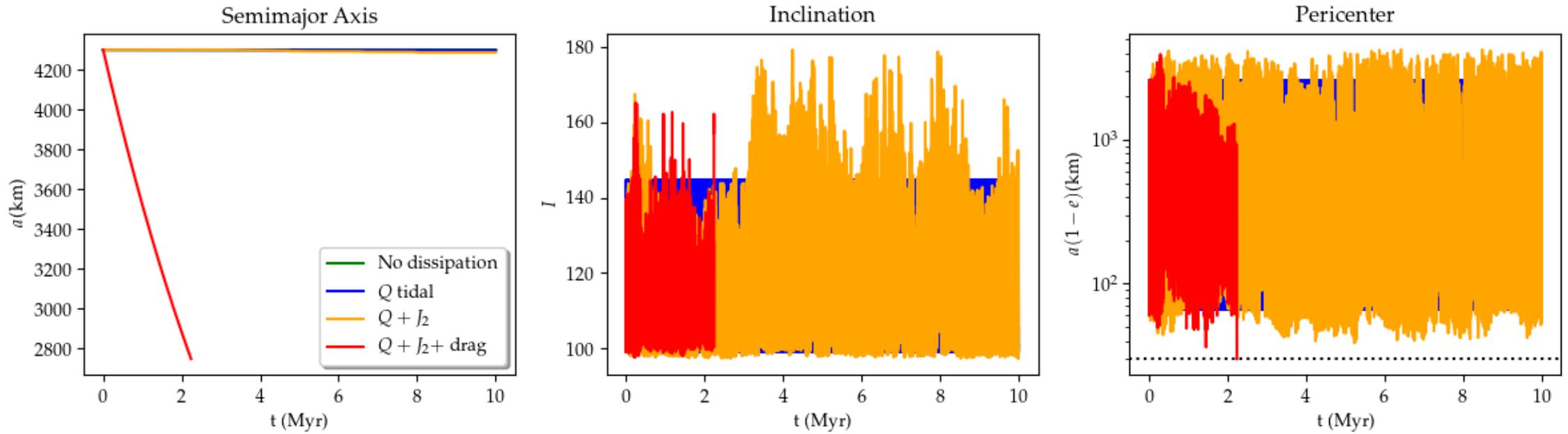
Critical Inclination

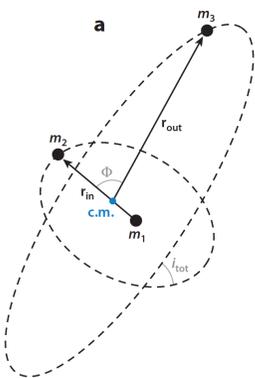


Kozai + Tidal Friction + Permanent Quadrupole + Drag



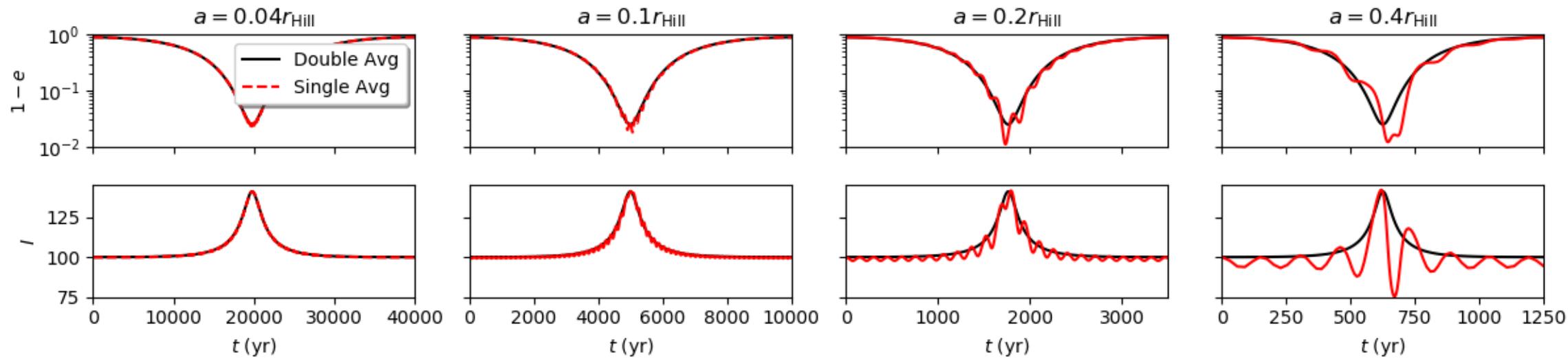
Effect of Drag



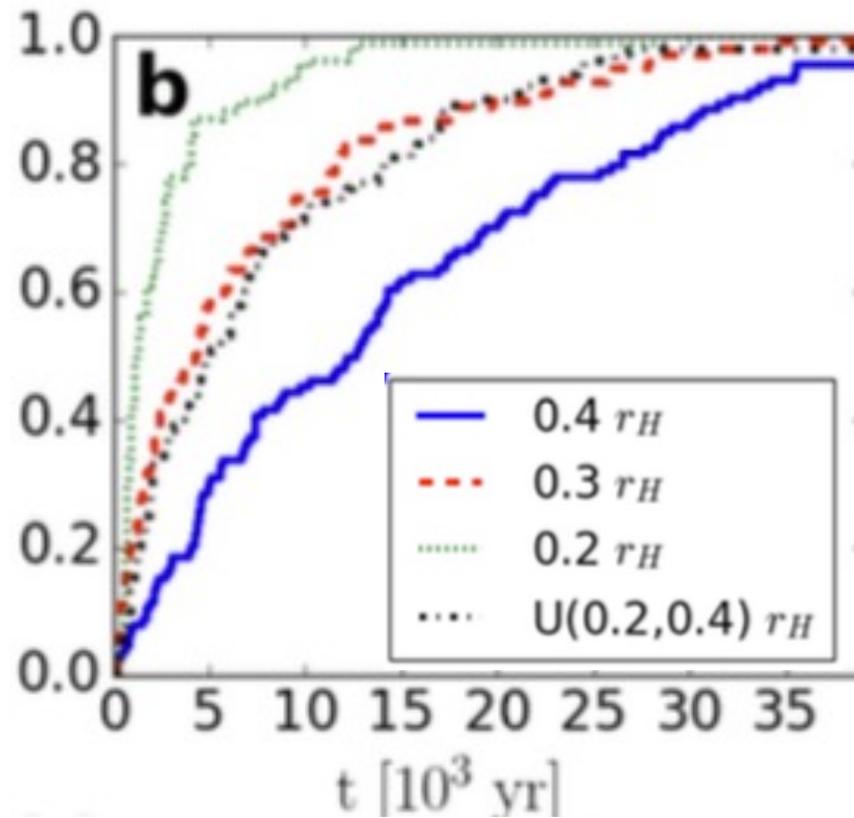


Caveat: limited by double-averaging

Double-Averaged vs Single-Averaged



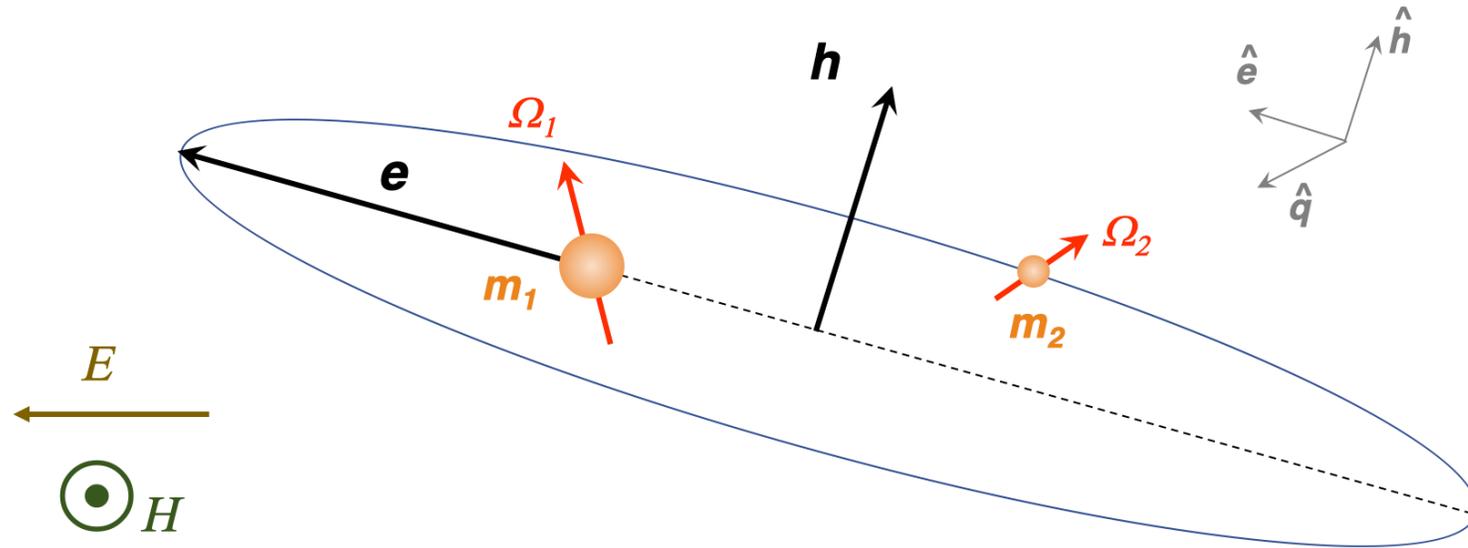
N-body simulations (no tides, J2, or drag)



Time to contact

Too short to allow for alignment

Alignment of the Spin Vectors



Mainly driven by J_2 (permanent quadrupole)

Timescale proportional to a^4 (4th power of semimajor axis)

5 Gyr for $a/R \sim 100$

0.5 Myr for $a/R \sim 10$

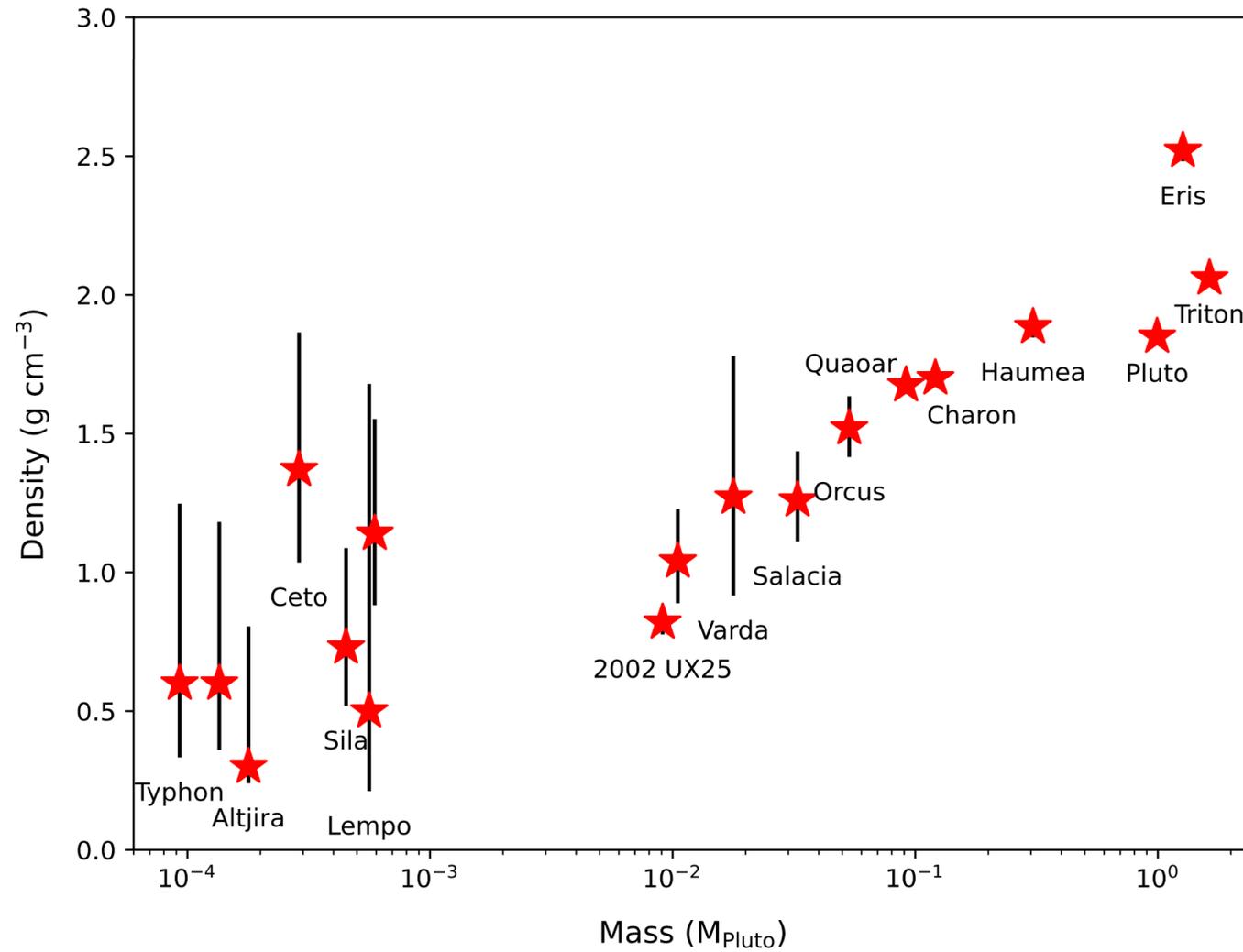
- Solved the hierarchical 3-body problem with gas drag
- Implemented the solution into a Kozai plus tidal friction code
- Contact via Kozai cycles in the Kuiper belt, orbits become grazing
- Window of contact increased by J_2 and drag
- 10% of KBCC binaries should be contact binaries
- Velocities at contact should be about 3-4 m/s

...1 January 2019.



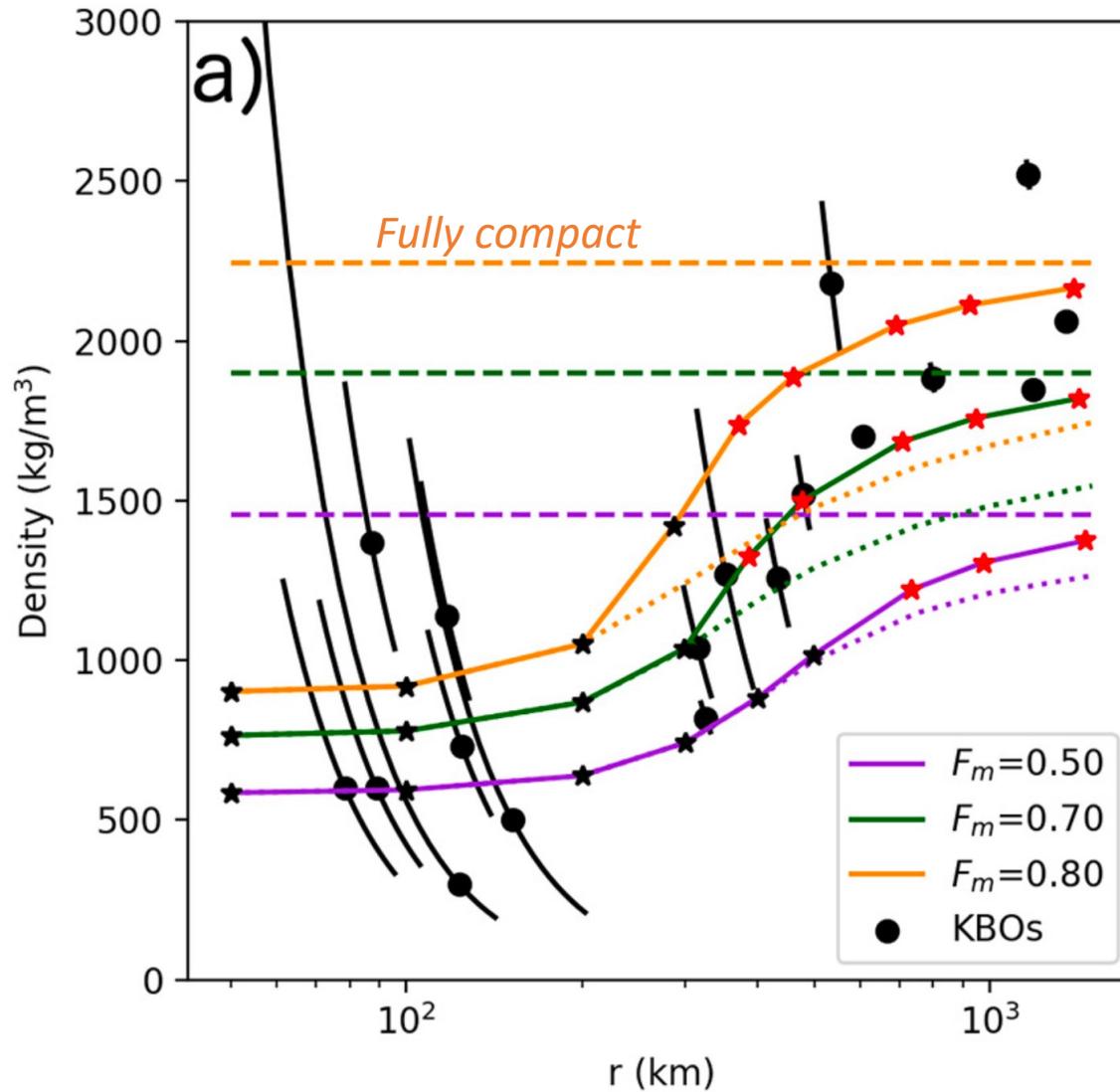
The two bodies slowly spiral closer until they touch, forming the bi-lobed object we see today.

The density dichotomy of Kuiper Belt objects



Possible Solution?

- Assumptions
 - Constant composition at birth and growth
 - Porosity removal by gravitational compaction

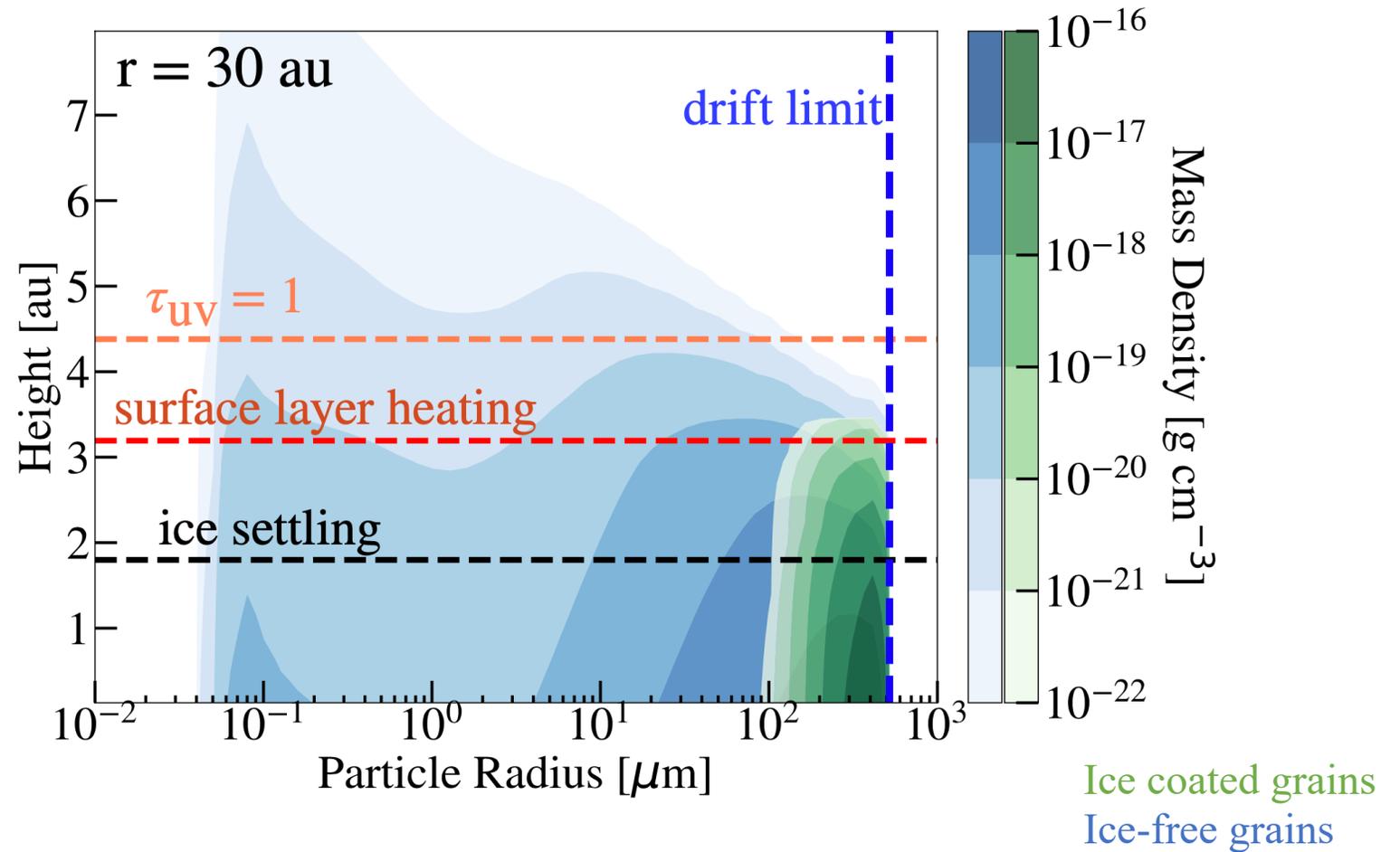


- Problems
 - Low-mass objects need to be unreasonably porous
 - Timing! ^{26}Al would melt if formed within 4 Myr

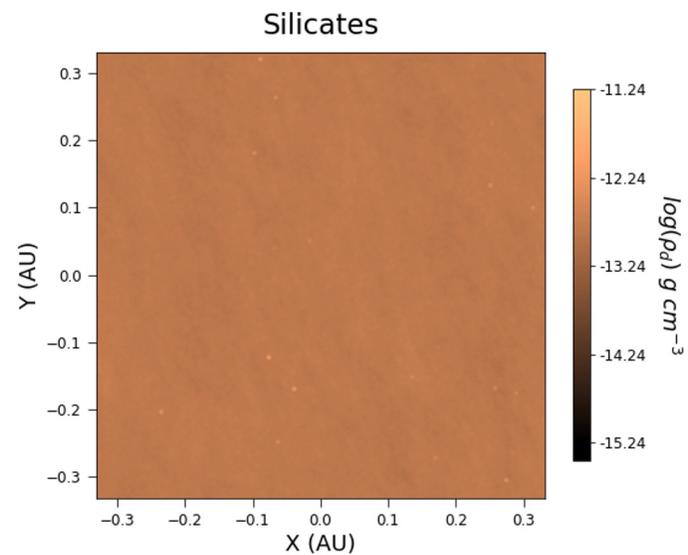
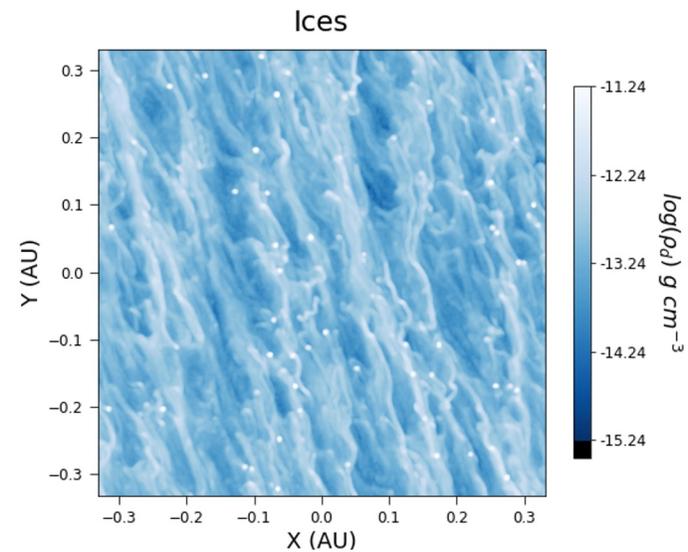
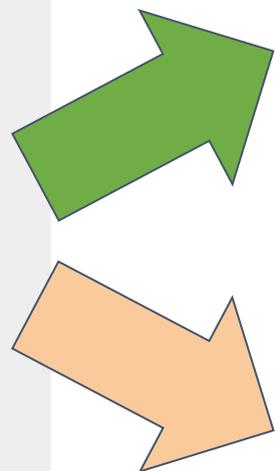
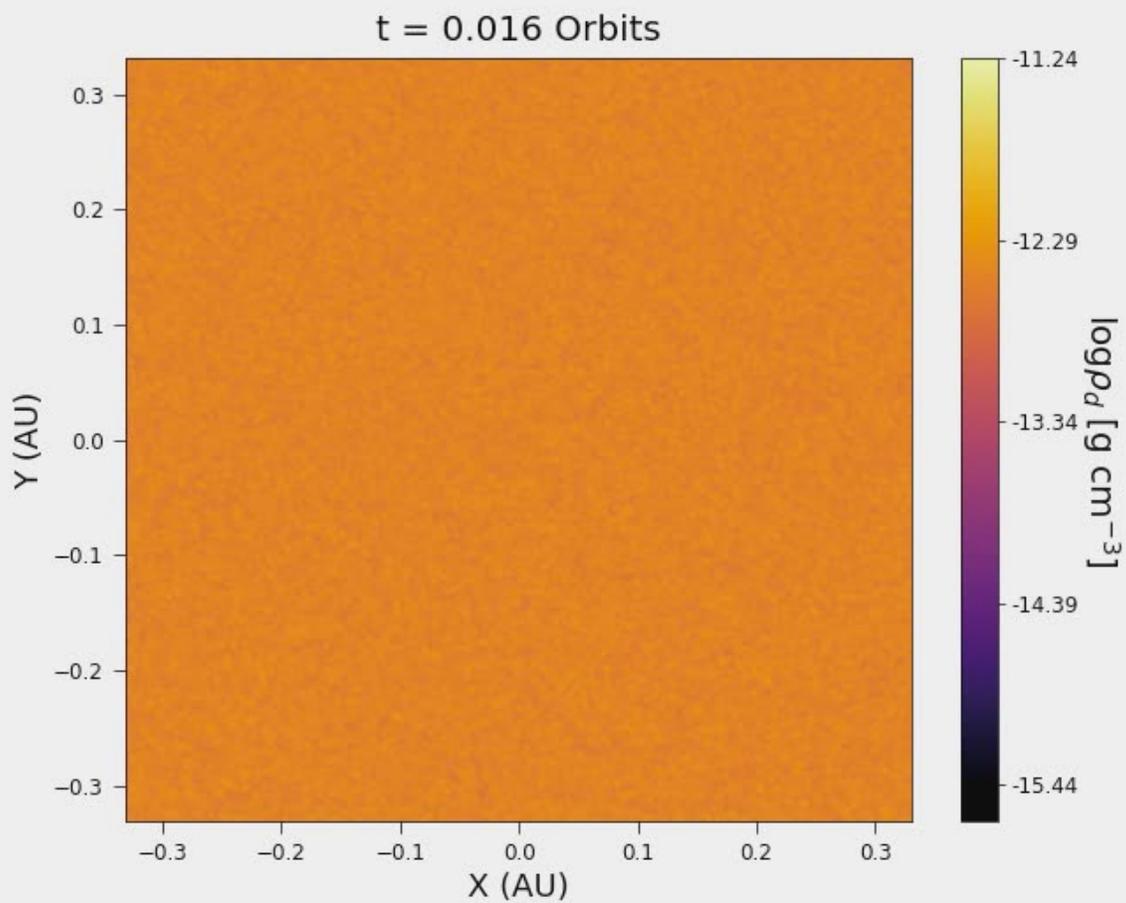
Abandoning Constant Composition

Heating and UV irradiation remove ice on Myr timescales

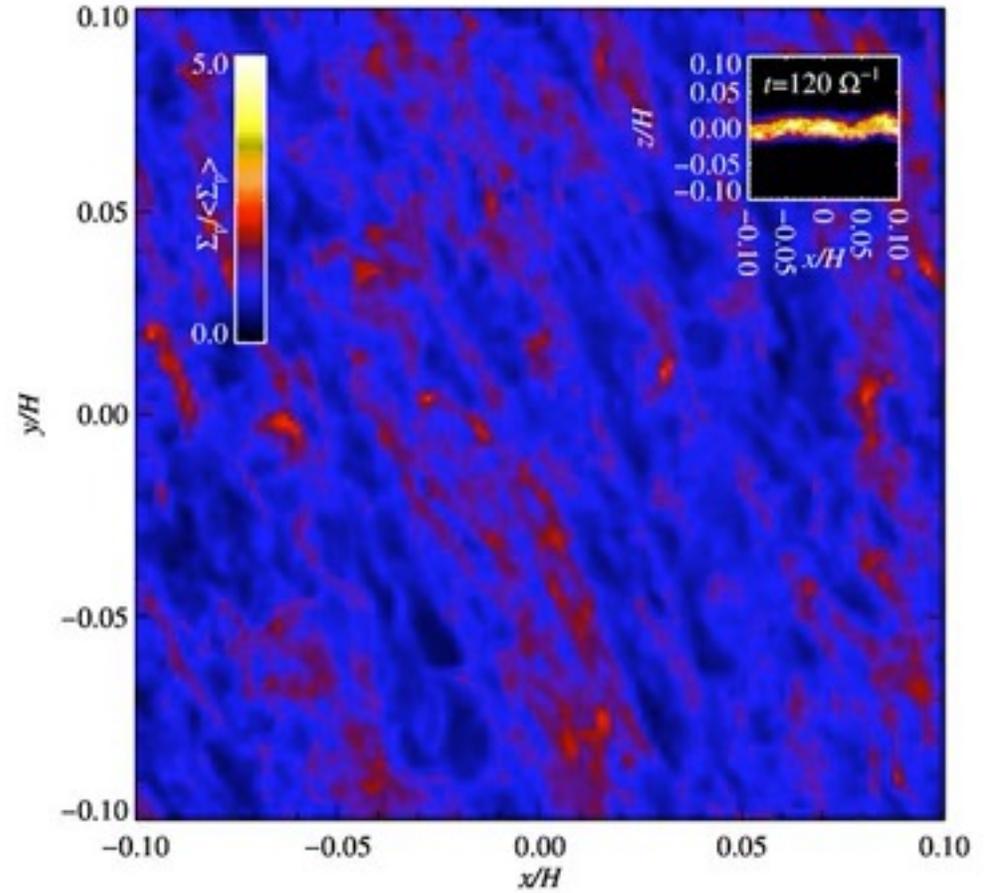
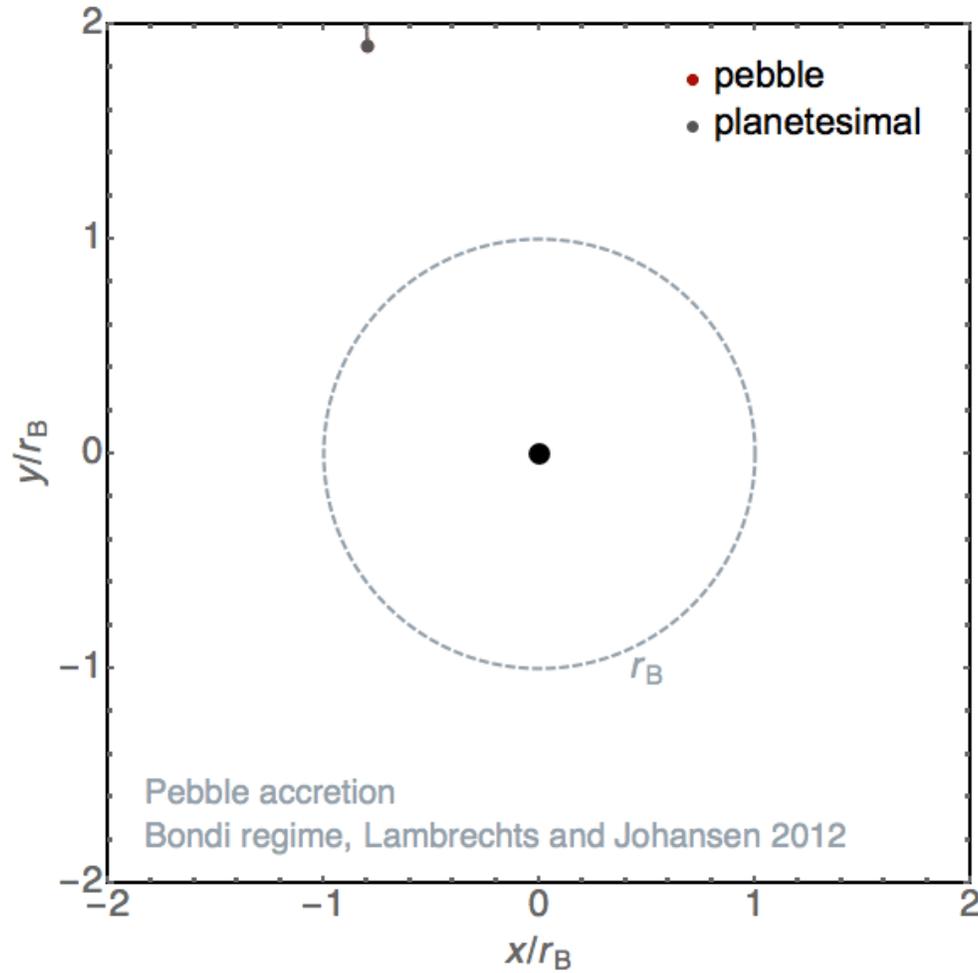
- Small grains lofted in the atmosphere lose ice
- Big grains are shielded and remain icy.



Split into icy and silicate pebbles



Pebble Accretion



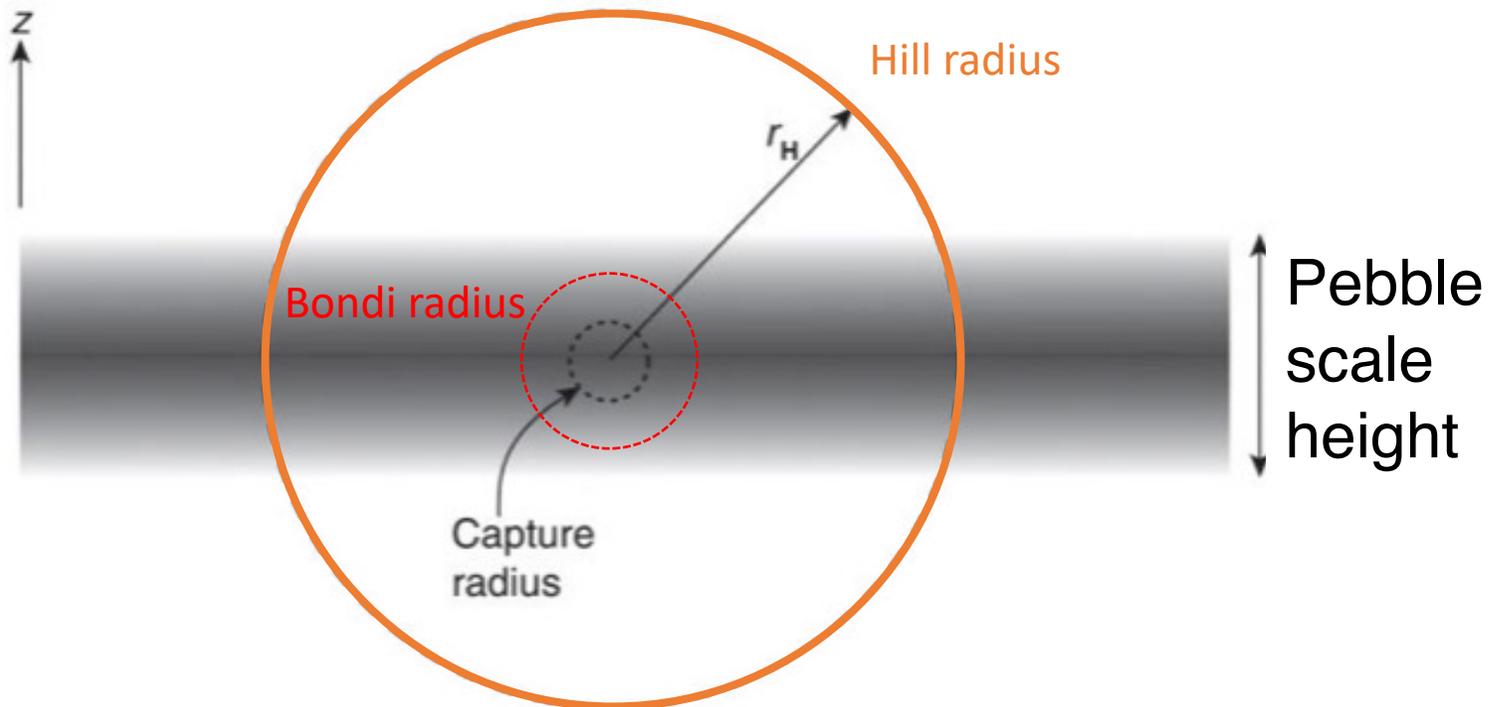
Lyra+ '08, '09, '23, Ormel & Klahr '10, Lambrechts & Johansen '12
See Johansen & Lambrechts '17 for a review

Pebble Accretion: Geometric, Bondi, and Hill regime

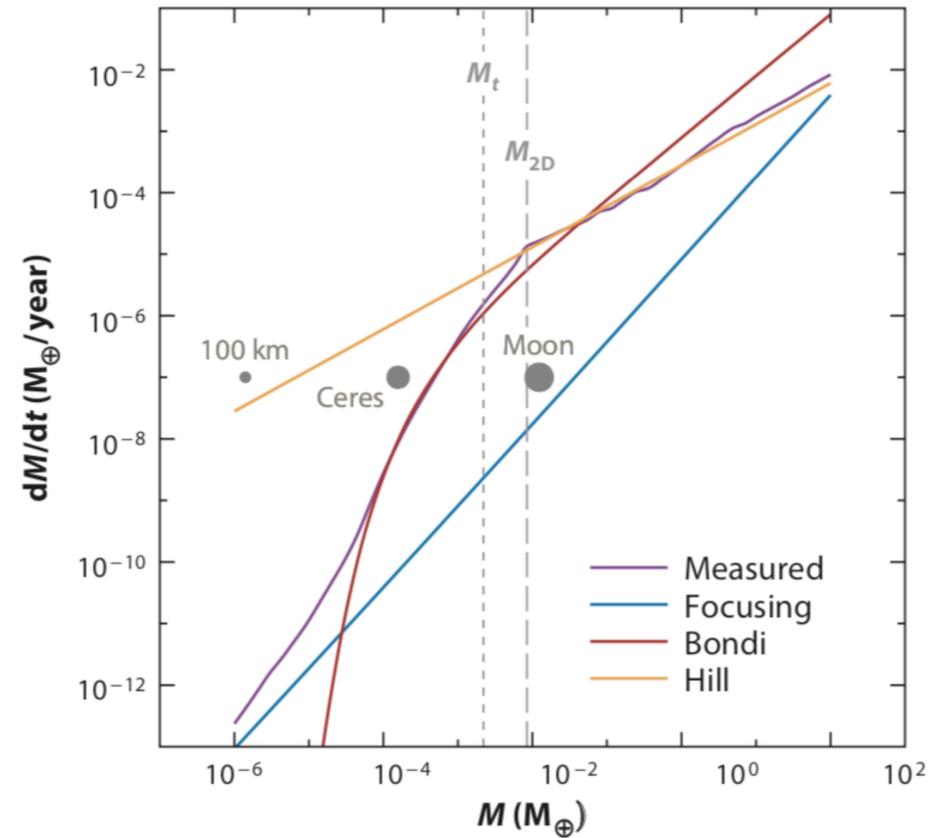
Bondi accretion - Bound against thermal (dynamic) **kinetic energy**

Hill accretion - Bound against **stellar tide**

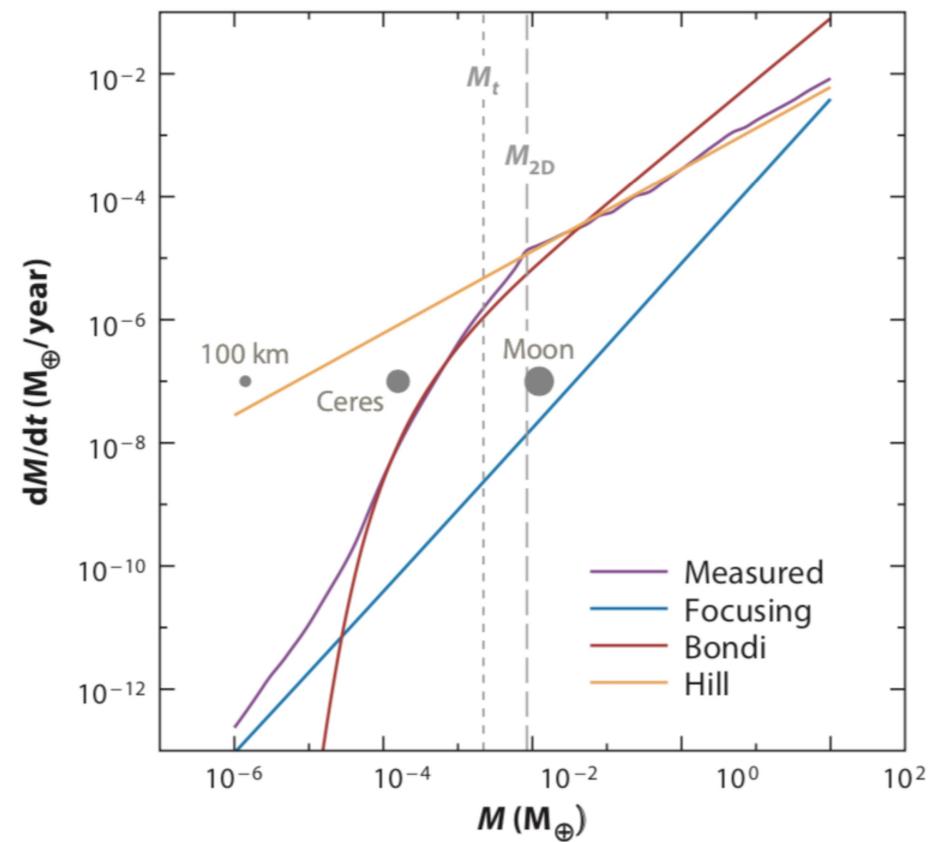
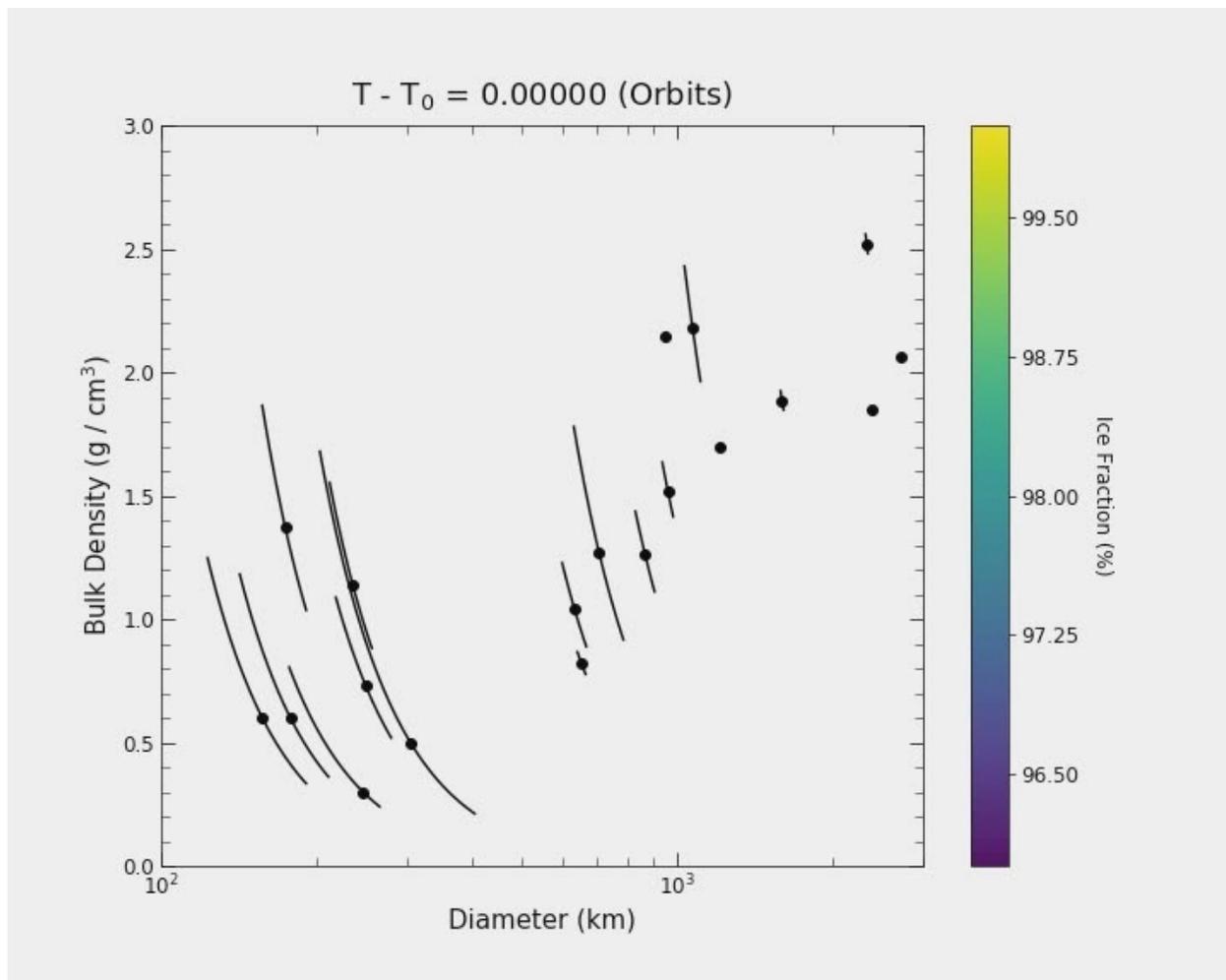
$$\xi \equiv \left(\frac{R_{\text{acc}}}{2H_d}\right)^2 \quad \begin{aligned} \dot{M}_{3D} &= \lim_{\xi \rightarrow 0} \dot{M} = \pi R_{\text{acc}}^2 \rho_{d0} \delta v, \\ \dot{M}_{2D} &= \lim_{\xi \rightarrow \infty} \dot{M} = 2R_{\text{acc}} \Sigma_d \delta v, \end{aligned}$$



Mass Accretion rates

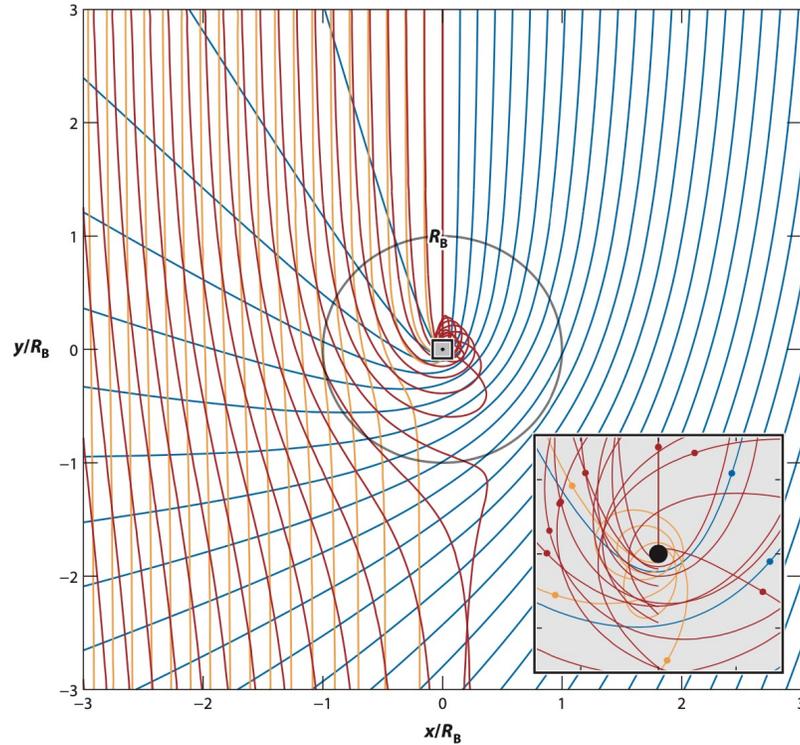


Integrate pebble accretion



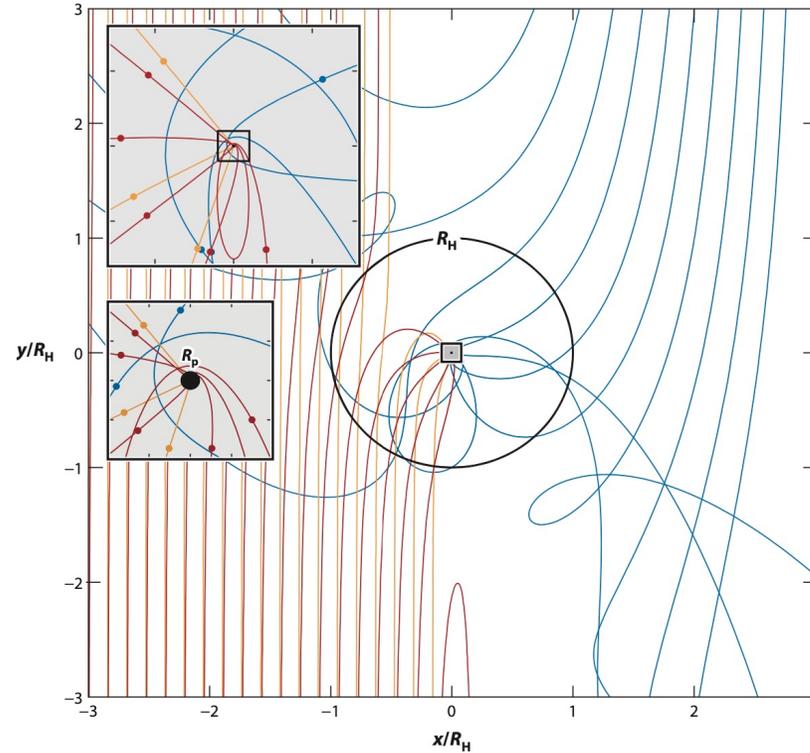
Pebble Accretion: Pebbles of different size accrete differently

Bondi Regime



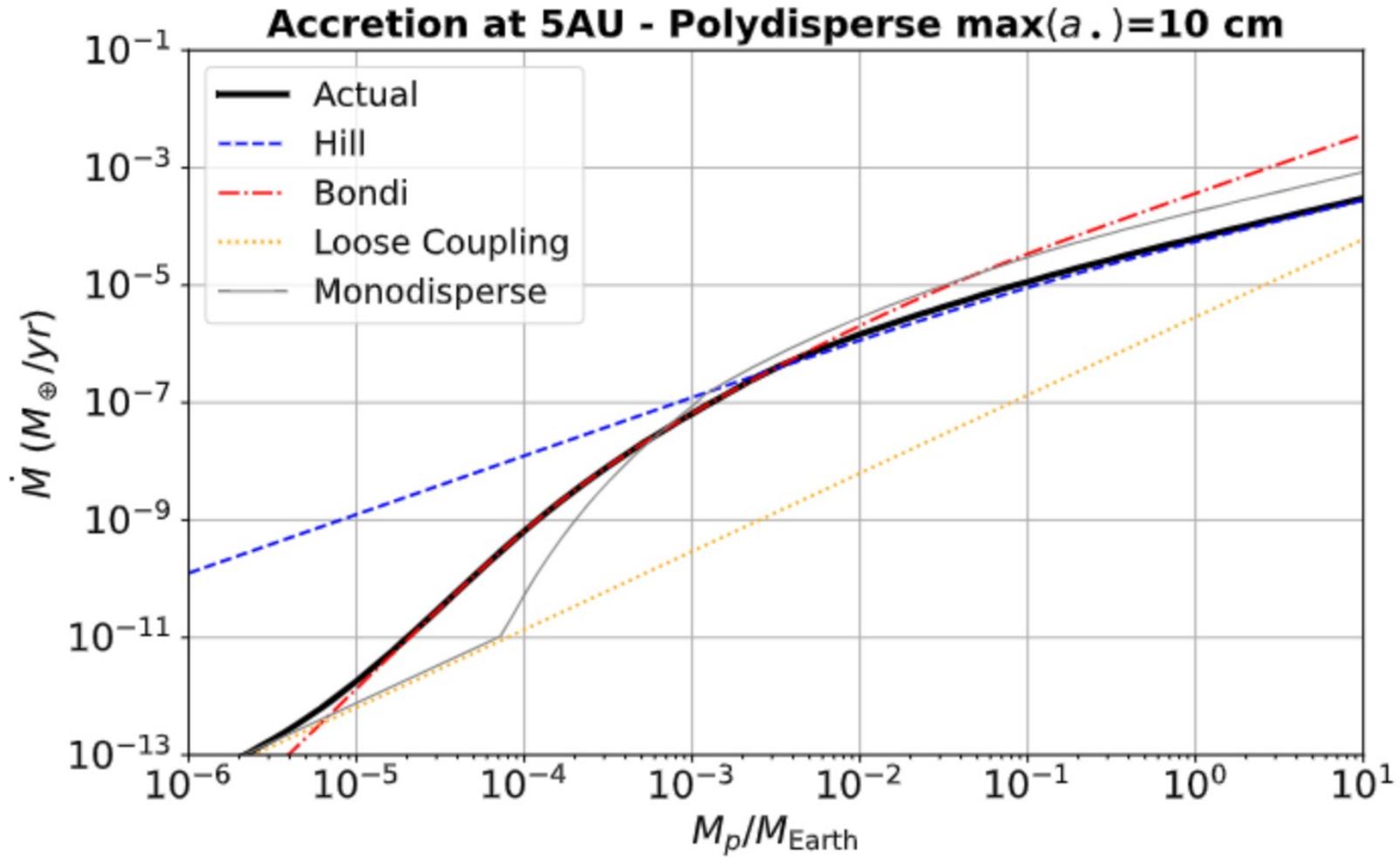
Best accreted
Drag time = Bondi Time

Hill Regime



Best accreted
Drag time \sim Orbital Time

Accretion Rates



Analytical theory of polydisperse (multi-species) pebble accretion

Monodisperse (single species)

$$\dot{M}_{3D} = \lim_{\xi \rightarrow 0} \dot{M} = \pi R_{\text{acc}}^2 \rho_{d0} \delta v,$$

$$\dot{M}_{2D} = \lim_{\xi \rightarrow \infty} \dot{M} = 2R_{\text{acc}} \Sigma_d \delta v,$$

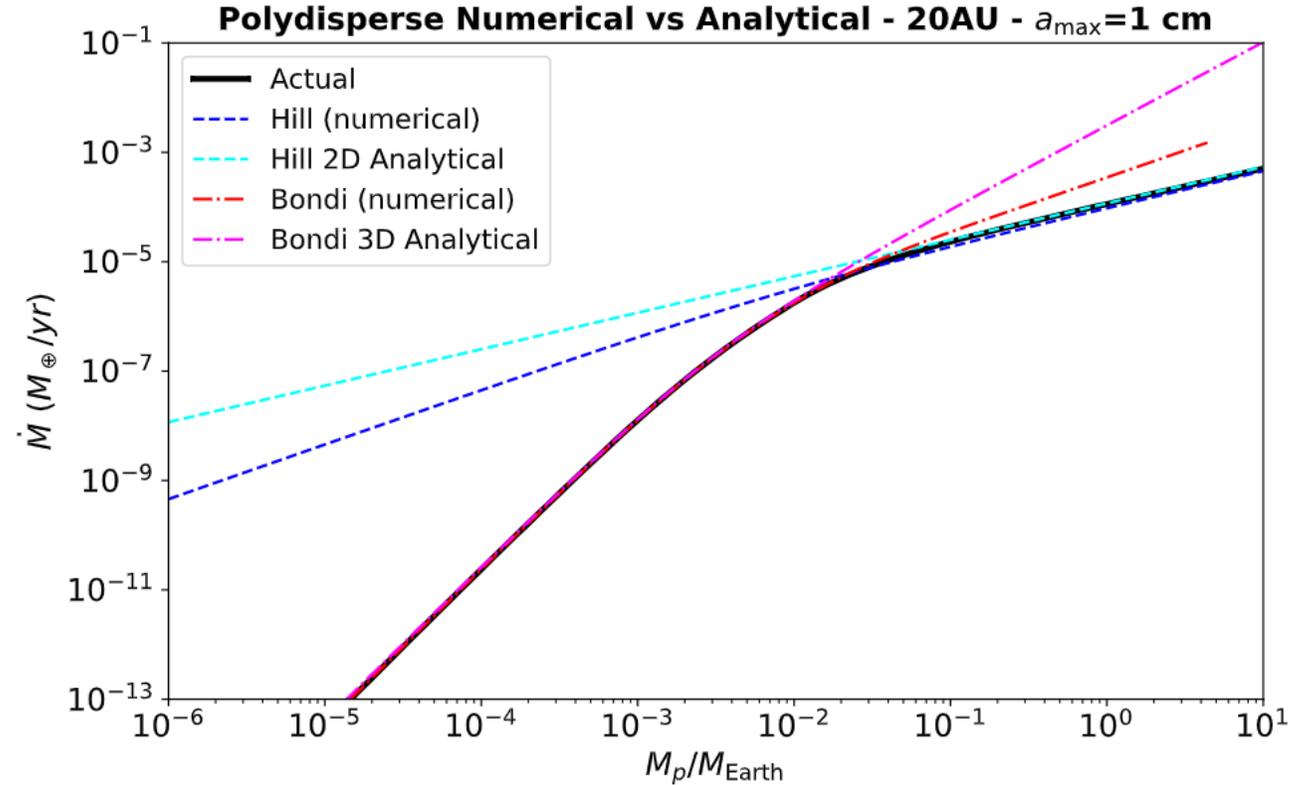
Lambrechts & Johansen (2012)

Polydisperse (multiple species)

$$\dot{M}_{2D,\text{Hill}} = \frac{6(1-p)}{14-5q-3k} \left(\frac{\text{St}_{\text{max}}}{0.1} \right)^{2/3} \Omega R_H^2 Z \Sigma_g.$$

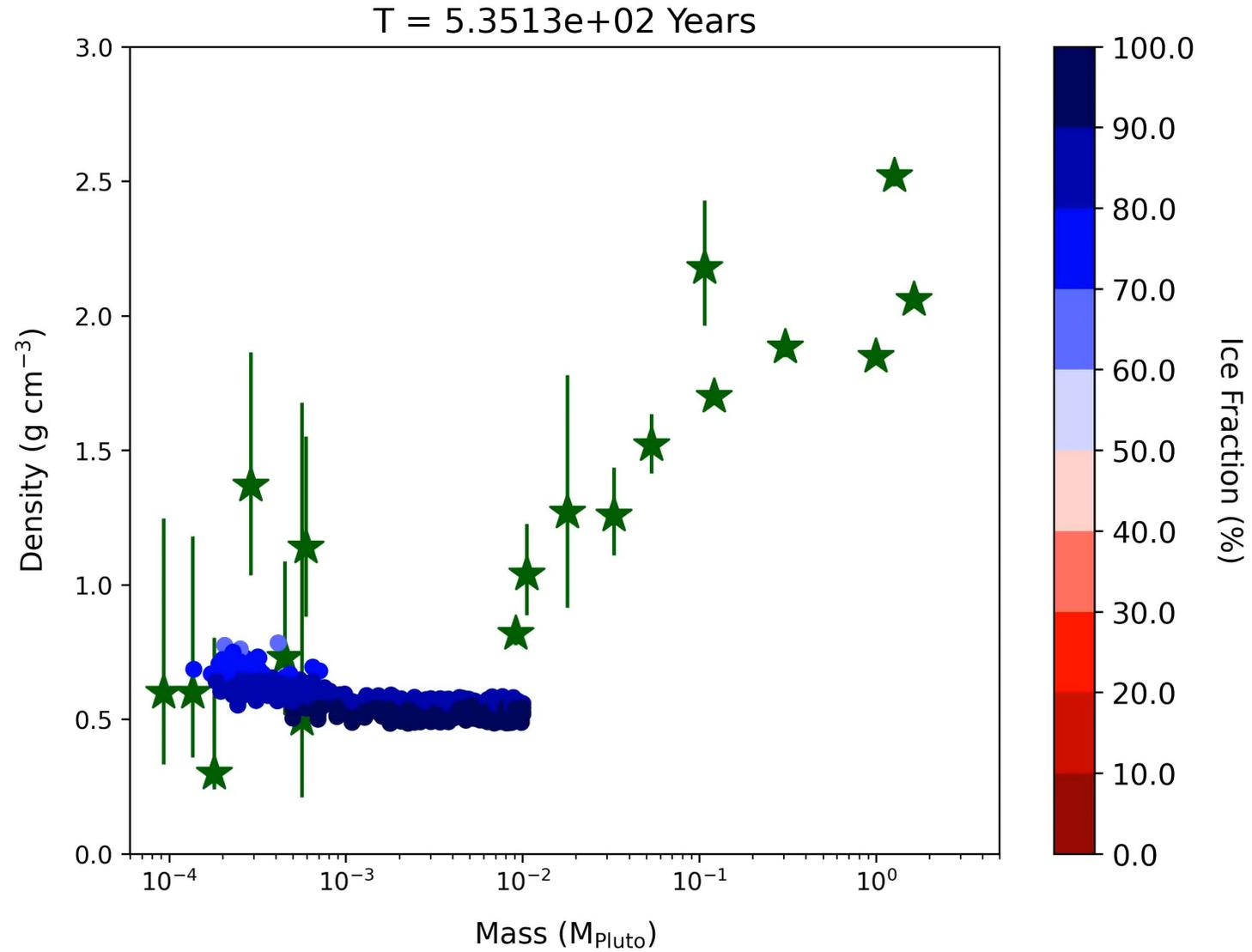
$$\dot{M}_{3D,\text{Bondi}} \approx C_1 \frac{\gamma_l \left(\frac{b_1+1}{s}, j_1 a_{\text{max}}^s \right)}{s J_1^{(b_1+1)/s}} + C_2 \frac{\gamma_l \left(\frac{b_2+1}{s}, j_2 a_{\text{max}}^s \right)}{s J_2^{(b_2+1)/s}} + C_3 \frac{\gamma_l \left(\frac{b_3+1}{s}, j_3 a_{\text{max}}^s \right)}{s J_3^{(b_3+1)/s}} + C_4 \frac{\gamma_l \left(\frac{b_4+1}{s}, j_4 a_{\text{max}}^s \right)}{s J_4^{(b_4+1)/s}},$$

Lyra et al. (2023)



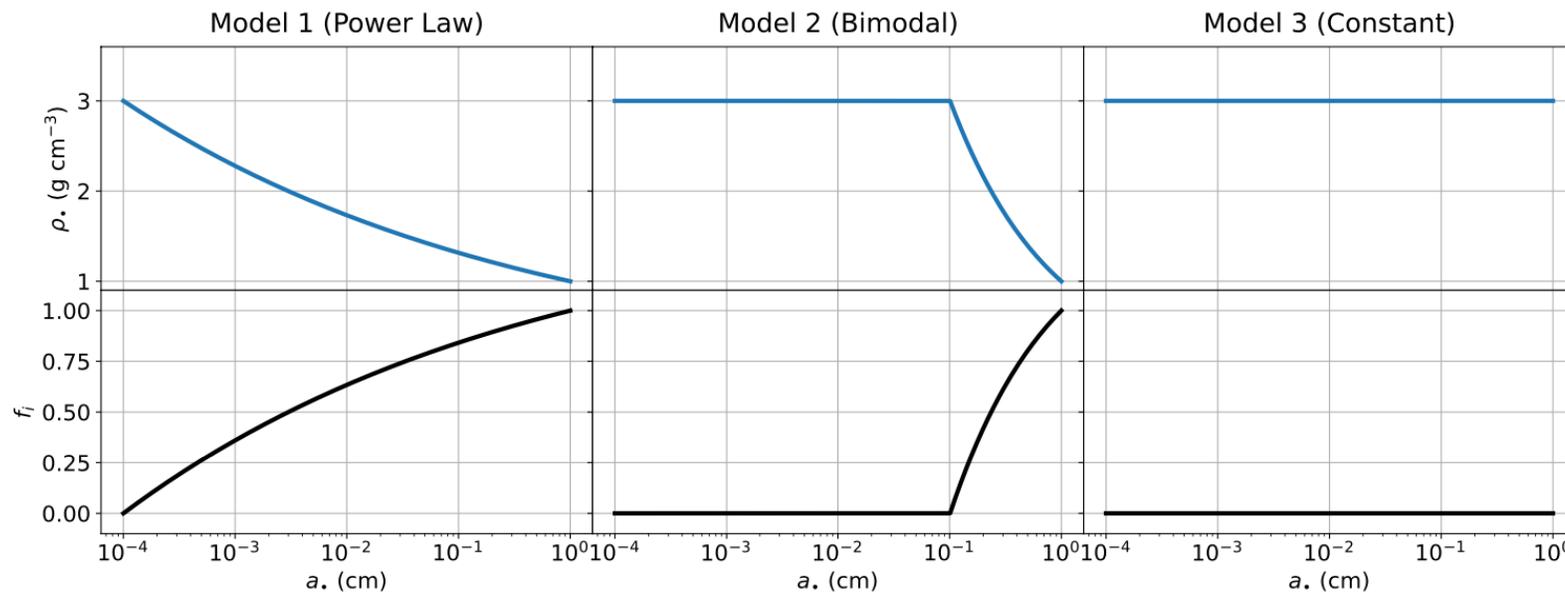
Lyra et al. 2023

Growing Pluto by silicate pebble accretion

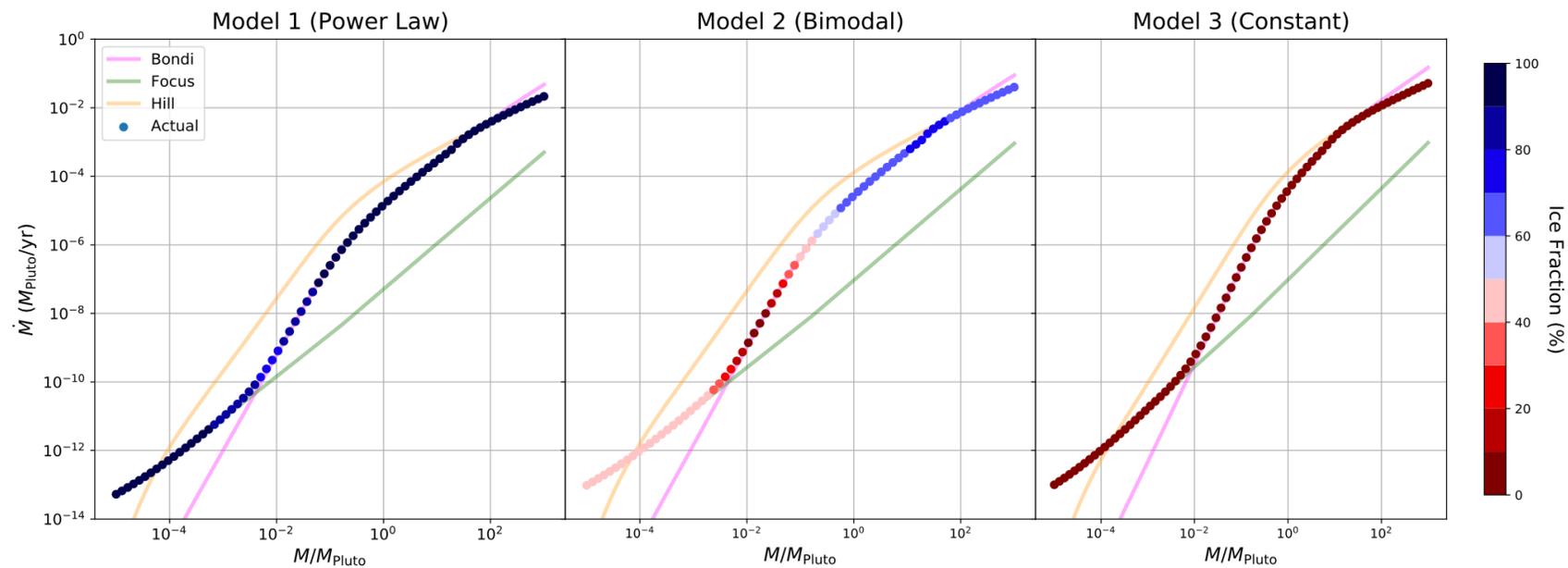


Pebble Density

Ice Fraction

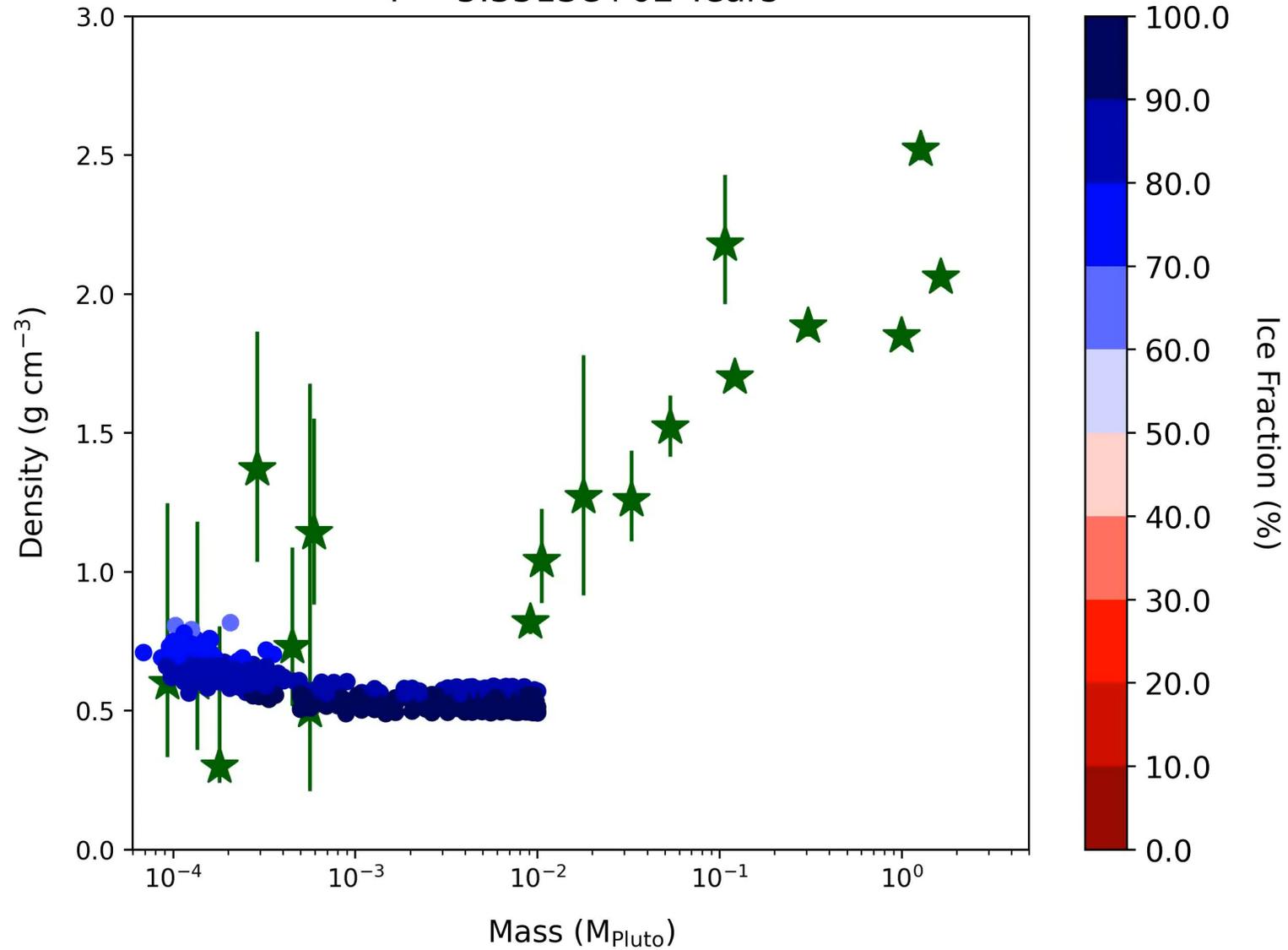


Mass Accretion rate

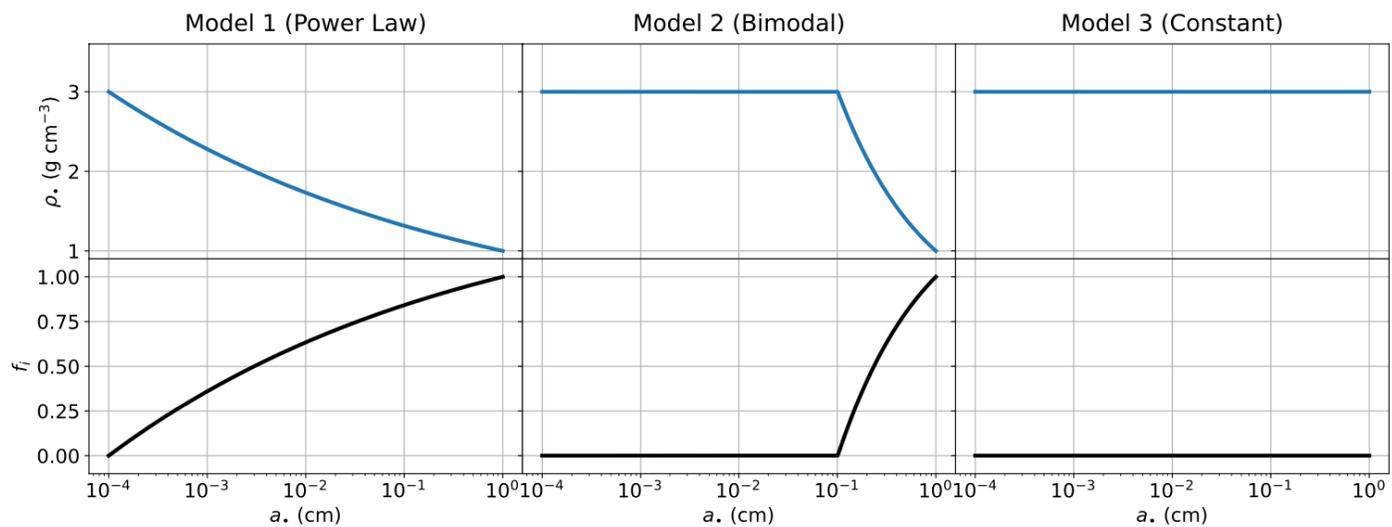


Growing Pluto by silicate pebble accretion

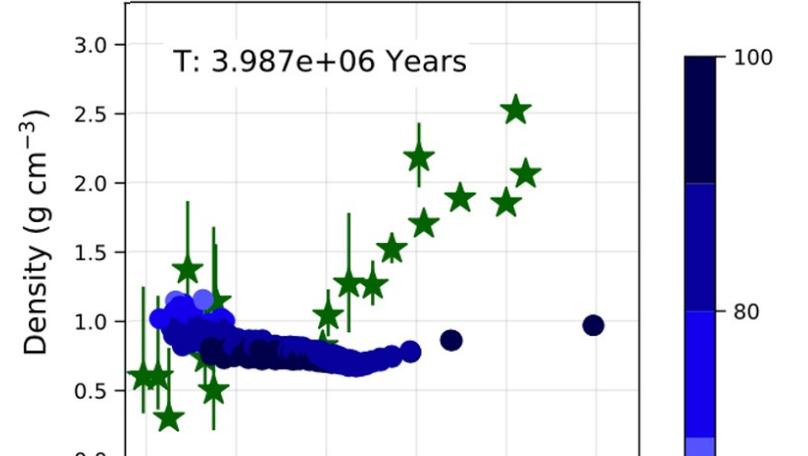
T = 5.3513e+02 Years



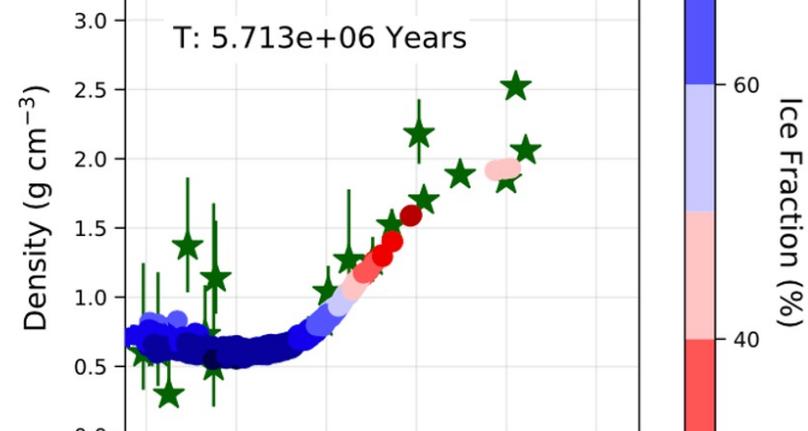
Resulting Densities vs Mass relations



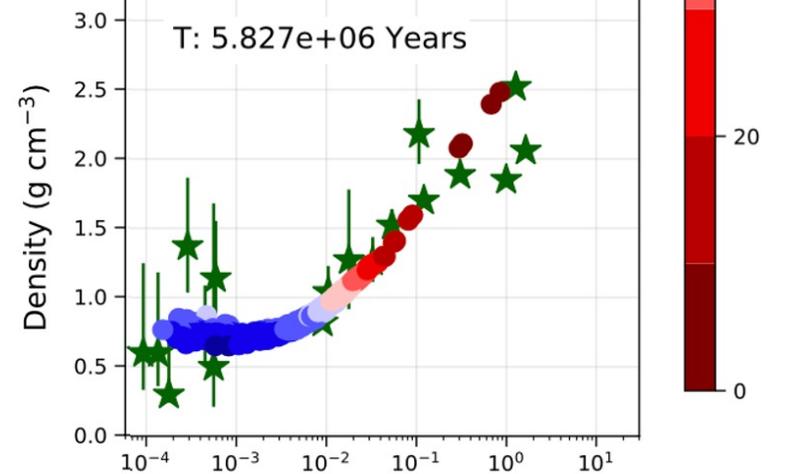
Model 1 (Power Law)



Model 2 (Bimodal)

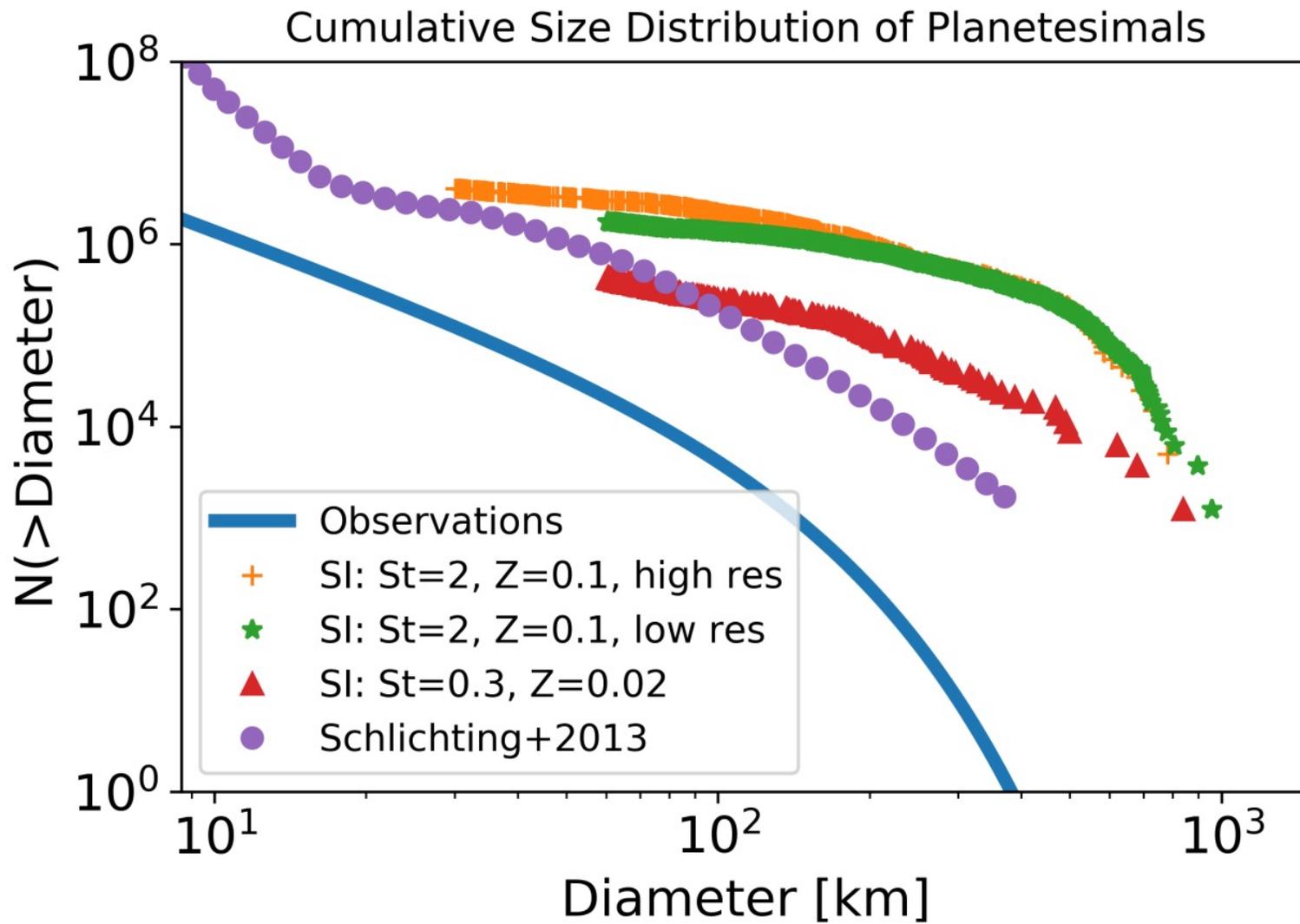


Model 3 (Constant)



- Polydisperse Bondi accretion 1-2 orders of magnitude more efficient than monodisperse
 - Best accreted pebbles are those of drag time \sim Bondi time, not the largest ones
 - The largest ones dominate the mass budget, but accrete poorly
- Onset of Bondi accretion 1-2 orders of magnitude lower in mass compared to monodisperse
 - Reaches 100-350km objects within Myr timescales
 - Bondi accretion possible on top of Streaming Instability planetary embryos within disk lifetime
- Analytical solution to
 - Polydisperse 2D Hill and 3D Bondi

Problem: wrong number density



Conclusions

- Streaming Instability fits
 - slope of asteroid belt distribution,
 - prograde-retrograde distribution of Kuiper belt objects
 - Low density of small classical Kuiper belt objects
- Pebble accretion is a very efficient planetary growth mechanism
 - Polydisperse Bondi accretion 1-2 orders of magnitude more efficient than monodisperse
 - Silicate pebble accretion explains densities of high-mass Kuiper belt objects