

Formation and Retention of Planets in Disks

Wladimir (Wlad) Lyra

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American Museum of Natural History

Max-Planck Institute for Astronomy

University of Uppsala

NASA-IPAC, April 2012

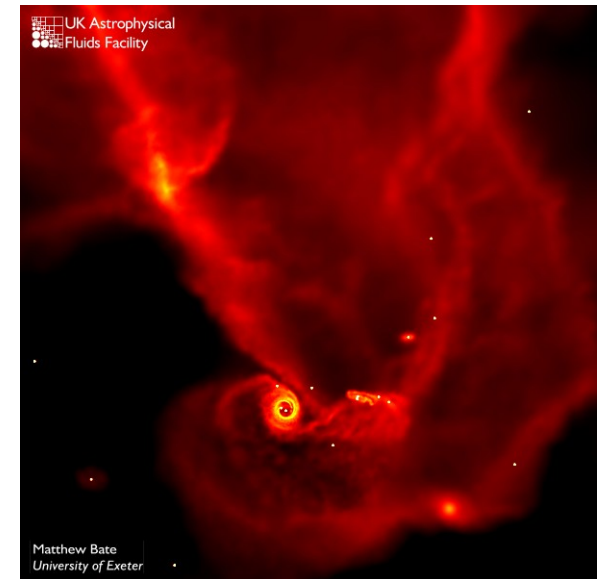
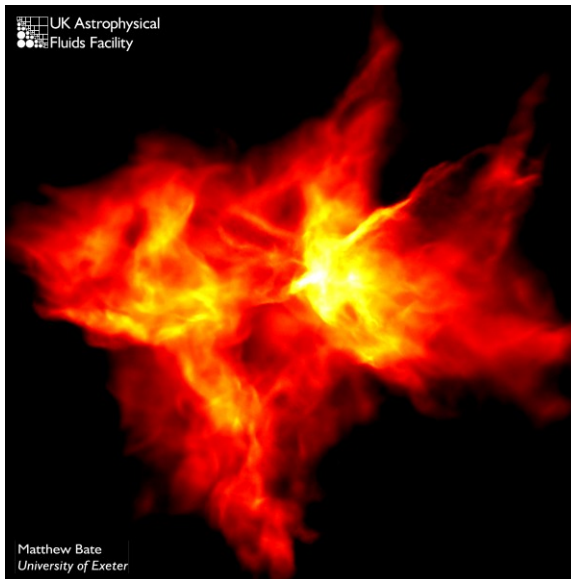
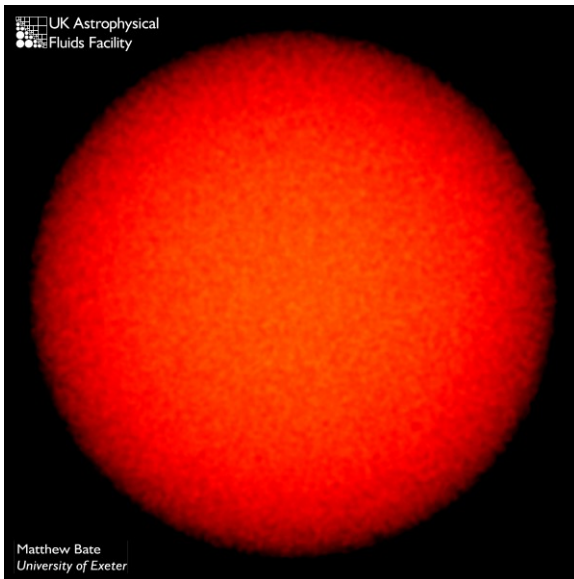
Collaborators:

Axel Brandenburg (Stockholm), Kees Dullemond (Heidelberg), Anders Johansen (Lund),
Brandon Horn (Columbia), Hubert Klahr (Heidelberg), Mordecai-Mark Mac Low (AMNH),
Sijme-Jan Paardekooper (Cambridge), Nikolai Piskunov (Uppsala), Natalie Raettig
(Heidelberg), Zsolt Sandor (Innsbruck), Neal Turner (JPL), Andras Zsom (Heidelberg).

Star Formation - Bate, Bonnell & Bromm (2003)



Star Formation - Bate, Bonnell & Bromm (2003)



time

Some stars are seen to be born with lots of **surrounding gas**.

This gas is bound to the star and referred to as

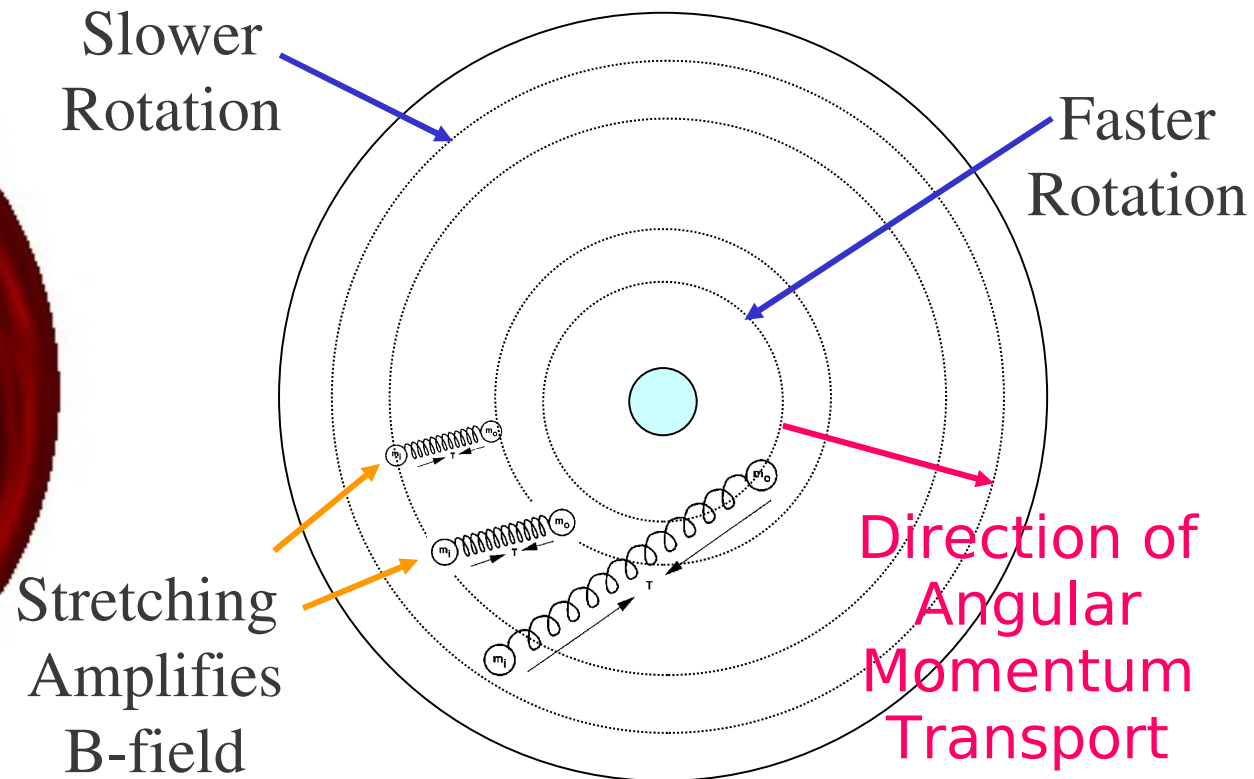
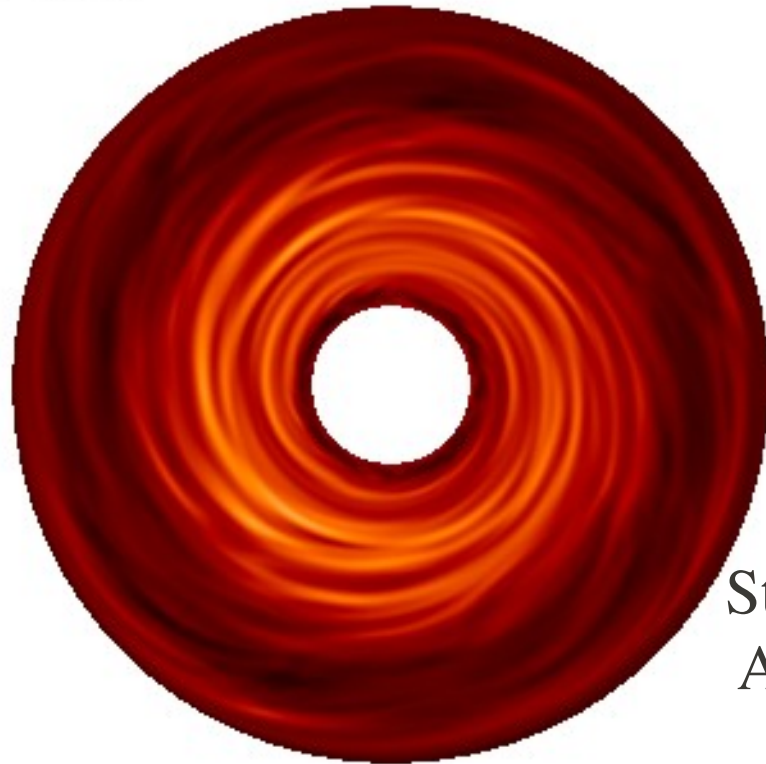
circumstellar disk or *protoplanetary disk*.

Accretion in disks occurs via turbulent viscosity

Turbulence in disks is enabled by the **Magneto-Rotational Instability**

MRI sketch

$t=46.3/88\text{yr}$



Unstable if angular velocity decreases outward

Accretion in disks occurs via turbulent viscosity

Turbulence in disks is enabled by
the **Magneto-Rotational Instability**

MRI sketch



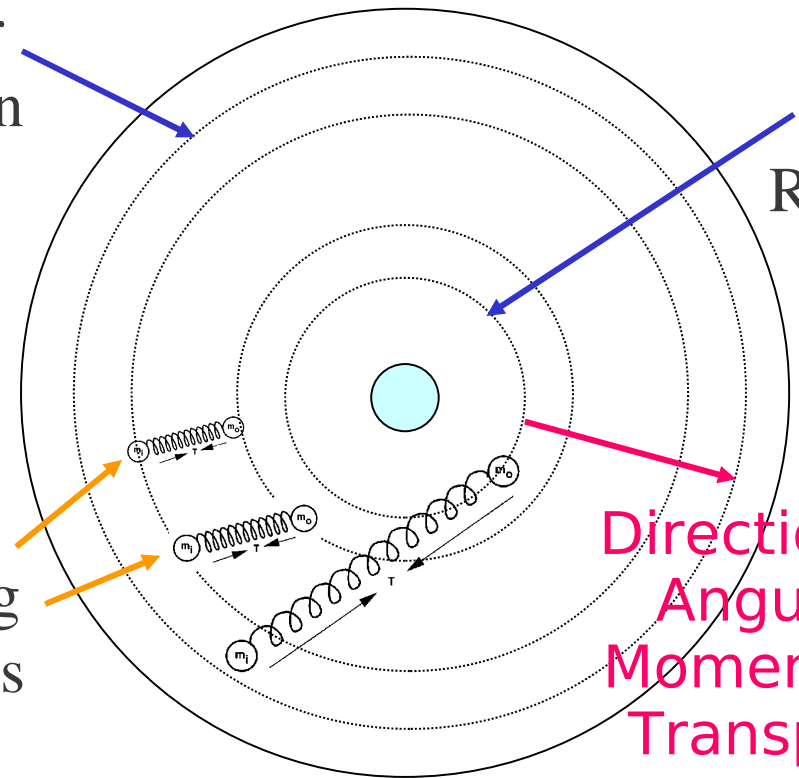
Slower
Rotation

Faster
Rotation

etching
mplifies
-field

Direction of
Angular
Momentum
Transport

Unstable if angular
velocity decreases
outward



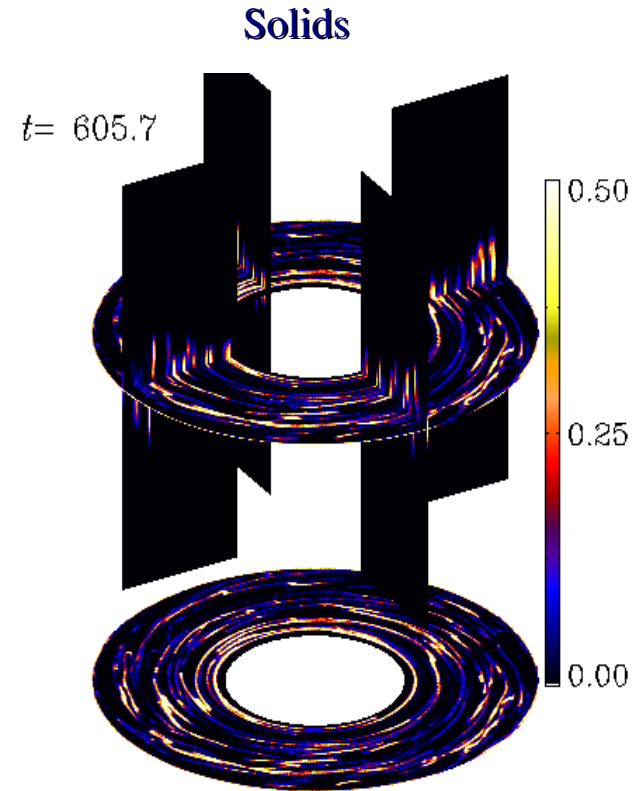
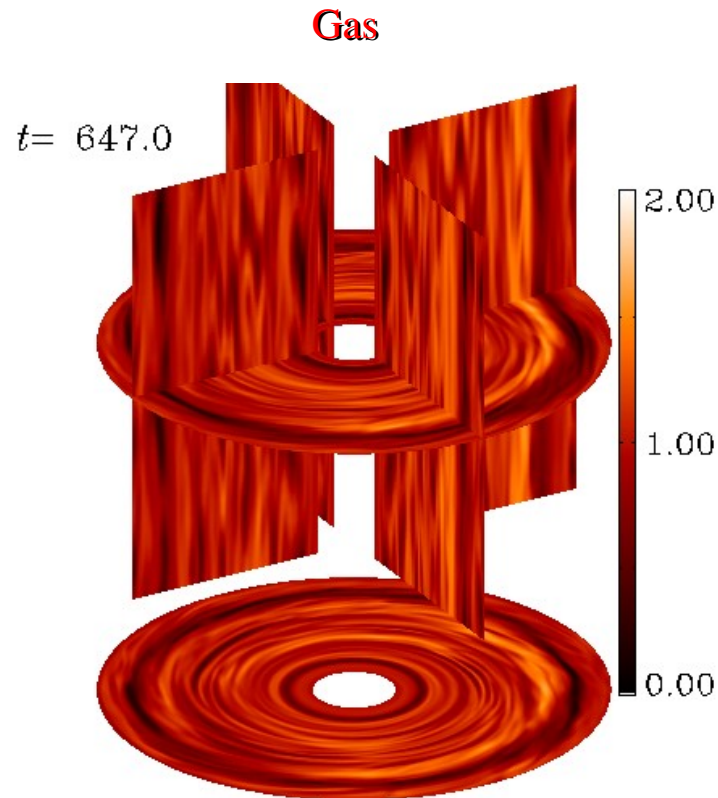
Turbulence concentrates solids mechanically in pressure maxima

Gas $\frac{D u}{D t} = -\nabla \Phi - \rho^{-1} \nabla p$

Solids $\frac{d w}{d t} = -\nabla \Phi - \frac{(w - u)}{\tau}$

$$w = u + \tau \rho^{-1} \nabla p$$

The drag force
pushes the solids *towards*
the pressure gradient



Intense Clumping!!

Source: Lyra et al. (2008a)

Solids particles

move toward

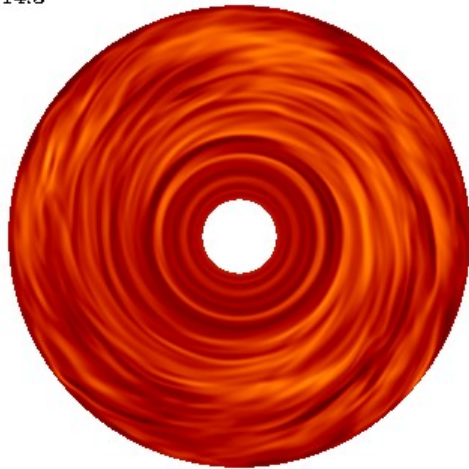
pressure maxima

Turbulence concentrates solids mechanically in pressure maxima

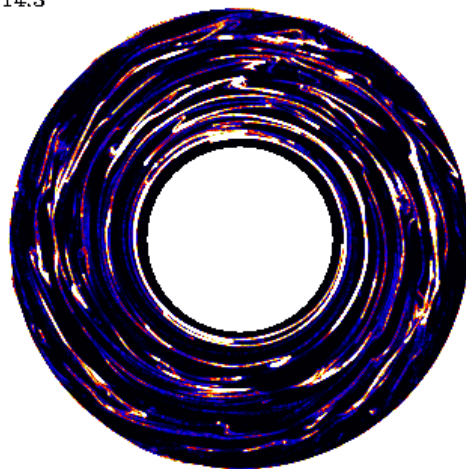


Solids in a turbulent disk

$t=614.3$

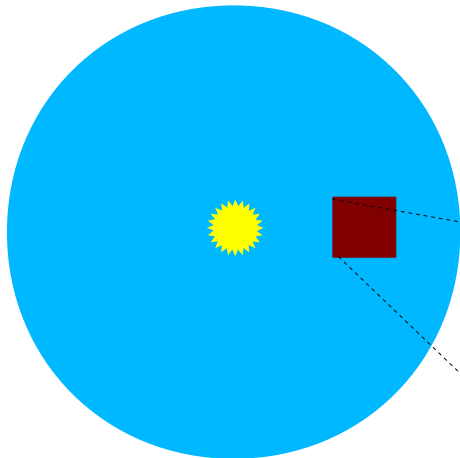


$t=614.3$

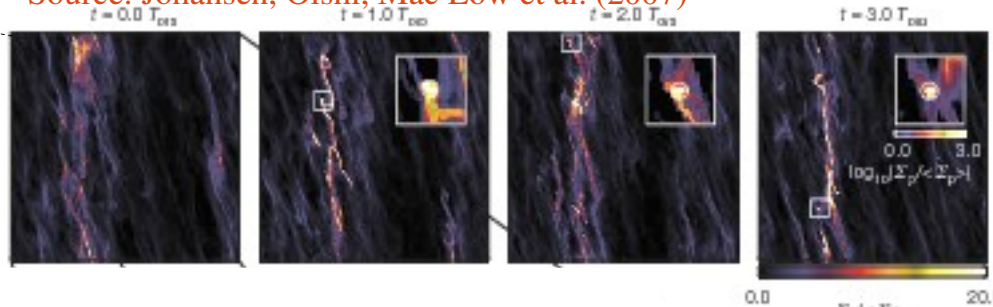


Source: Lyra et al. (2008a)

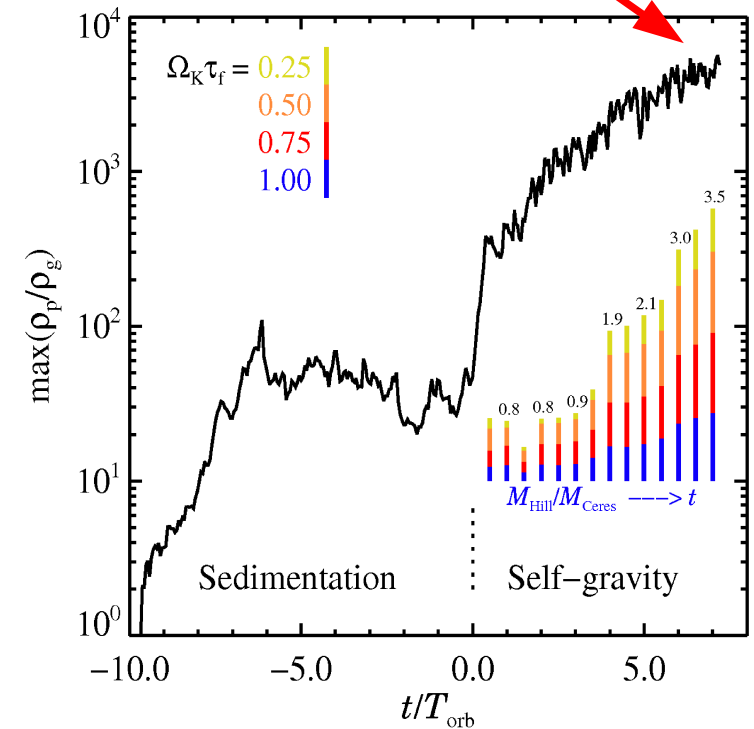
- Turbulent eddies are very efficient particle traps
- Correlation between gas and solids density maxima
- Critical density for gravitational collapse of clumps



Source: Johansen, Oishi, Mac Low et al. (2007)

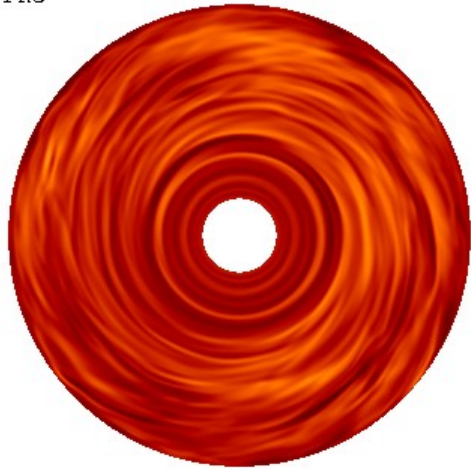


3x Ceres mass!

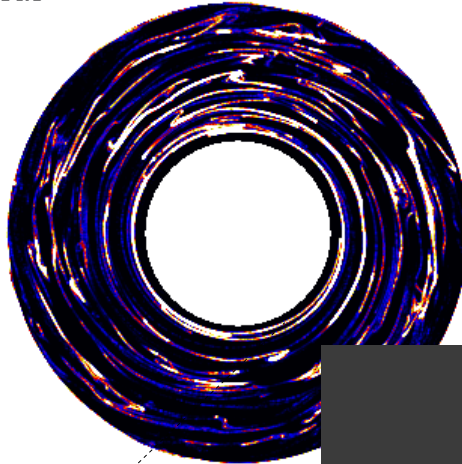


Solids in a turbulent disk

$t=614.3$



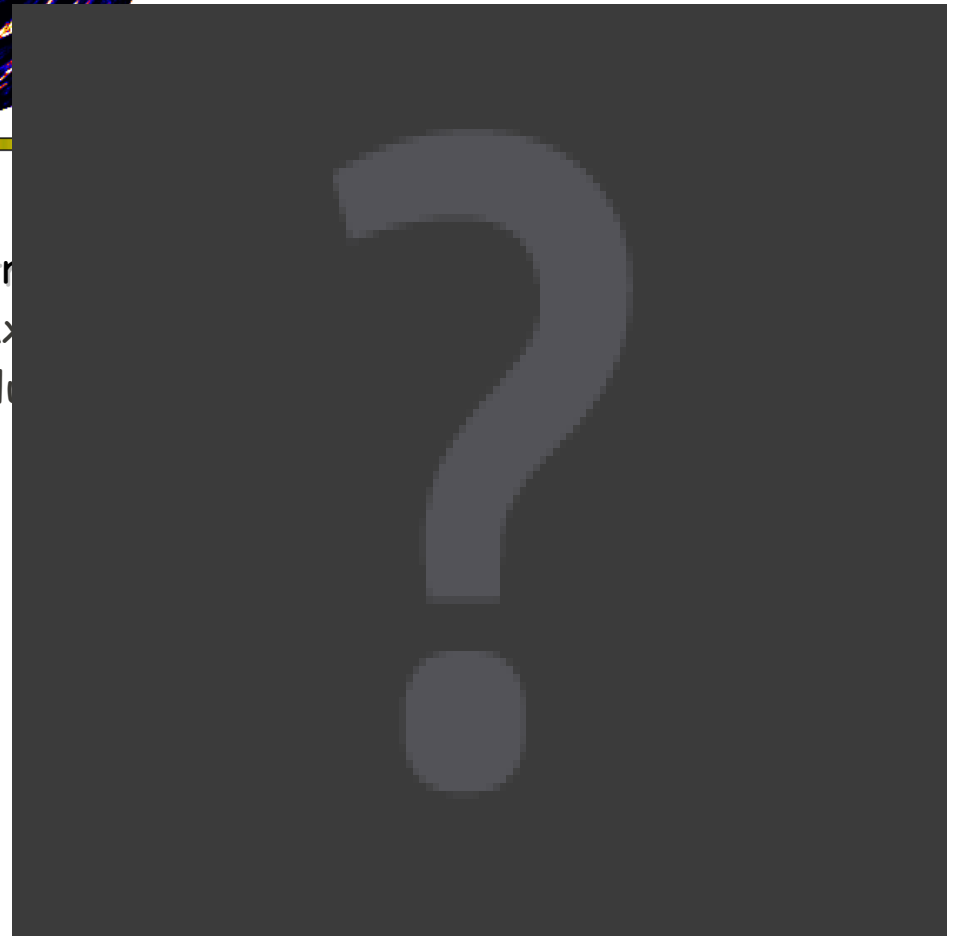
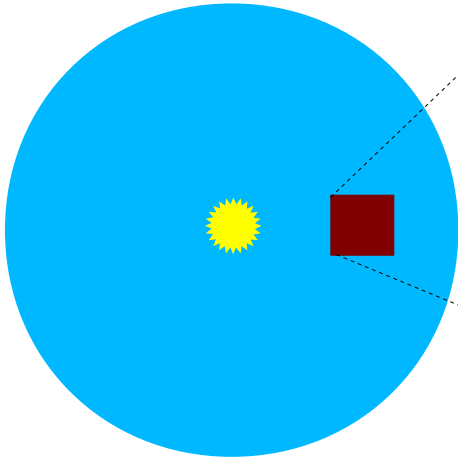
$t=614.3$



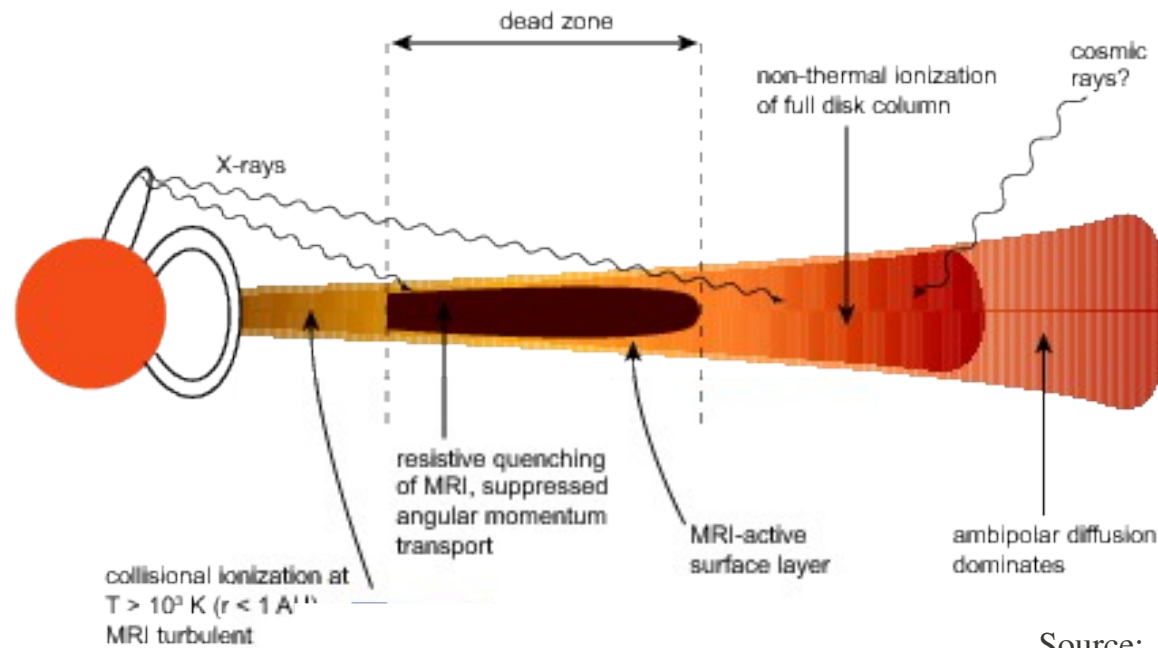
Source: Johansen, Oishi, Mac Low et al. (2007)

Source: Lyra et al. (2008a)

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- Correlation between gas and solids density max
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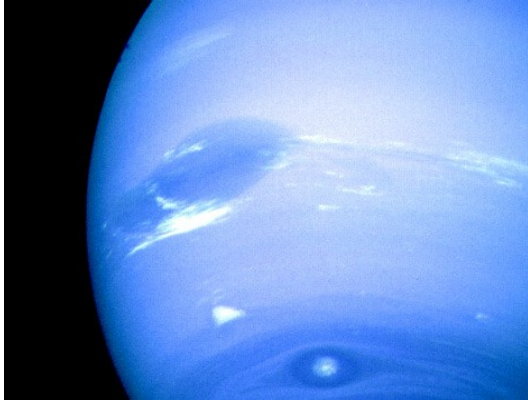
Alas... Dead zones are robust features of accretion disks



Therefore....

The search for **hydrodynamical routes**
for turbulence **continues**.

A possibility: Baroclinic Instability



- Well known in planetary atmospheres

And **vortices** are:

- A solution of the NS equations: **persistent structures**
 - Very interesting for planet formation:

THE ASTROPHYSICAL JOURNAL, 582:869–892, 2003 January 10
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TURBULENCE IN ACCRETION DISKS: VORTICITY GENERATION AND ANGULAR MOMENTUM
TRANSPORT VIA THE GLOBAL BAROCLINIC INSTABILITY

H. H. KLAHR¹ AND P. BODENHEIMER
UCO/Lick Observatory, University of California, S
Received 2000 June 7; accepted 2002 Sep

Klahr & Bodenheimer (2003)

THE ASTROPHYSICAL JOURNAL, 606:1070–1082, 2004 May 10
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THE GLOBAL BAROCLINIC INSTABILITY IN ACCRETION DISKS. II.
LOCAL LINEAR ANALYSIS

Klahr (2004)

THE ASTROPHYSICAL JOURNAL, 658:1236–1251, 2007 April 1
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Petersen et al. (2007a)

BAROCLINIC VORTICITY PRODUCTION IN PROTOPLANETARY DISKS. I. VORTEX FORMATION

THE ASTROPHYSICAL JOURNAL, 658:1252–1263, 2007 April 1
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BAROCLINIC VORTICITY PRODUCTION IN PROTOPLANETARY DISKS. II.
VORTEX GROWTH AND LONGEVITY

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Petersen et al. (2007b)

The subcritical baroclinic instability in local accretion disc models

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Received date / Accepted 13 January 2010

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Lesur & Papaloizou (2010)

A&A 527, A138 (2011)
DOI: 10.1051/0004-6361/201015568
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**Astronomy
&
Astrophysics**

Lyra & Klahr (2011)

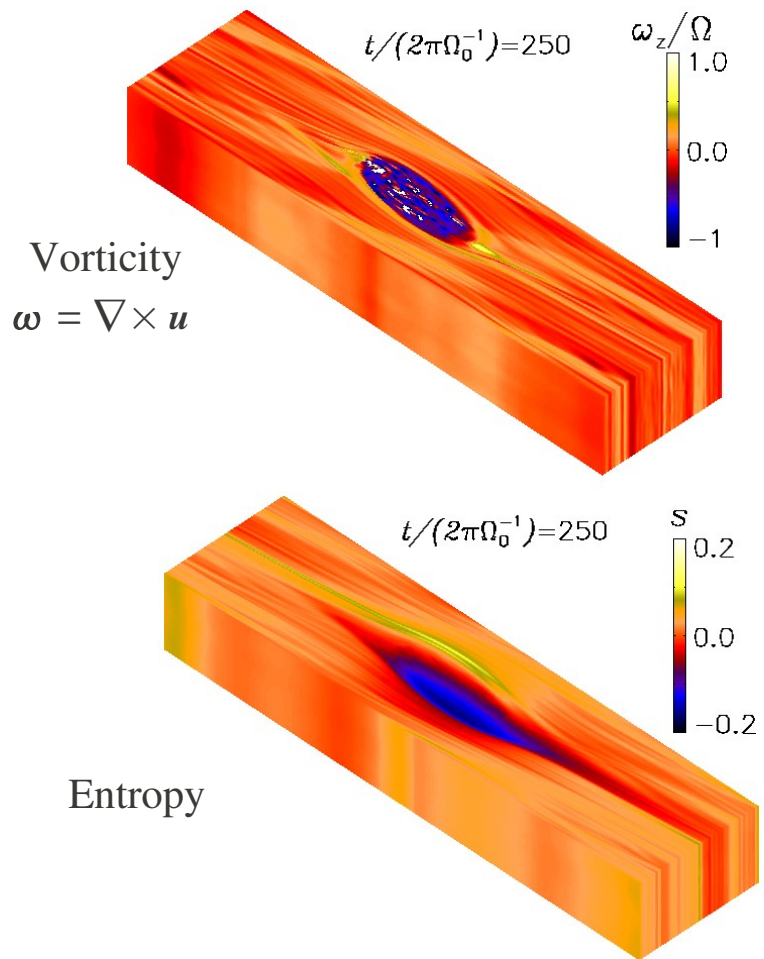
The baroclinic instability in the context of layered accretion
Self-sustained vortices and their magnetic stability in local compressible
unstratified models of protoplanetary disks

W. Lyra^{1,2} and H. Klahr¹

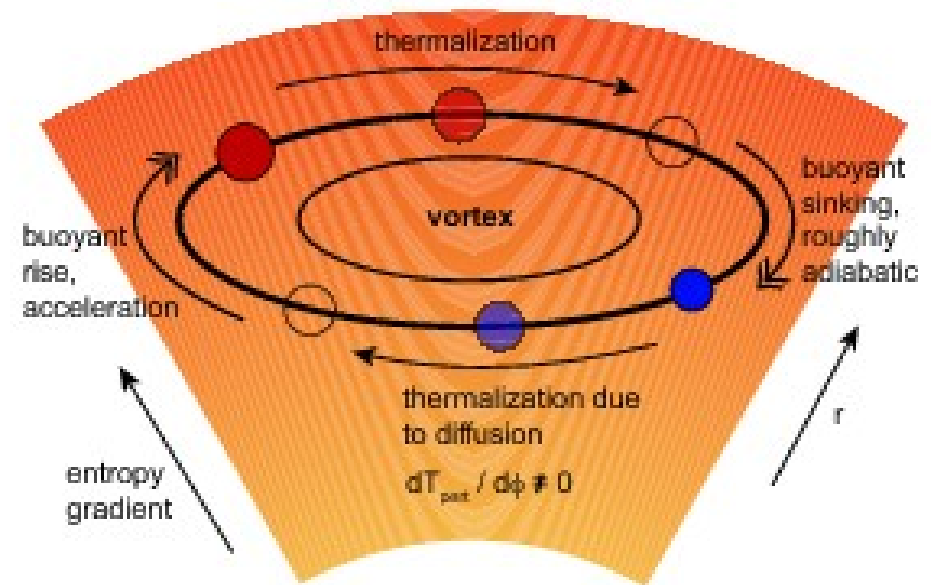
Baroclinic Instability - Excitation and self-sustenance of vortices



Baroclinic Instability - Excitation and self-sustenance of vortices



Sketch of the Baroclinic Instability

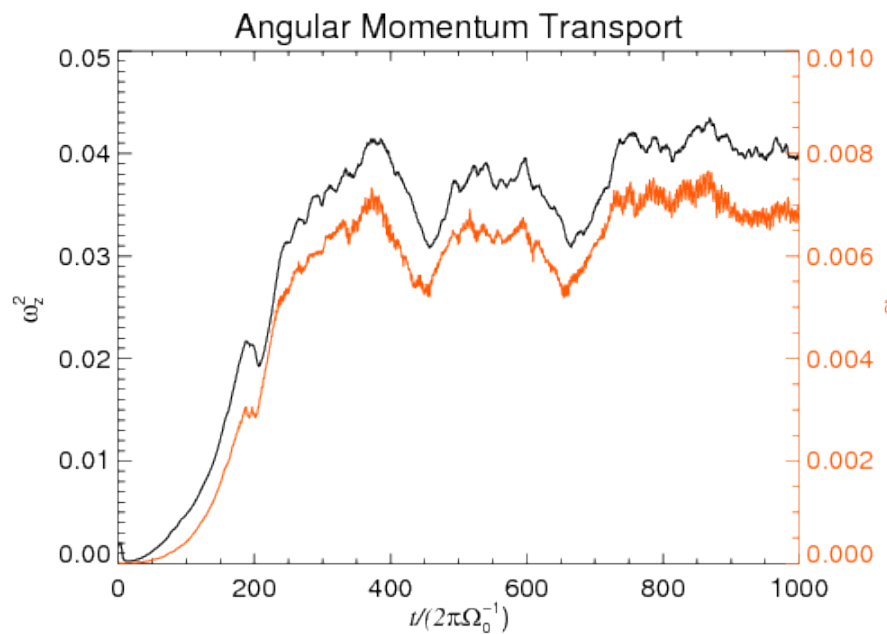


Source: Armitage (2010)

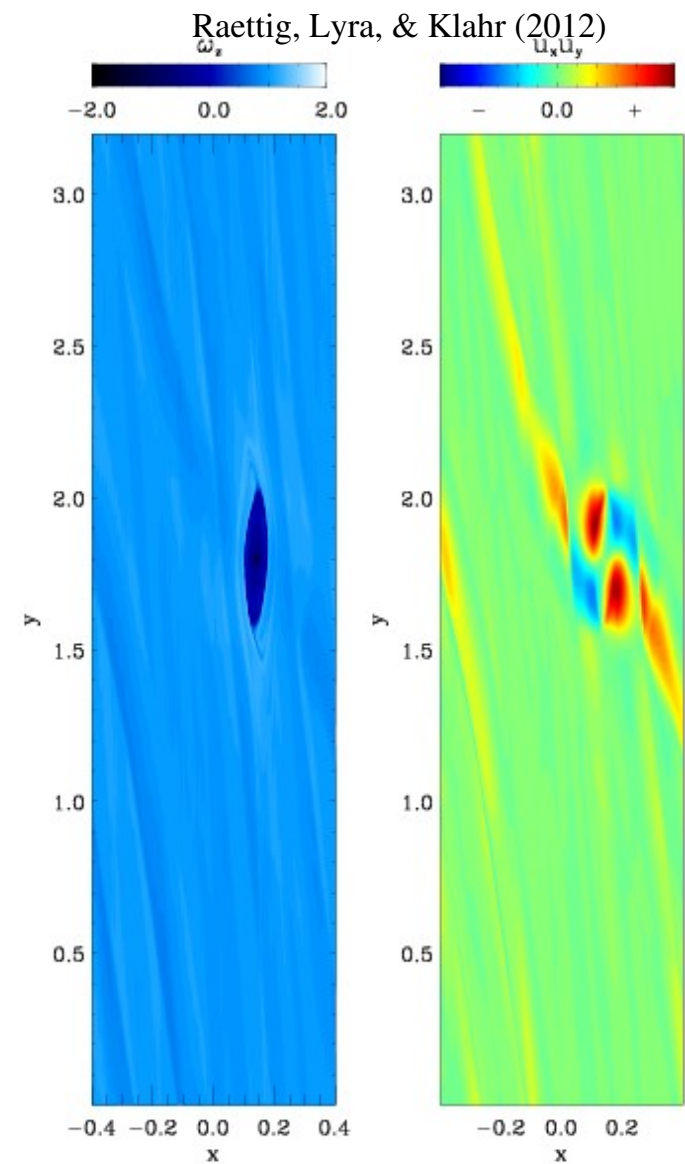
$$\frac{\partial \omega}{\partial t} = \underbrace{-(u \cdot \nabla) \omega}_{\text{advection}} - \underbrace{\omega (\nabla \cdot u)}_{\text{compression}} + \underbrace{(\omega \cdot \nabla) u}_{\text{stretching}} + \underbrace{\frac{1}{\rho^2} \nabla \rho \times \nabla p}_{\text{baroclinicity}} + \underbrace{\nu \nabla^2 \omega}_{\text{dissipation}}$$

Baroclinic Instability and Accretion

Large mass accretion rates,
comparable to the MRI!



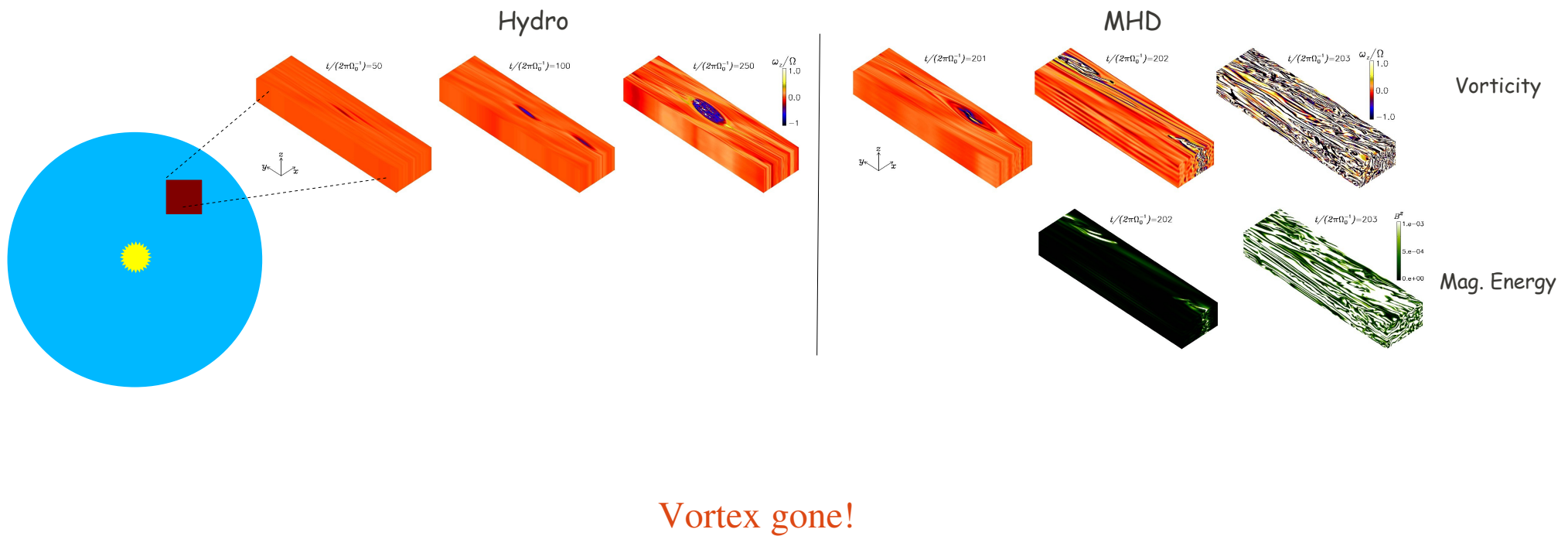
Lyra & Klahr (2011)



The angular momentum is carried by
waves excited by the vortex

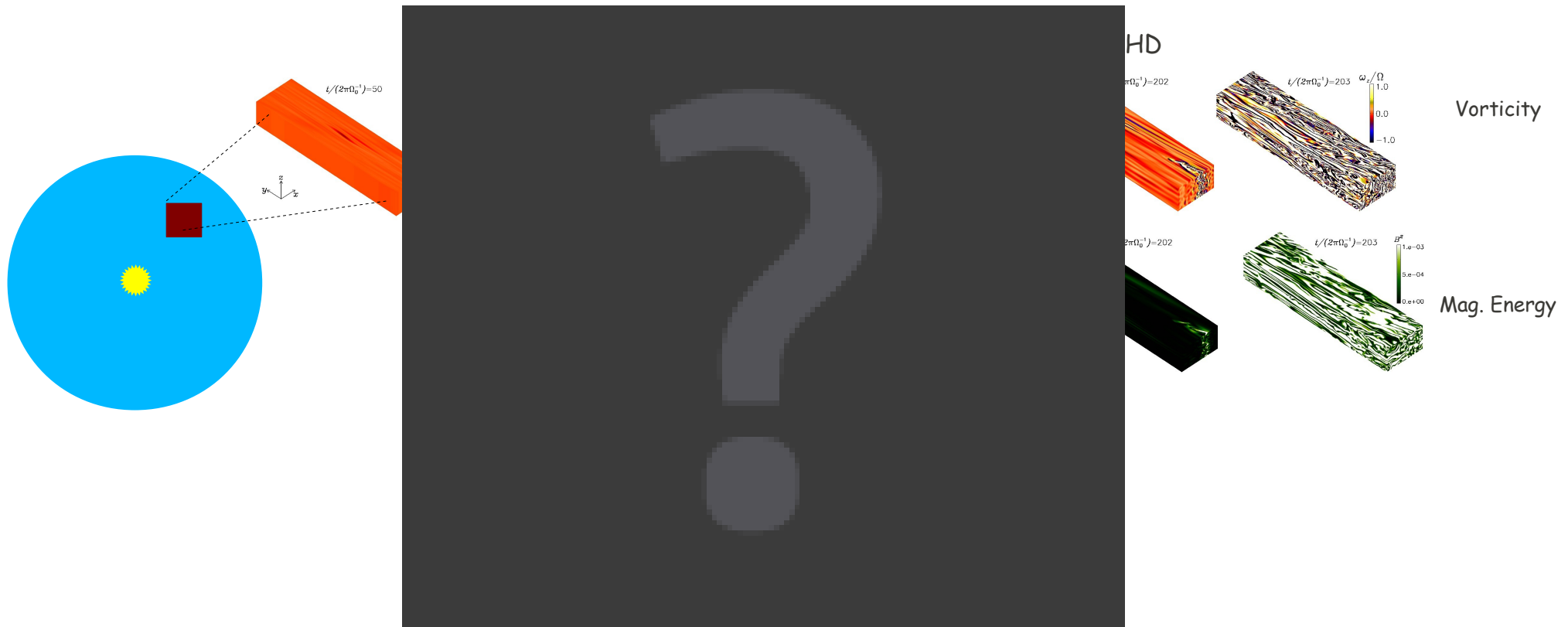
Interaction of Baroclinic and Magneto-Rotational Instabilities

What happens when the vortex is magnetized?



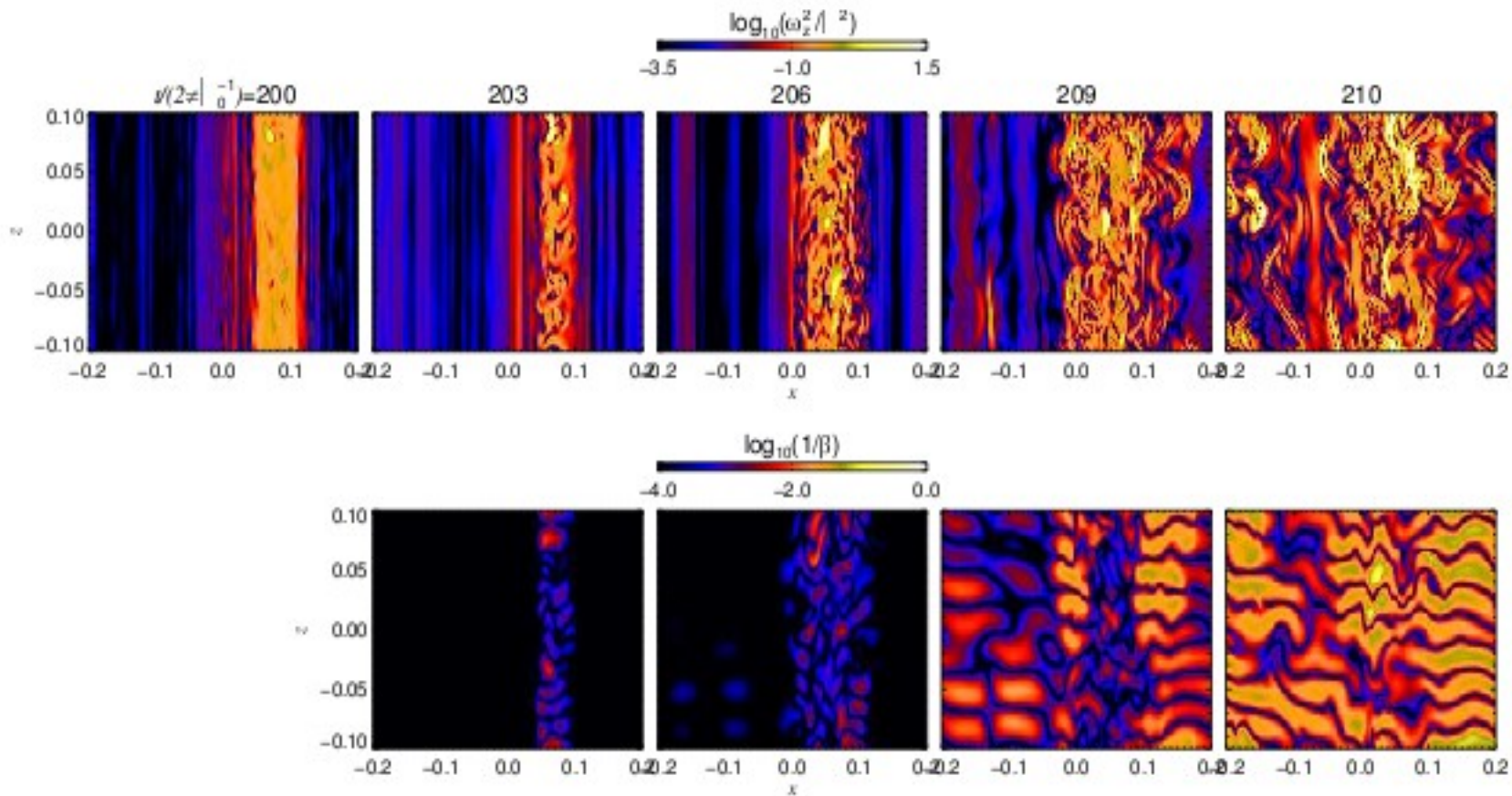
Interaction of Baroclinic and Magneto-Rotational Instabilities

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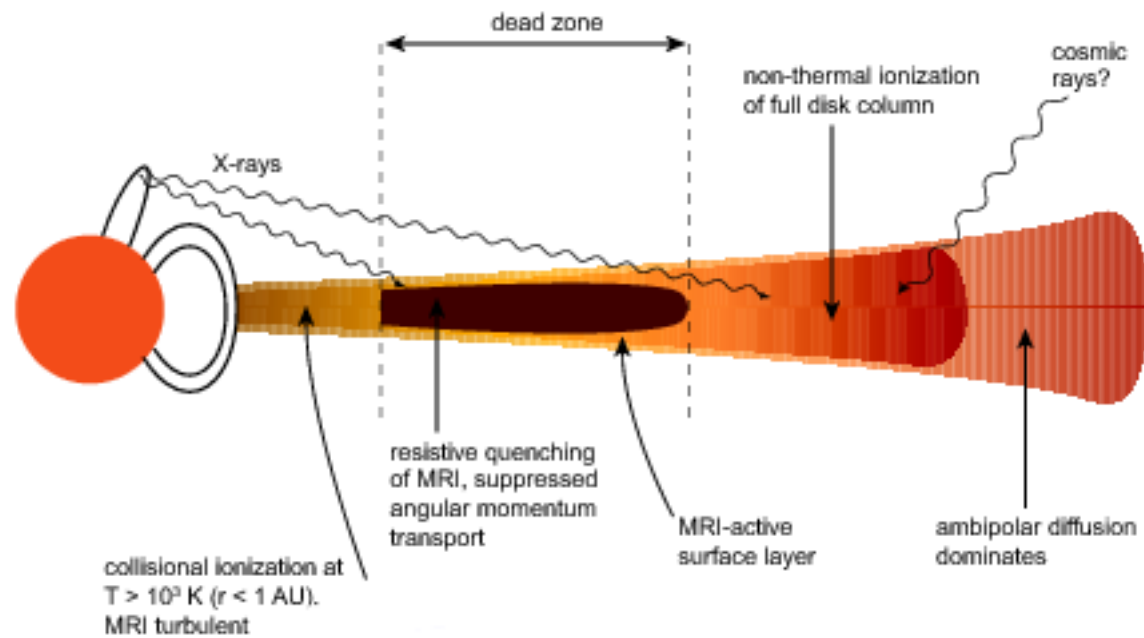
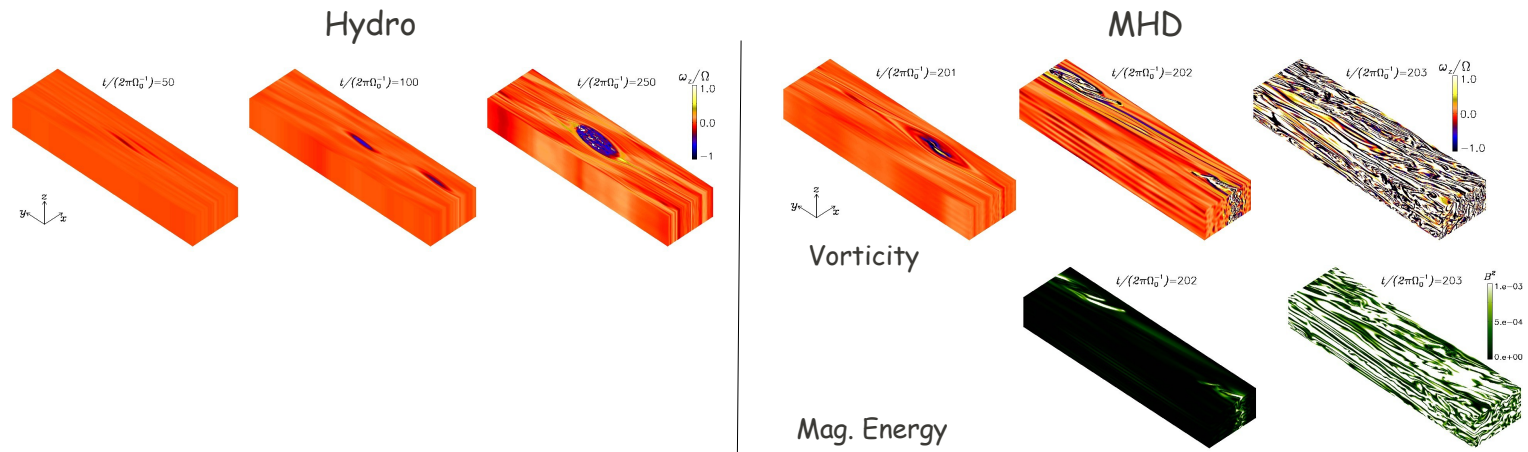
Lyra & Klahr (2011)

Interaction of Baroclinic and Magneto-Rotational Instabilities

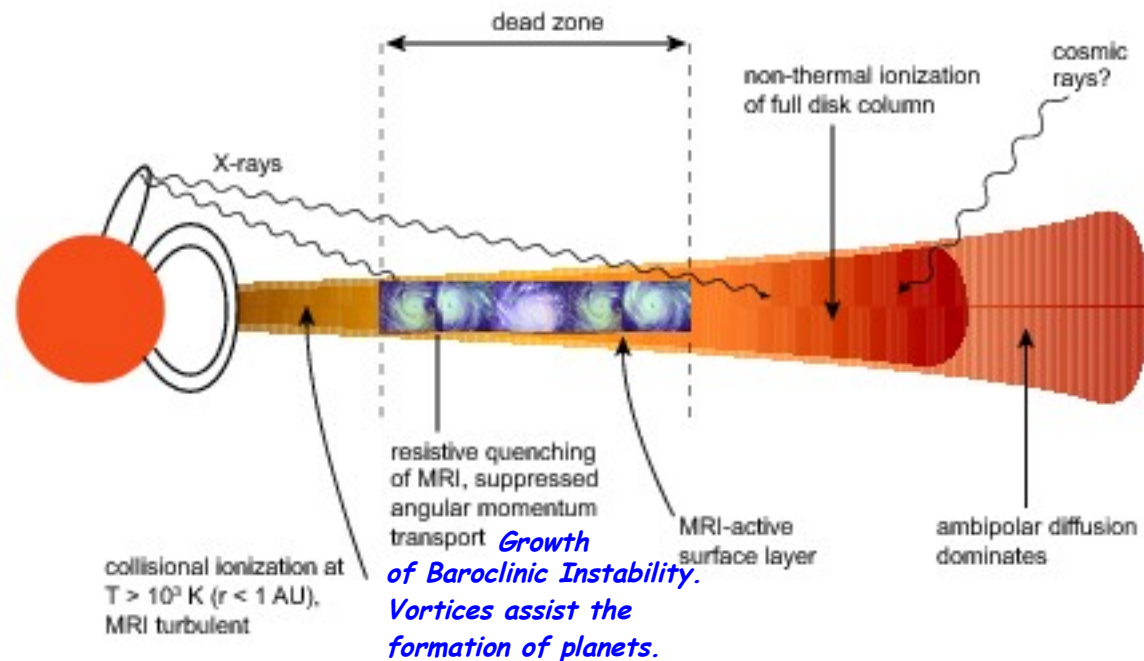
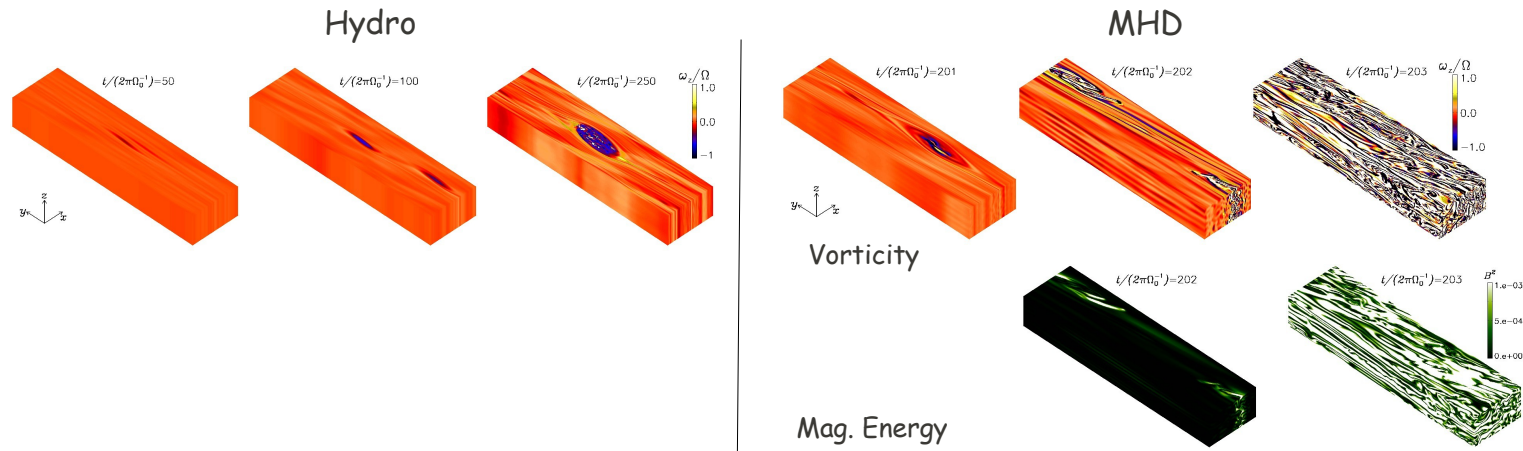


Vortices do not survive magnetization.
Restricted to dead zones.

Suggested large-scale phenomenology

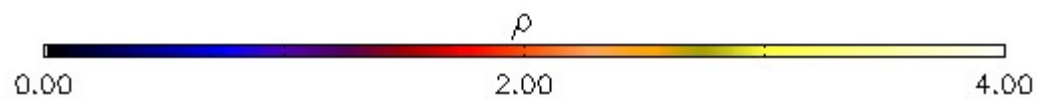
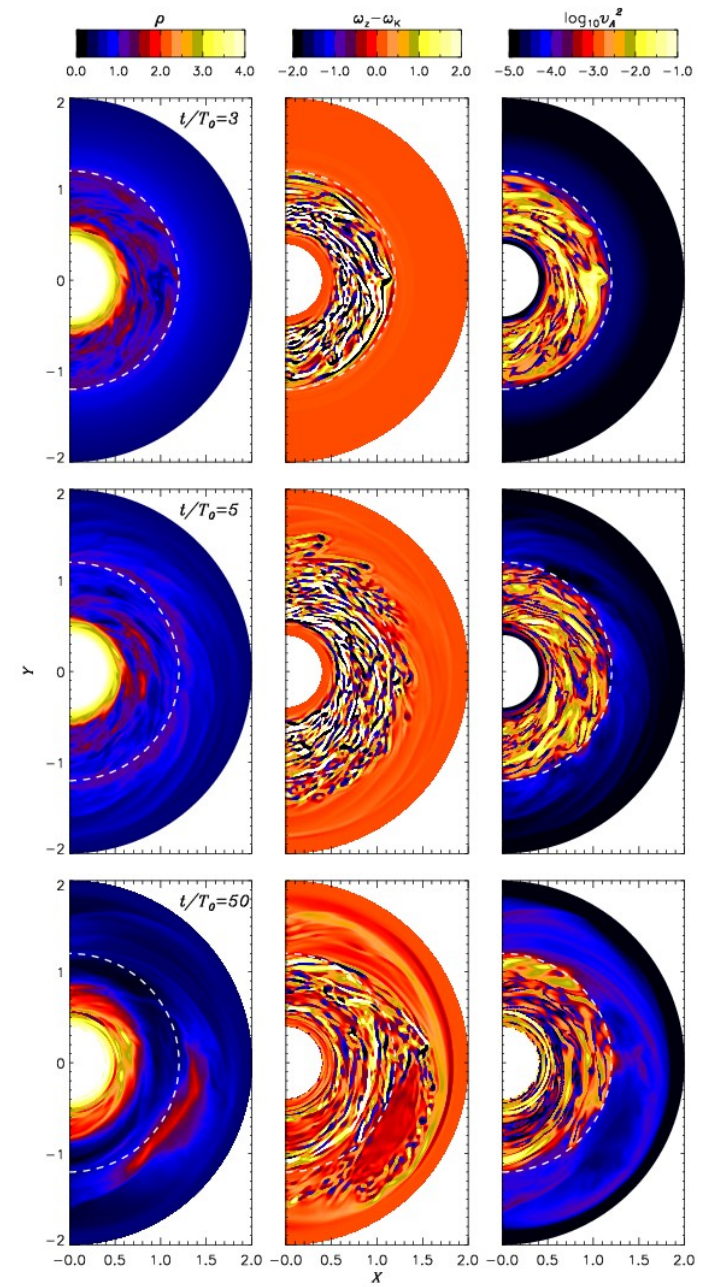
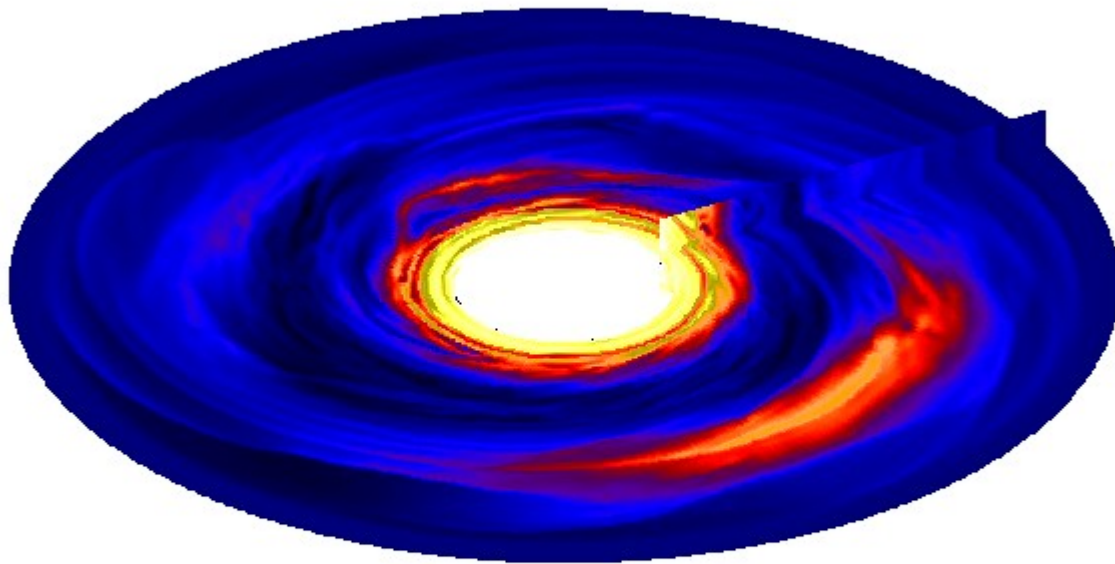


Suggested large-scale phenomenology



Active/dead zone boundary

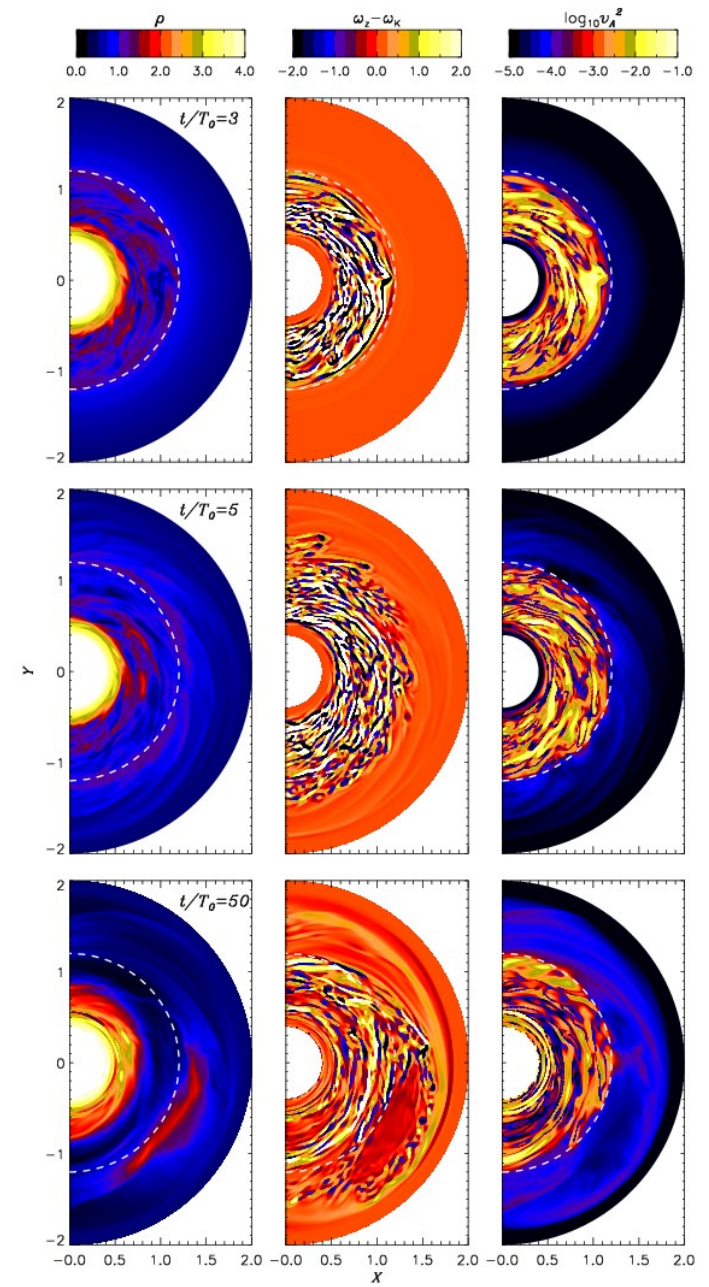
$t = 22.28 \tau_0$



Magnetized inner disk + resistive outer disk

Lyra & Mac Low (submitted)

Active/dead zone boundary

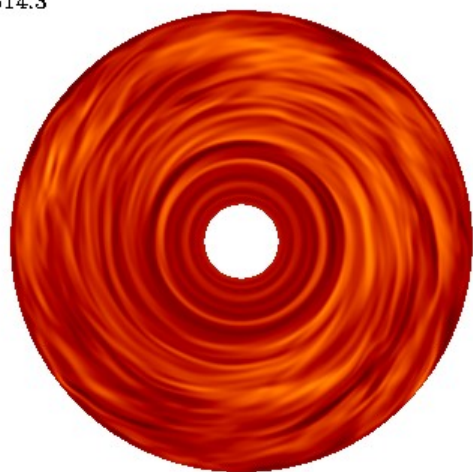


Magnetized inner disk + resistive outer disk

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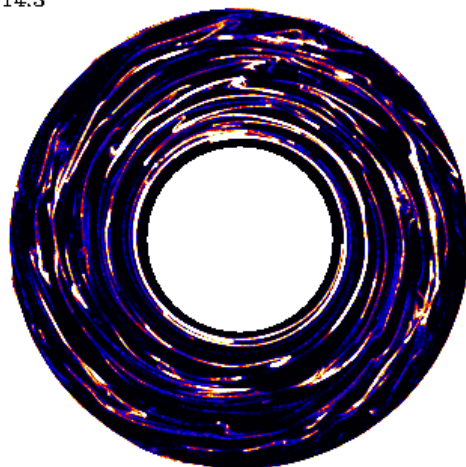
Forming planetesimals

$t=614.3$



0.00 1.00 2.00

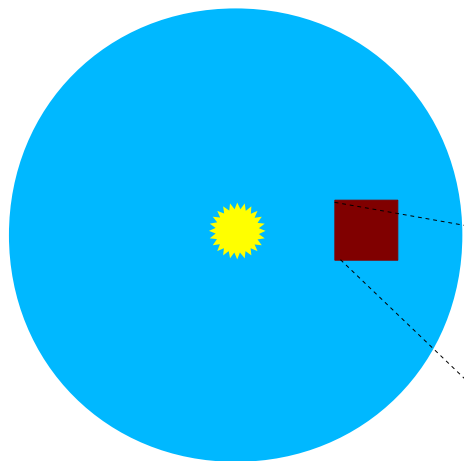
$t=614.3$



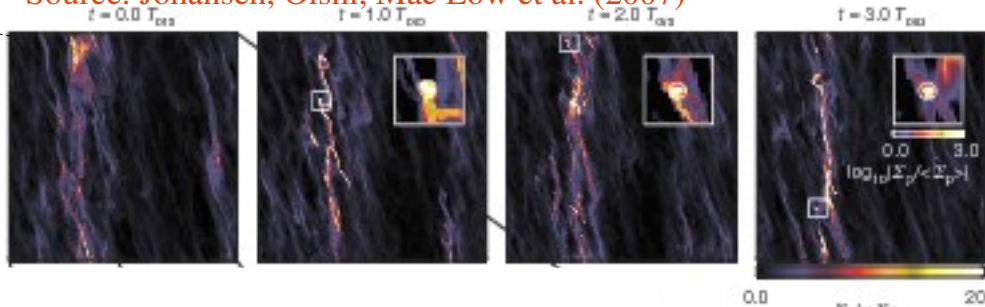
0.00 0.25 0.50

Source: Lyra et al. (2008a)

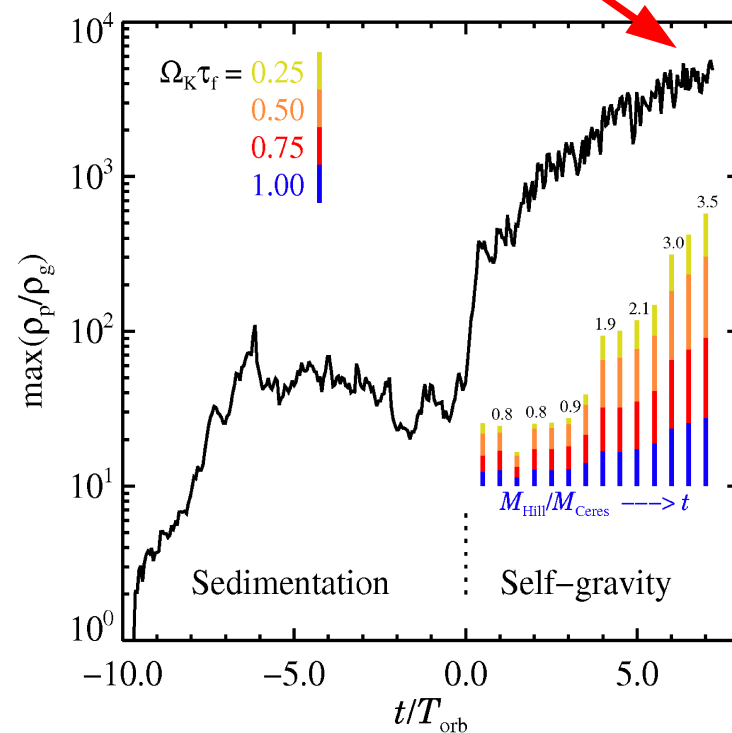
- Turbulent eddies are very efficient particle traps
- Correlation between gas and solids density maxima
- Critical density for gravitational collapse of clumps



Source: Johansen, Oishi, Mac Low et al. (2007)



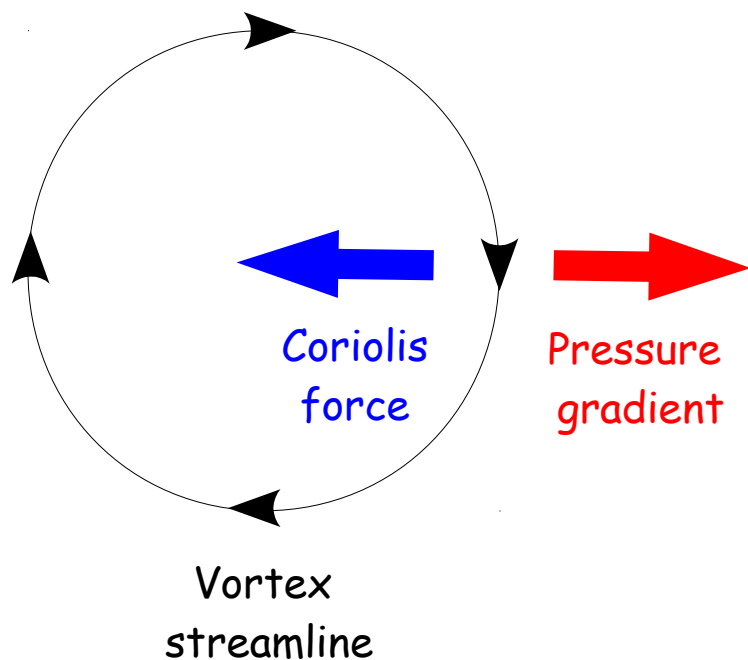
3x Ceres mass!



Eddies concentrate solids,
turning them into planetesimals...

...and vortices are **huge** eddies!

Vortex Equilibrium



Geostrophic balance:

$$2\boldsymbol{\Omega} \times \boldsymbol{u} = -\rho^{-1} \nabla p$$

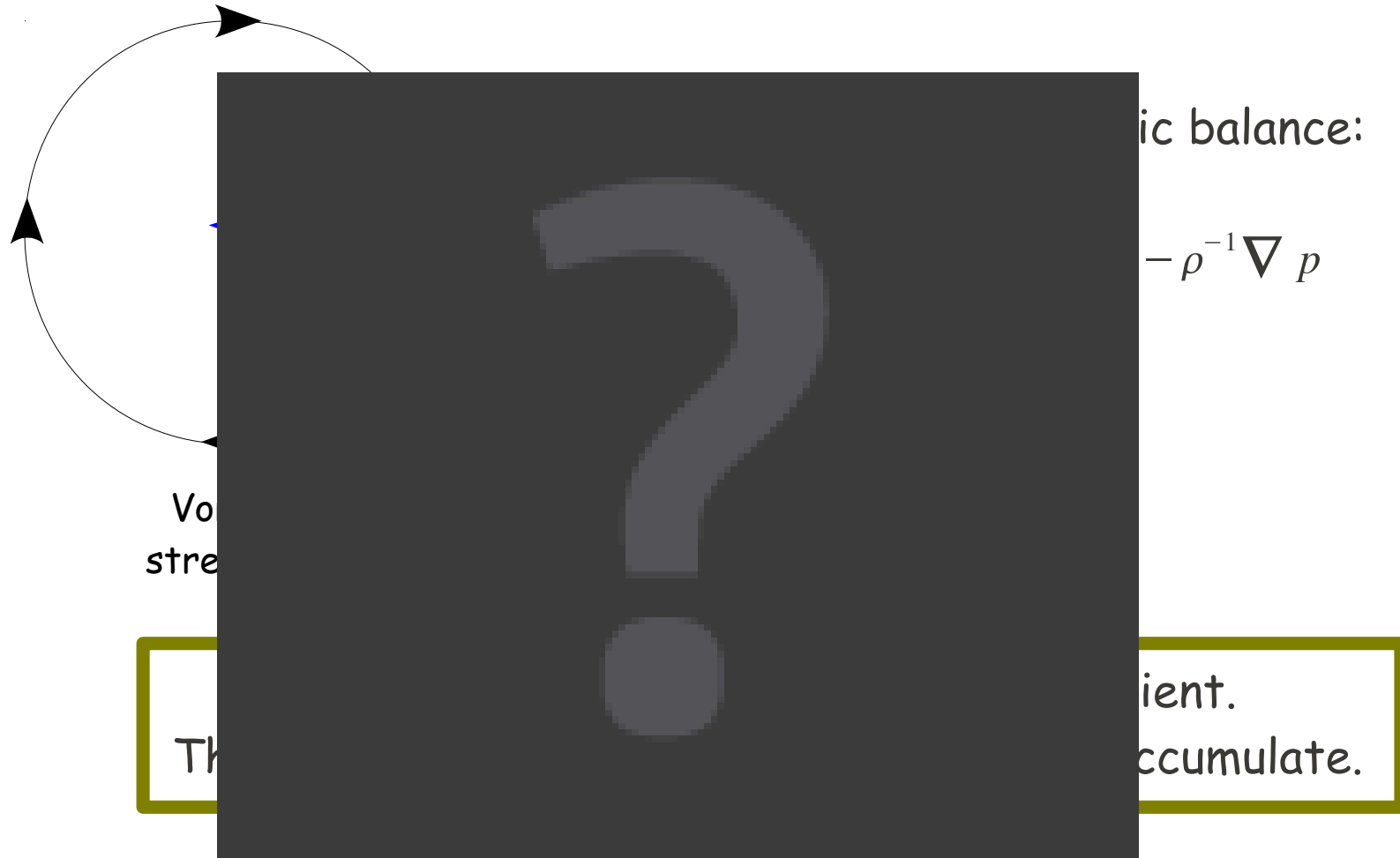
Particles do not feel the pressure gradient.
They sink towards the center, where they accumulate.

Aid to planet formation (von Weizsäcker, 1946)

Revisited by Barge & Sommeria (1995)

Raettig, Lyra, & Klahr (submitted)

Vortex Equilibrium

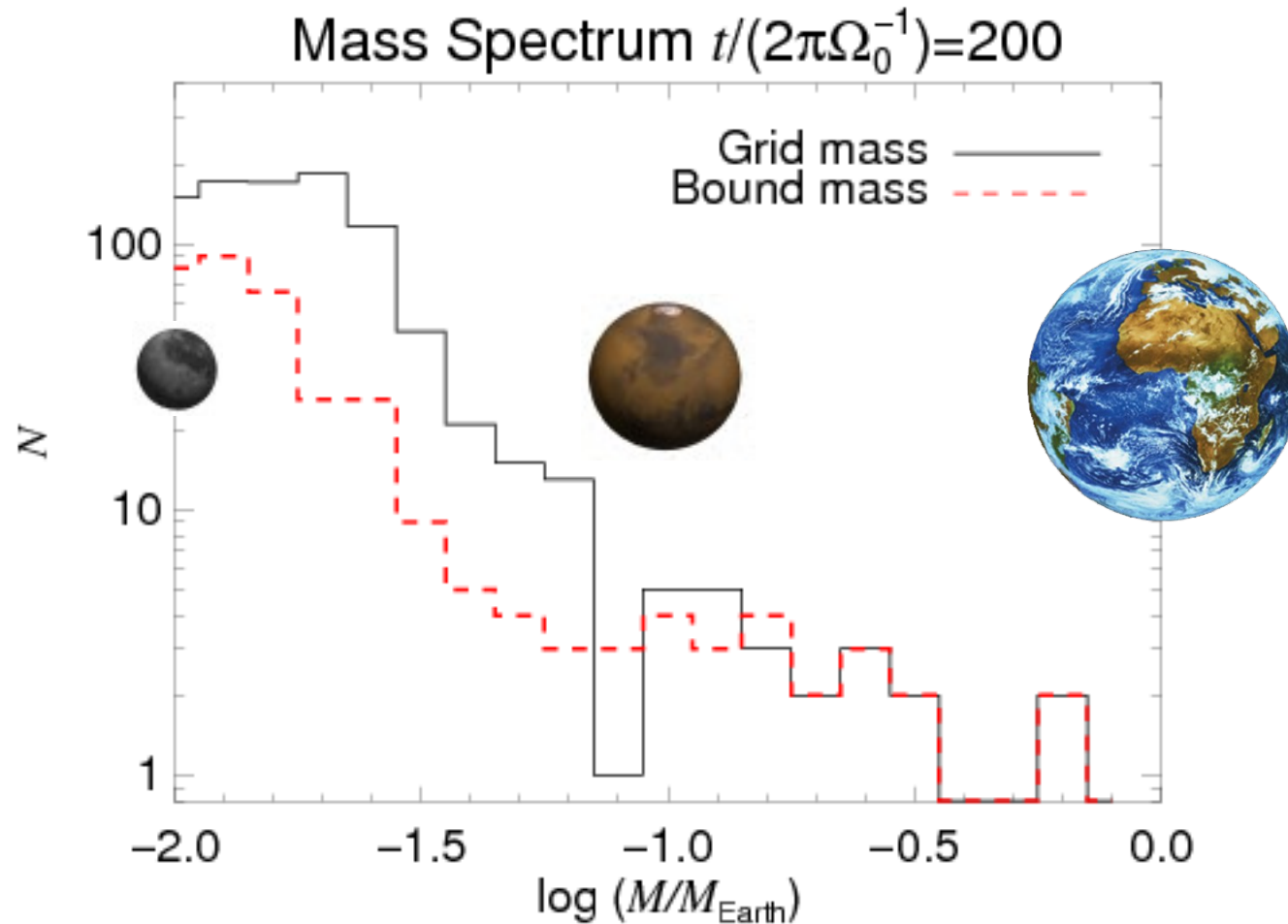


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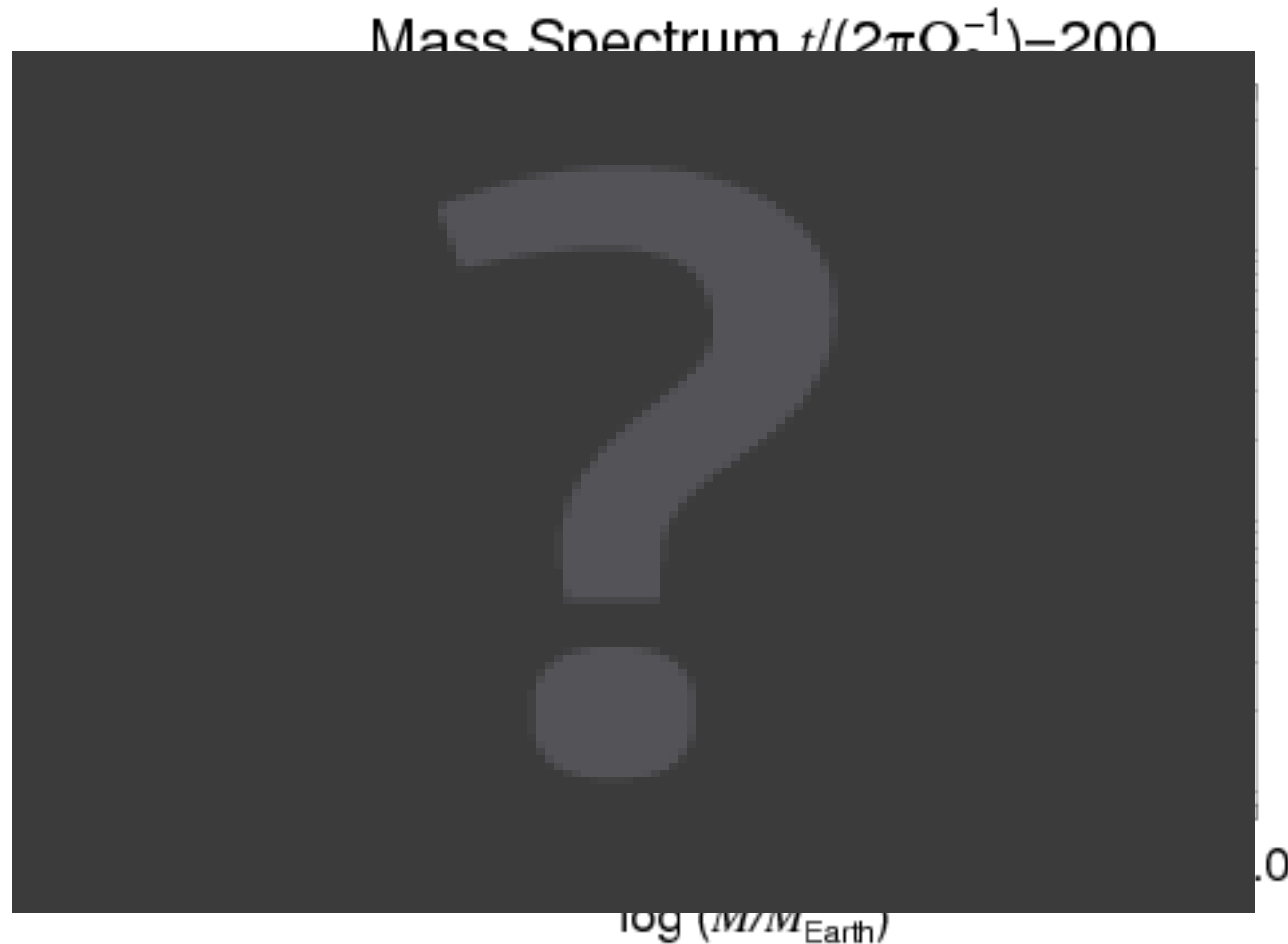
Raettig, Lyra, & Klahr (submitted)

The Initial Mass Function of planets



- Mass spectrum by the end of the simulation
 - 300 bound clumps were formed
- Power law $d(\log N)/d(\log M) = -2.3 \pm 0.2$
- 20 of these are more massive than Mars

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Planets form and start to migrate

Planet-disk interaction leads to **angular momentum exchange**

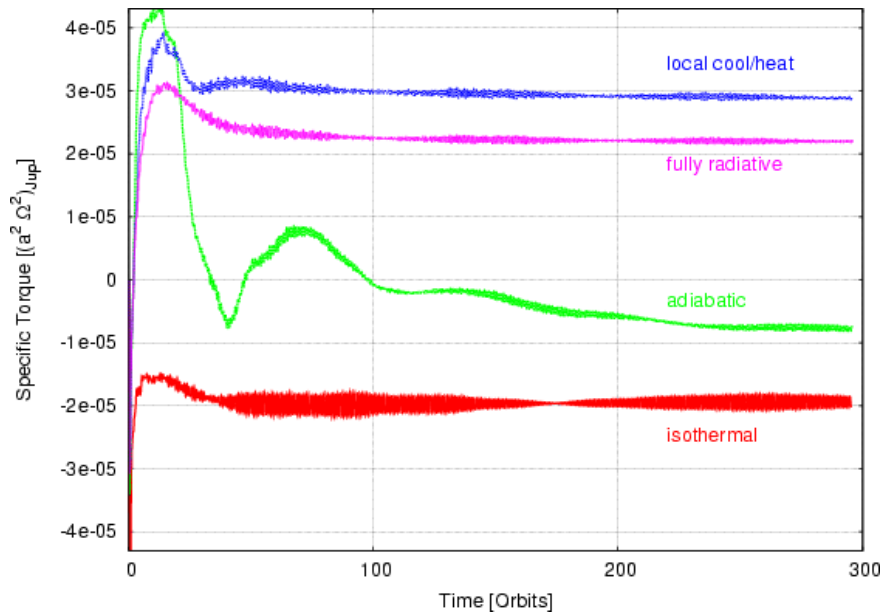
One armed spiral: Lindblad resonance
Horseshoe libration: Co-rotational torques



Source: Lubow et al. (1999)
Animations by Frederic Masset.

In isothermal disks,
the result is *inward migration*.

Planets form and start to migrate



Source: Kley & Crida (2008)

Paardekooper & Mellema (2006)

Non-isothermal
co-rotational torque may lead
to outward migration

Hot topic!

Paardekooper & Mellema 2008

Baruteau & Masset 2008

Paardekooper & Papaloizou 2008

Kley & Crida 2009

Kley et al 2009

Paardekooper et al. 2010

Bitsh & Kley 2010

Lyra et al. 2010

Paardekooper et al. 2011

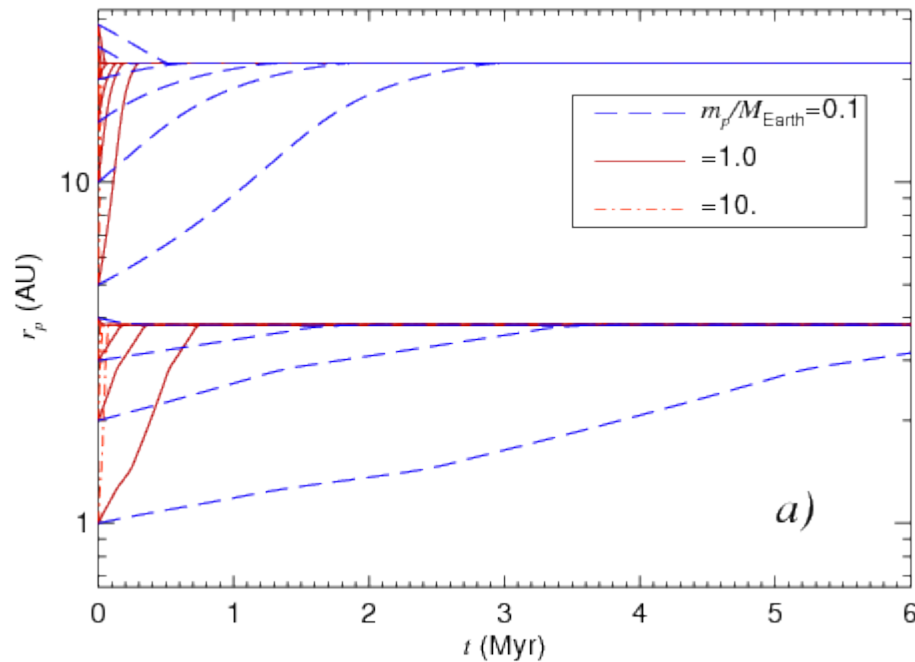
Ayliffe & Bate 2011

Yamada & Inaba 2011

Kley 2011

Planets form and start to migrate

Planet-disk interaction leads to **angular momentum exchange**

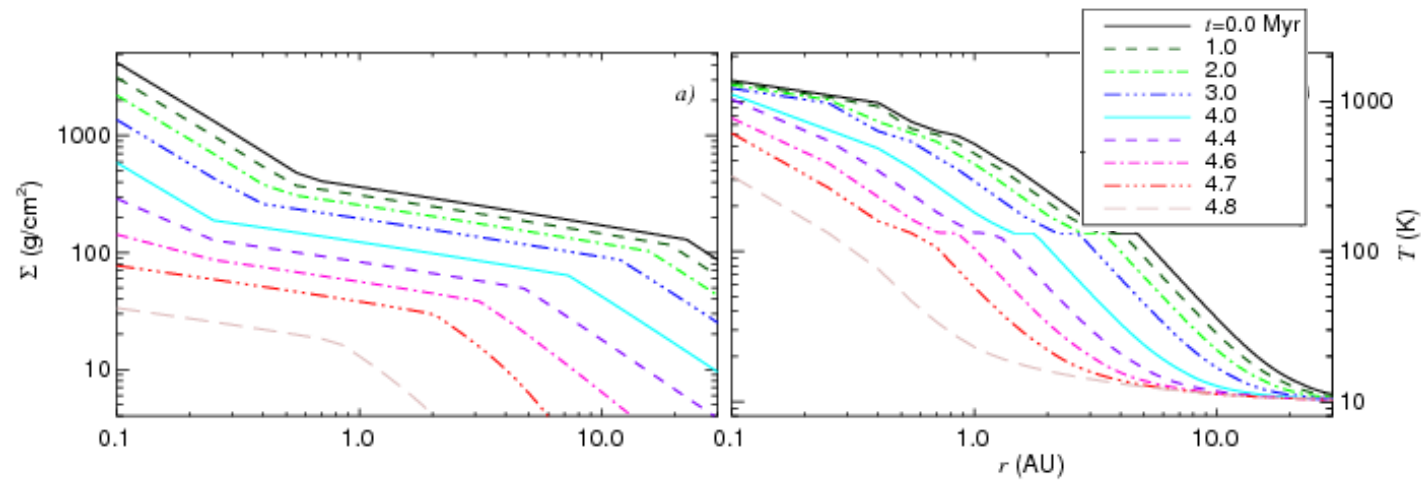


Source: Lyra, Paardekooper, & Mac Low (2010)

Planet traps where migration
is **convergent**
($\tau=0$, $d\tau/dr < 0$).

Migration in Evolutionary Models

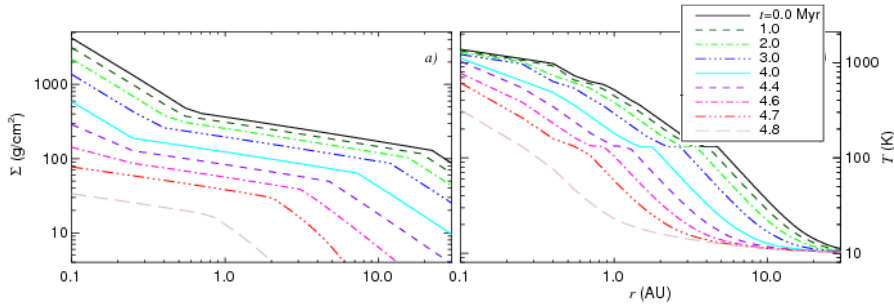
Disks evolve in time, due to
photoevaporative winds and viscous evolution



Source: Lyra, Paardekooper, & Mac Low (2010)

Migration in Evolutionary Models

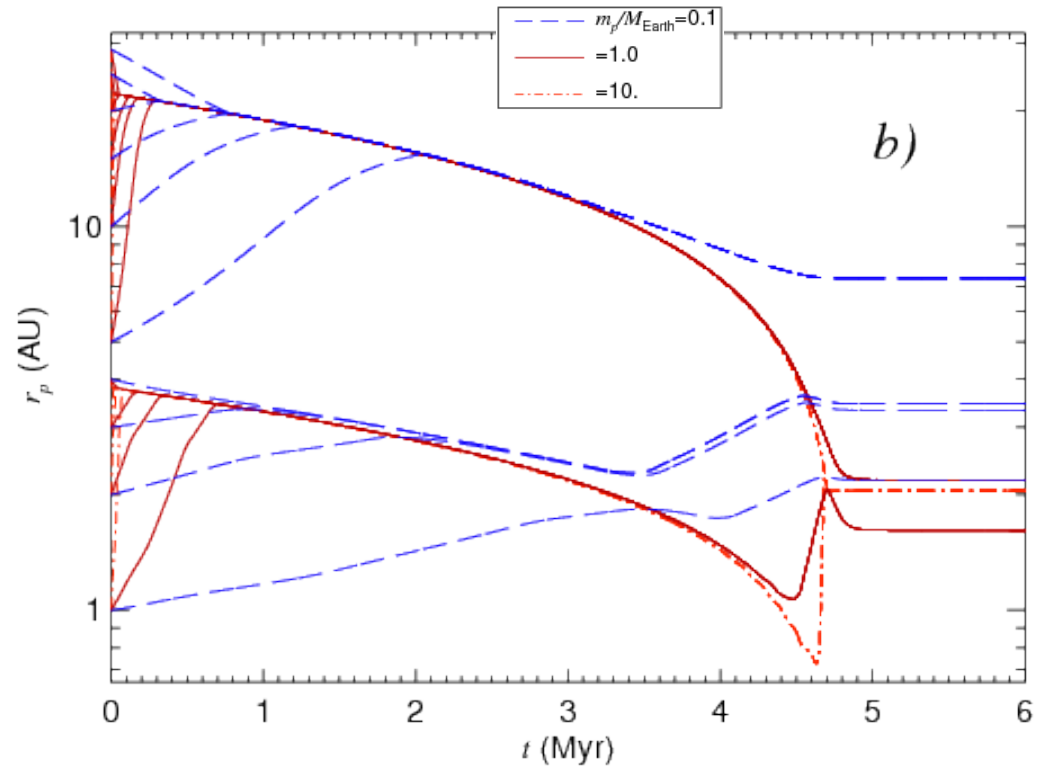
Disks evolve in time, due to
photoevaporative winds and viscous evolution



Single planets in a planetary trap
evolve in **lockstep** with the gas at the
accretion timescale.

At some point, the disk becomes **too thin**
to drive accretion. The planet **decouples**
and is **released** in a safe orbit.

Rule of thumb: *Migration is*
outwards in
steep temperature gradients,
inwards in
isothermal regions.



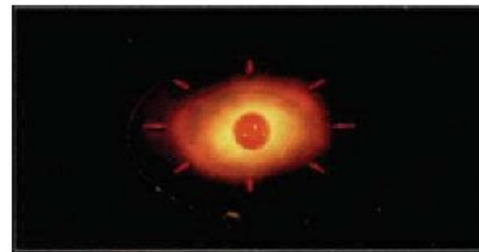
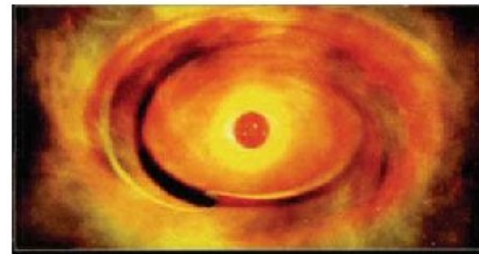
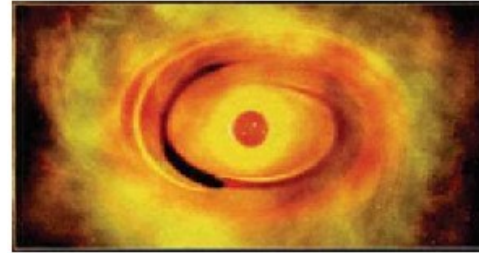
Source: Lyra, Paardekooper, & Mac Low (2010)

Migration in Evolutionary Models

Single planets in a planetary trap evolve in **lockstep with the gas** at the accretion timescale.

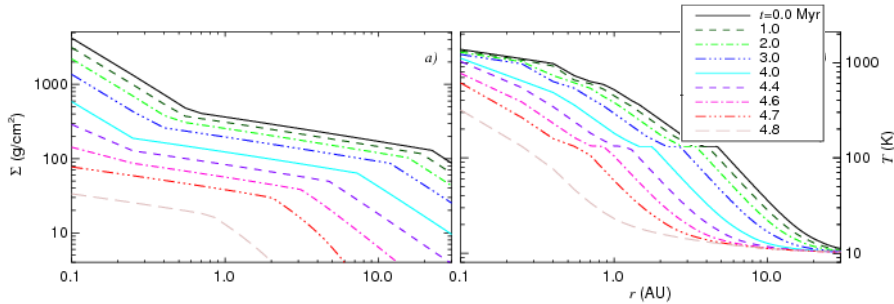
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Migration in Evolutionary Models

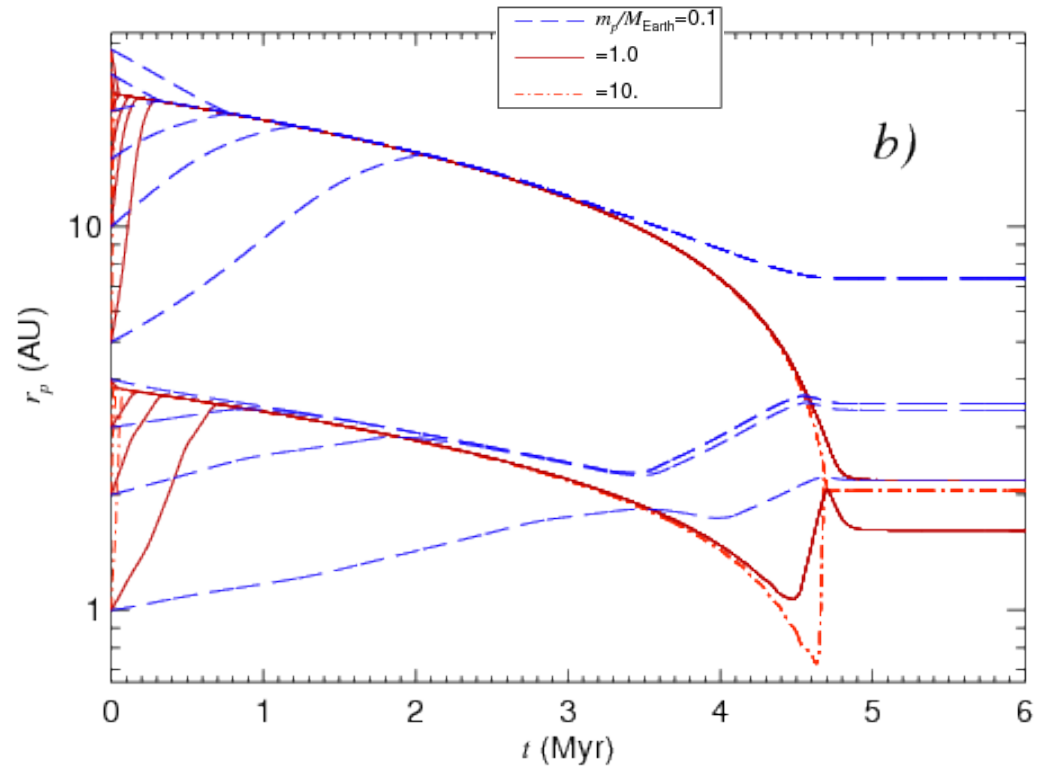
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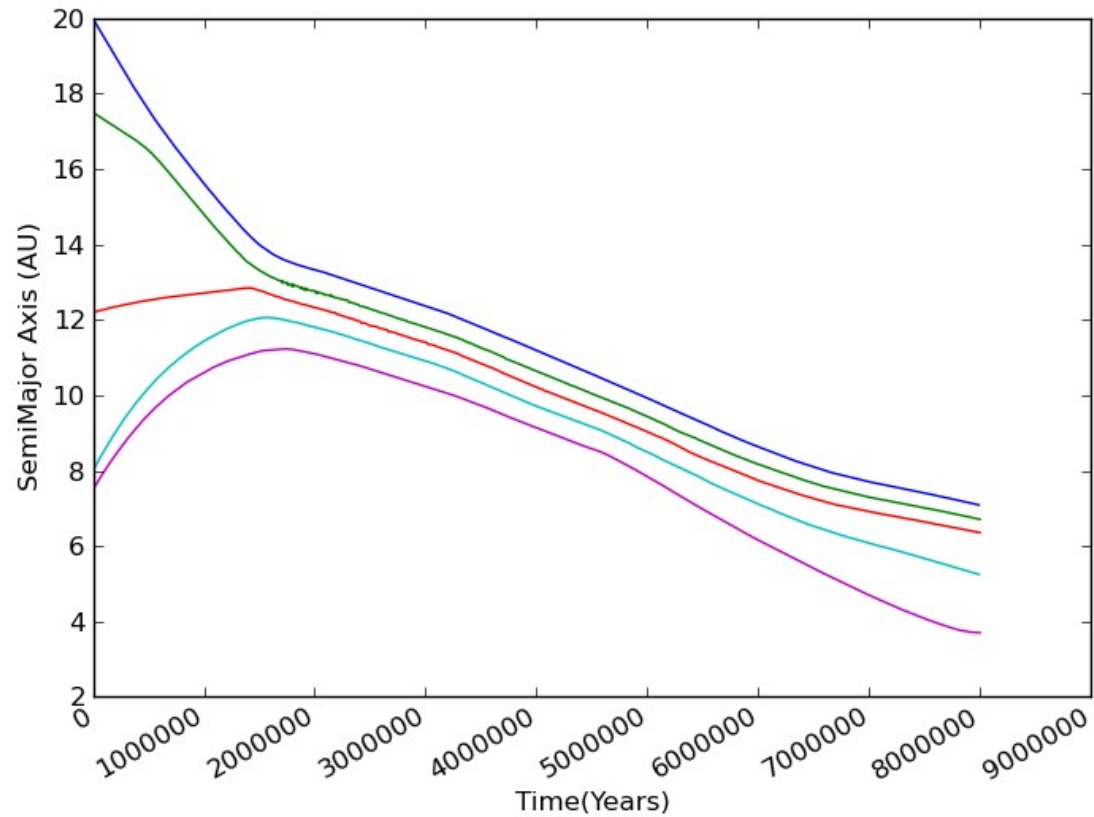
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Source: Lyra, Paardekooper, & Mac Low (2010)

Migration + N-Body in Evolutionary Models

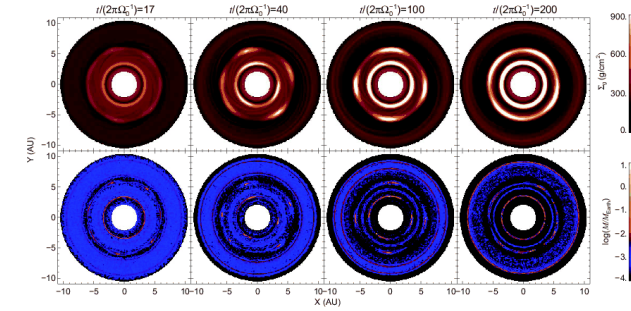


Migration in resonance!

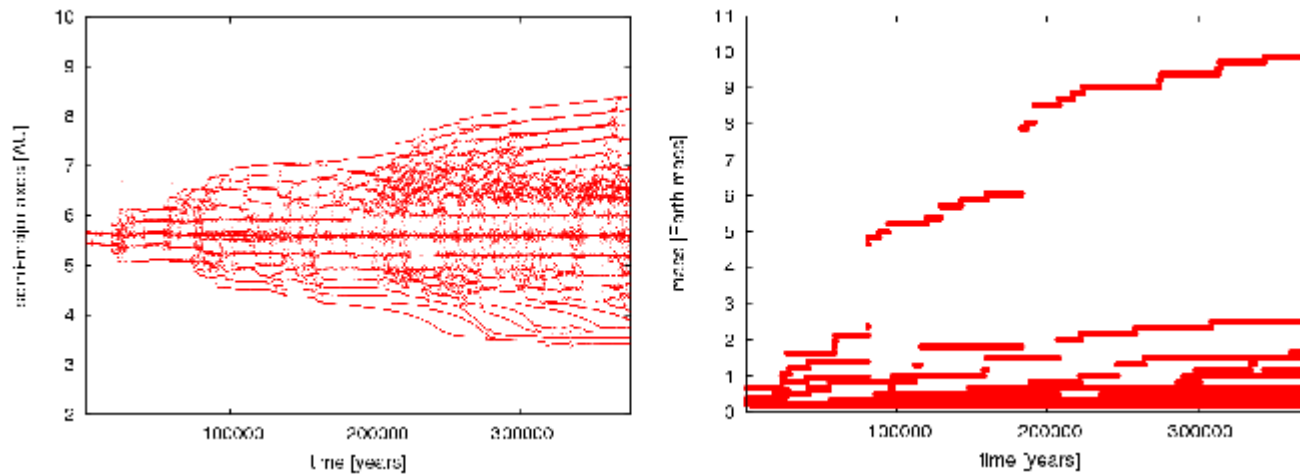
Forming giant planet cores at migration traps

Continuous planet formation:

a Mars-mass planet appears
at the migration trap, following a Poisson rate.



Source: Lyra et al. (2008b)



Source: Sándor, Lyra, & Dullemond (2011)

Planets escape trap via N-body interactions

Find inner/outer equilibrium position by
resonance trapping!

Resonance broken by further
planet formation, that disturbs the structure.

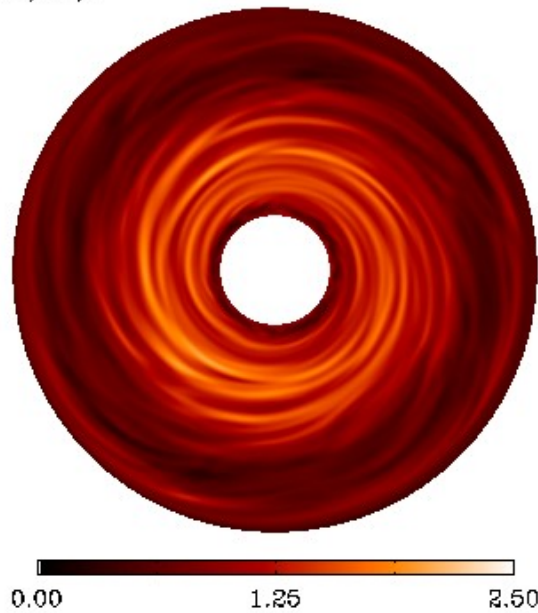
Parametrized turbulence

Stochastic forcing (Laughlin et al. 2004, Ogihara et al. 2007)

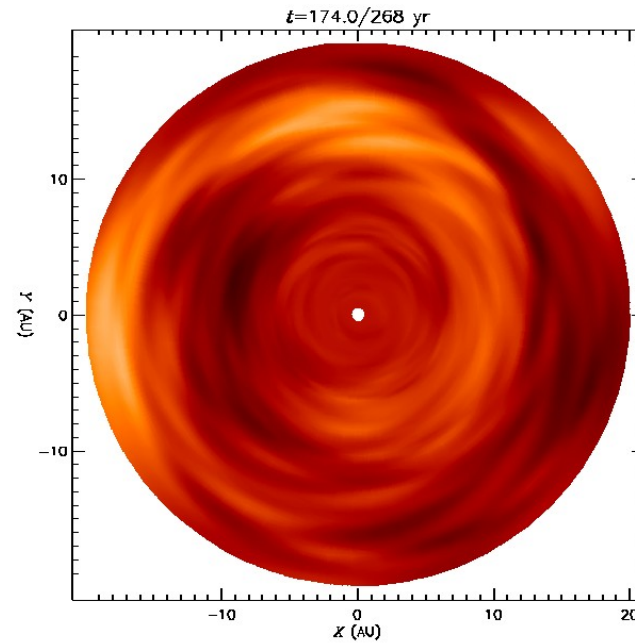
$$\Phi = A r^2 \Omega^2 \sum_{i=1}^n \Lambda_{c,m}$$
$$\Lambda_{c,m} = e^{-(r-r_c)^2/\sigma^2} \cos(m\theta - \phi_c - \Omega_c \tilde{t}) \sin(\pi \tilde{t} / \Delta t)$$

MHD modeling

$t=46.3/88\text{yr}$



Linear superposition of modes



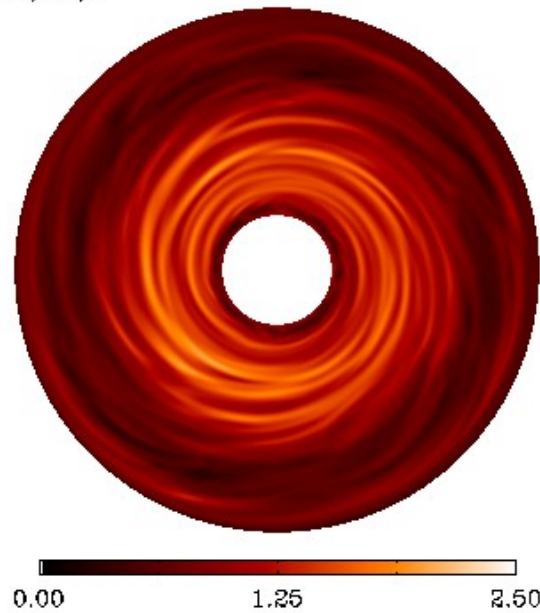
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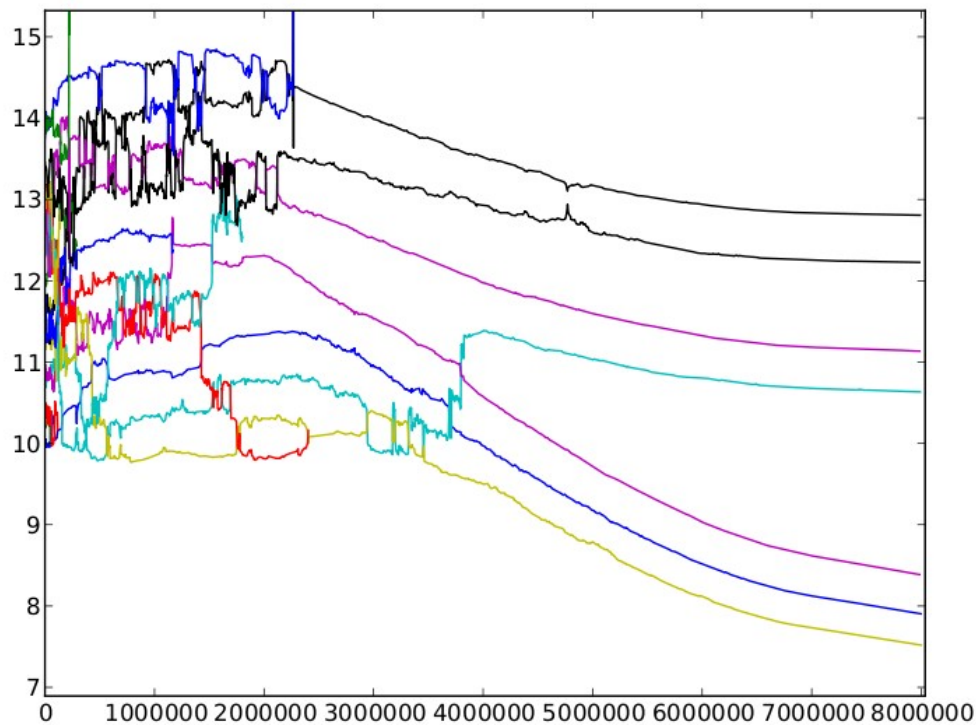
Orbital migration of interacting planets in a radiative evolutionary model

Combines

migration + N-body + photoevaporation + turbulence

modelled as stochastic forcing

(Laughlin et al. 2004, Ogiwara et al. 2007)



- 16 Earth mass bodies
- Resonances broken by turbulence
- System relaxes to oligarchs

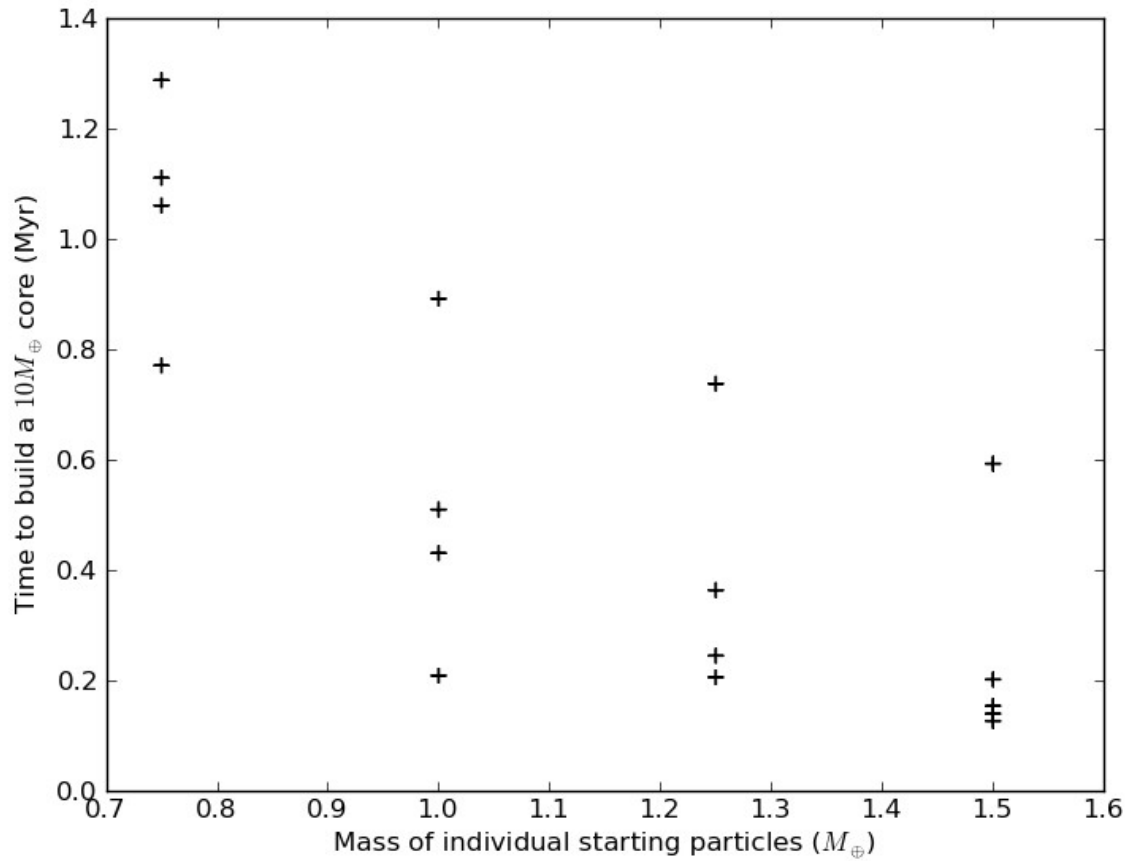
Horn, Lyra, Mac Low & Sandor (2012)

Orbital migration of interacting planets in a radiative evolutionary model



Horn, Lyra, Mac Low & Sandor (2012)

Orbital migration of interacting planets in a radiative evolutionary model

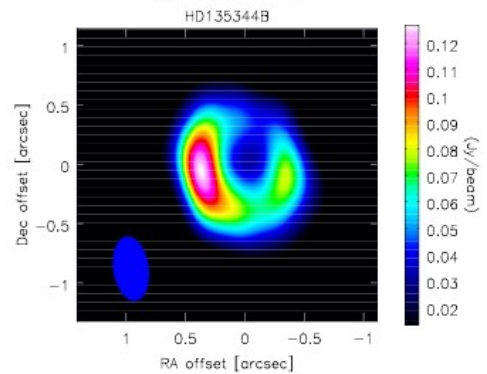
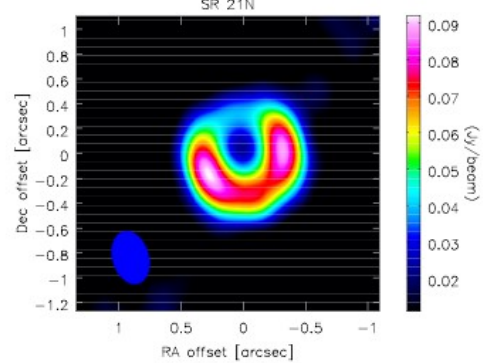
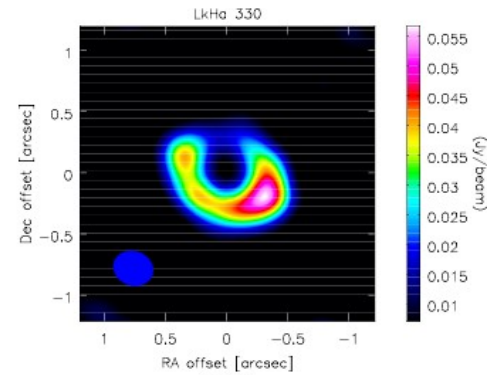
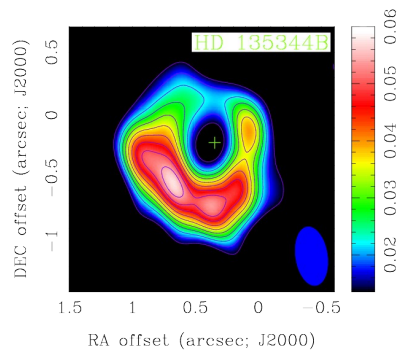
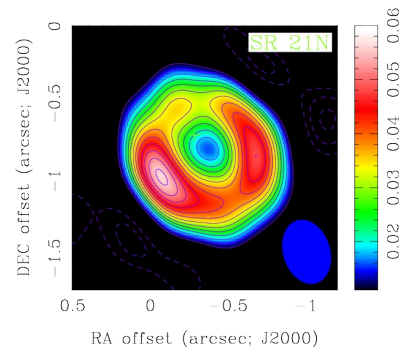
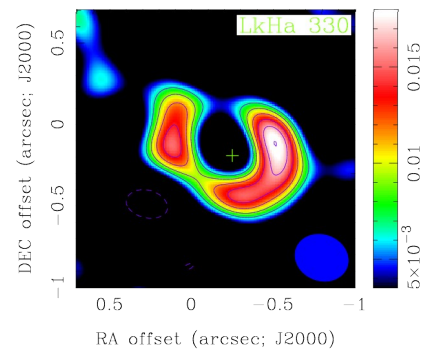


Horn, Lyra, Mac Low & Sandor (2012)

A possible detection of vortices in disks

Observations

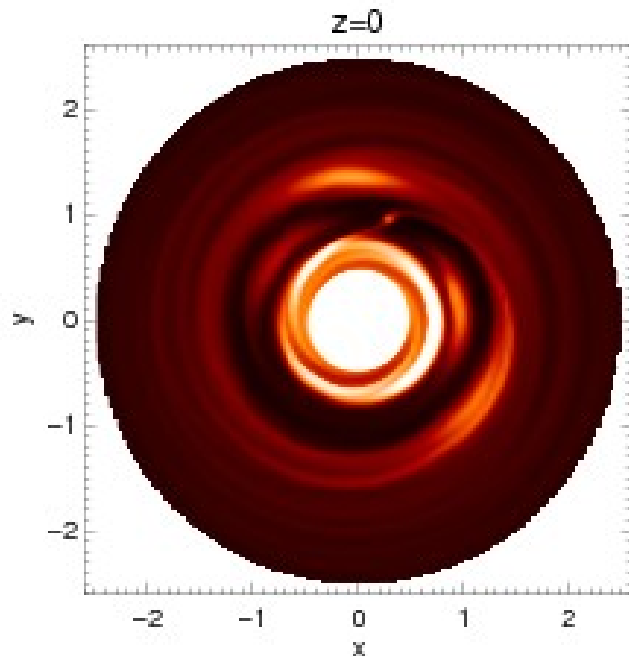
Brown et al. 2009



Simulated observations
of Rossby vortices

Regaly et al. (2012)

Another way of exciting vortices:



The edges of a planet-carved gap are also prone to vortex excitation.

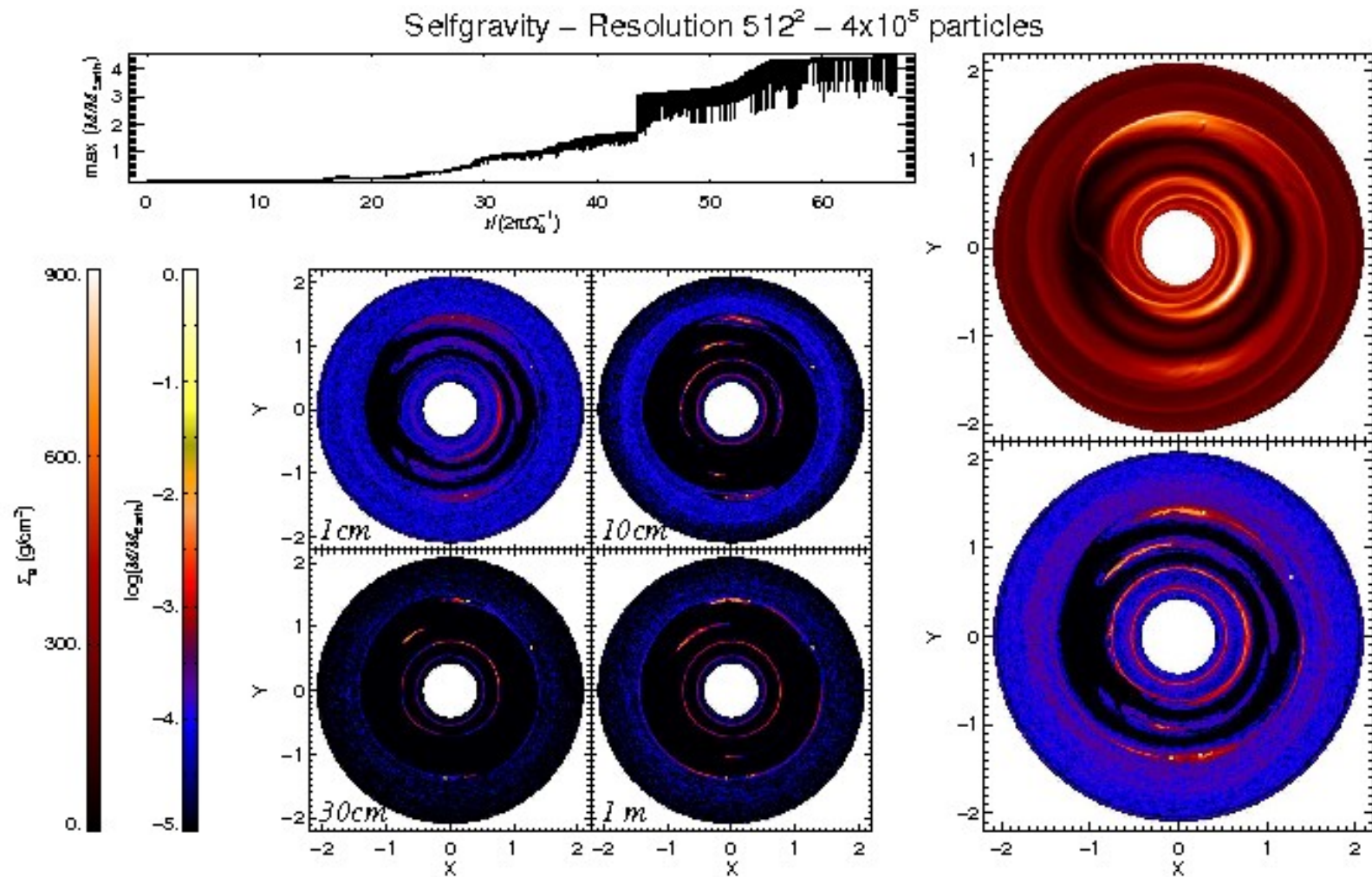
What happens when particles are introduced?

Another way of exciting vortices:



What happens when particles are introduced?

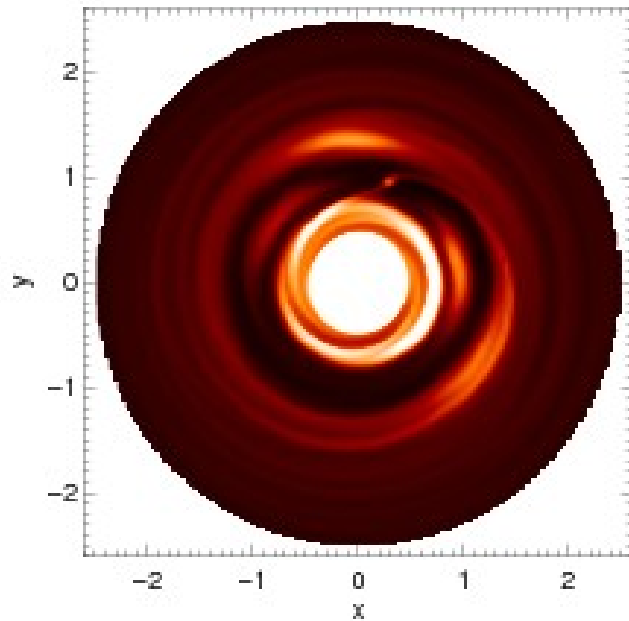
Trojan Planets!!



3 Super-Earths formed + Mars mass Trojans

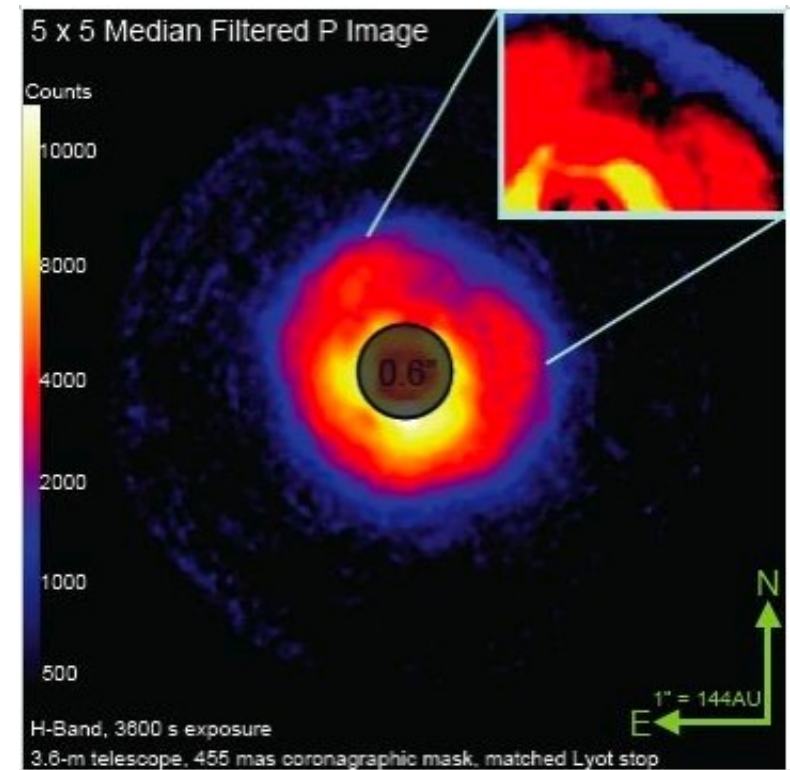
The wake of a planet in the AB Aurigae disk

Theoretical prediction



Lyra et al. (2009)

Observation



Oppenheimer et al. (2009)

Summarizing

Gravitational collapse of an interstellar cloud

Outward transport of angular momentum through turbulence generated by the MRI. Dust coagulates into pebbles and boulders, sedimenting towards the midplane.

Rocks in the turbulent medium are trapped in transient pressure maxima and undergo collapse into planetesimals and dwarf planets.

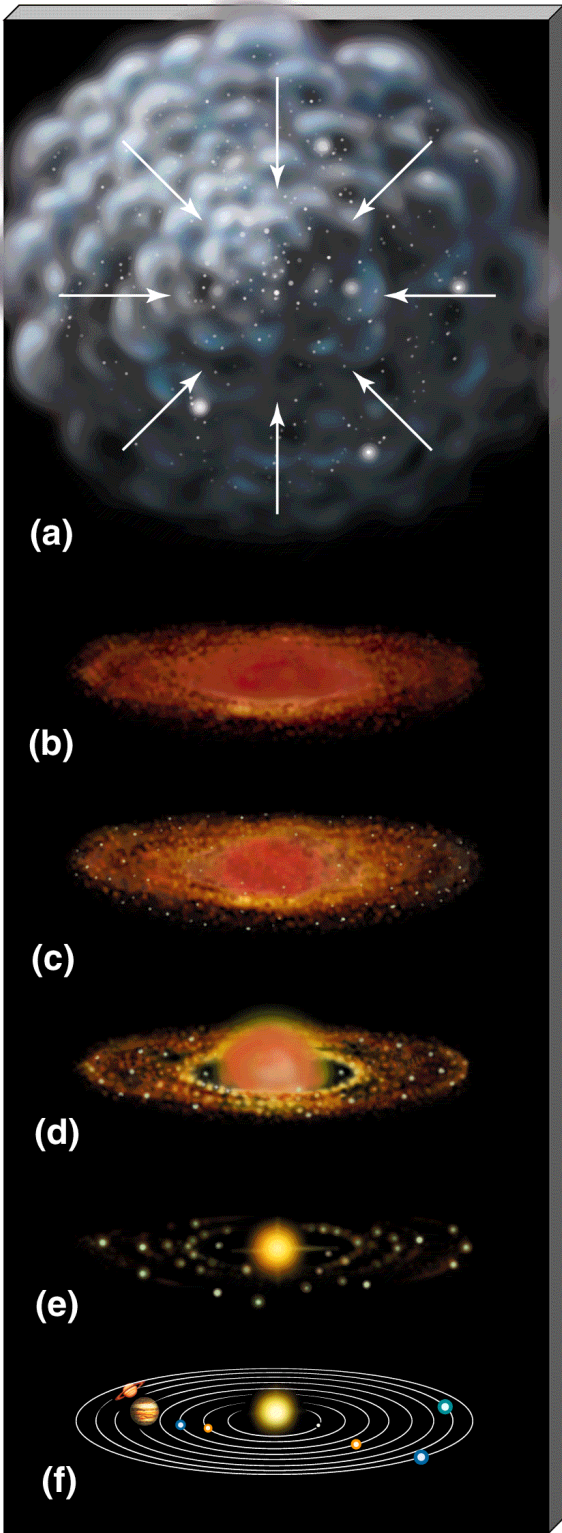
Vortices may be excited in the dead zone. Inside them, the first dozens of Mars-mass embryos are formed. IMF ~ -2

Opacity transitions develop into regions of convergent migration. Low mass planets converge to these zones by inward/outward migration.

Convergent migration leads to resonances, these are disrupted by turbulent forcing. Collisions between embryos gives rise to oligarchs.

The disk thins due to photoevaporation. Planets released into stable orbits.

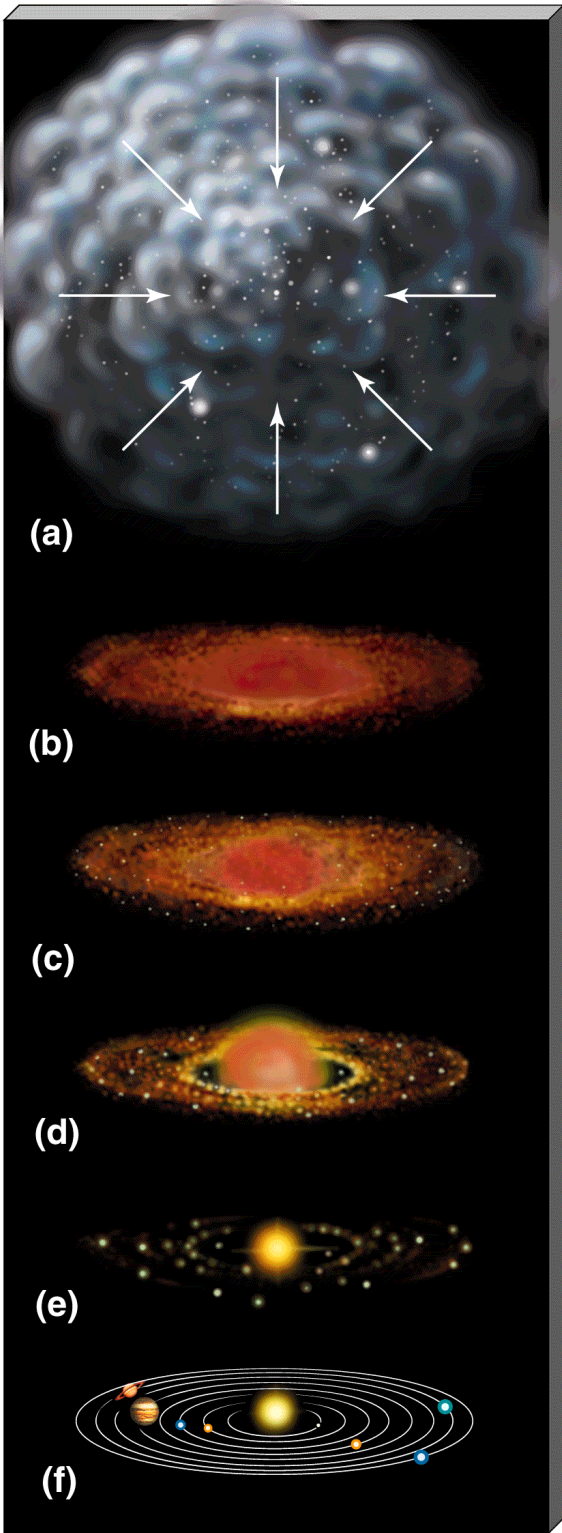
N-body interactions and stochastic forcing during disk evaporation produce the system's final architecture.



Summarizing

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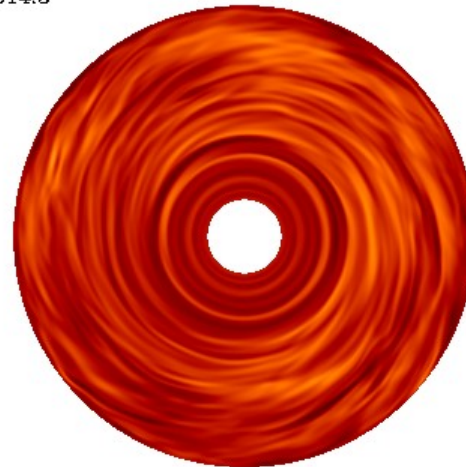


Gas

Solids

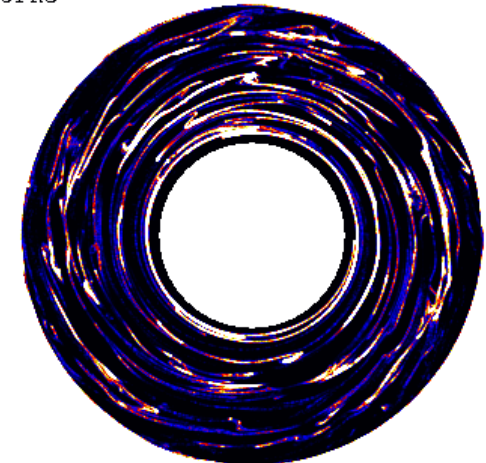
Rocks in the turbulent medium are trapped in transient pressure maxima and

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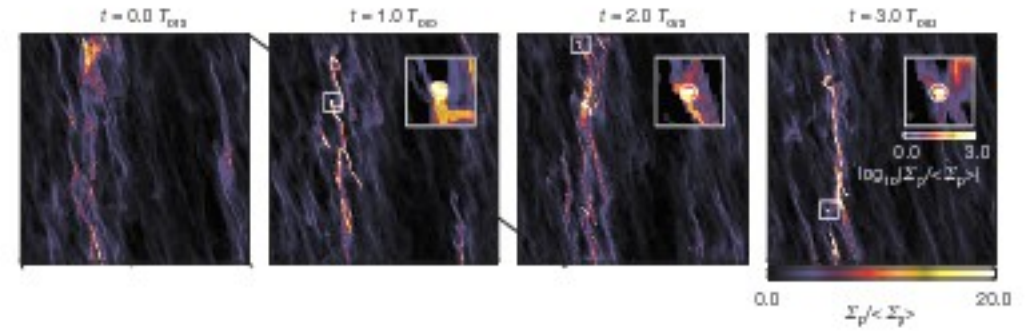
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Summarizing

Gravitational collapse

Outward transport of the MRI. Dust coagulation in the midplane.



Rocks in the turbulent medium are trapped in transient pressure maxima and undergo collapse into planetesimals and dwarf planets.

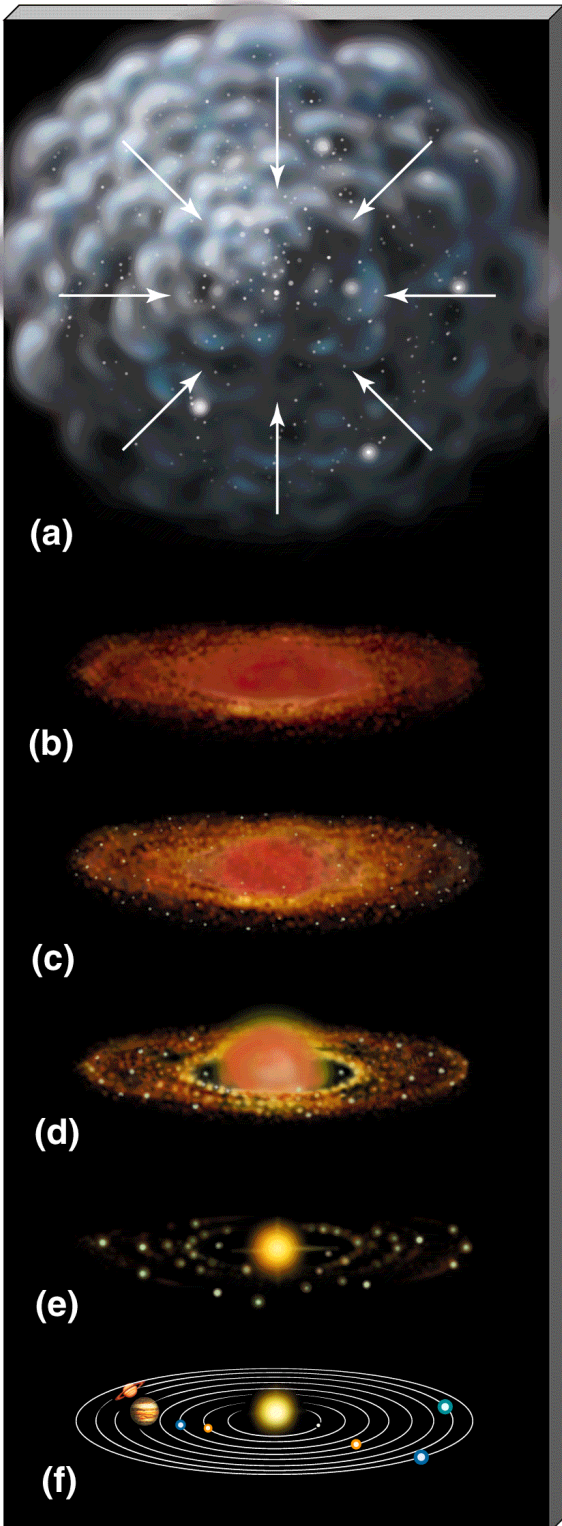
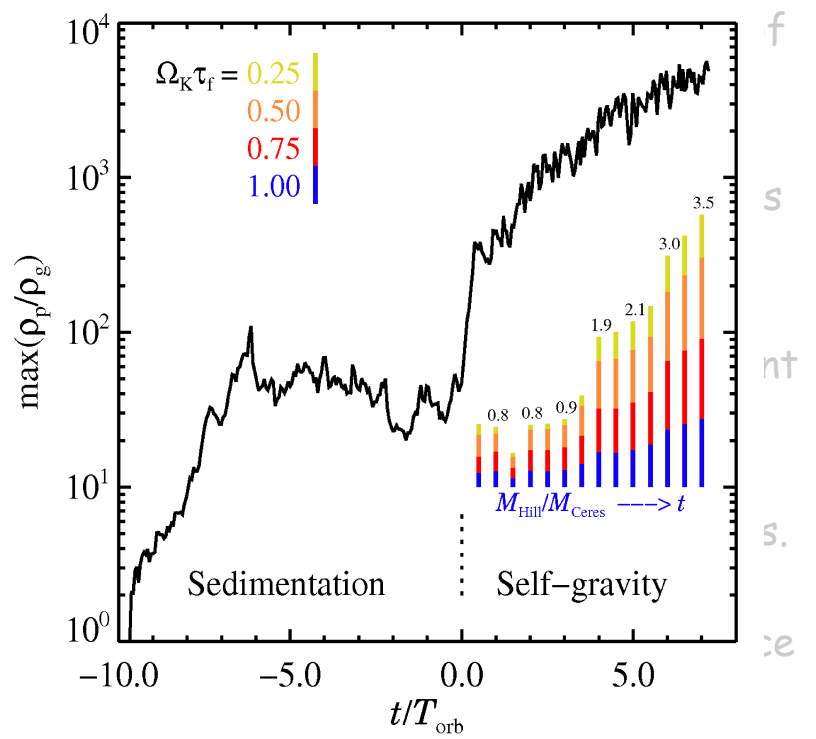
Vortices may be excited in the disk. Mars-mass embryos are formed.

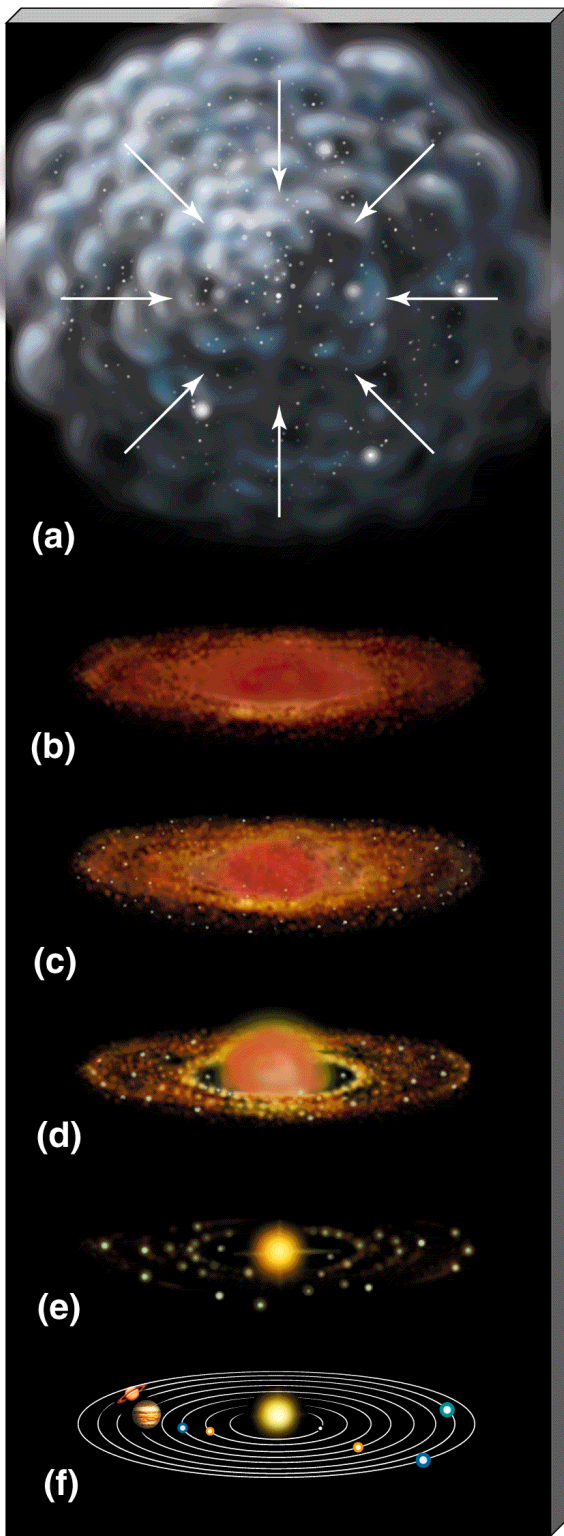
Opacity transitions develop into planets. Planets converge to these zones.

Convergent migration leads to reinforcing. Collisions between embryos.

The disk thins due to photoevaporation.

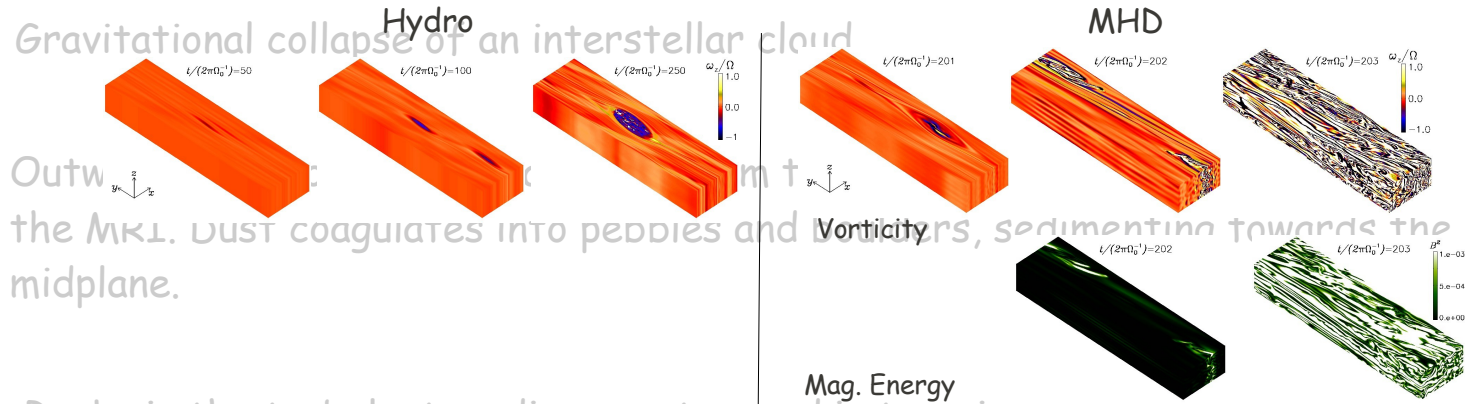
N-body interactions and stochasticity shape the system's final architecture.





Summarizing

Gravitational collapse of an interstellar cloud



Rocks in the turbulent medium are trapped in transient pressure maxima and undergo collapse into planetesimals and dwarf planets.

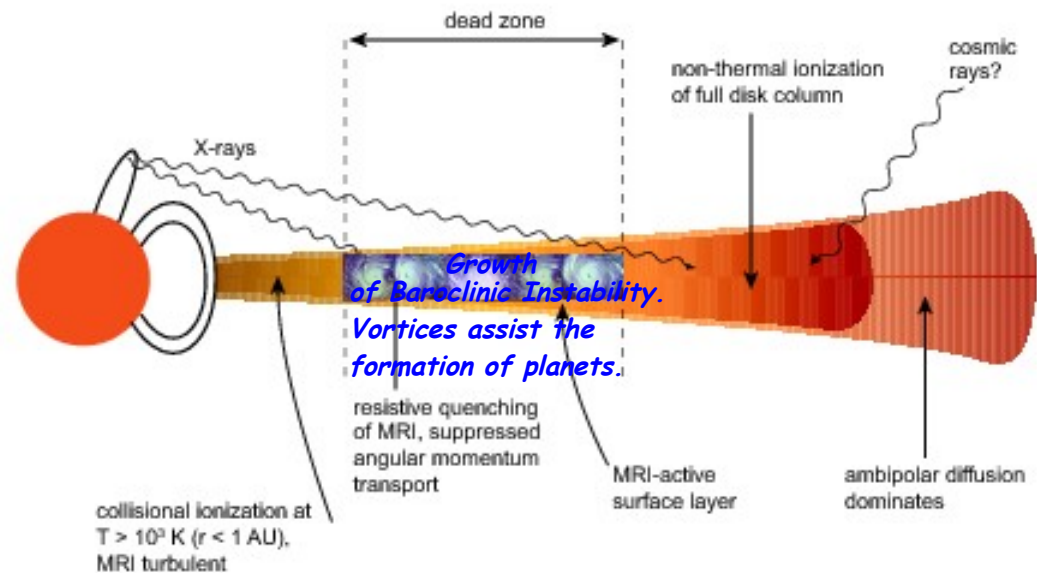
Vortices excited within the dead zone (BI). Inside them, the first dozens of Mars-mass embryos are formed TME ~ 2

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Summarizing

Gravitational collapse of an interstellar cloud

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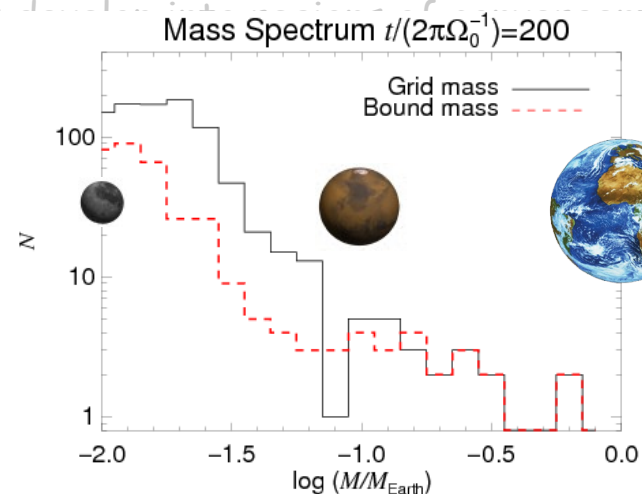
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Opacity transition
planets converge

Convergent migration
forcing. Collisions

The disk thins due

N-body interactions
the system's final architecture.

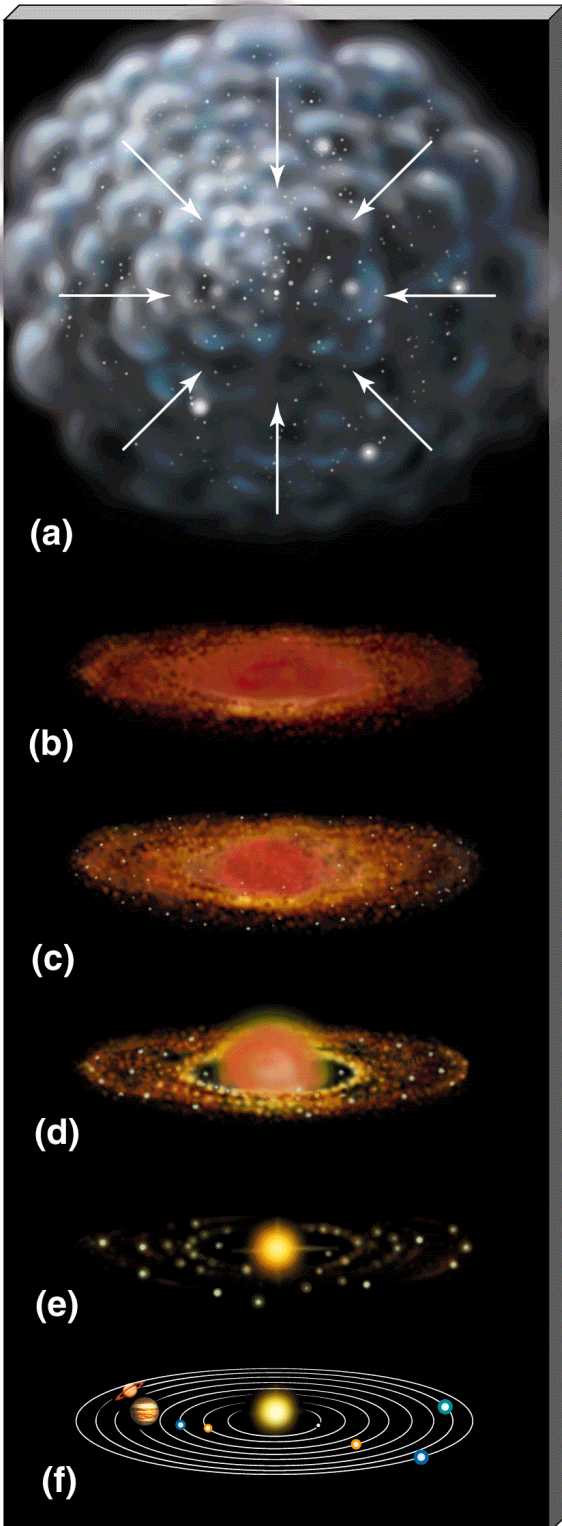


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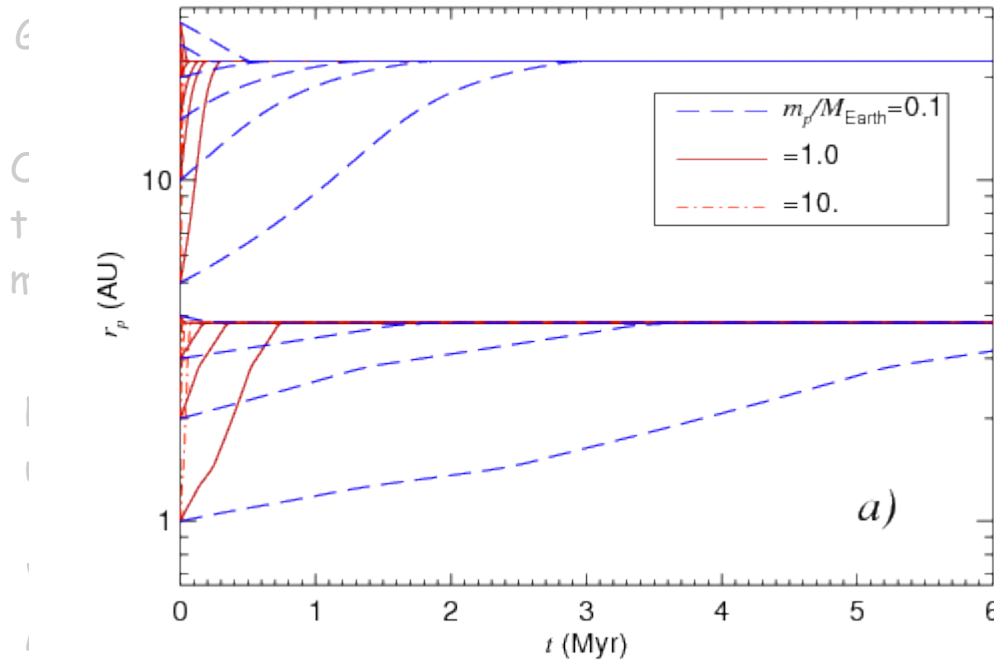
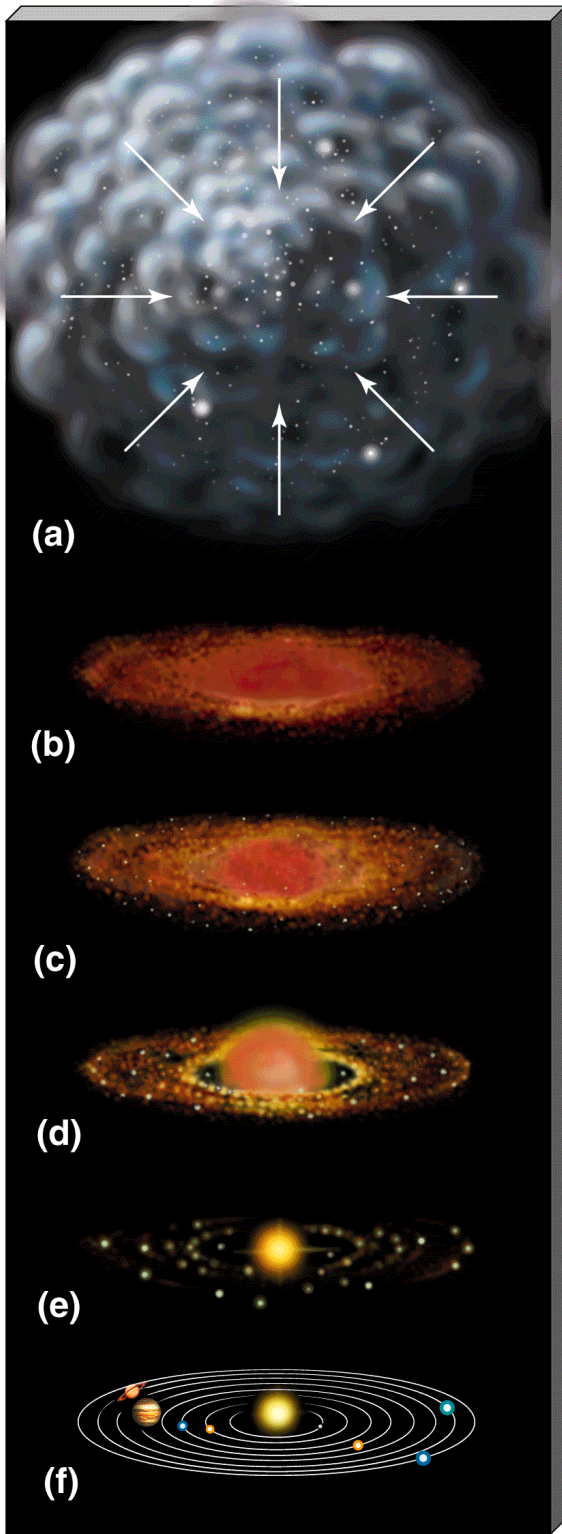
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Summarizing



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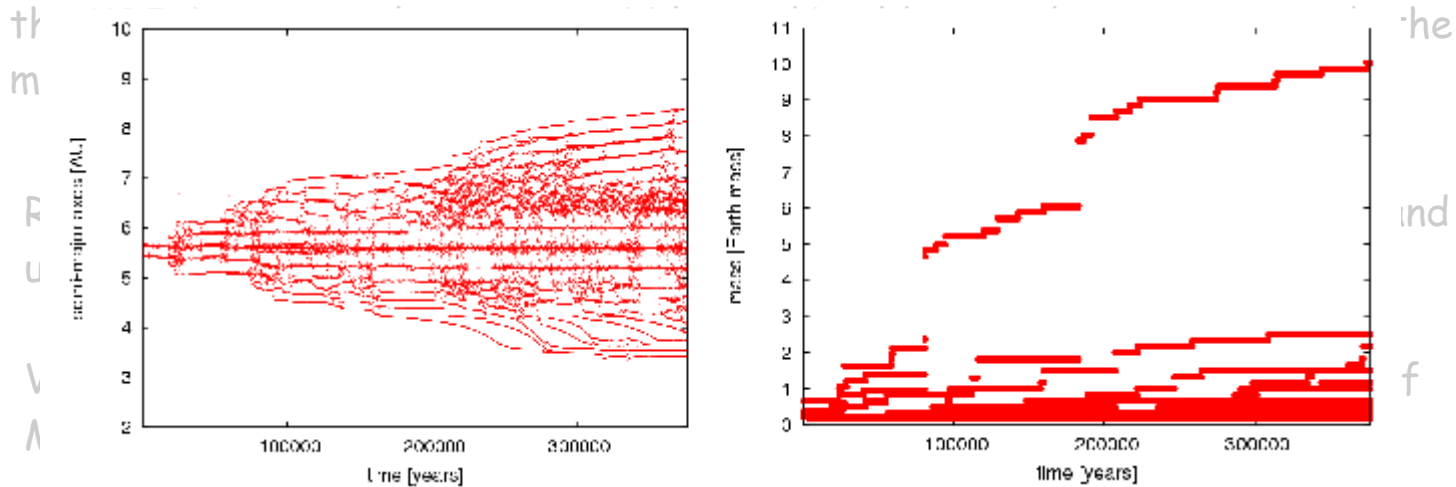
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Summarizing

Gravitational collapse of an interstellar cloud

Outward transport of angular momentum through turbulence generated by

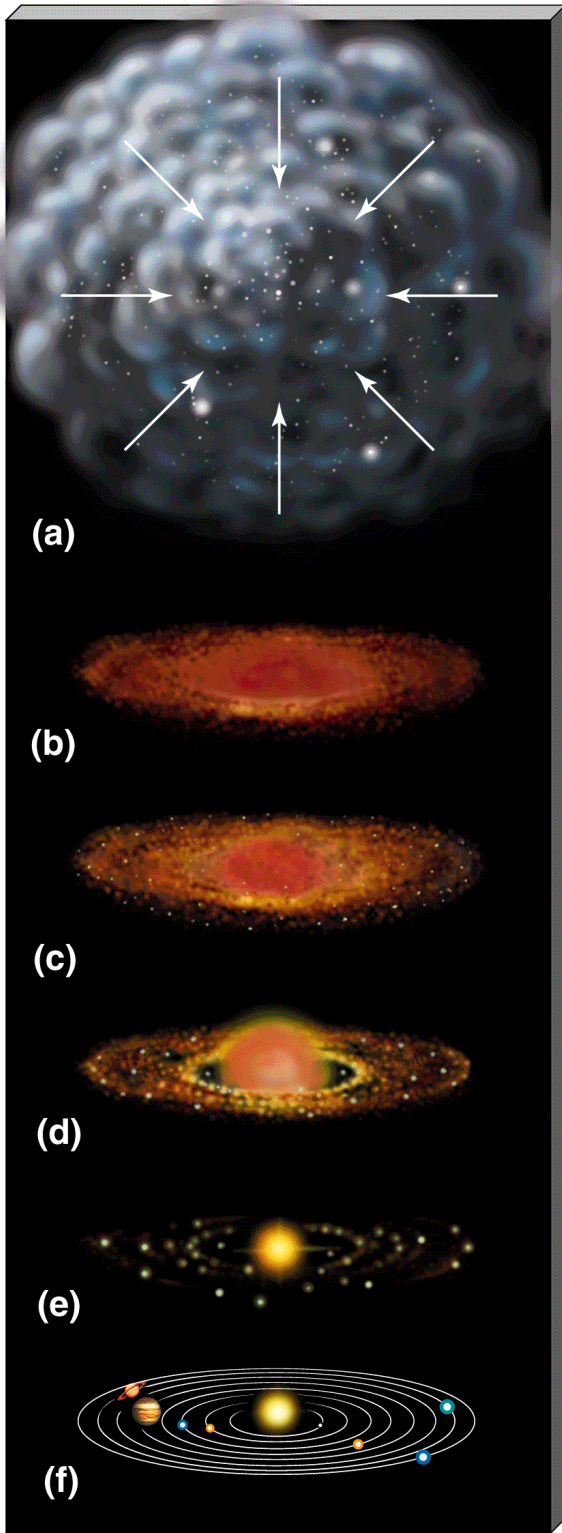


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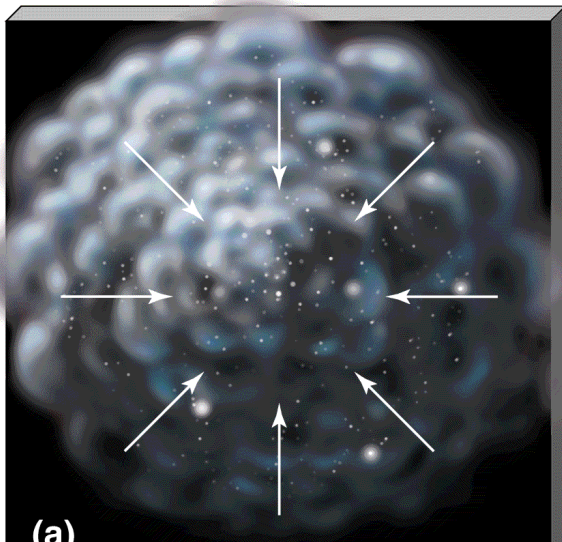
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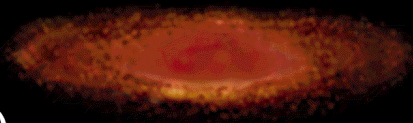
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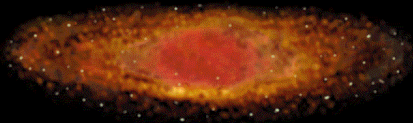
Summarizing



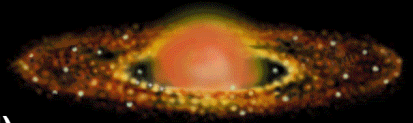
(a)



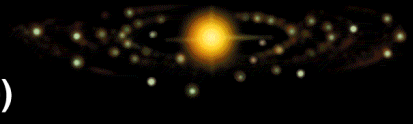
(b)



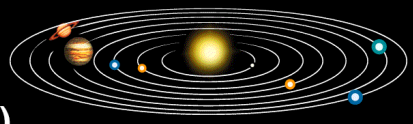
(c)



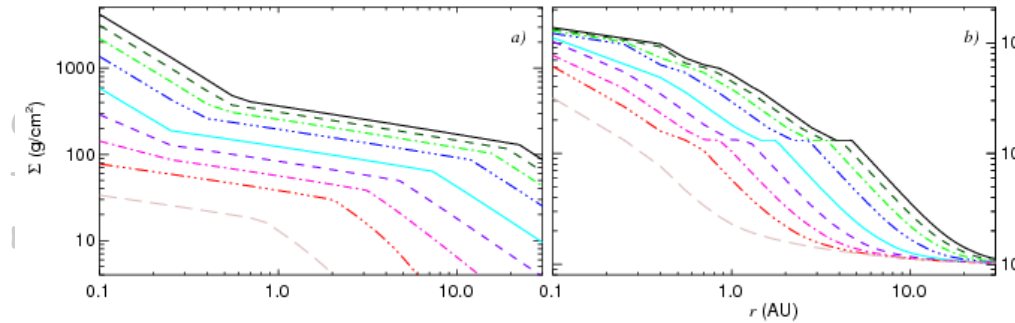
(d)



(e)



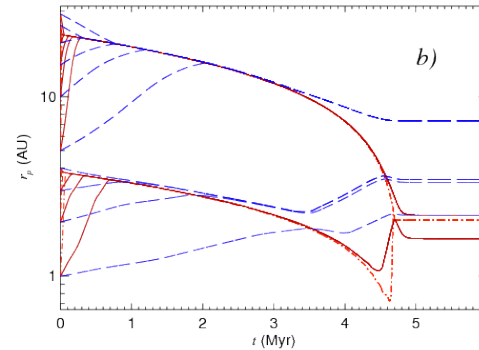
(f)



Rocks in the turbulent medium are trapped in transient zones and undergo collision and accretion to form dwarf planets.

Vortices migrate inward and trap Mars-mass embryos. Inside these zones, the surface density is enhanced by a factor of $\sim 10^{-2}$.

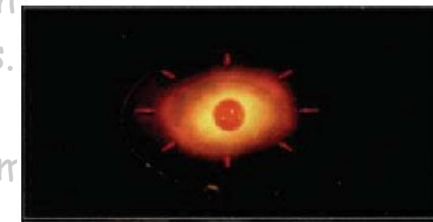
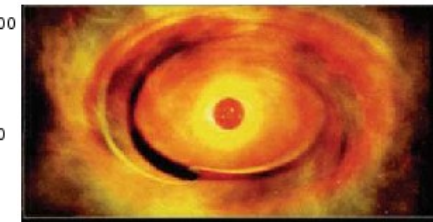
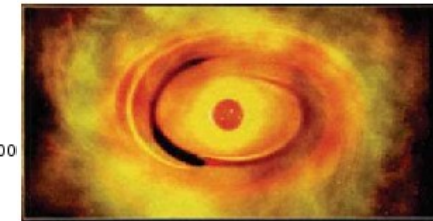
Opacity transitions create zones of convergent migration where planets converge to these zones by inward/outward migration.



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N-body interactions and stochastic forcing during disk evaporation produce the system's final architecture.



Summarizing

Gravitational collapse of an interstellar cloud

Outward
the MR
midplane

Rocks
undergo

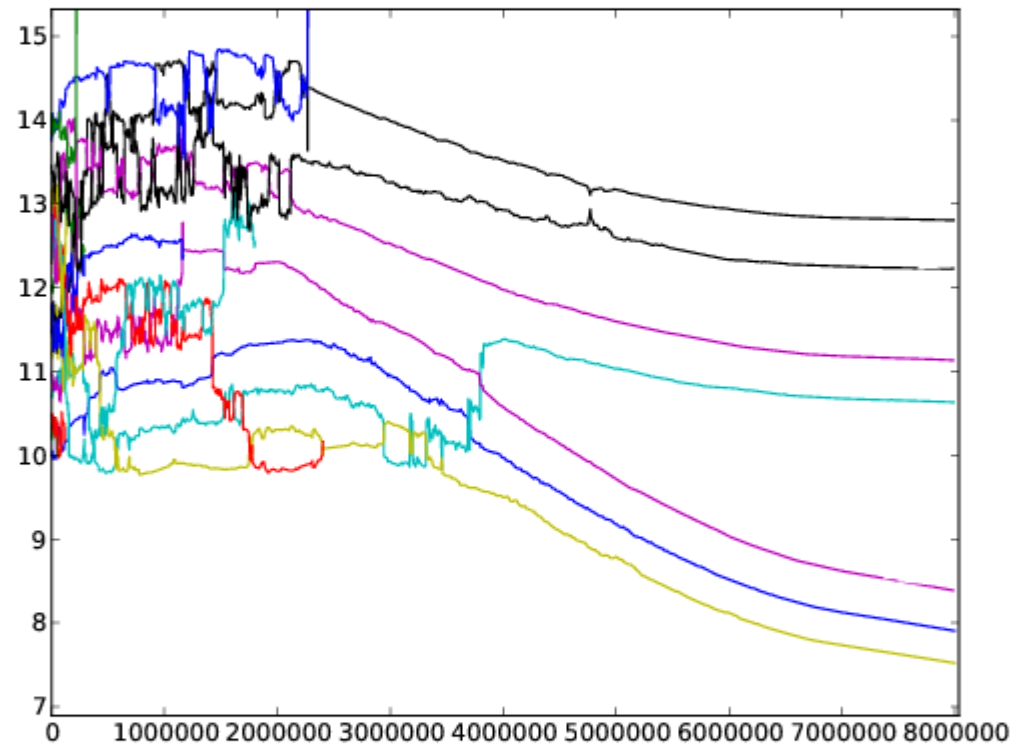
Vortices
Mars-size

Opacity
planet-size

Convergent
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