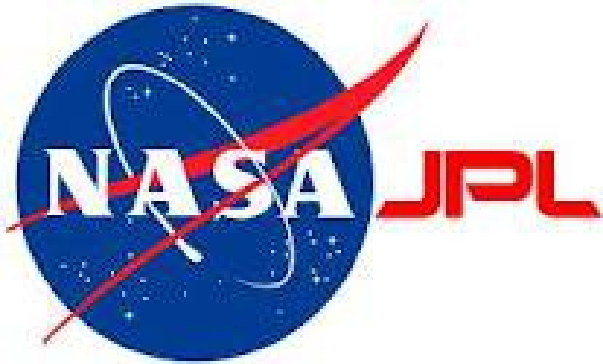


# The turbulent birth of planets



**Wladimir Lyra**

Carl Sagan Fellow

NASA/JPL-Caltech

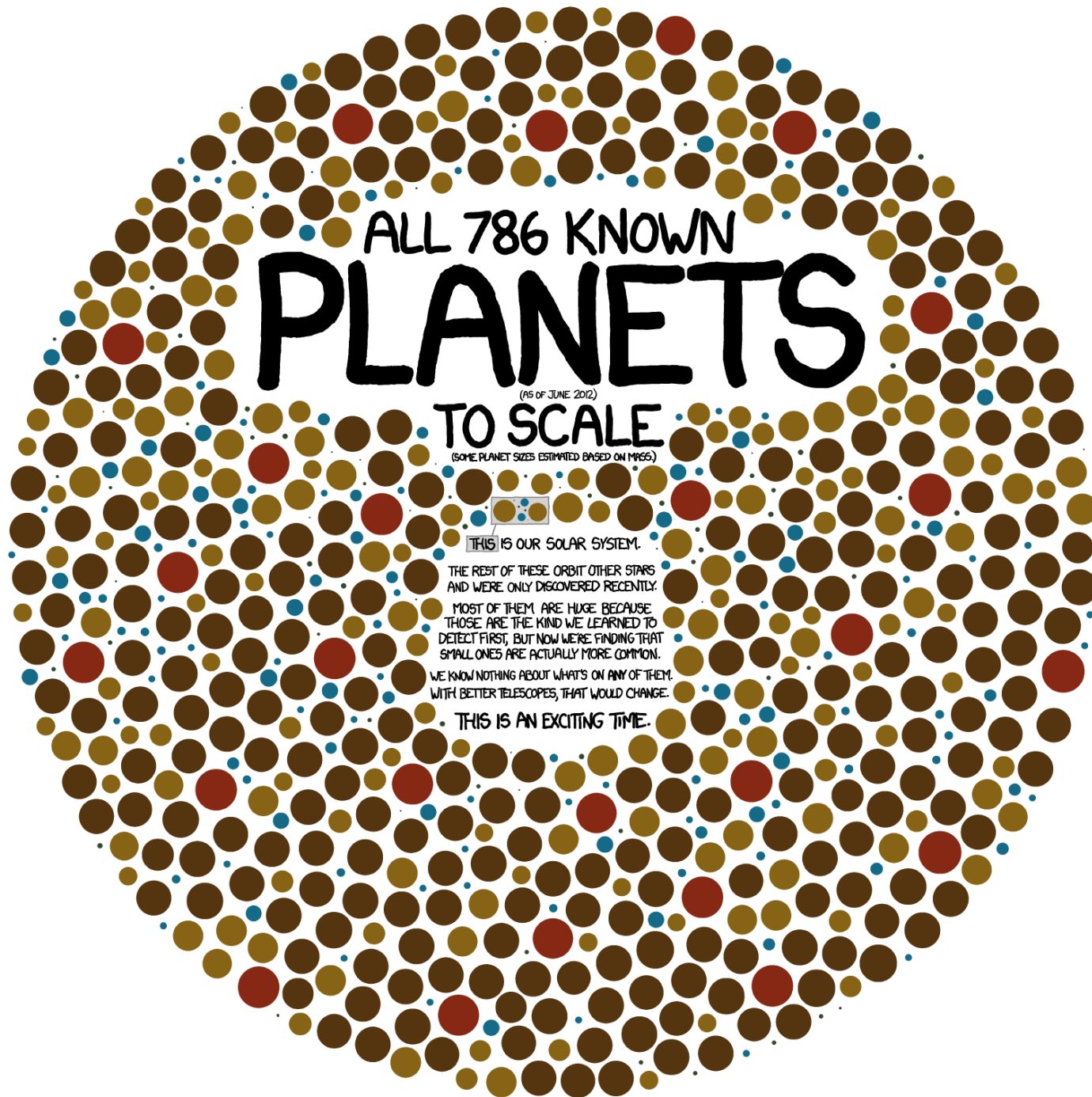


Ottawa, October 2012

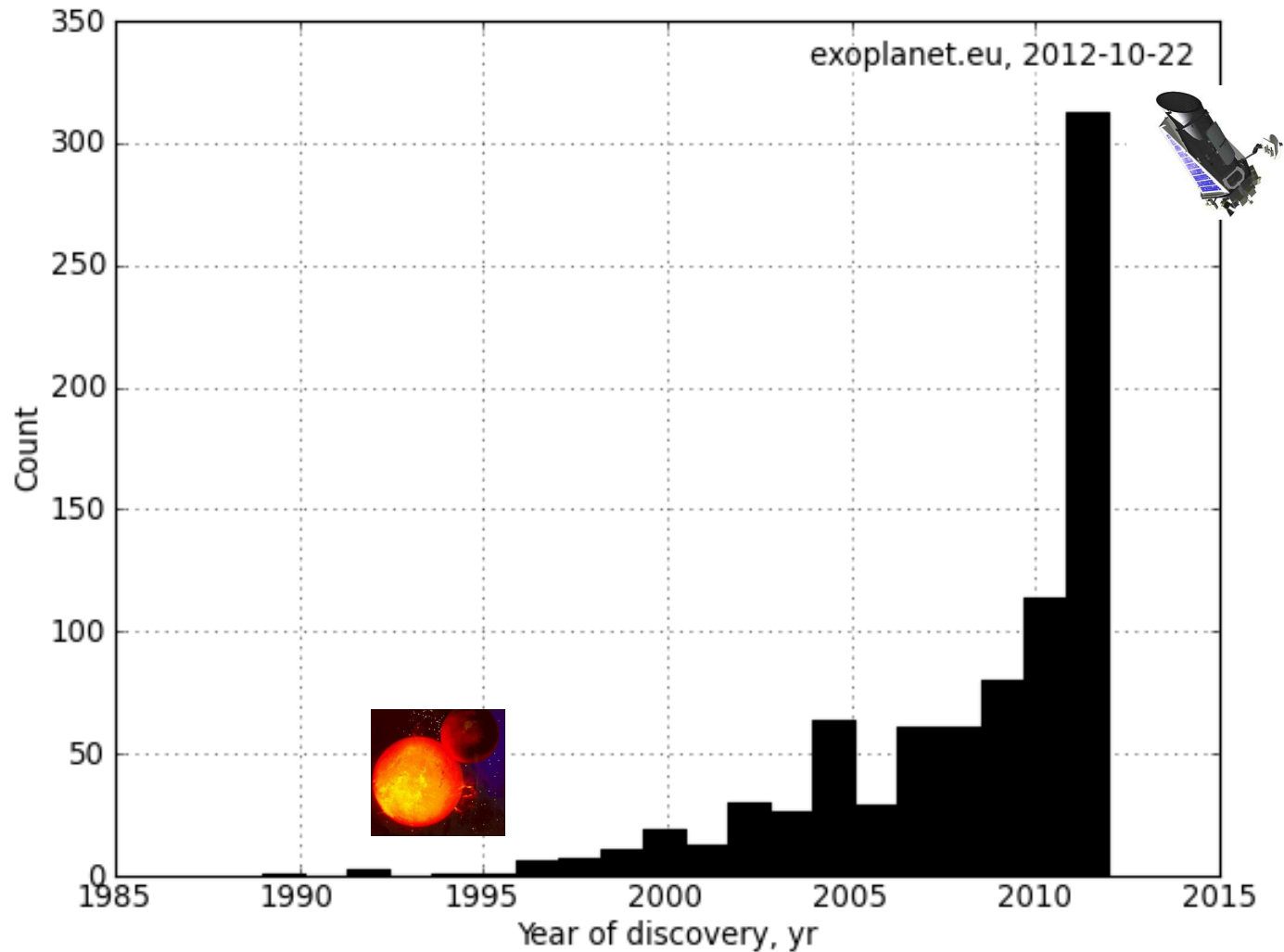
Collaborators:

Axel Brandenburg (Stockholm), Kees Dullemond (Heidelberg), Mario Flock (Paris),  
Sebastien Fromang (Paris), Anders Johansen (Lund), Brandon Horn (Columbia),  
Hubert Klahr (Heidelberg), Marc Kuchner (NASA-Goddard), Mordecai Mac Low (AMNH),  
Sijme-Jan Paardekooper (Cambridge), Nikolai Piskunov (Uppsala), Natalie Raettig  
(Heidelberg), Zsolt Sandor (Innsbruck), Neal Turner (JPL), Andras Zsom (MIT).

# Exoplanets



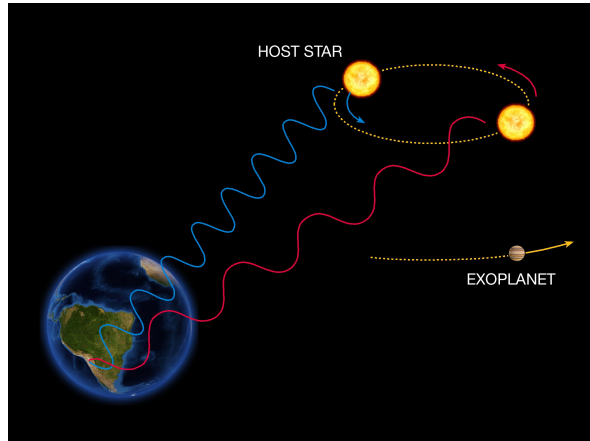
# Exoplanets



843 confirmed planets, and counting!  
(Maybe already 844 until the end of this talk....)

# Exoplanets

## Detection methods

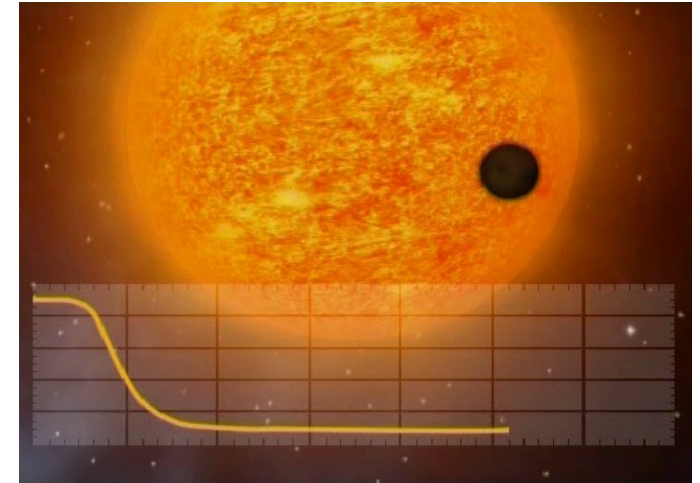


The Radial Velocity Method

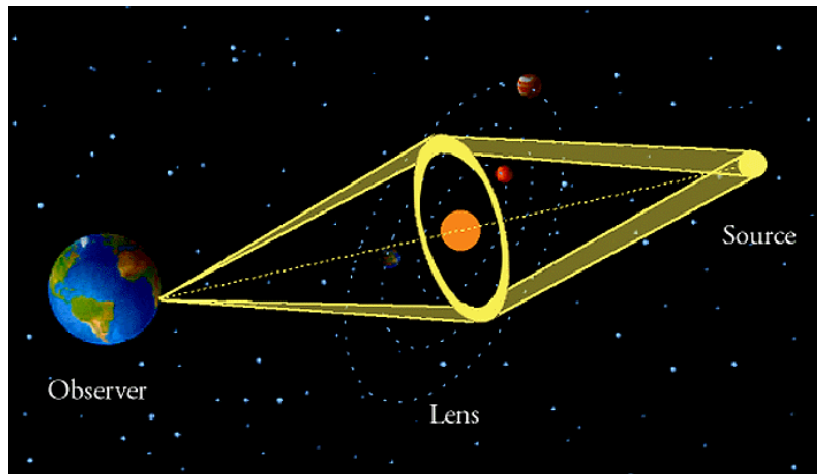
ESO Press Photo 22e/07 (25 April 2007)  
This image is copyright © ESO. It is released in connection with an ESO press release and may be used by the press on the condition that the source is clearly indicated in the caption.



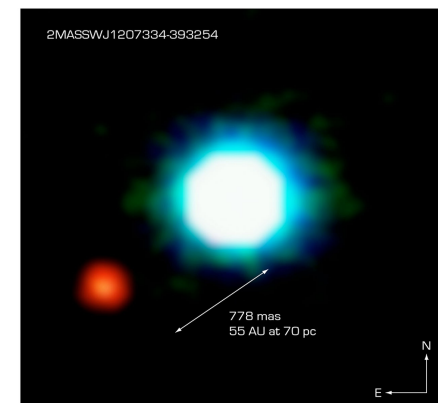
## Radial Velocity



## Transit



## Microlensing



NACO Image of the Brown Dwarf Object 2M1207 and GPCC

ESO PR Photo 26a/04 (10 September 2004)

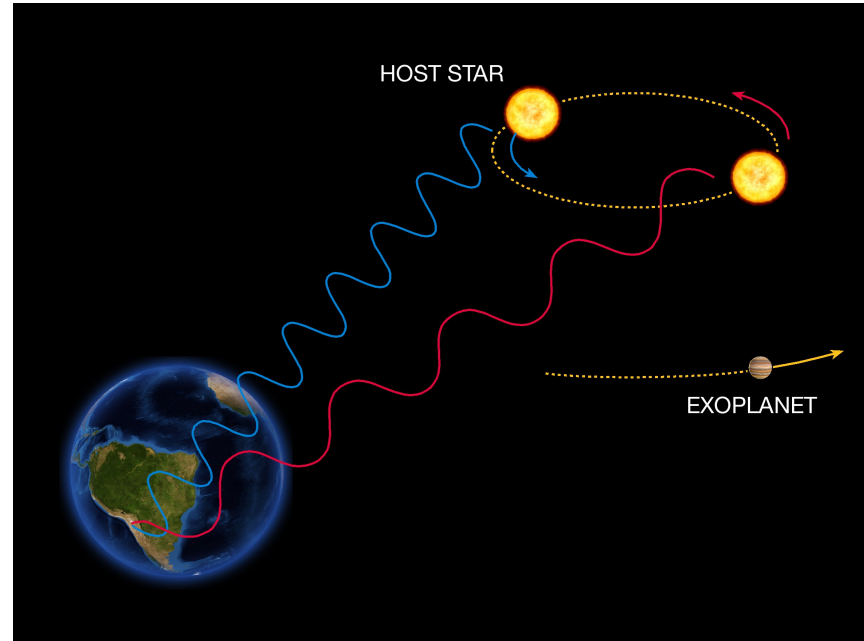
© European Southern Observatory



## Direct Imaging



# Exoplanets - Radial Velocity



The Radial Velocity Method

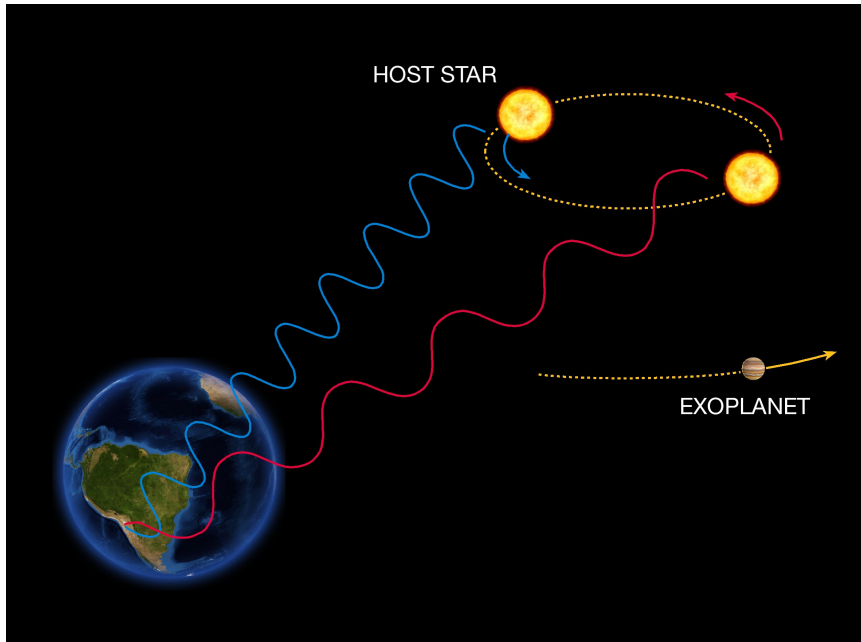
ESO Press Photo 22e/07 (25 April 2007)

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Star and planet orbit a  
common center of mass

# Exoplanets - Radial Velocity



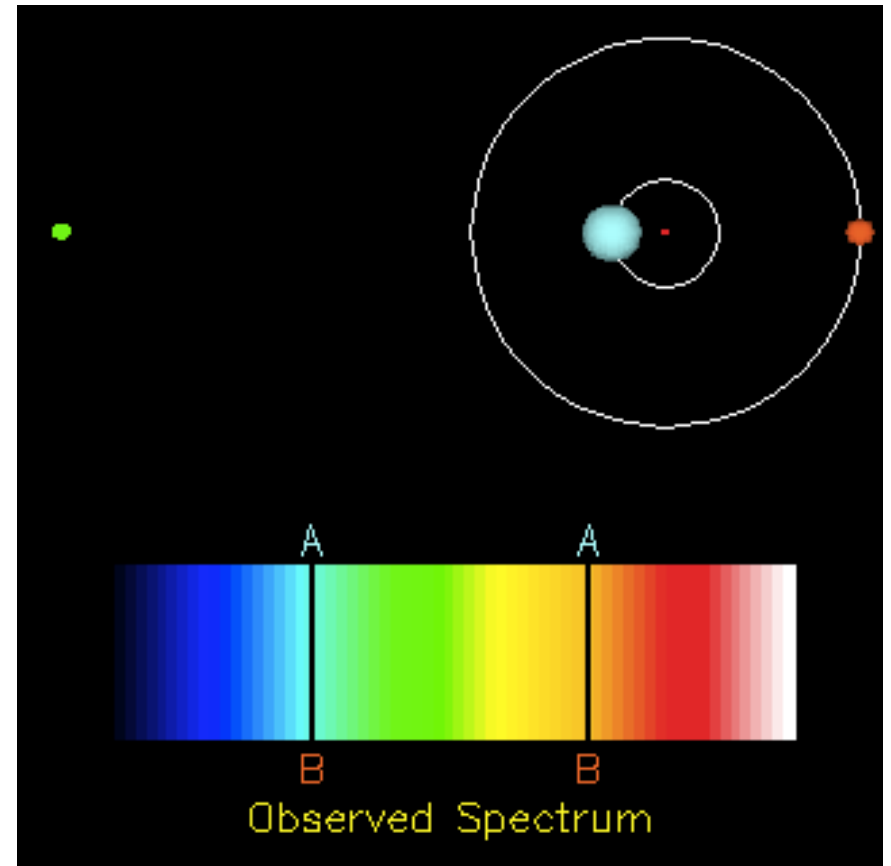
The Radial Velocity Method

ESO Press Photo 22e/07 (25 April 2007)

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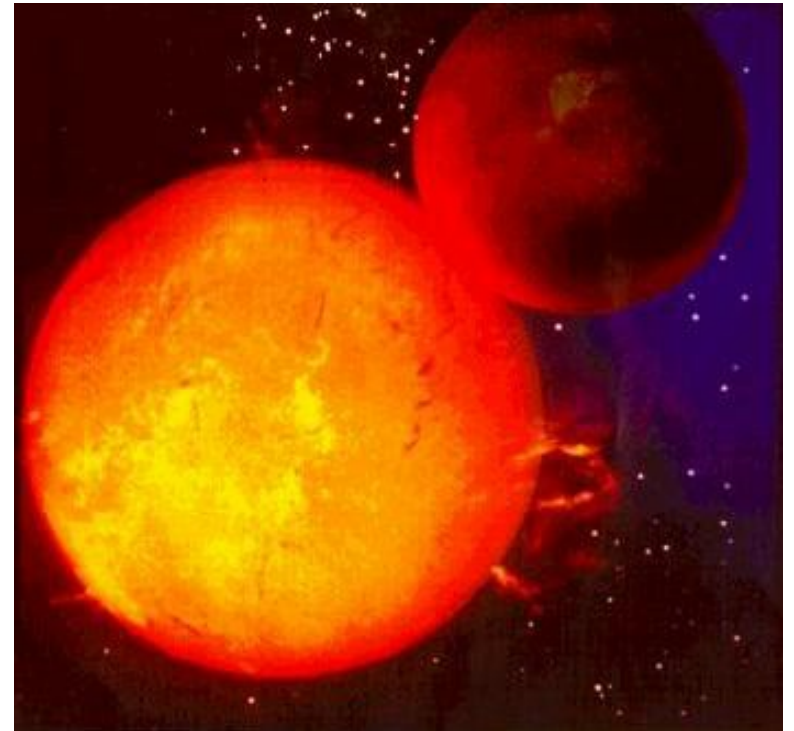
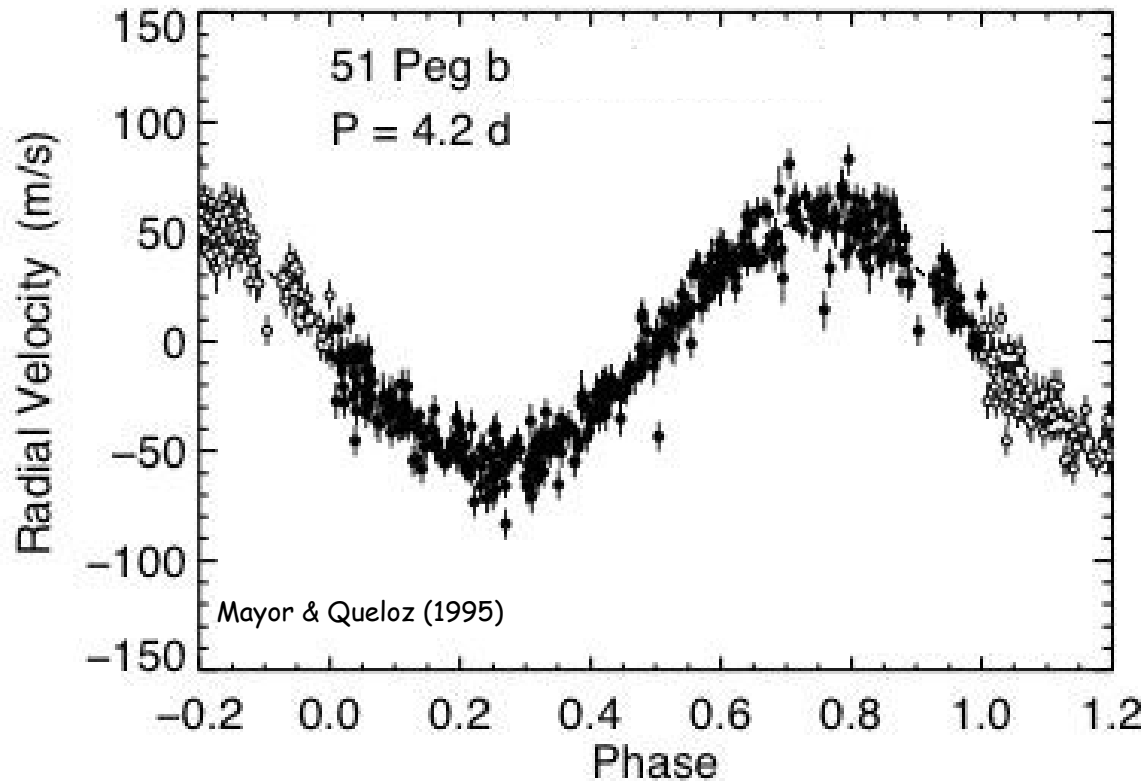
Star and planet orbit a  
common center of mass



Even if we cannot see the planet,  
we can measure the motion of the star

# 51 Pegasi b

The first exoplanet around a solar-type star



$$M \sin i = 0.472 \pm 0.039 M_J$$

$$T_{eq} = 1284 \pm 19 \text{ K}$$

*A Hot Jupiter !!*

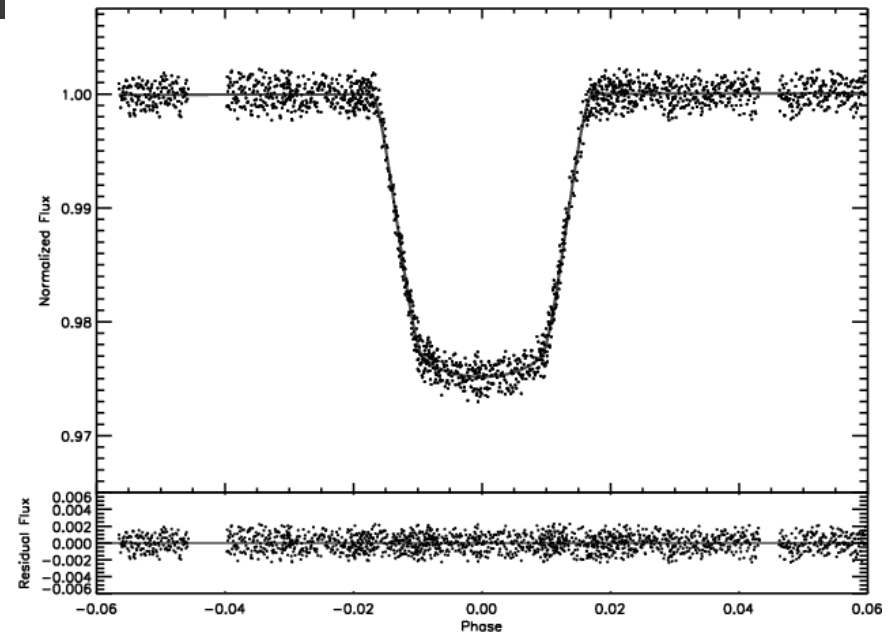
# Exoplanets - Transit



The planet transits the star if the orientation of the orbit is favorable

A Jupiter-size planet produces a flux dip at the 0.01 level.

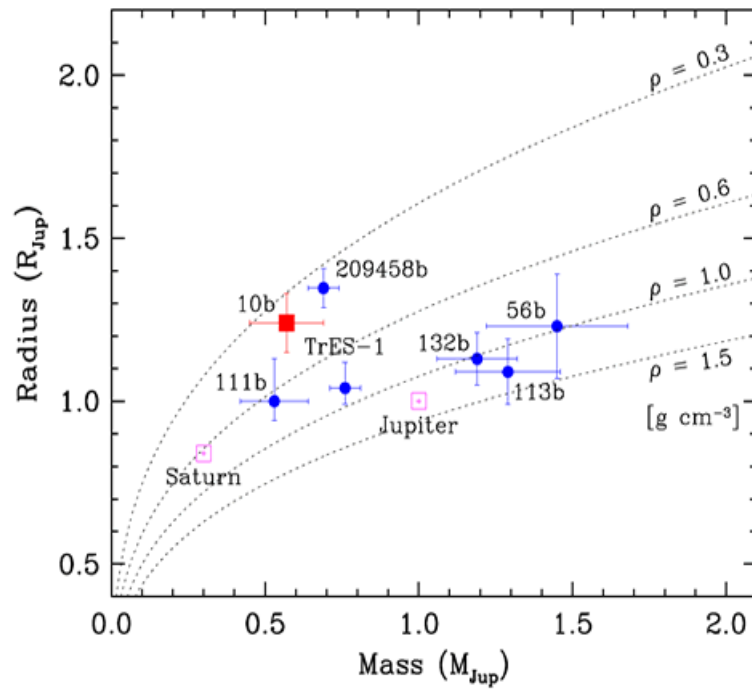
**Detectable!!**



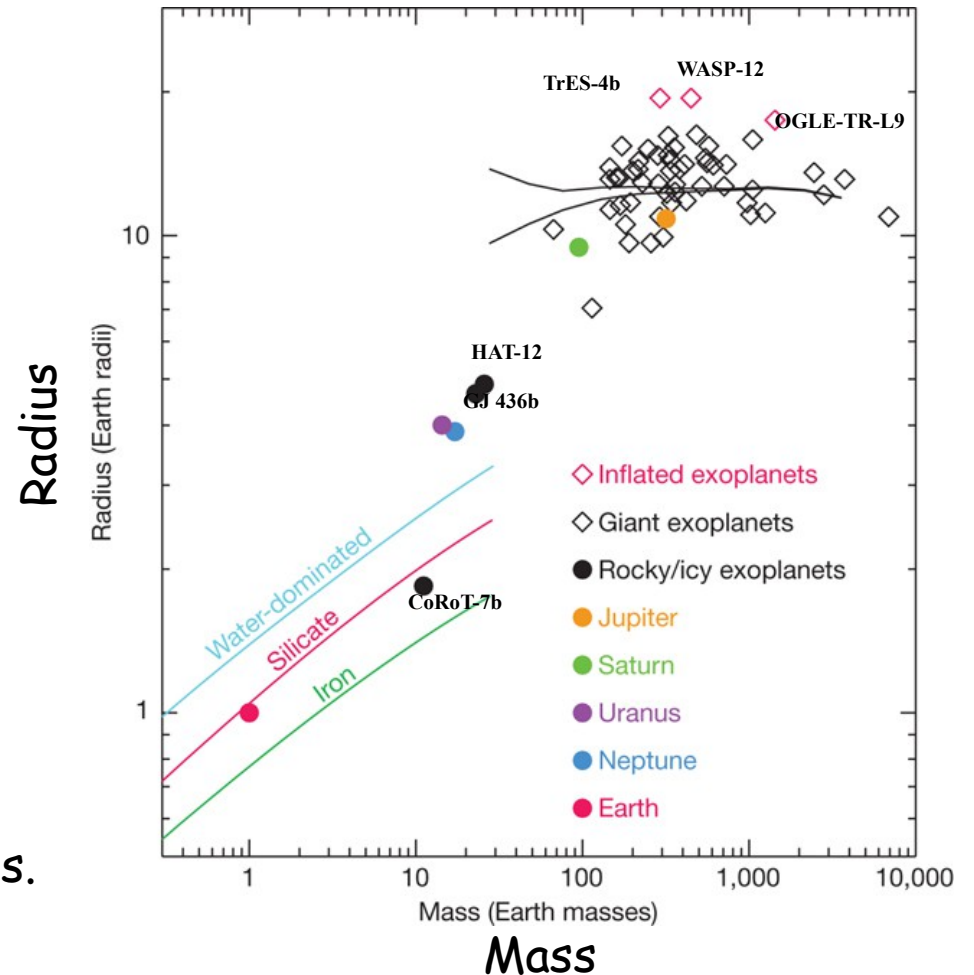
# Exoplanets - Transit

Transits allow for determination of both mass and radius!

We can measure **densities**...

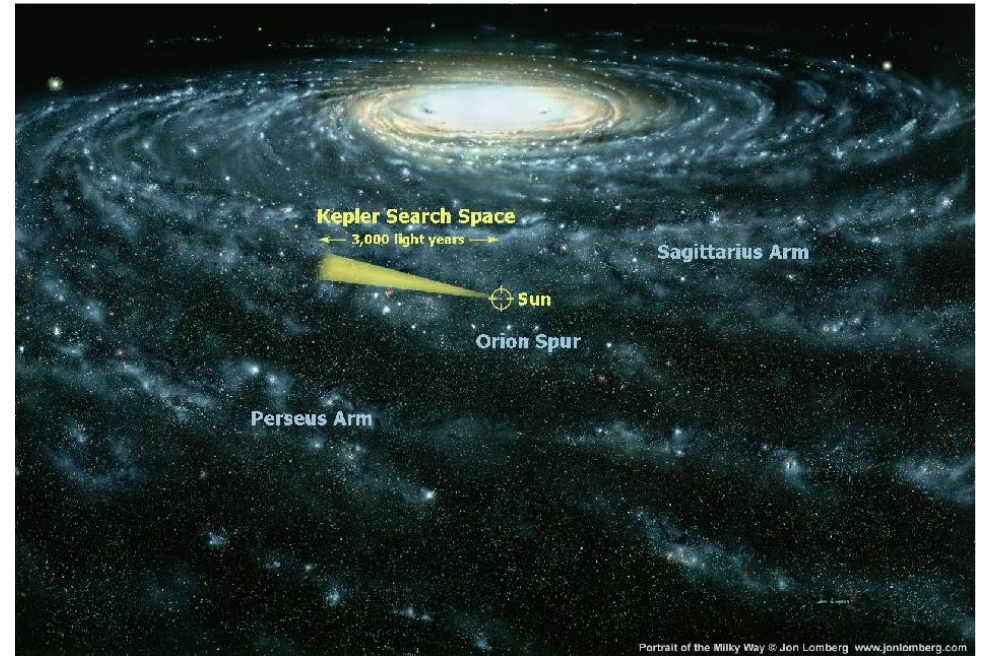
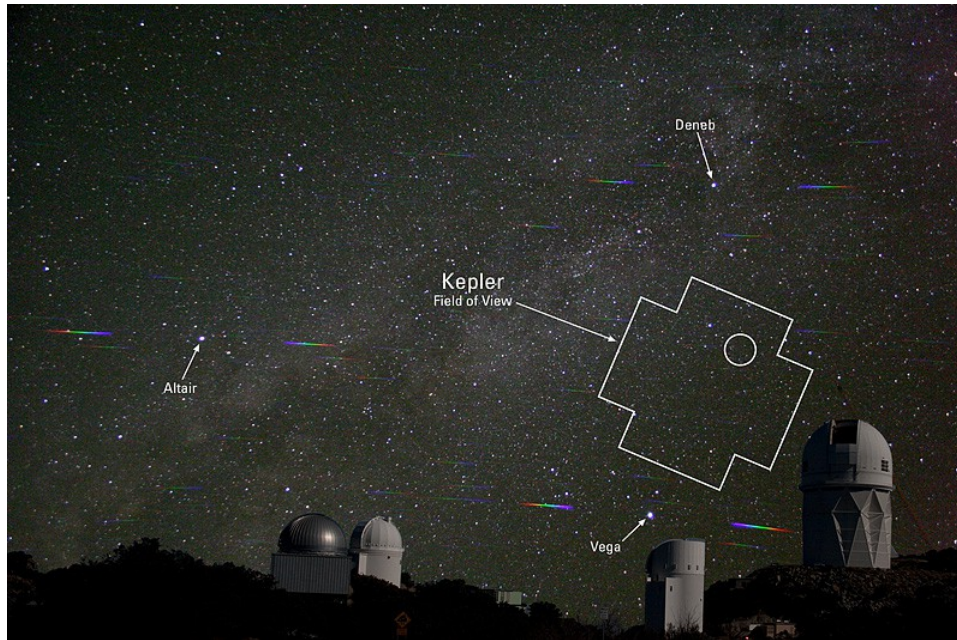


... and make educated guesses about **composition and structure** of the planets.

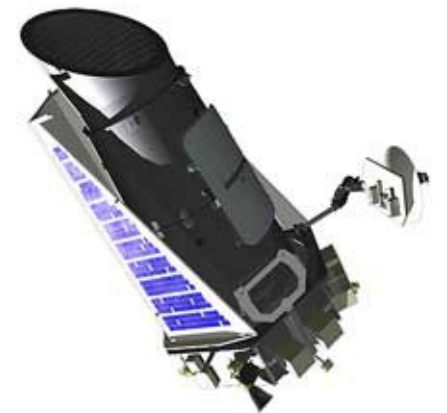




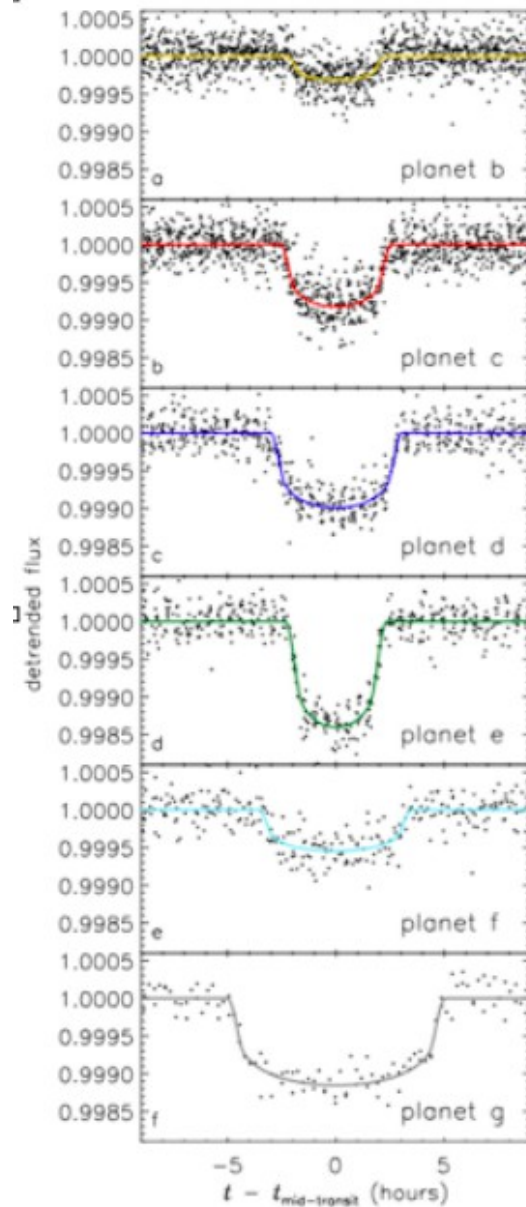
# Kepler mission



Continuously observe a single area of the sky,  
**monitoring 150,000 stars for transits**



# Kepler mission



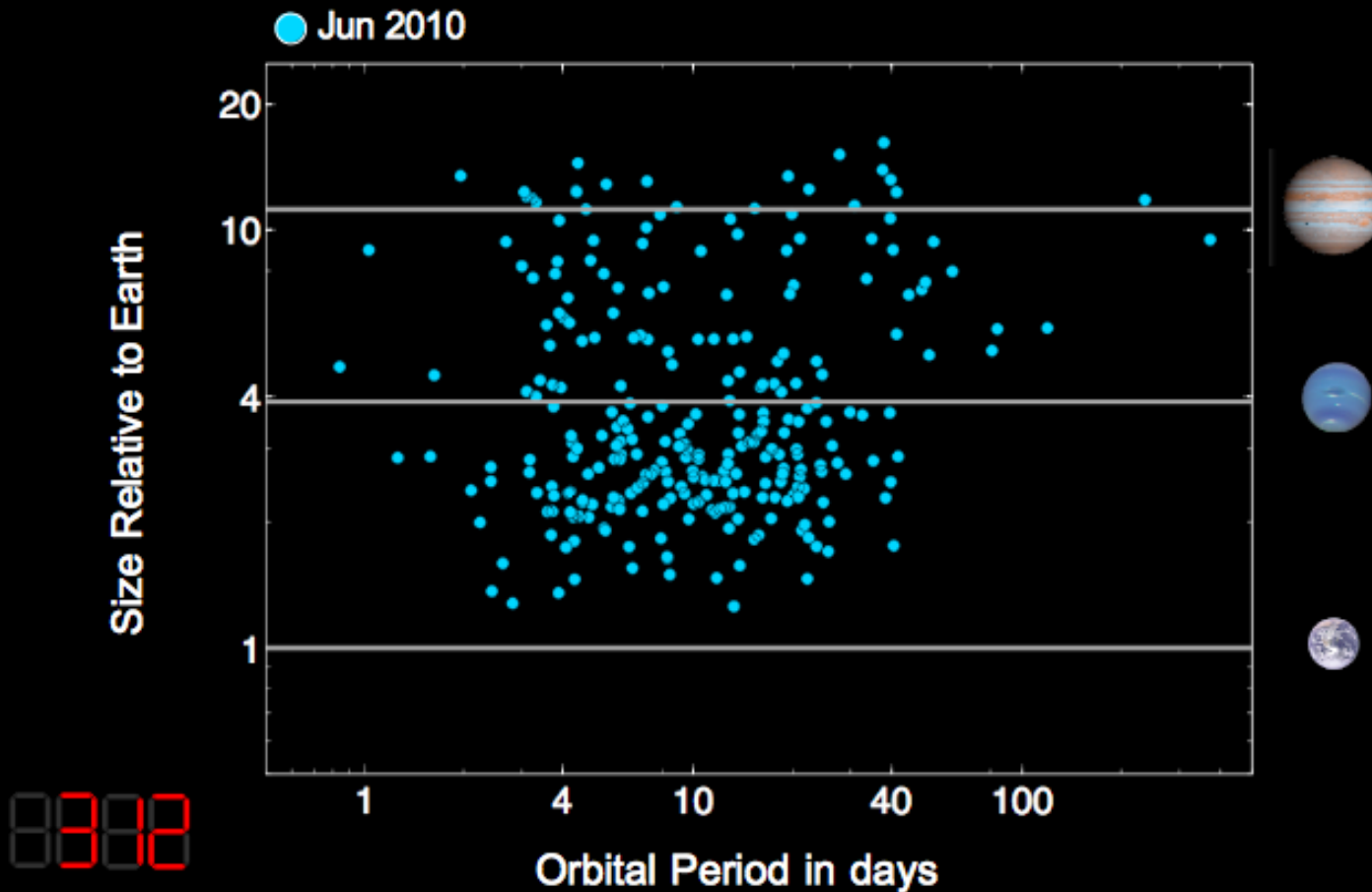
Photometry at  
 **$10^{-4}$**  precision



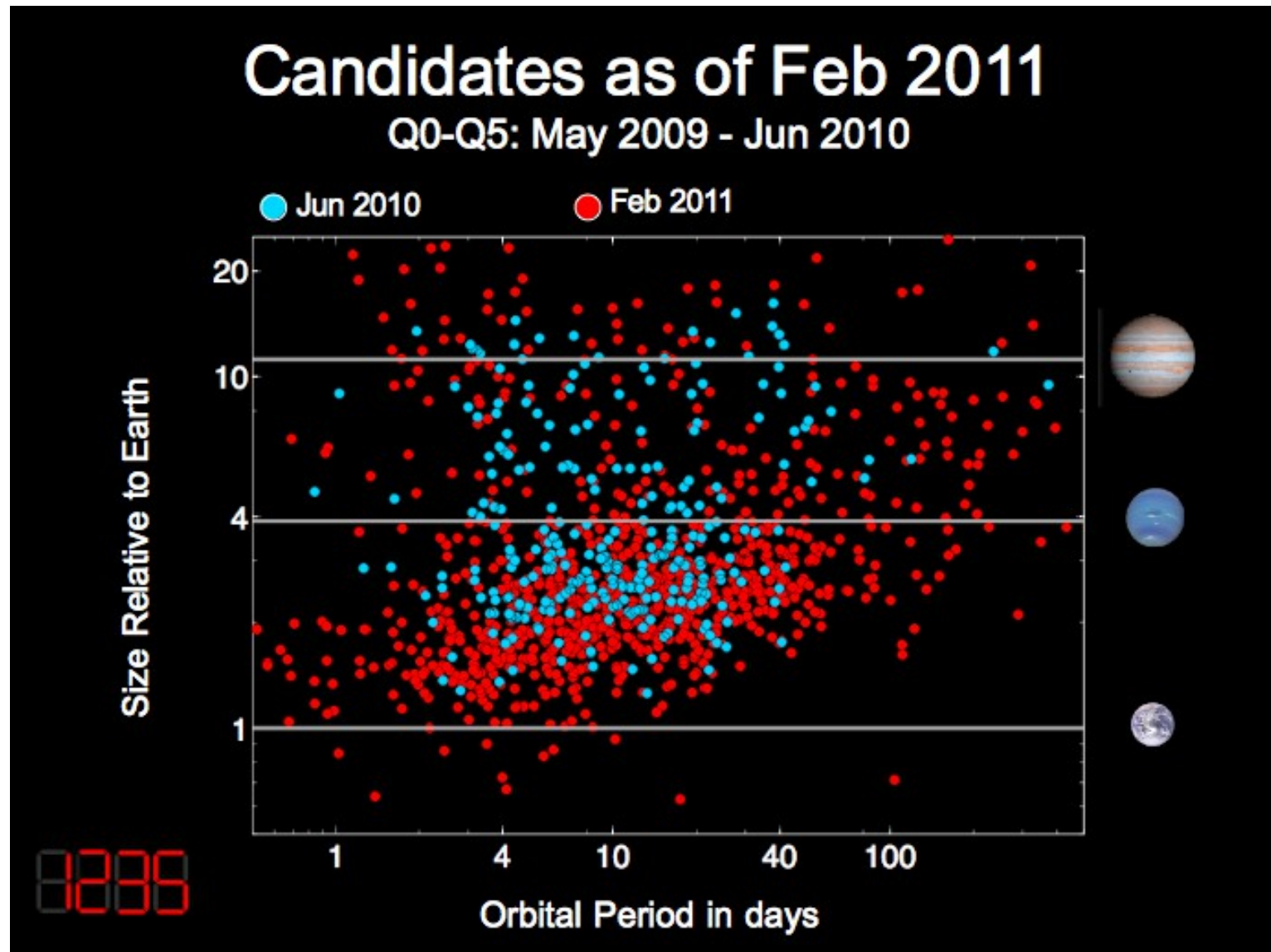
# Kepler mission

## Candidates as of June 2010

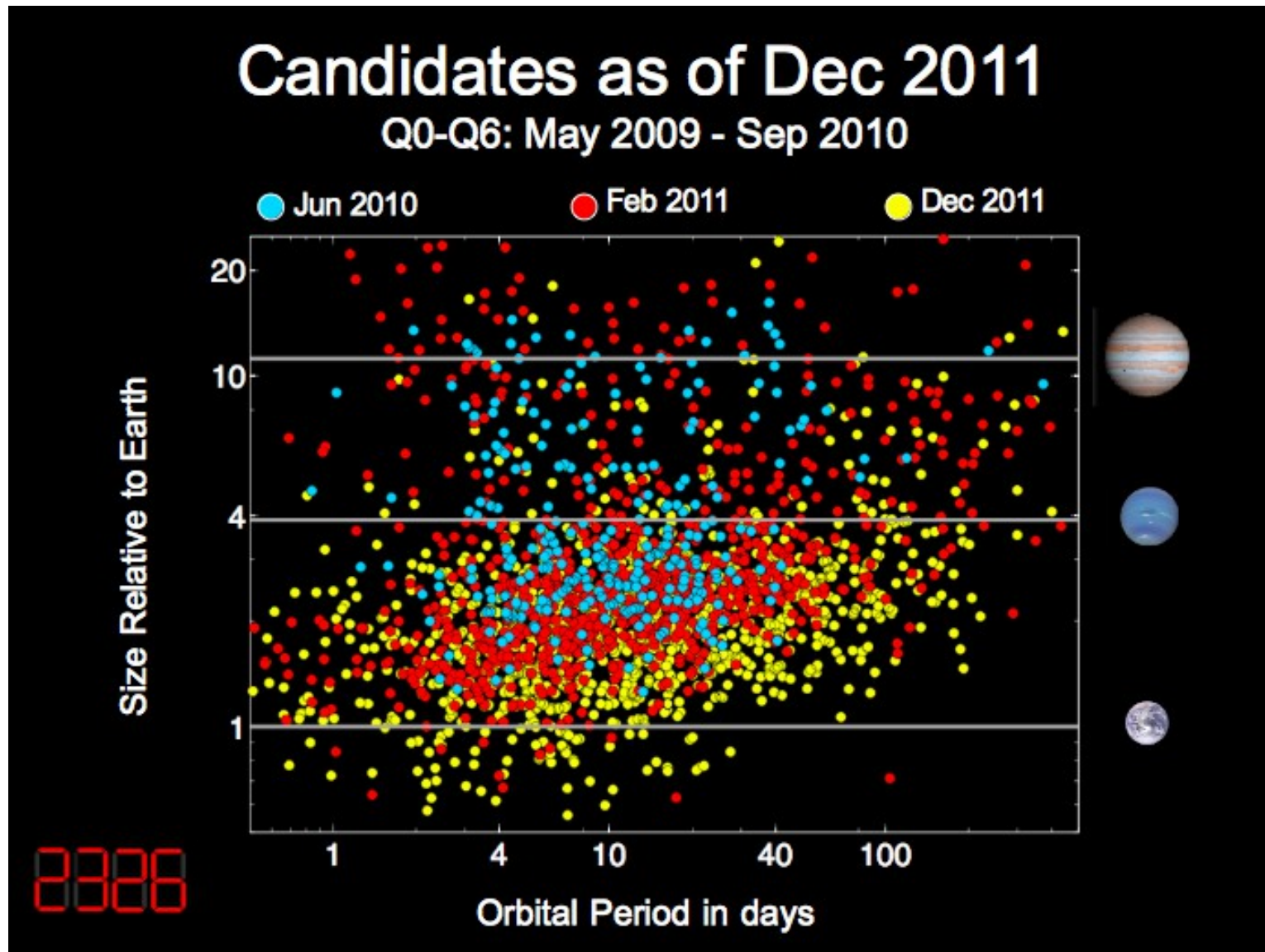
Q0-Q1: May-June 2009



# Kepler mission



# Kepler mission

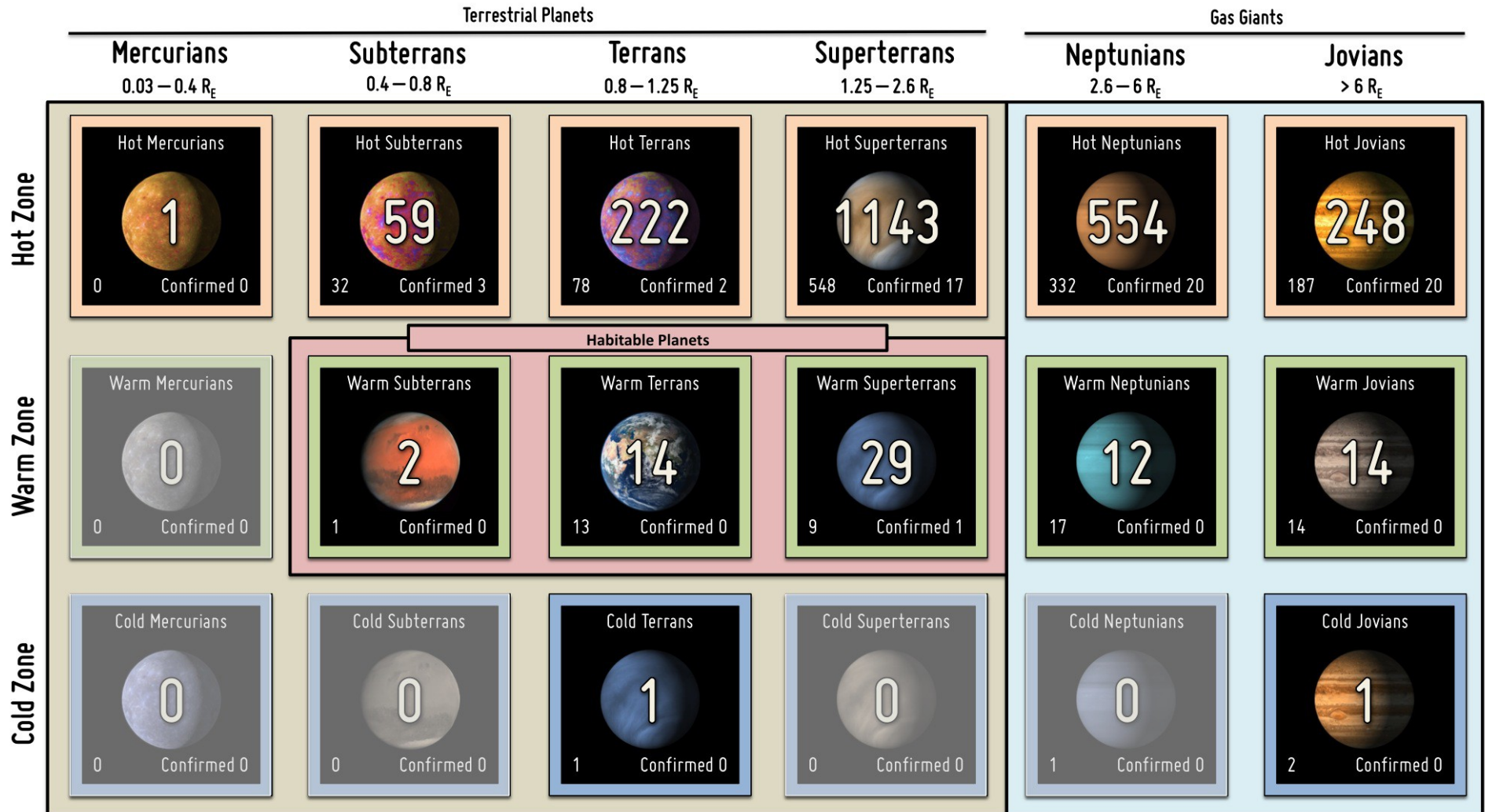


# Kepler mission

# Kepler's "periodic table" of planets

NASA Kepler 2,321 Exoplanet Candidates as of March 2012

The Habitable Exoplanets Catalog

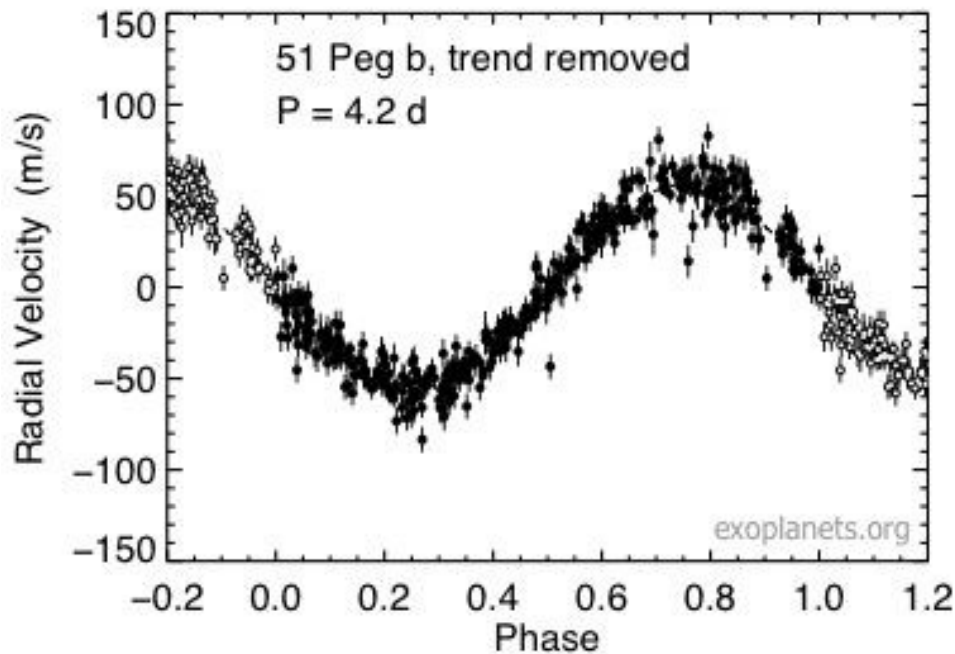




# Radial Velocity can still impress

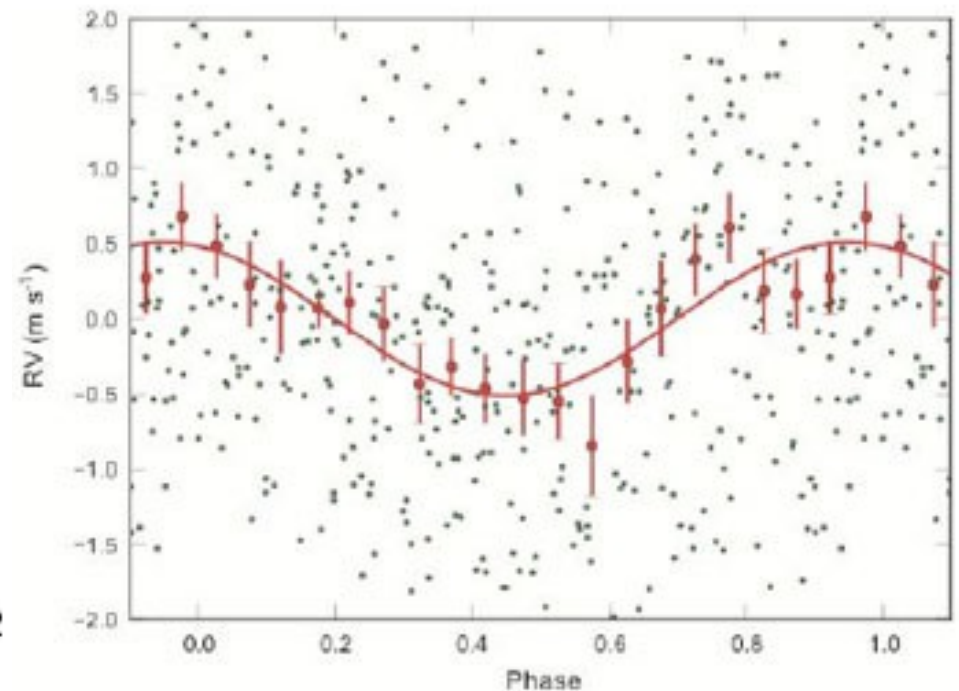


## *Alpha Centauri Bb*



The first RV exoplanet  
20 m/s precision

Mayor & Queloz (1995)



The latest RV exoplanet

**< 1 m/s precision**

Pepe et al. (2012)

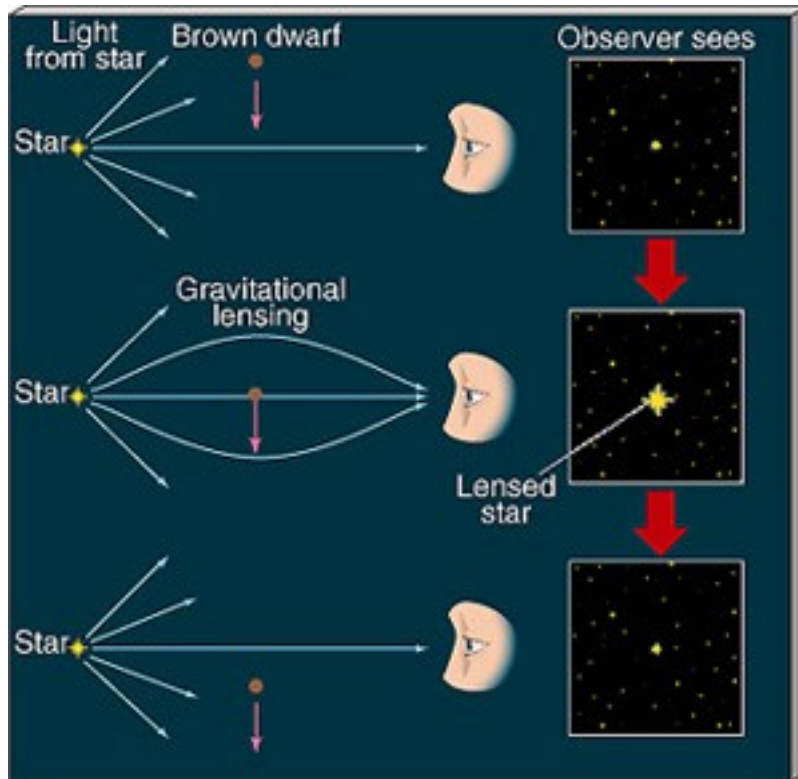
# Gravitational Lensing

Lensing Galaxy





# Exoplanets - Microlensing

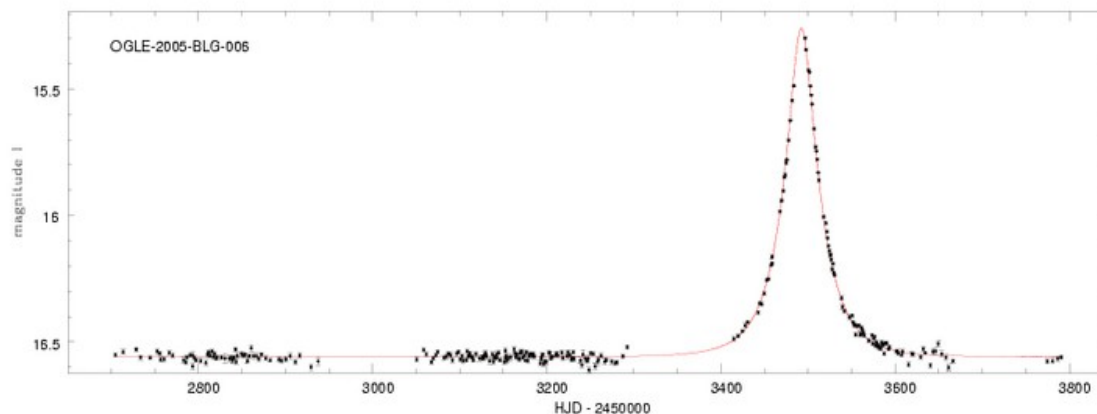


## **Microlensing**

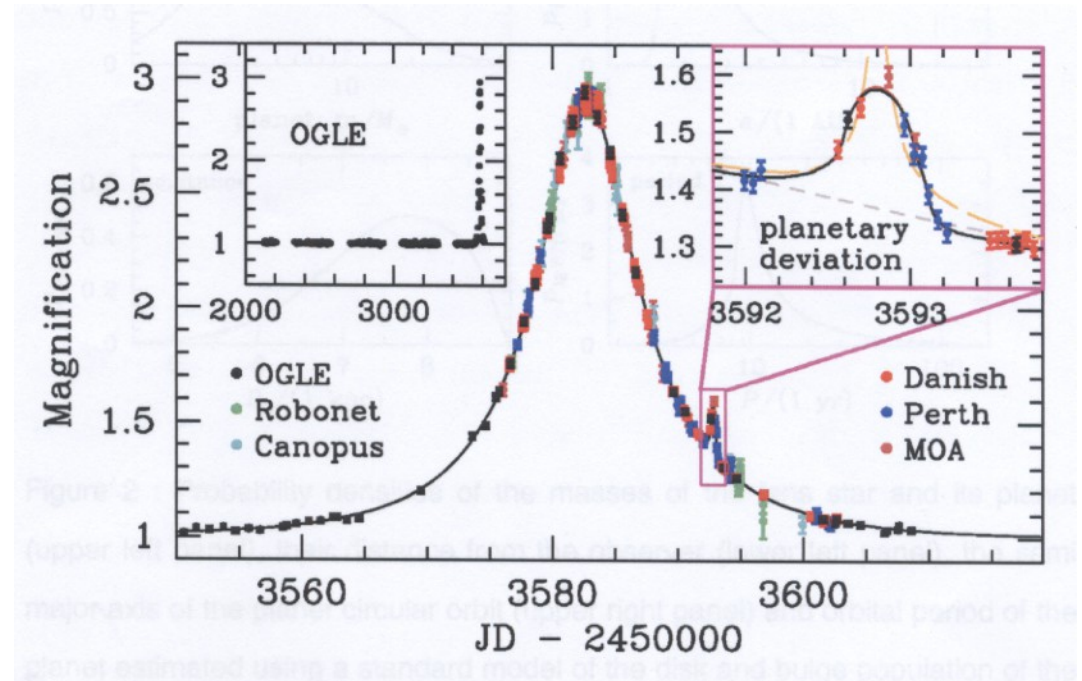
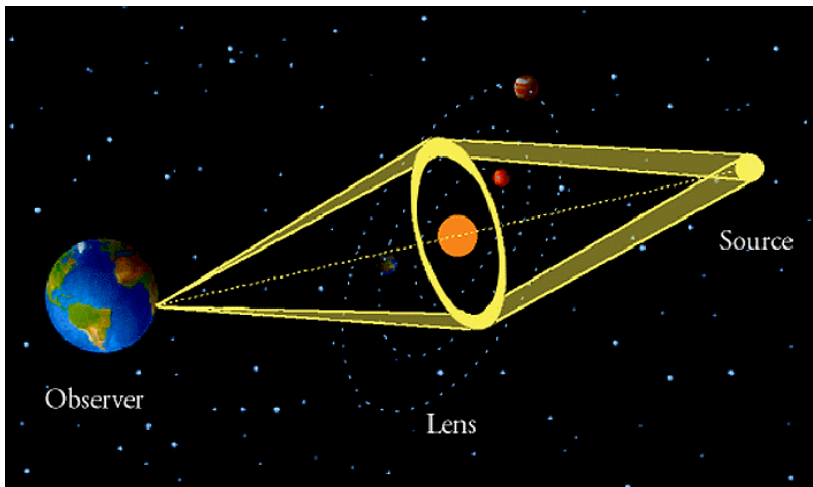
is a gravitational lensing event produced not by a galaxy but by a **star or substellar object**

We do not resolve the multiple images:  
They all appear blurred

**The lensing event is seen as a magnification of the lensed star.**



# Exoplanets - Microlensing



A **planet** around a lens star may produce a **secondary** lensing event

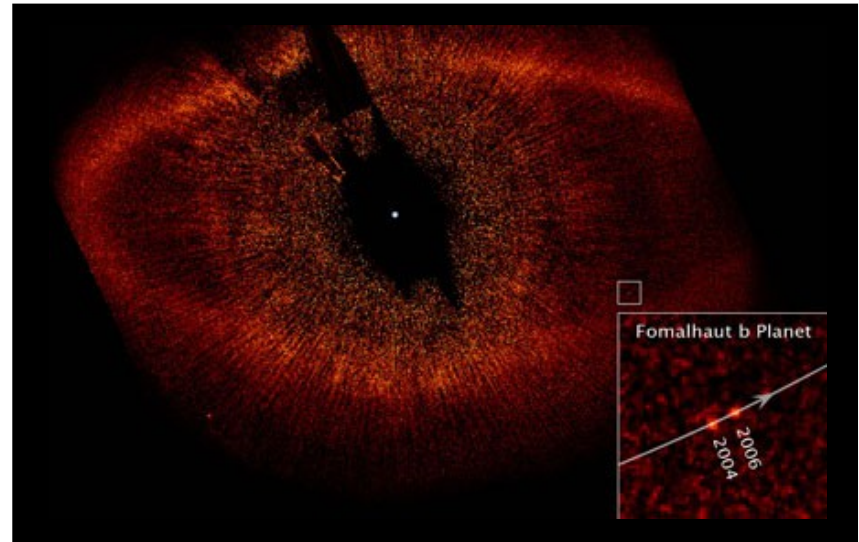
# Exoplanets - Direct Imaging

*A firefly next to a lighthouse*

Block the starlight  
and check the surroundings

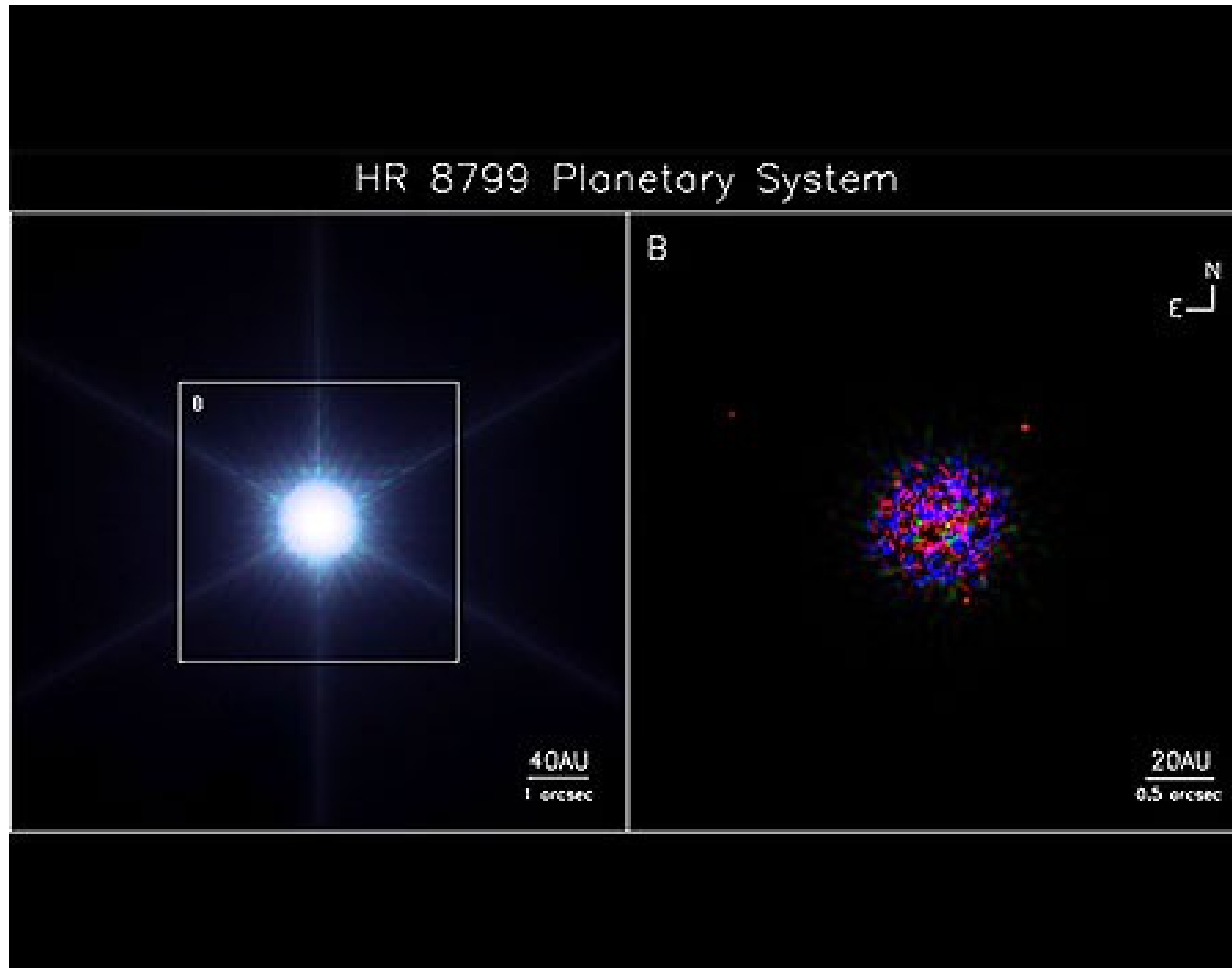


The bright star **Fomalhaut**  
8 parsecs away



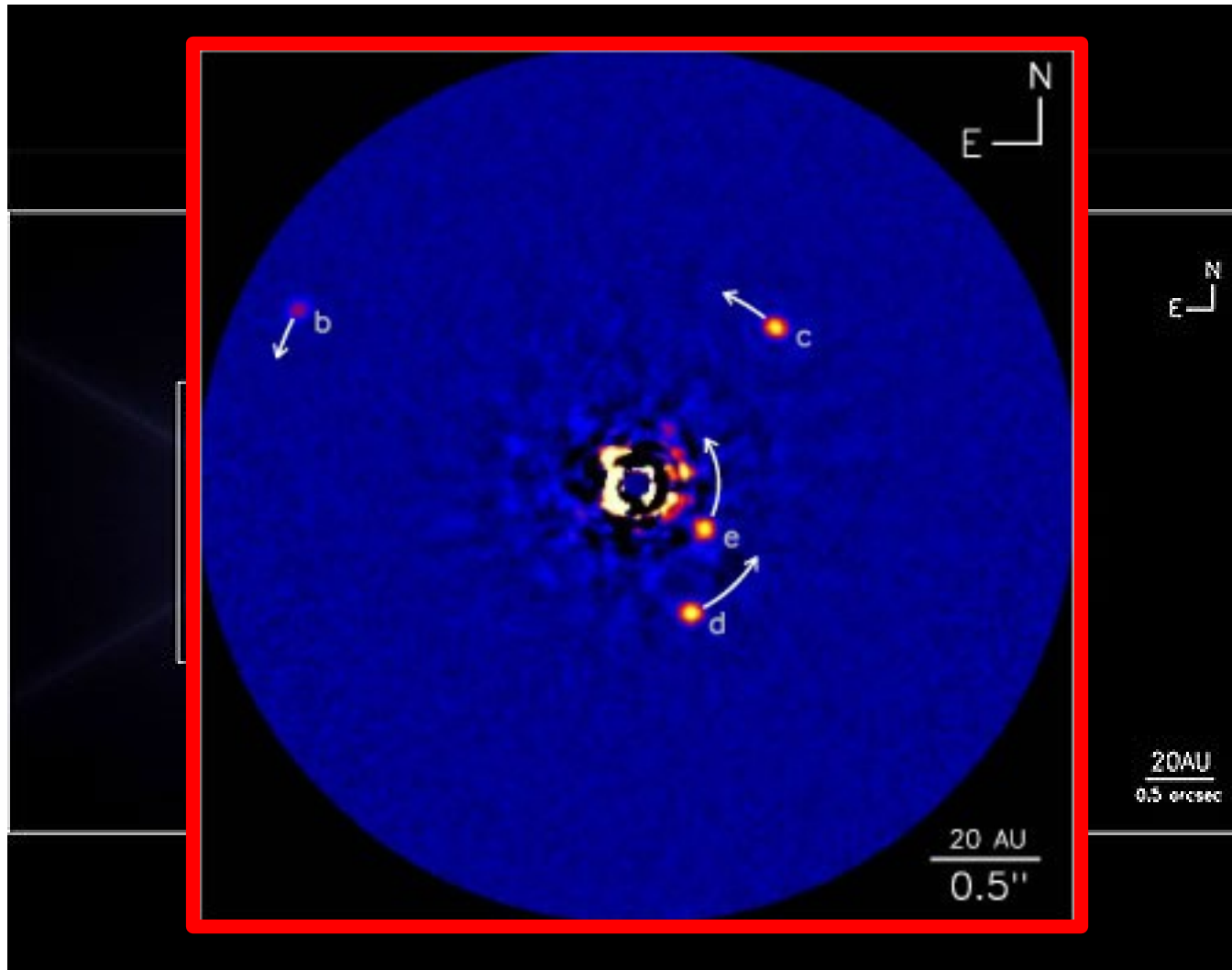
A (controversial) planet,  
**Fomalhaut b**, detected in 2006,  
at ~100 AU from the star.

# Exoplanets - Direct Imaging



**Four planets** around HR 8799 !!

# Exoplanets - Direct Imaging

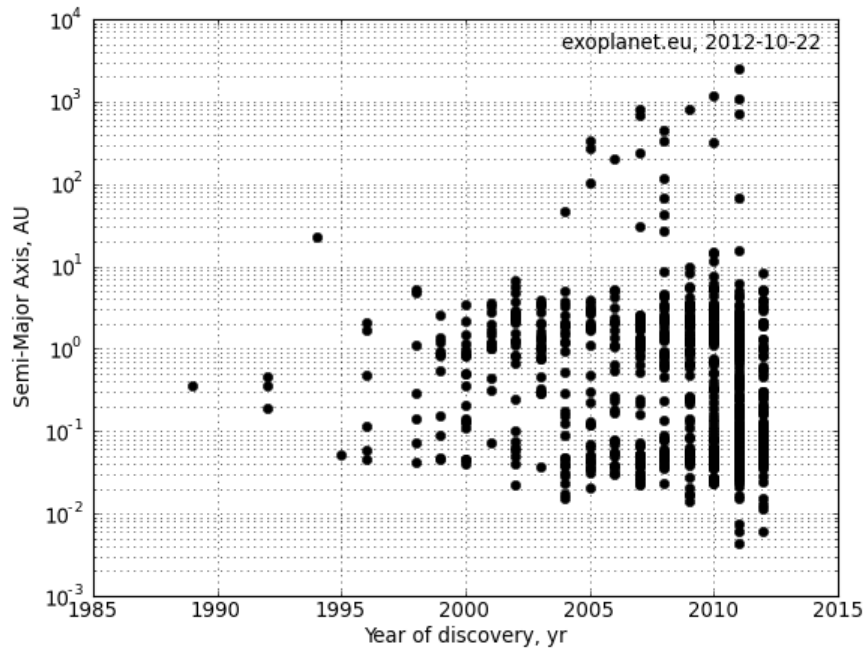


**Four planets** around HR 8799 !!

# Timeline of exoplanet discoveries

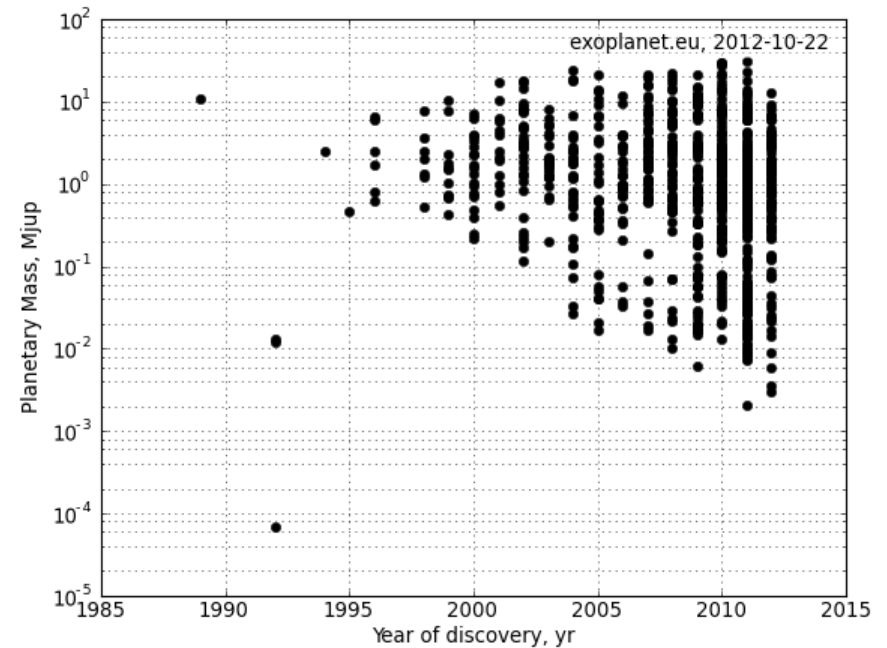
In time...

**Semi-major axis** vs time



.... we have access to **longer monitoring periods**, enabling detection of planets in **wider orbits**.

**Mass** vs time

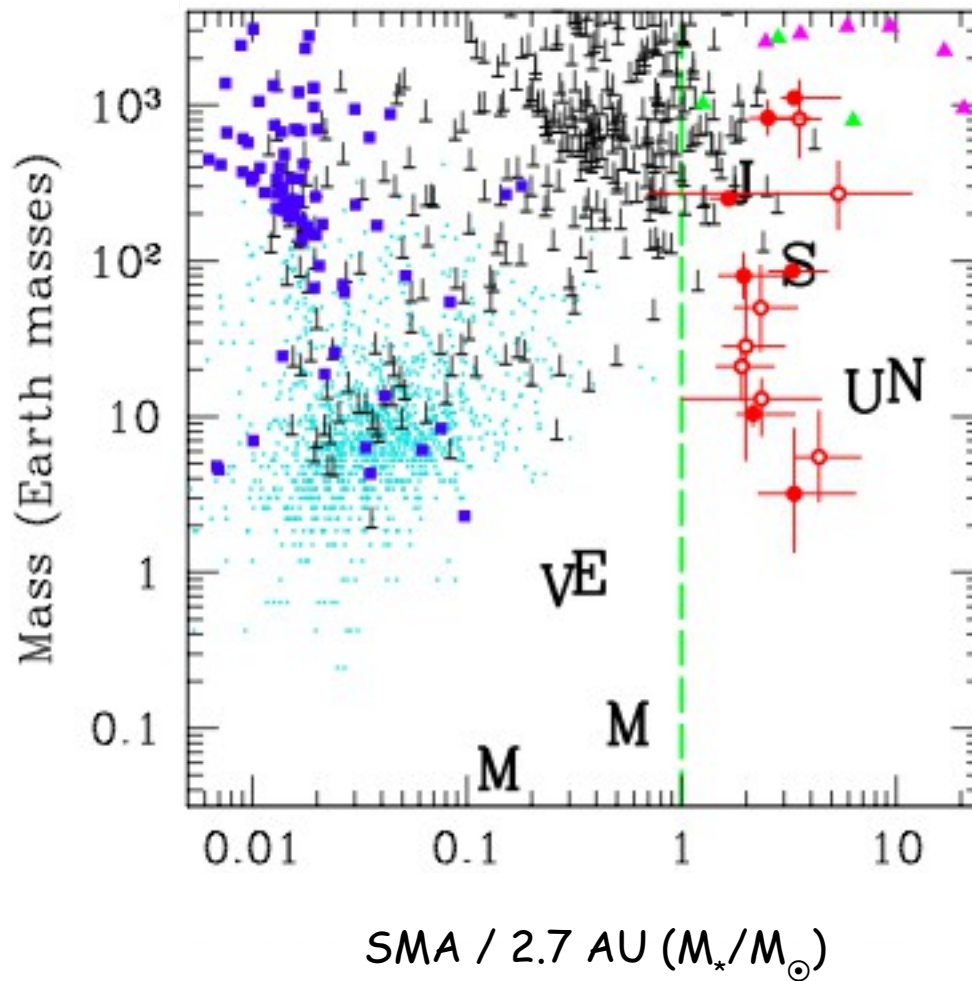


.... and the **increasing sensitivity** of the instruments, allows for the detection of **lower mass** planets.



# The situation

Exoplanet discoveries



Transit

Kepler Transit

Radial Velocity

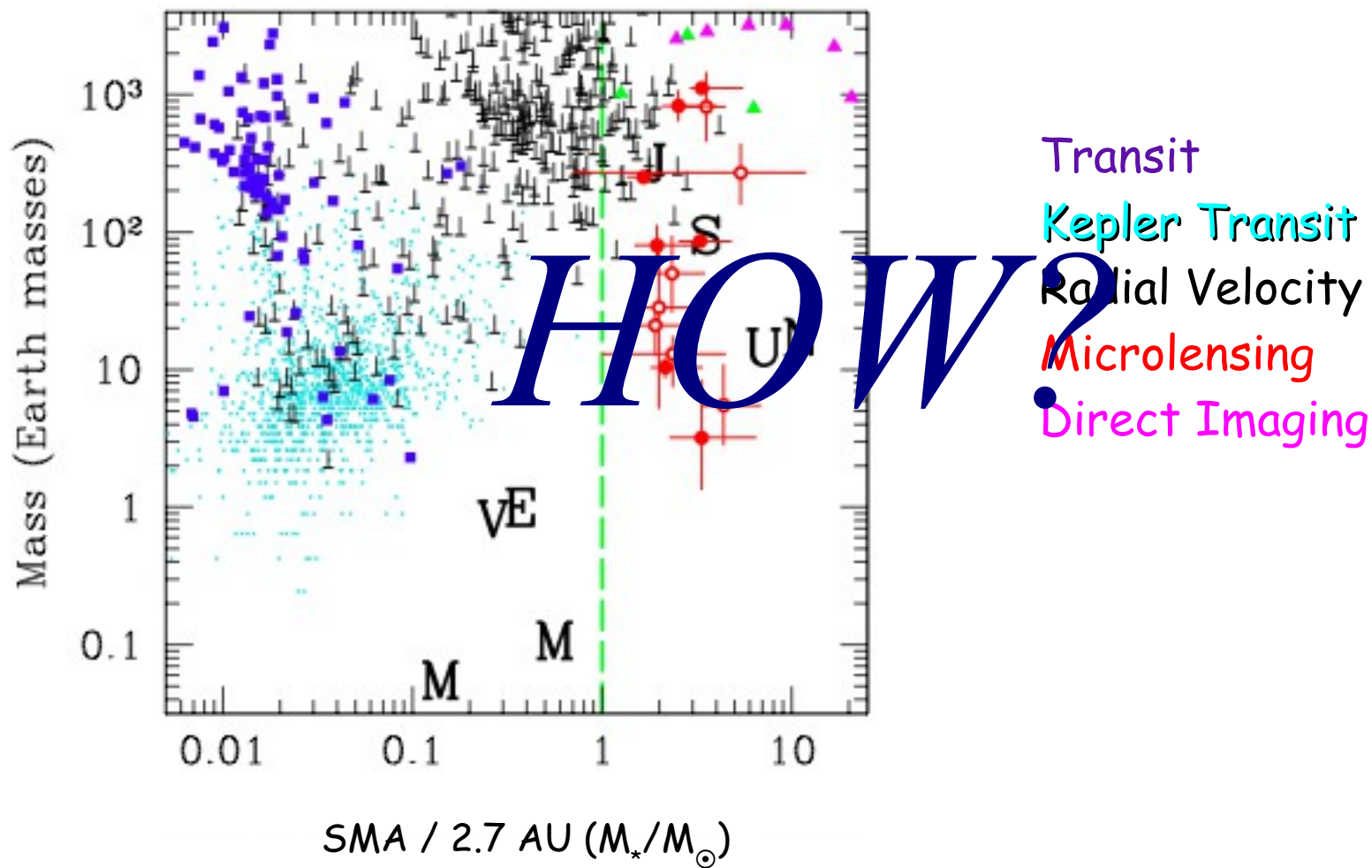
Microlensing

Direct Imaging



# The situation

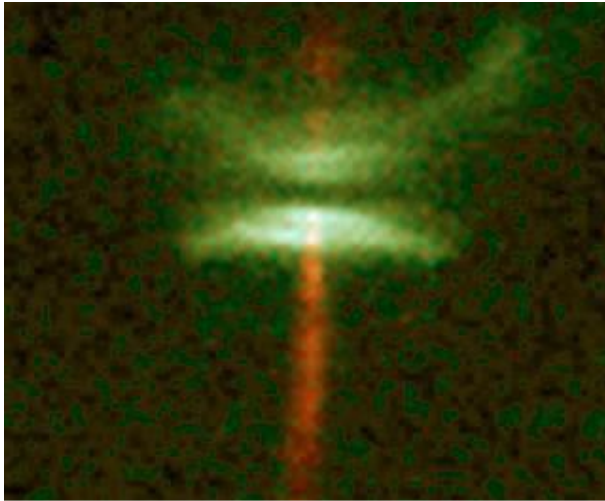
Exoplanet discoveries



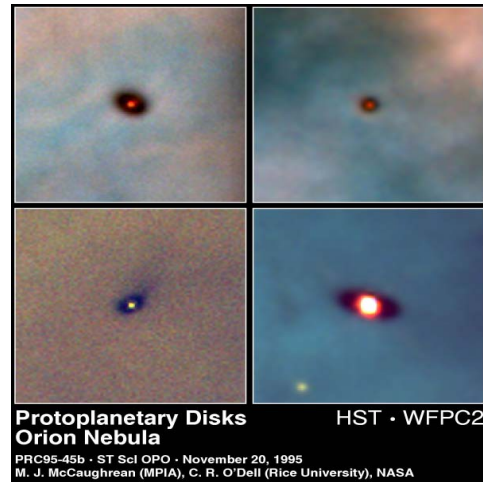
# Star Formation



# Protoplanetary Disks



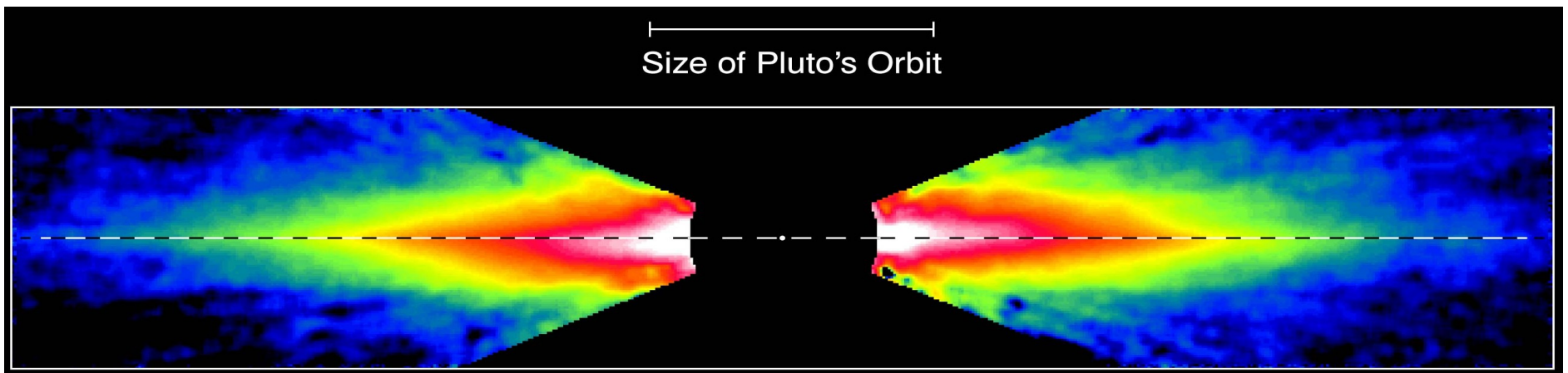
Dust lane  
blocks view



A light background  
reveals the disks



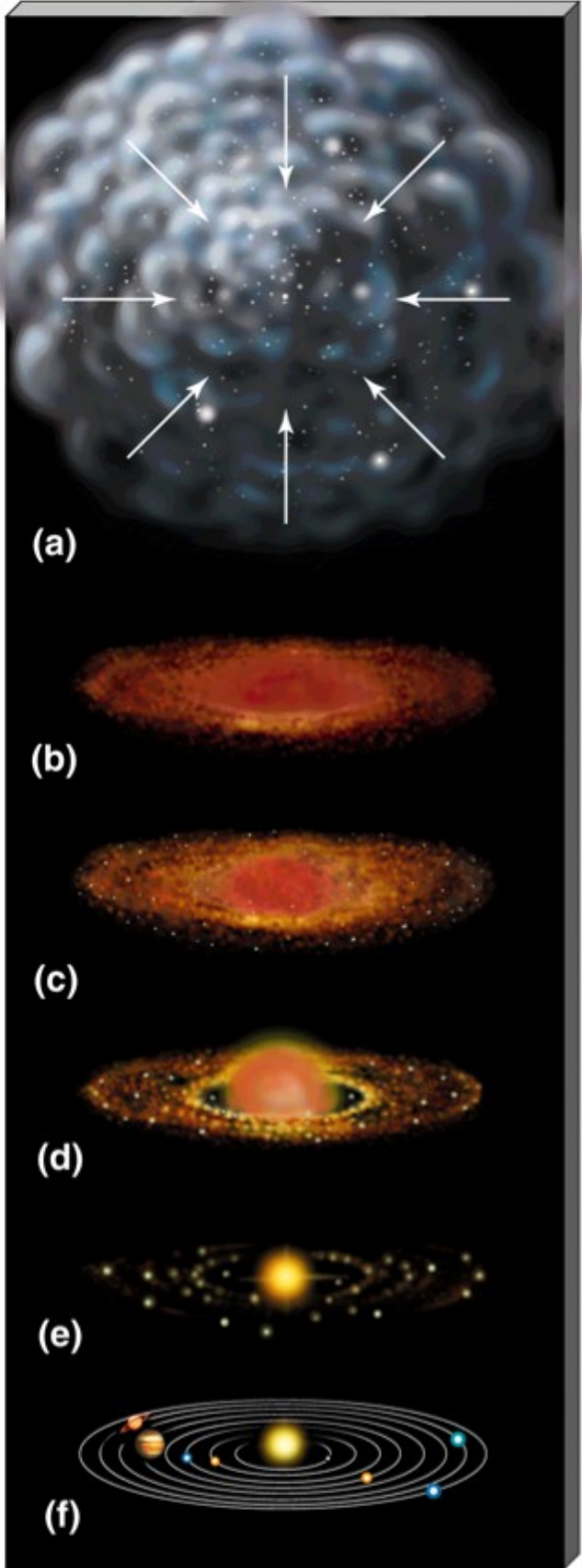
Face-on disk  
in reflected light



The disk of Beta Pictoris

# Protoplanetary Disks





## *A disk life story*

**Gas-rich phase (< 10 Myr)**

**T-Tauri Disks**

Accretion and Planet Formation

**Thinning phase (~10 Myr)**

**Transitional Disks**

Planet retention

**Gas-poor phase (>10 Myr)**

**Debris Disks**

Stabilization of architecture and Planet Detection

# Protoplanetary Disks



## PP disk fact sheet

Density:  $10^{13} - 10^{15} \text{ cm}^{-3}$   
(Air:  $10^{21} \text{ cm}^{-3}$ )

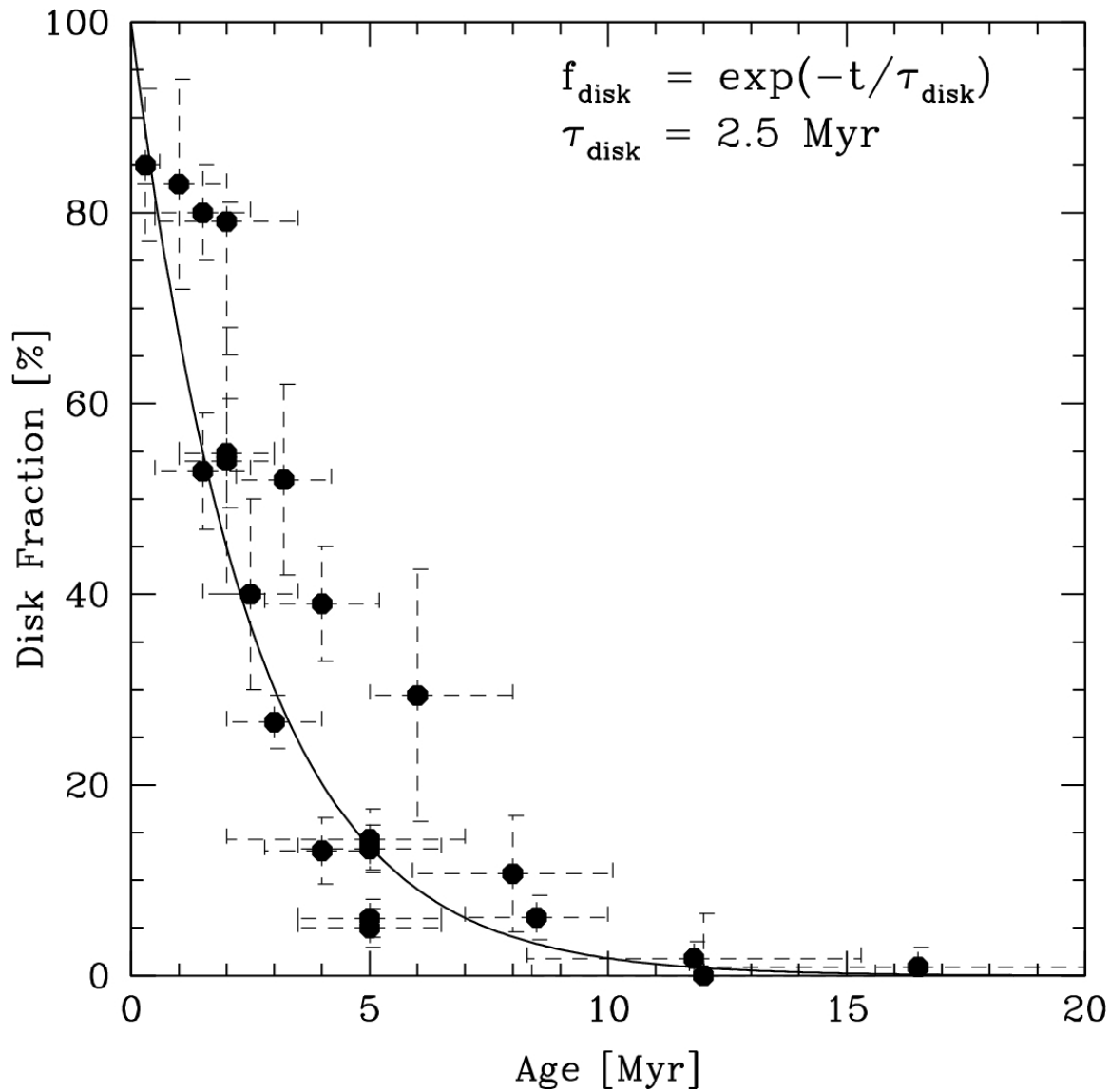
Temperature: 10-1000 K

Scale: 0.1-100 AU  
(1 AU =  $1.49 \times 10^{13} \text{ cm}$ )

Mass:  $10^{-3} - 10^{-1} M_{\odot}$   
(1  $M_{\odot}$  =  $2 \times 10^{33} \text{ g}$ )



# Disk Lifetime



Mamajek et al. (2009)



Disks evaporate with an  
*e*-folding time of  
*2.5 Myr*.



# Protoplanetary Disks



## PP disk fact sheet

Density:  $10^{13} - 10^{15} \text{ cm}^{-3}$   
(Air:  $10^{21} \text{ cm}^{-3}$ )

Temperature: 10-1000 K

Scale: 0.1-100 AU  
(1 AU =  $1.49 \times 10^{13} \text{ cm}$ )

Mass:  $10^{-3} - 10^{-1} M_{\text{sun}}$   
( $M_{\text{sun}} = 2 \times 10^{33} \text{ g}$ )

*Lifetime: ~10 Myr*

## Accretion

“The central problem  
of nearly 30 years of accretion disk theory  
is to understand how they accrete”

Balbus & Hawley 1998

Accretion time for molecular viscosity

$$\nu: cm^2 s^{-1} \quad \nu = l^2 / t_{coll} = l V_t \quad t_{acc} = r^2 / \nu$$

For a newly formed disk

$$r = 10^{14} cm; n = 10^{15} cm^{-3}; \sigma = 10^{-16} cm^{-2}$$
$$l = 1/(n\sigma) = 10 cm; V_t = 10^5 cm s^{-1}$$

$$t_{acc} = 10^{13} yr$$

Observations reveal that disks only live up to  $10^7 - 10^8$  yr

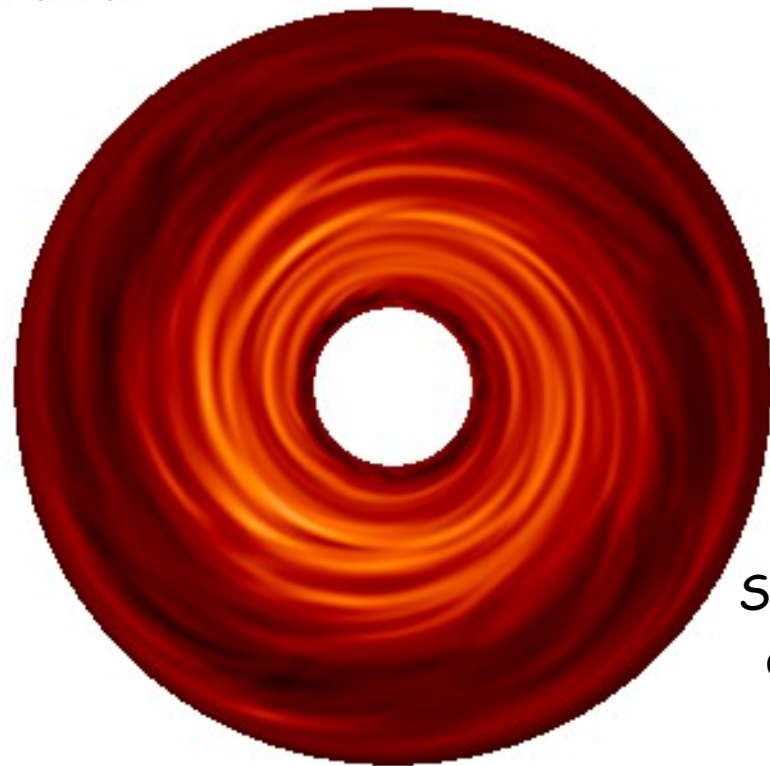
*Much more powerful viscosity needed!*

# Accretion in disks occurs via turbulent viscosity

Turbulence in disks is enabled by the **Magneto-Rotational Instability**

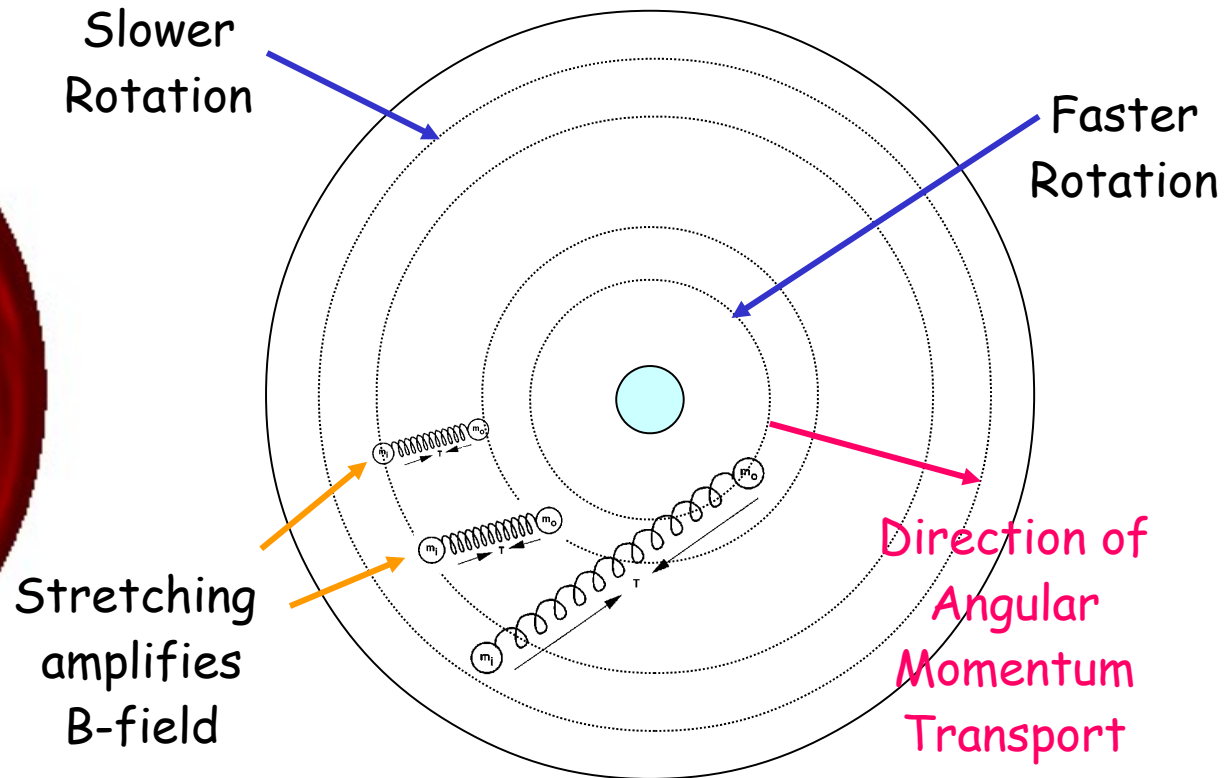
$t=46.3/88\text{yr}$

**MRI sketch**



**Magnetized disk**

Lyra et al. (2008a)

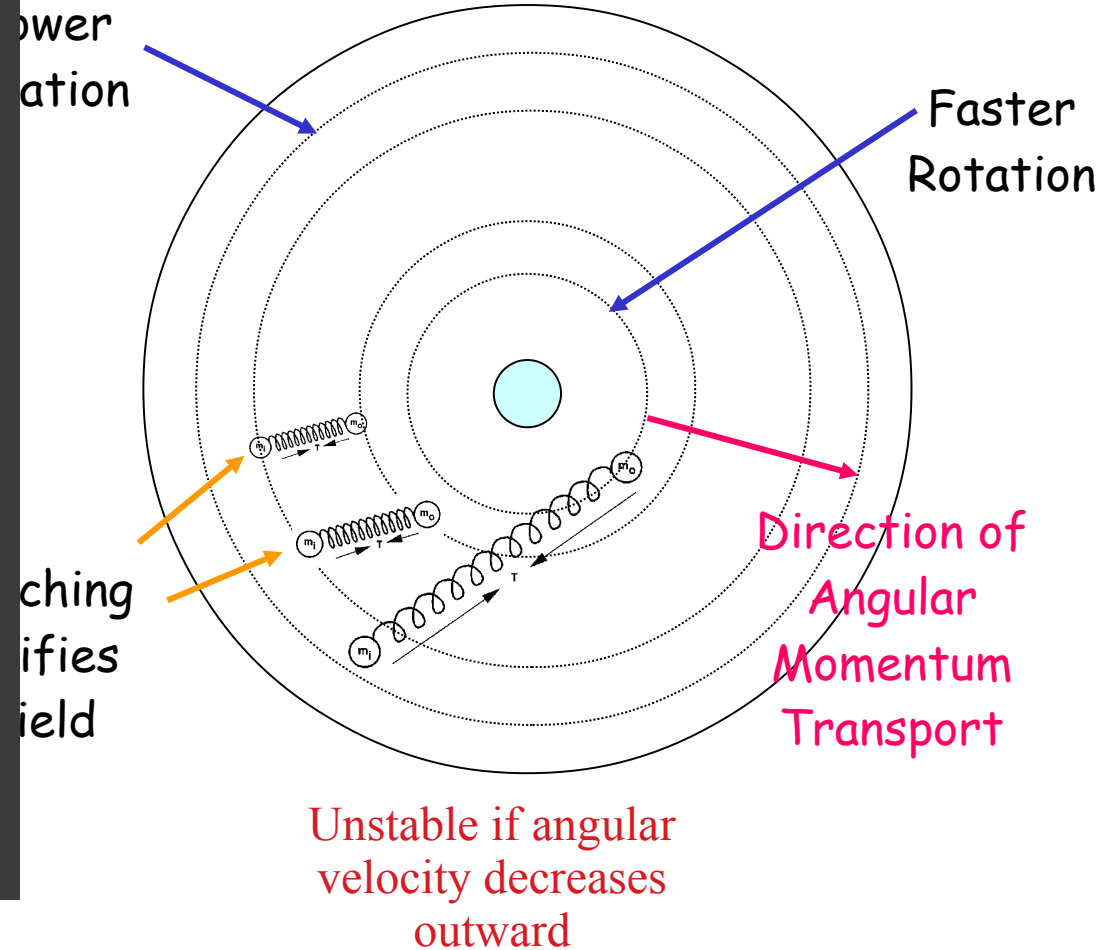


Unstable if angular velocity decreases outward

# Accretion in disks occurs via turbulent viscosity

Turbulence in disks is enabled by  
the **Magneto-Rotational Instability**

**MRI sketch**

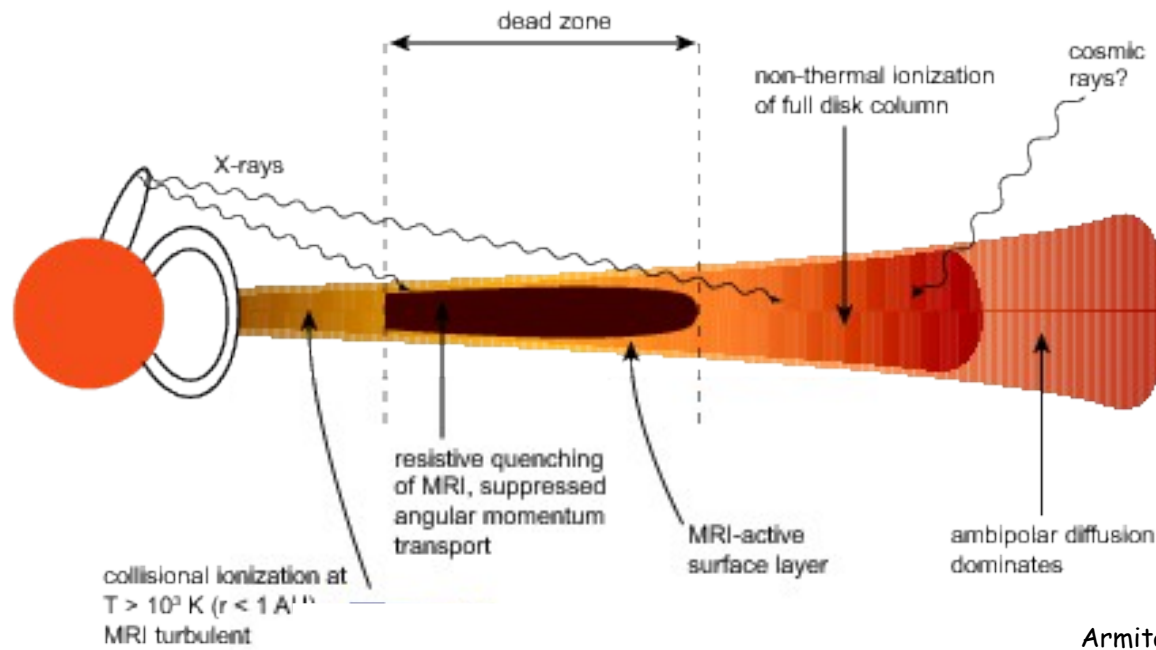


Magnetized disk

Lyra et al. (2008a)



## Alas... Dead zones are robust features of accretion disks



Disks are cold and thus poorly ionized  
(Blaes & Balbus 1994)

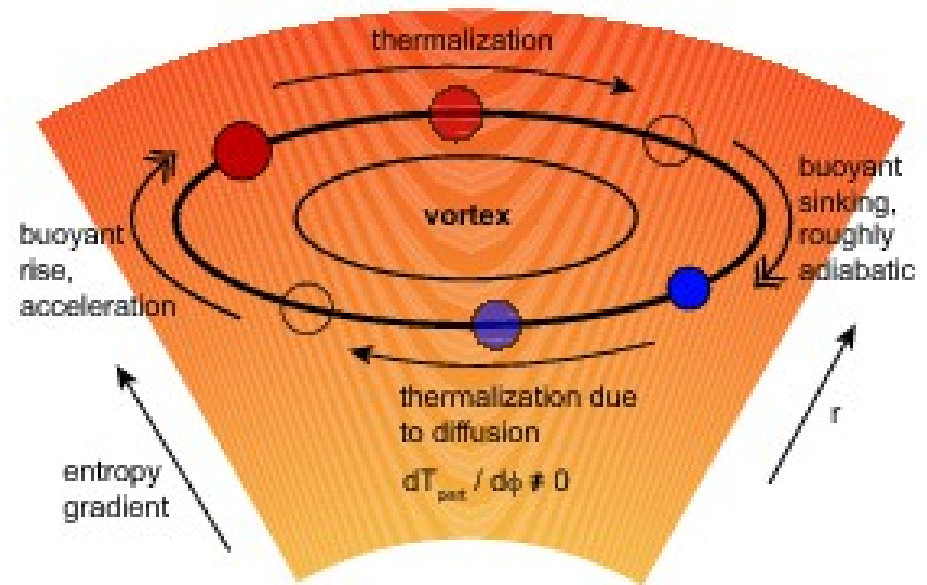
Therefore, accretion is **layered** (Gammie 1996)

There should be a non-magnetic,  
**hydrodynamical**, source of turbulence in the **dead zone**.

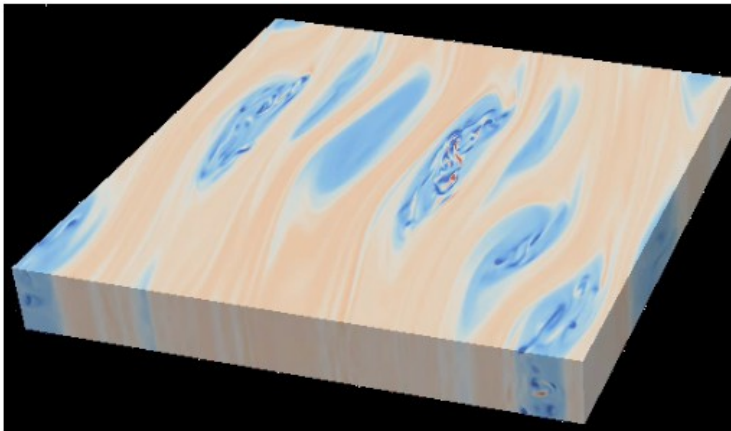


# Baroclinic Instability - Excitation and self-sustenance of vortices

Sketch of the Baroclinic Instability



Armitage (2010)

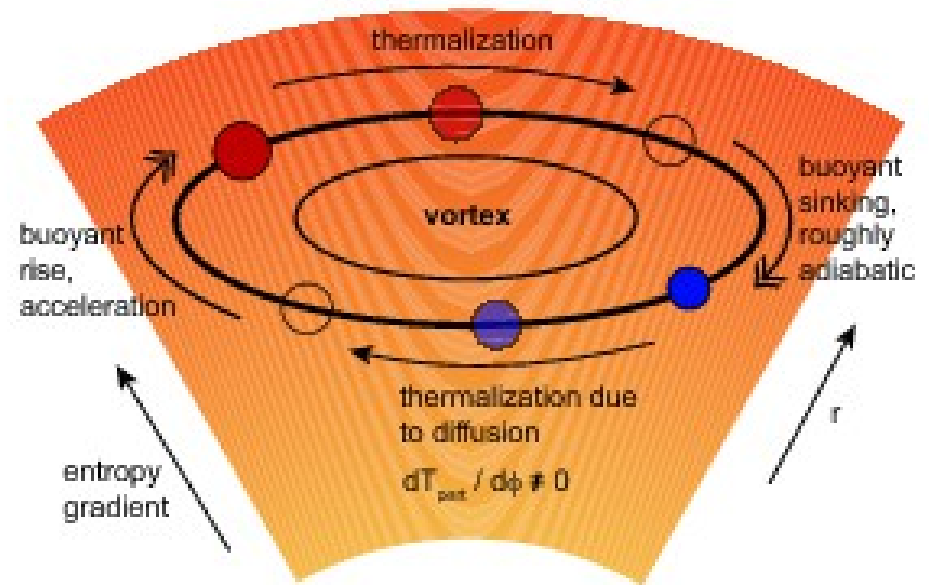


Lesur & Papaloizou (2010)

$$\frac{\partial \omega}{\partial t} = \underbrace{-(\mathbf{u} \cdot \nabla) \omega}_{\text{advection}} - \underbrace{\omega (\nabla \cdot \mathbf{u})}_{\text{compression}} + \underbrace{(\omega \cdot \nabla) \mathbf{u}}_{\text{stretching}} + \frac{1}{\rho^2} \underbrace{\nabla \rho \times \nabla p}_{\text{baroclinicity}} + \underbrace{\nu \nabla^2 \omega}_{\text{dissipation}}$$

# Baroclinic Instability - Excitation and self-sustenance of vortices

## Sketch of the Baroclinic Instability



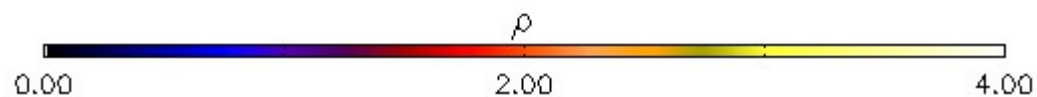
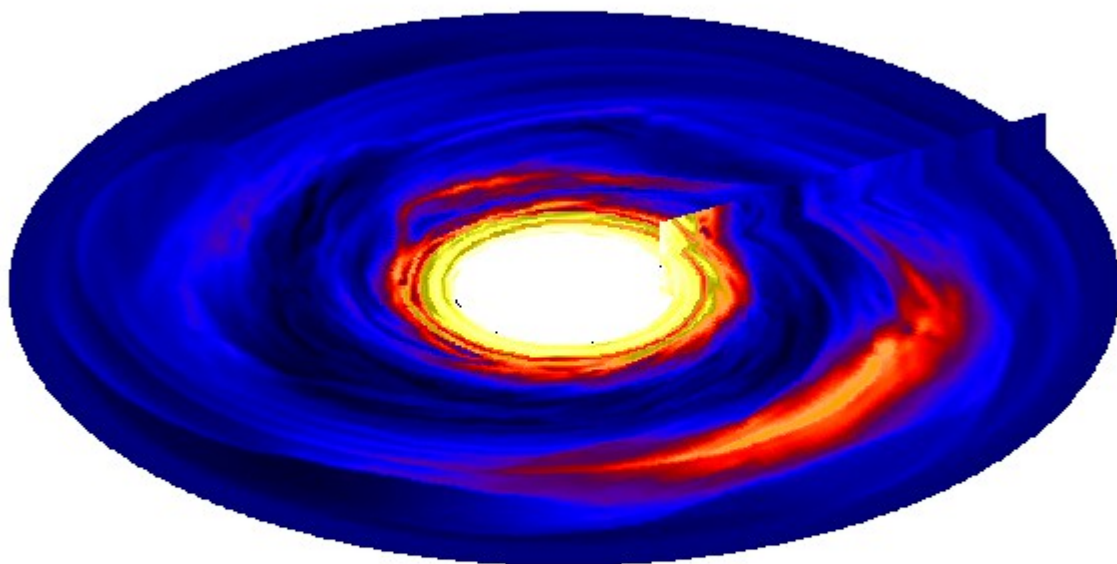
Armitage (2010)

Lyra & Klahr (2011)

$$\frac{\partial \omega}{\partial t} = \underbrace{-(\mathbf{u} \cdot \nabla) \omega}_{\text{advection}} - \underbrace{\omega (\nabla \cdot \mathbf{u})}_{\text{compression}} + \underbrace{(\omega \cdot \nabla) \mathbf{u}}_{\text{stretching}} + \frac{1}{\rho^2} \underbrace{\nabla \rho \times \nabla p}_{\text{baroclinicity}} + \underbrace{\nu \nabla^2 \omega}_{\text{dissipation}}$$

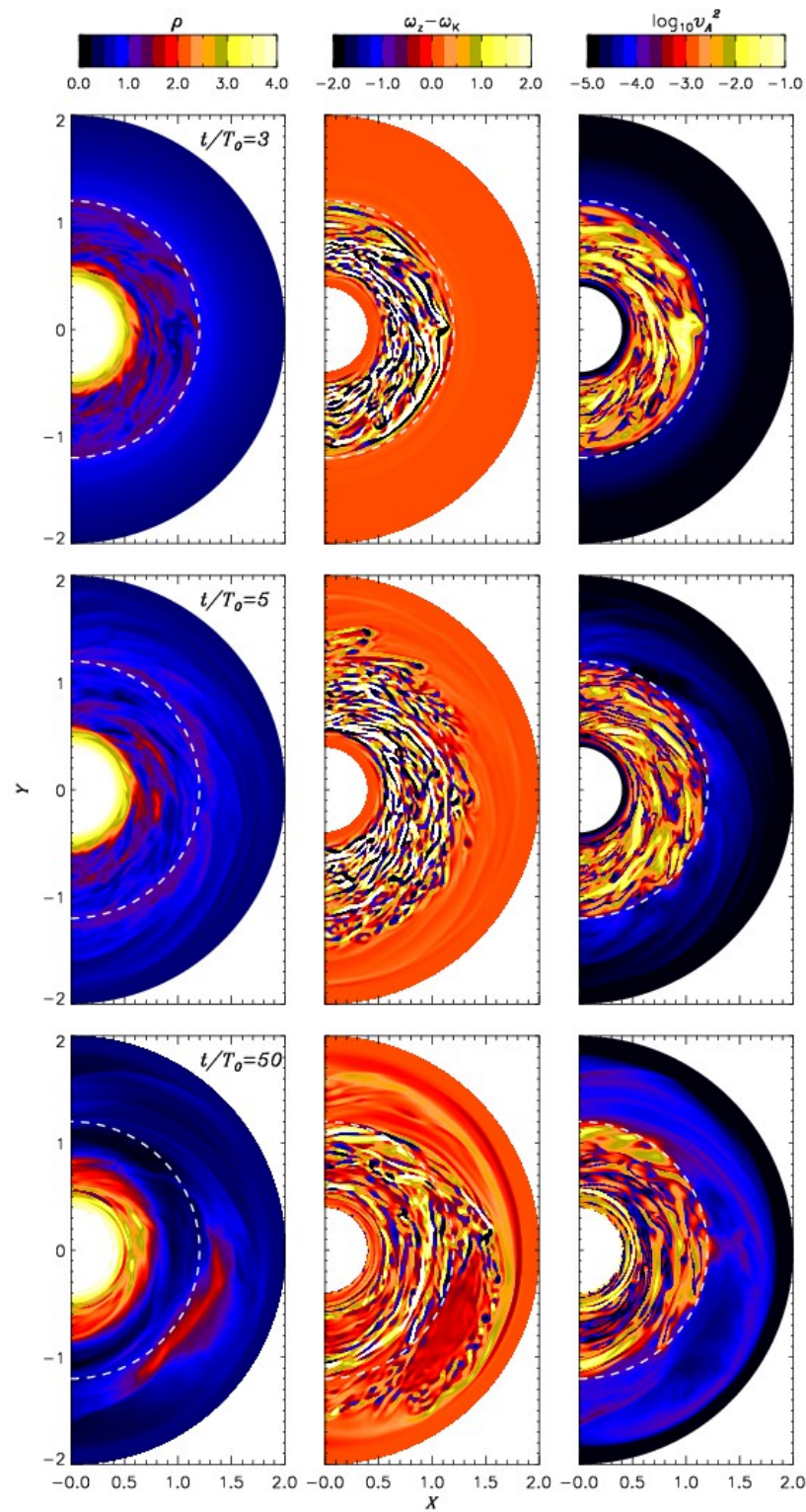
# Active/dead zone boundary

$t = 22.28 \tau_0$



Magnetized inner disk + resistive outer disk

Lyra & Mac Low (2012)

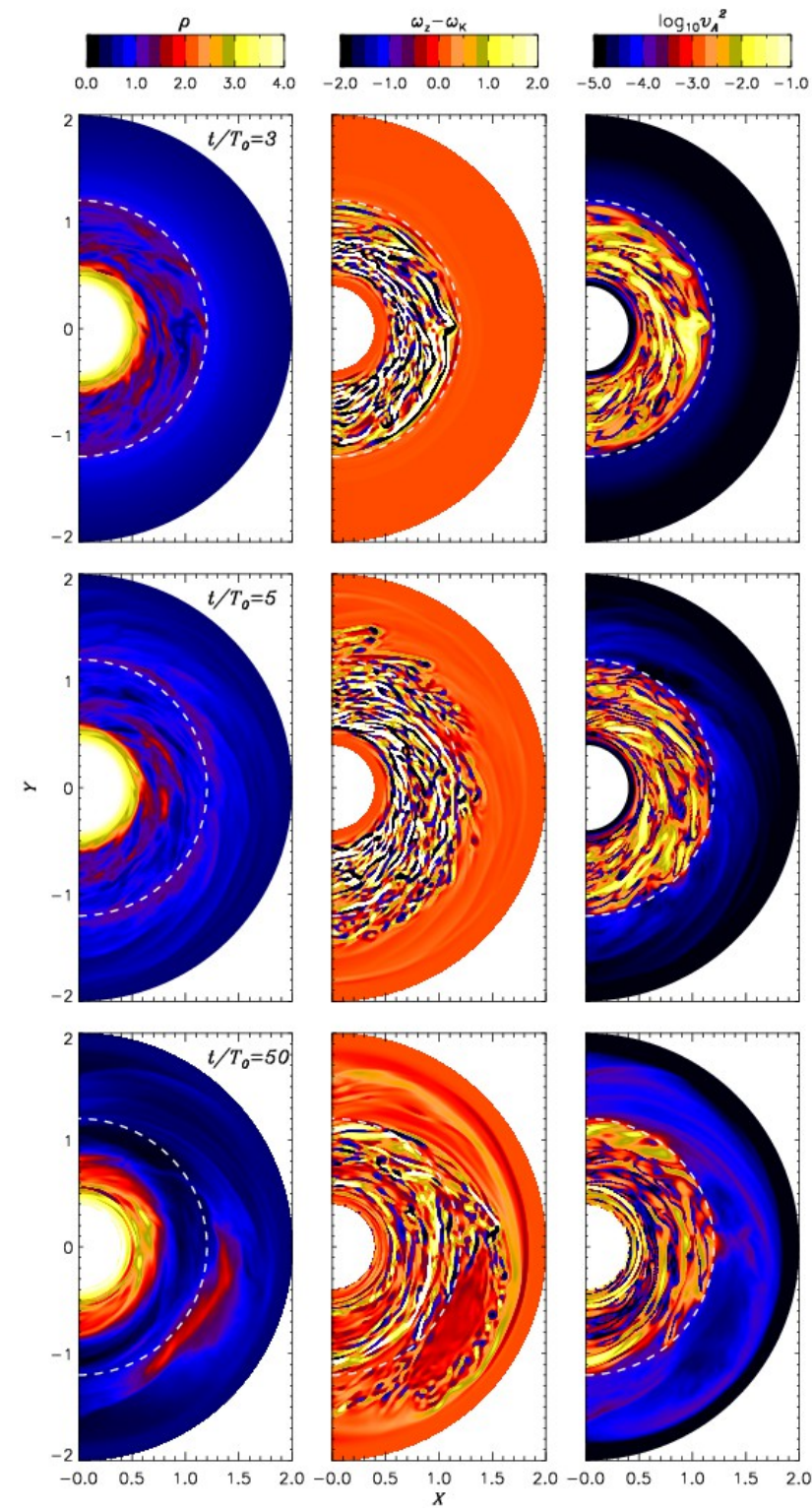


## Active/dead zone boundary



Magnetized inner disk + resistive outer disk

Lyra & Mac Low (2012)



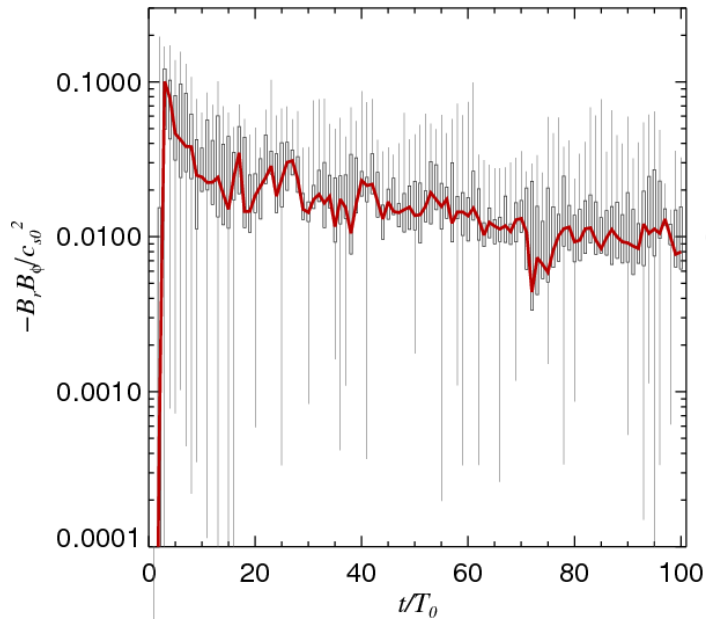


# Significant angular momentum transport

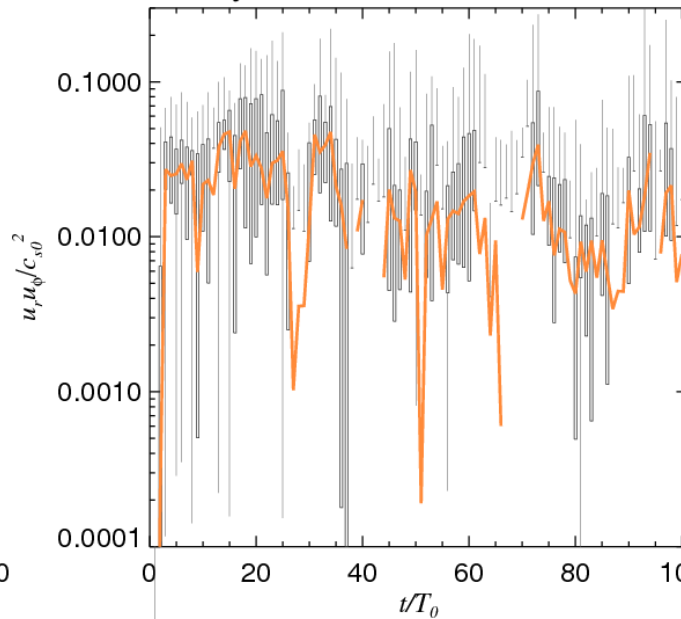
Active zone

Dead zone

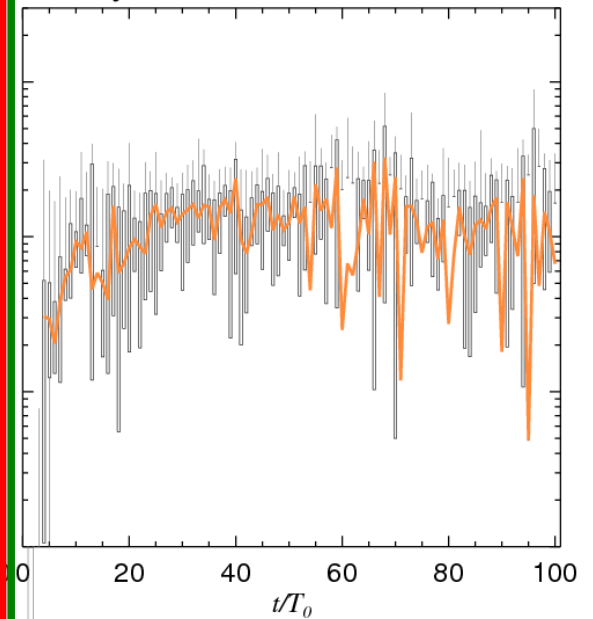
Maxwell stress – active zone



Reynolds stress – active zone



Reynolds stress – dead zone

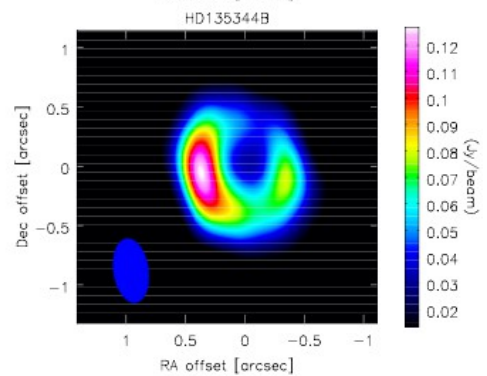
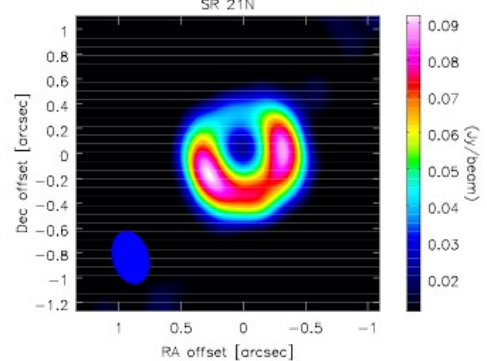
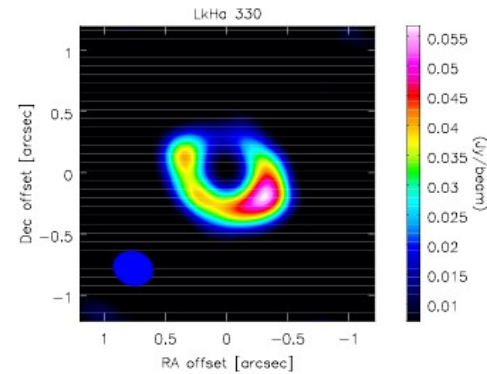
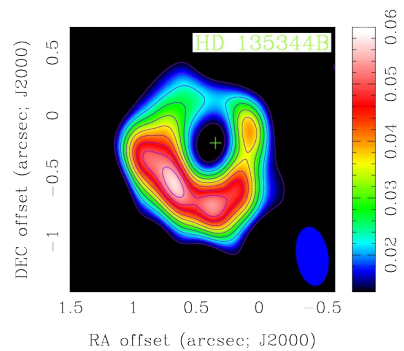
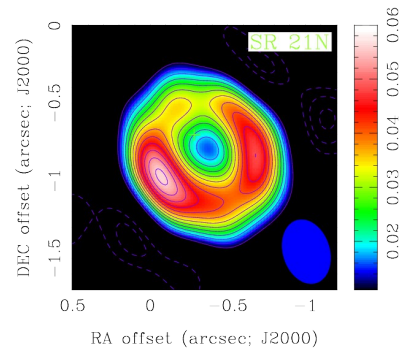
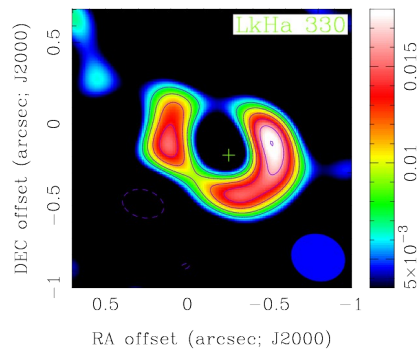


Large mass accretion rates in the **dead zone**,  
comparable to the MRI in the **active zone**!

# A possible detection of vortices in disks

Observations

Brown et al. (2009)

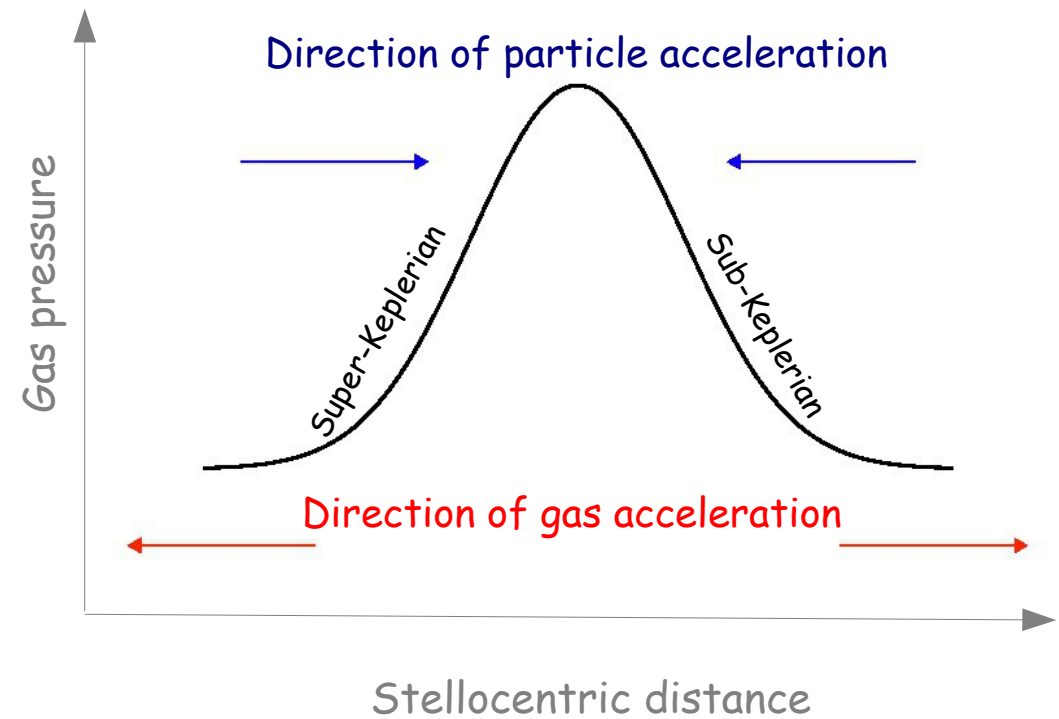
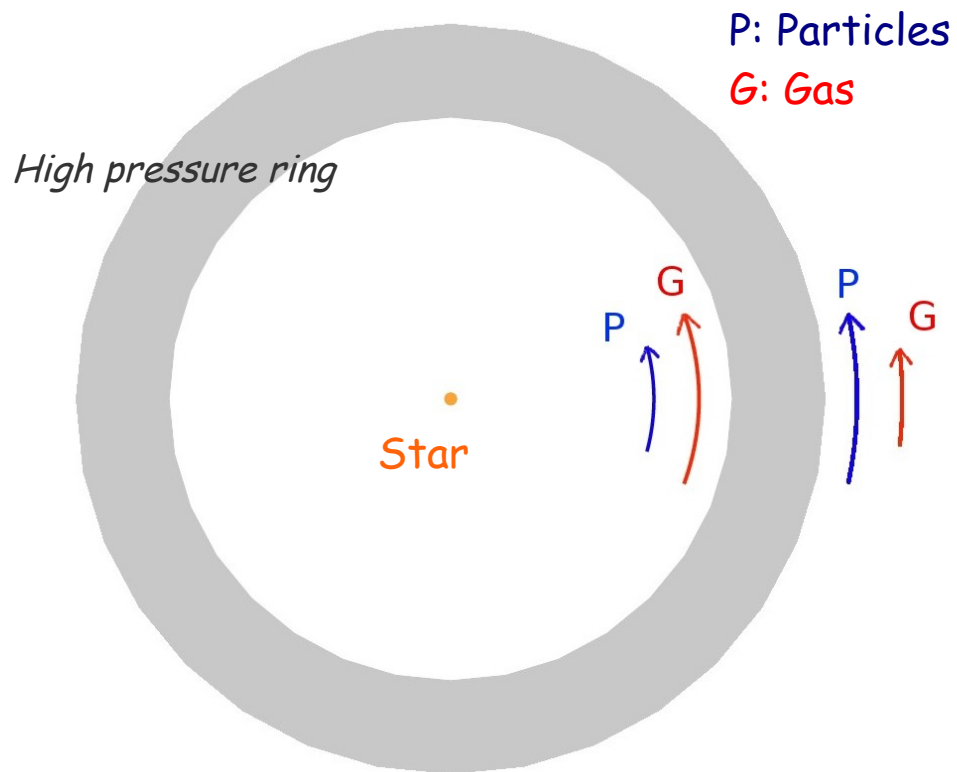


Simulated observations  
of Rossby vortices

Regaly et al. (2012)



# Forming planets in turbulent disks



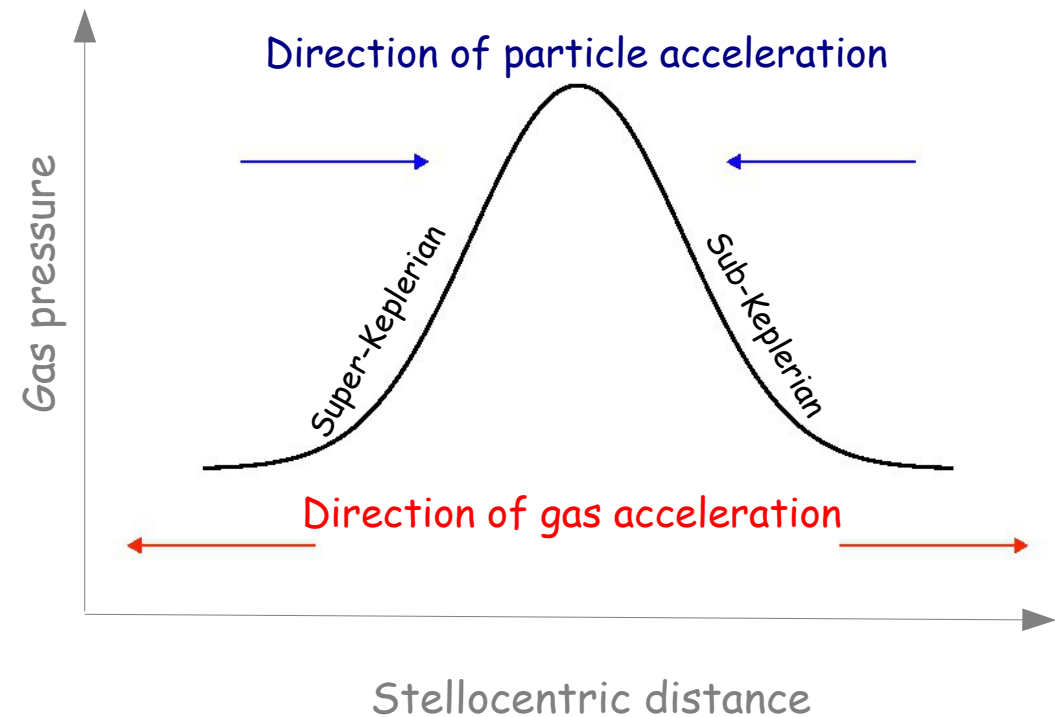
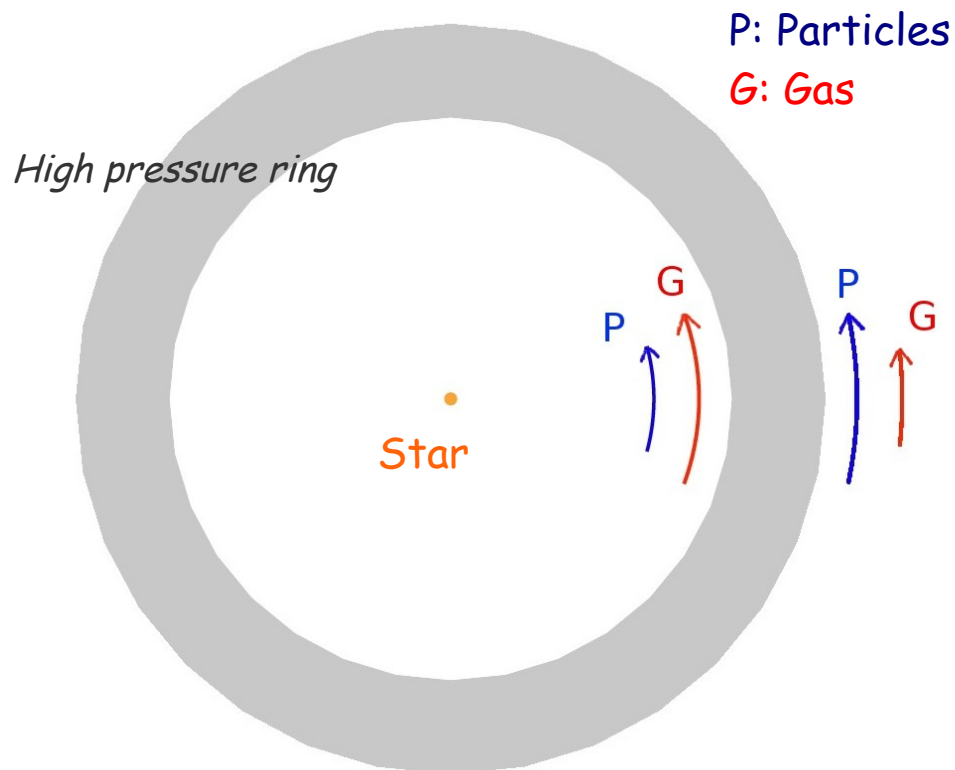
# Forming planets in turbulent disks

**Gas**  $\frac{D \mathbf{u}}{Dt} = -\nabla \Phi - \rho^{-1} \nabla p$

**Particles**  $\frac{d \mathbf{w}}{dt} = -\nabla \Phi - \frac{(\mathbf{w} - \mathbf{u})}{\tau}$

$$\mathbf{w} = \mathbf{u} + \tau \rho^{-1} \nabla p$$

The drag force pushes the particles *toward* the pressure gradient



*Solid particles*

move toward

*pressure maxima*

*Turbulence concentrates solids mechanically in pressure maxima*



Lyra et al. (2008)

# Gravitational collapse into planetesimals



Johansen et al. (2007)

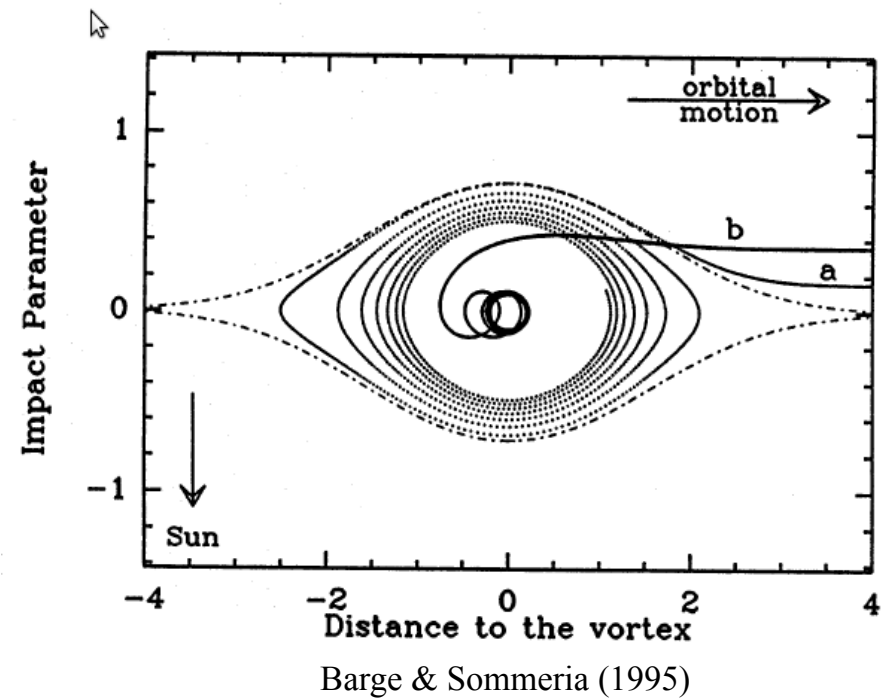
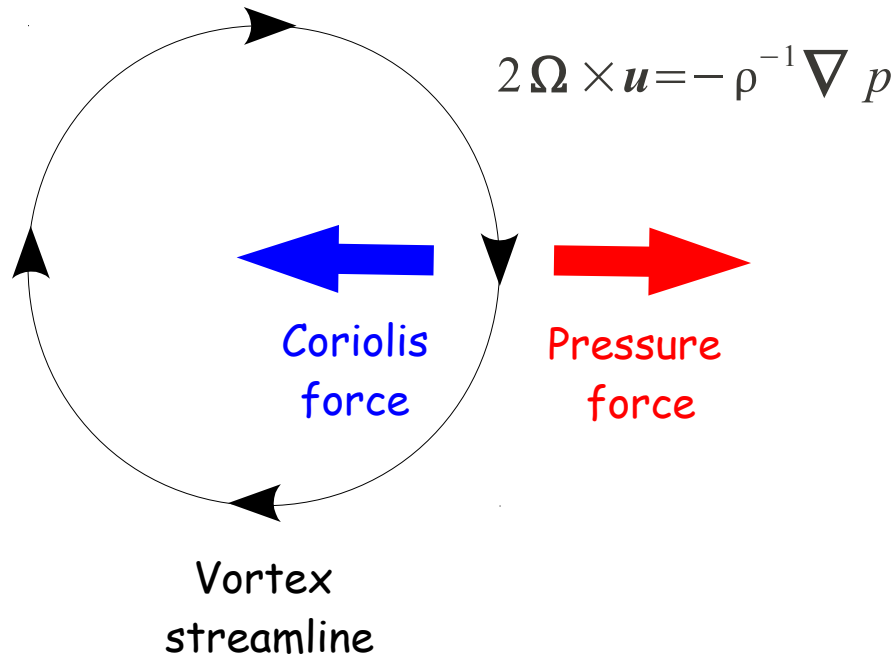
Turbulent eddies concentrate solids,  
turning them into planetesimals...

...and vortices are **huge** eddies!



# Planet Formation via *Vortex Thruway*

Geostrophic balance:



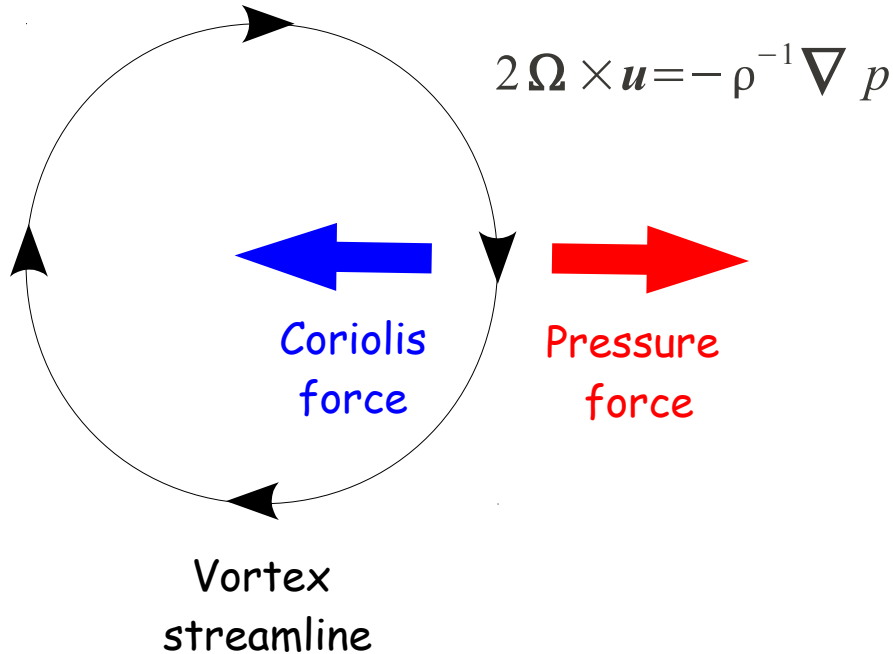
Particles do not feel the pressure gradient.  
They sink towards the center, where they accumulate.

Aid to planet formation (Barge & Sommeria 1995)

Speed up planet formation enormously  
(Lyra et al. 2008b, 2009a, 2009b, Raettig, Lyra & Klahr 2012)

# Planet Formation via *Vortex Thruway*

Geostrophic balance:



Raettig et al. (2012)

Particles do not feel the pressure gradient.  
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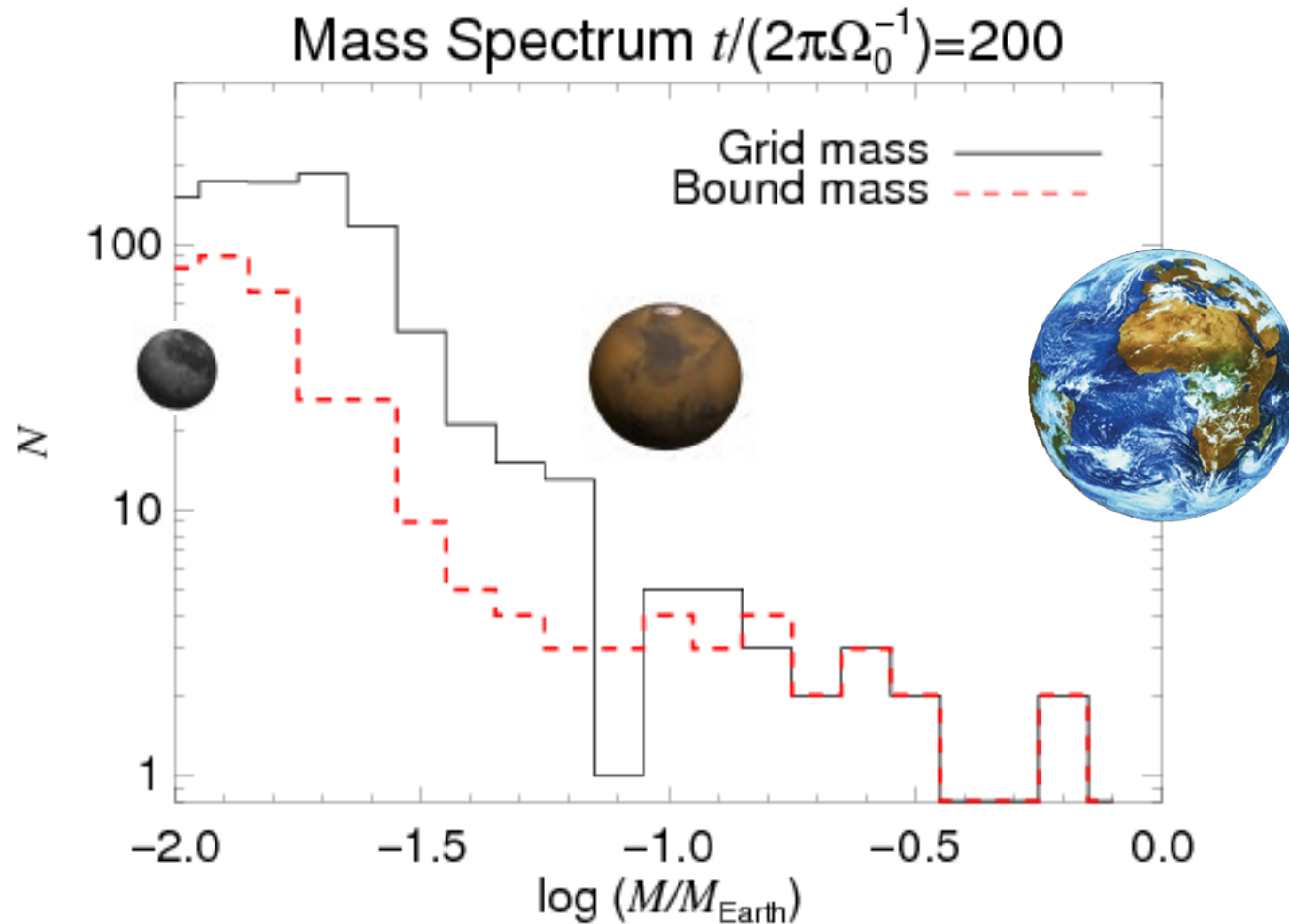
Speed up planet formation enormously  
(Lyra et al. 2008b, 2009a, 2009b, Raettig, Lyra & Klahr 2012)

## *The Initial Mass Function of planets*



- Mass spectrum by the end of the simulation
  - 300 bound clumps were formed
- Power law  $d(\log N)/d(\log M) = -2.3 \pm 0.2$
- 20 of these are more massive than Mars

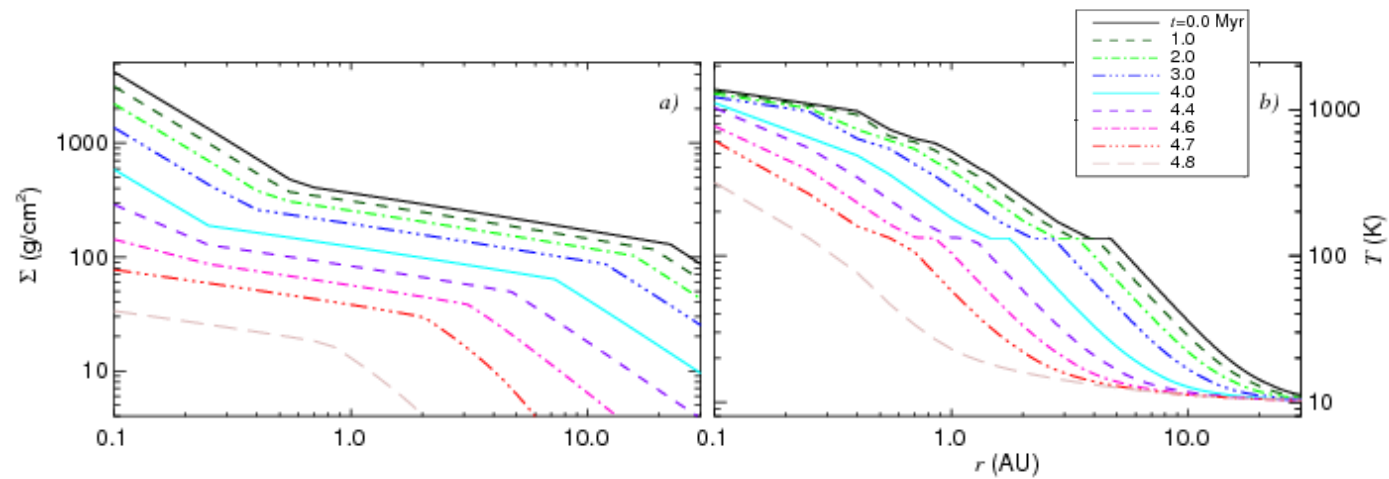
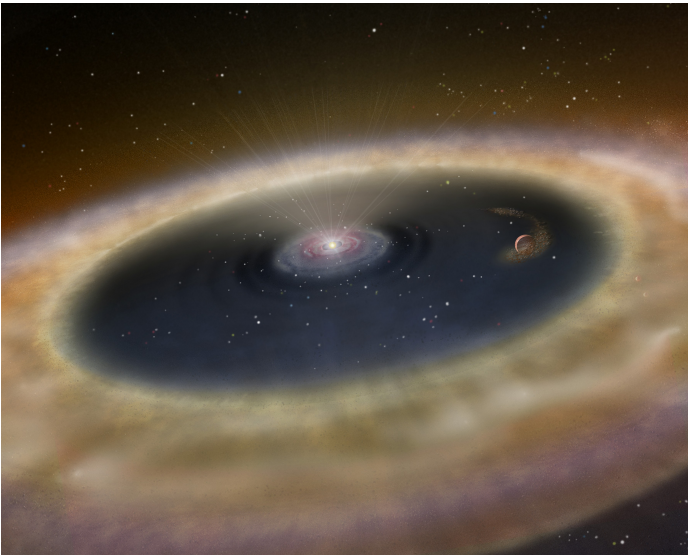
## The Initial Mass Function of planets



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  - 300 bound clumps were formed
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# Transitional disks - The thinning phase

Disks evolve in time, due to  
photoevaporative winds and viscous evolution



Lyra, Paardekooper, & Mac Low (2010)

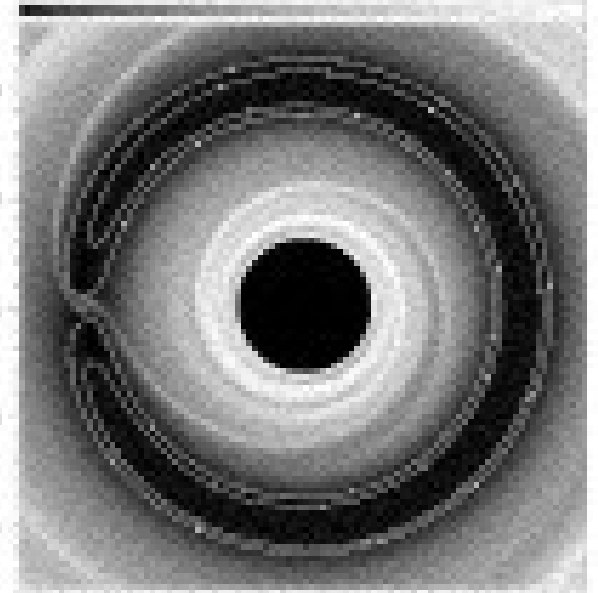
## Planets form and start to migrate

Planet-disk interaction leads to **angular momentum exchange**

One armed spiral: Lindblad resonance  
Horseshoe libration: Co-rotational torques



Nelson & Kley (2012, Annual Review)

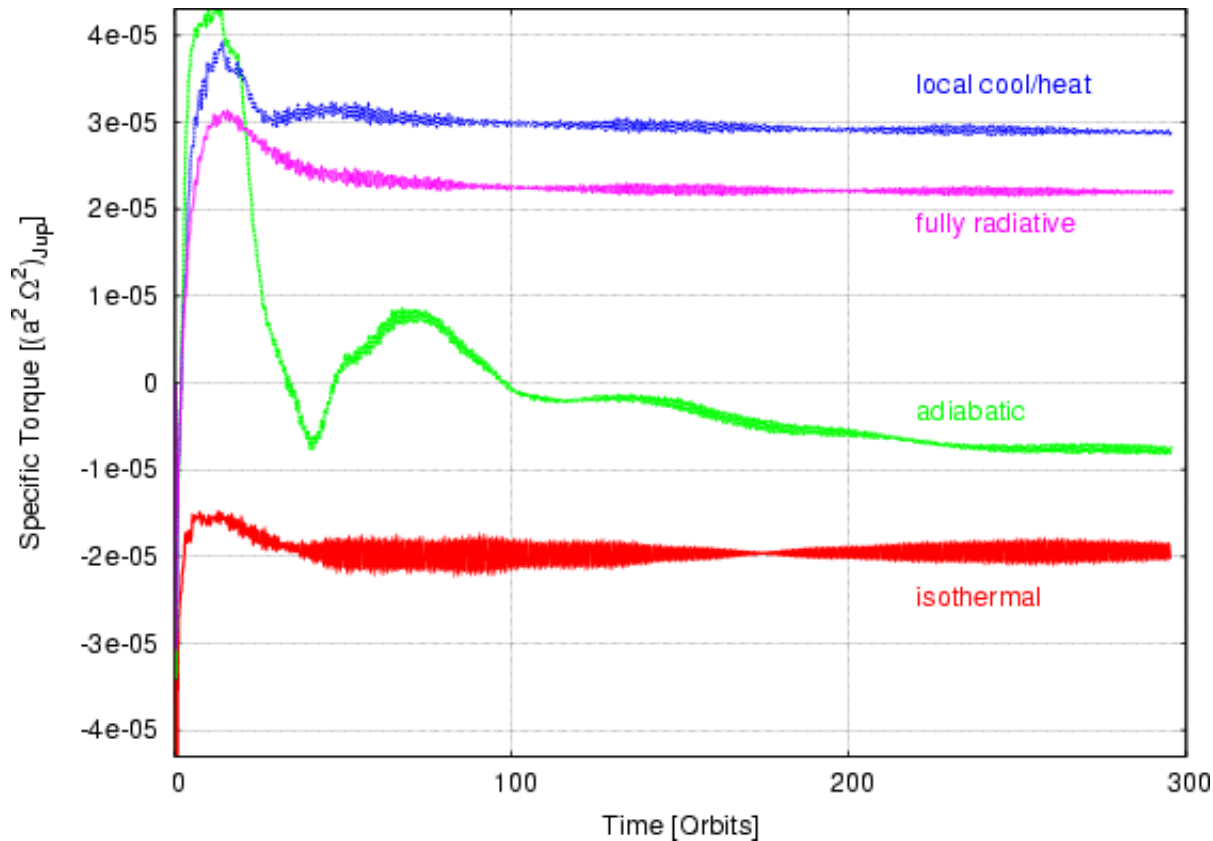


Lubow et al. (1999)

In isothermal disks,  
the result is *inward migration*.



## Planets form and start to migrate



Kley & Crida (2008)

*Rule of thumb: Migration is*  
*outwards in*  
*steep temperature gradients,*  
*inwards in*  
*isothermal regions.*

Paardekooper & Mellema (2006)

*Non-isothermal*  
*co-rotational torque may lead*  
*to outward migration*

**Hot topic!**

Paardekooper & Mellema 2008

Baruteau & Masset 2008

Paardekooper & Papaloizou 2008

Kley & Crida 2009

Kley et al 2009

Paardekooper et al. 2010

Bitsch & Kley 2010

Lyra et al. 2010

Paardekooper et al. 2011

Ayliffe & Bate 2011

Yamada & Inaba 2011

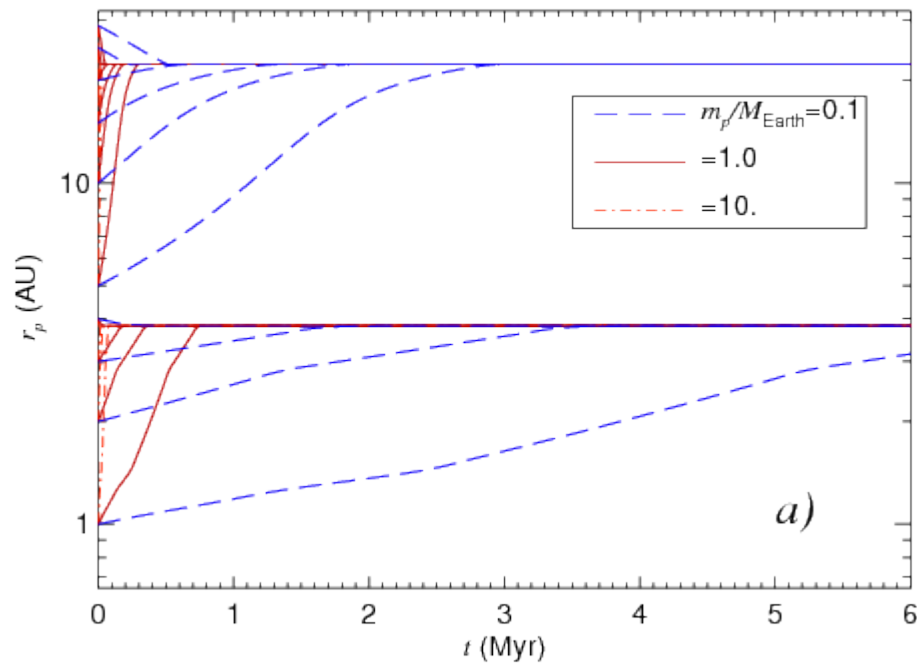
Kley 2011

Bitsch et al. 2012

Nelson & Kley 2012

## Planets form and start to migrate

Planet-disk interaction leads to **angular momentum exchange**

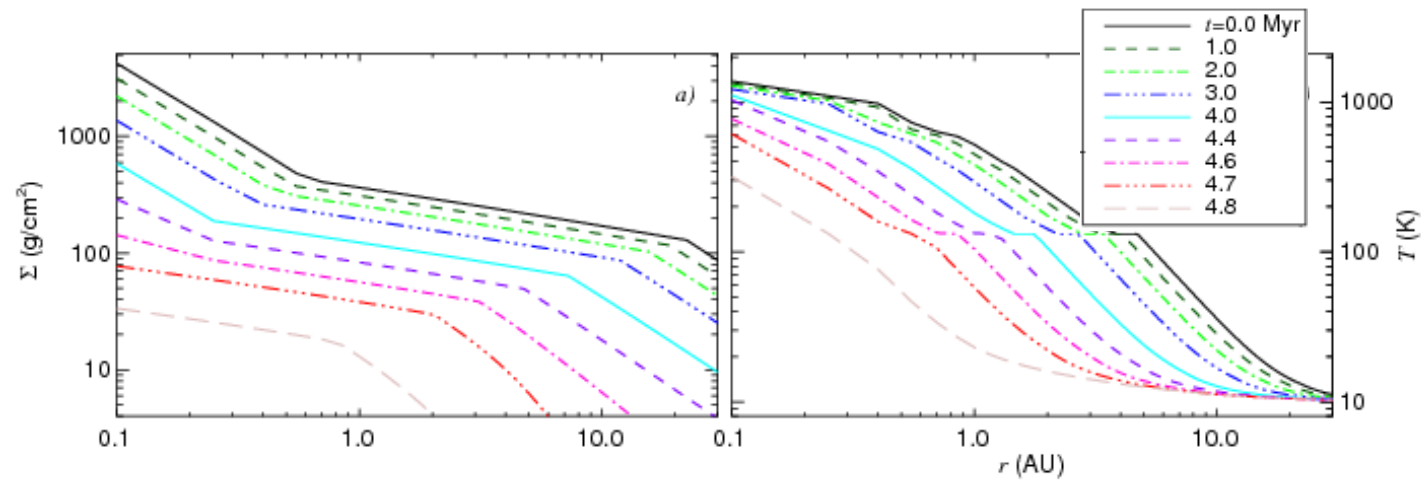


Lyra, Paardekooper, & Mac Low (2010)

Planet traps where migration  
is **convergent**  
( $\tau \neq 0$ ,  $d\tau/dr < 0$ ).

## Migration in Evolutionary Models

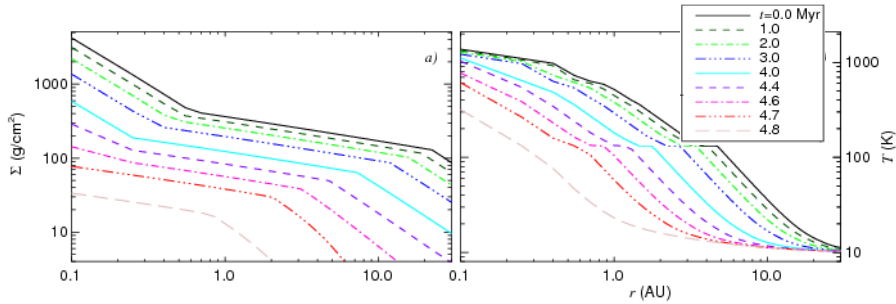
Disks evolve in time, due to  
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Lyra, Paardekooper, & Mac Low (2010)

# Migration in Evolutionary Models

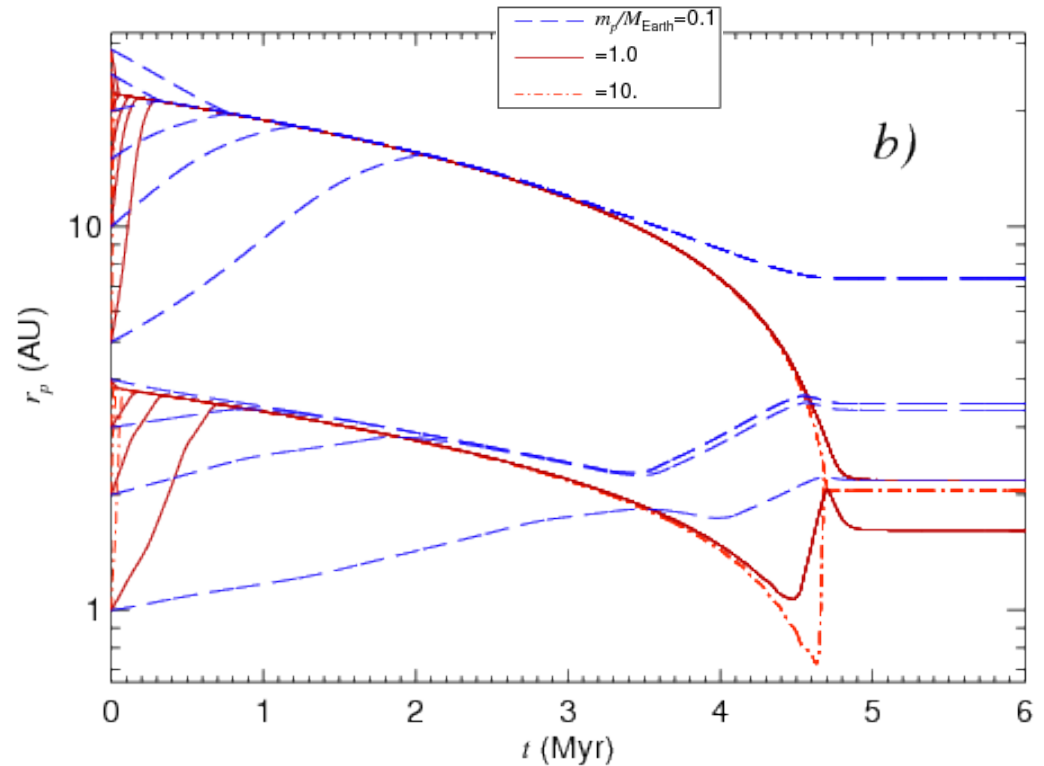
Disks evolve in time, due to  
photoevaporative winds and viscous evolution



**Single planets** in a planetary trap  
evolve in **lockstep with the gas** at the  
accretion timescale.

At some point, the **disk becomes too thin**  
to drive accretion. The **planet decouples**  
and is **released** in a safe orbit.

Rule of thumb: *Migration is*  
**outwards** in  
**steep temperature gradients,**  
**inwards** in  
**isothermal regions.**



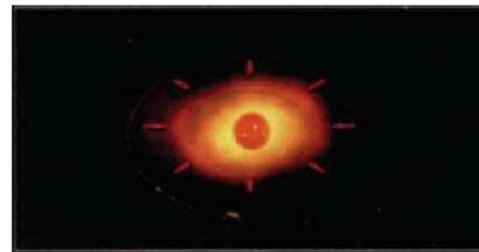
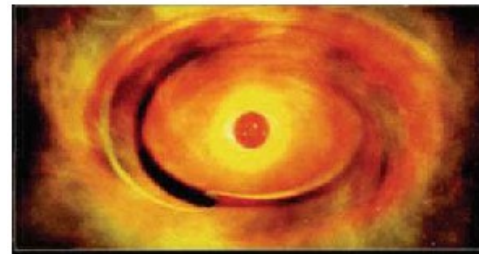
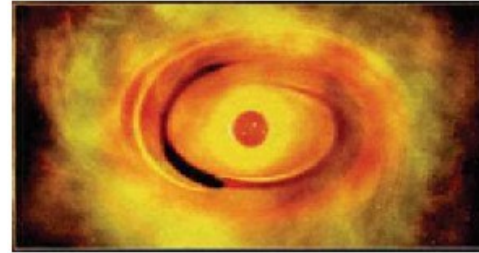
Lyra, Paardekooper, & Mac Low (2010)

## Migration in Evolutionary Models

**Single planets** in a planetary trap evolve in **lockstep with the gas** at the accretion timescale.

At some point, the **disk becomes too thin** to drive accretion.

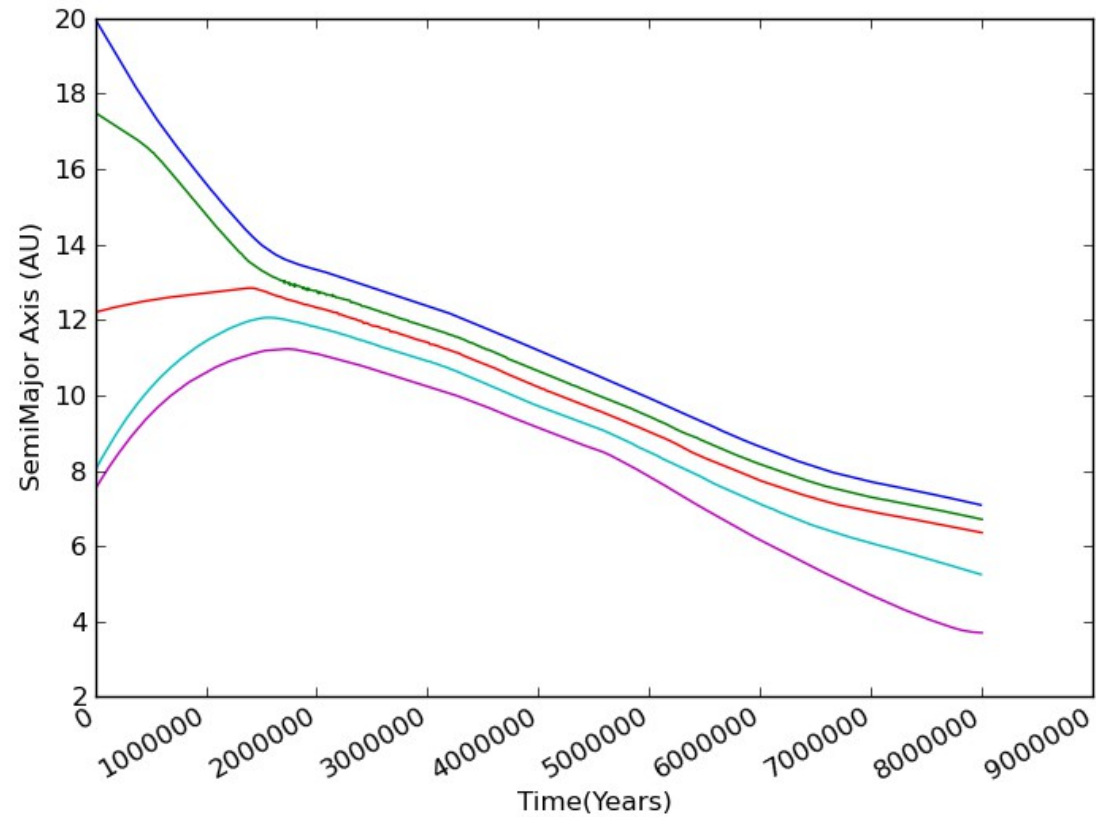
The planet **decouples** and is **released** in a safe orbit.







# Migration + N-Body in Evolutionary Models



Migration in resonance!

see also

Sandor, Lyra & Dullemond (2011)

Hellary & Nelson (2012)



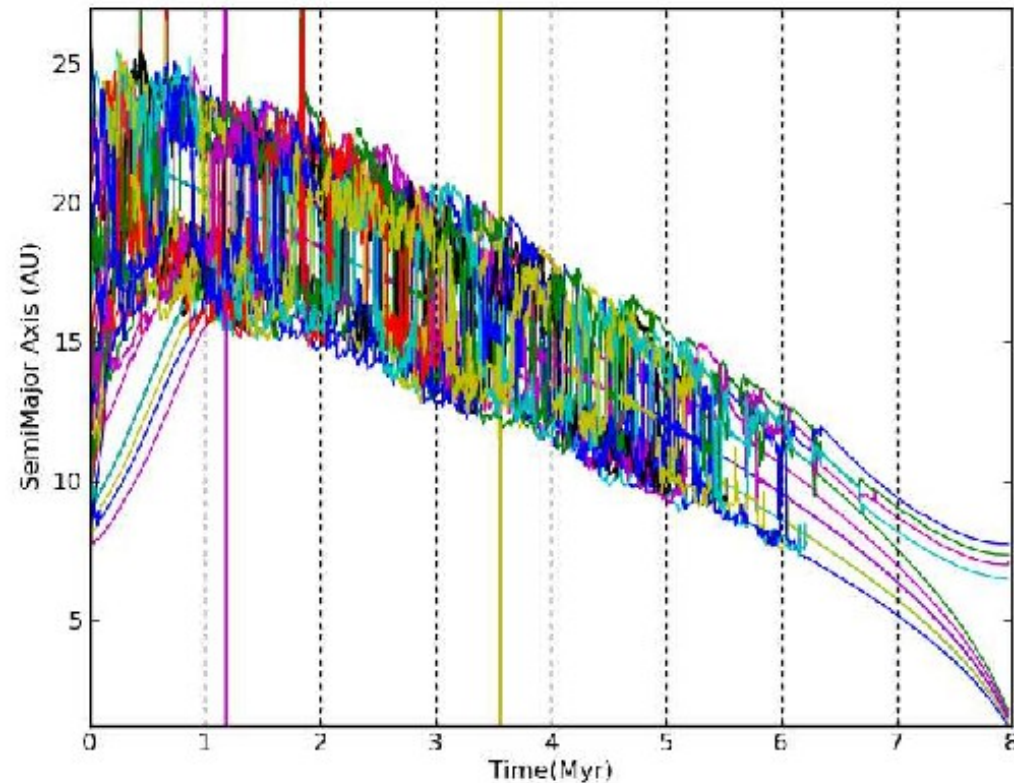
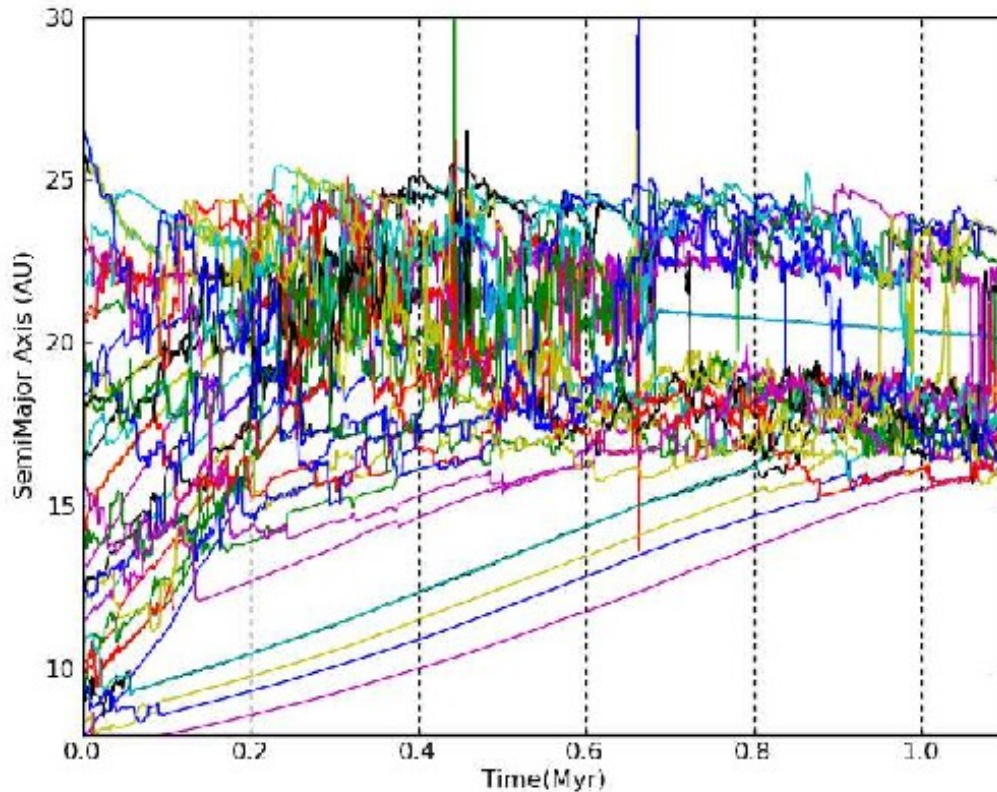
# Orbital migration of interacting planets in a radiative evolutionary model

Combines

**migration + N-body + photoevaporation + turbulence**

modelled as stochastic forcing

(Laughlin et al. 2004, Ogiwara et al. 2007)



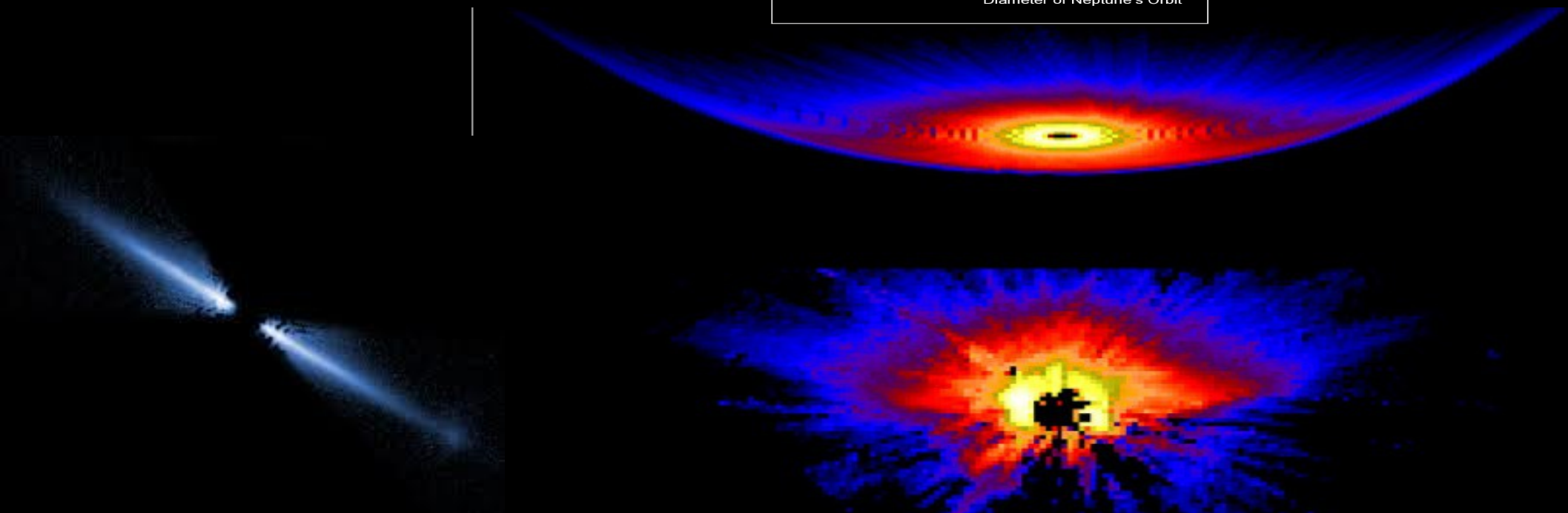
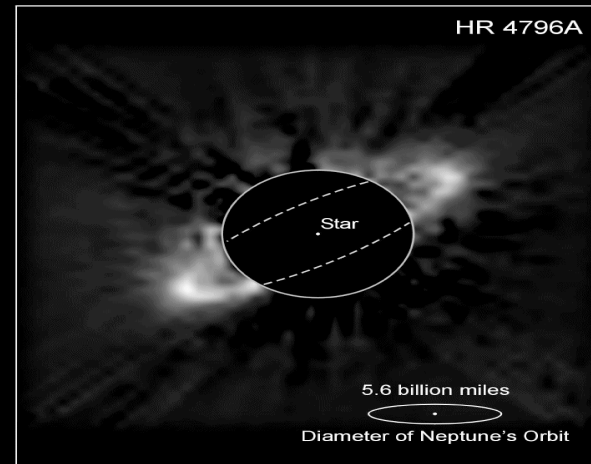
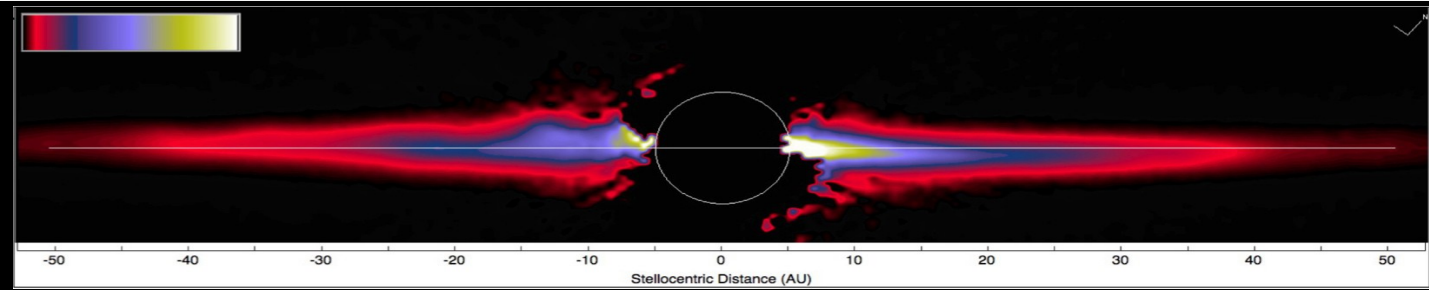
Horn et al. (2012)

# Orbital migration of interacting planets in a radiative evolutionary model

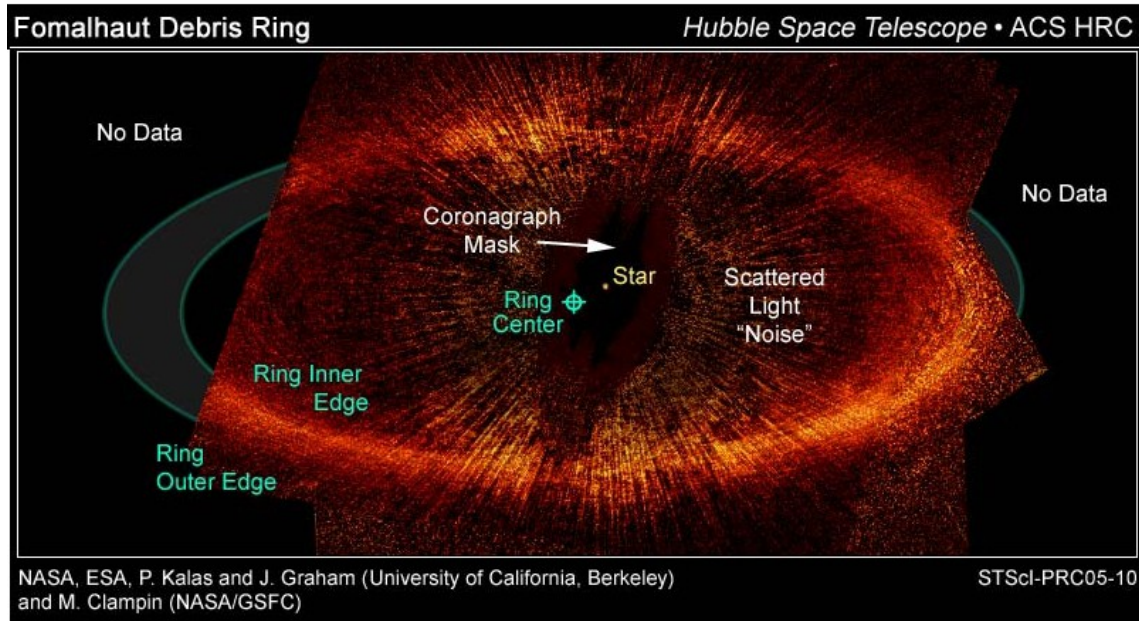


Horn et al. (2012)

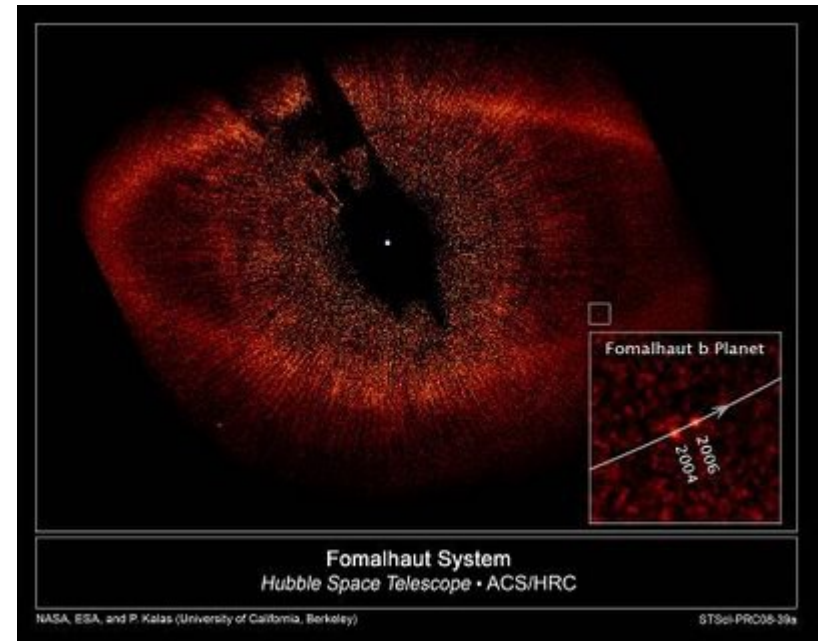
# Debris disks - The gas-poor phase



# Sharp and eccentric rings in debris disks: Signposts of planets



Narrow sharp eccentric ring



Detection of a source  
quickly heralded as a planet  
Fomalhaut b



# Sharp and eccentric rings in debris disks: Signposts of planets ?

However.....

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doi:10.1088/0004-637X/747/2/116

## INFRARED NON-DETECTION OF FOMALHAUT b: IMPLICATIONS FOR THE PLANET INTERPRETATION

MARKUS JANSON<sup>1,5</sup>, JOSEPH C. CARSON<sup>2</sup>, DAVID LAFRENIÈRE<sup>3</sup>, DAVID S. SPIEGEL<sup>4</sup>, JOHN R. BENT<sup>2</sup>, AND PALMER WONG<sup>2</sup>

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<sup>4</sup> Institute for Advanced Studies, Princeton, NJ, USA

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### ABSTRACT

The nearby A4-type star Fomalhaut hosts a debris belt in the form of an eccentric ring, which is thought to be caused by dynamical influence from a giant planet companion. In 2008, a detection of a point source inside the inner edge of the ring was reported and was interpreted as a direct image of the planet, named Fomalhaut b. The detection was made at  $\sim 600\text{--}800\text{ nm}$ , but no corresponding signatures were found in the near-infrared range, where the bulk emission of such a planet should be expected. Here, we present deep observations of Fomalhaut with *Spitzer*/IRAC at  $4.5\text{ }\mu\text{m}$ , using a novel point-spread function subtraction technique based on angular differential imaging and Locally Optimized Combination of Images, in order to substantially improve the *Spitzer* contrast at small separations. The results provide more than an order of magnitude improvement in the upper flux limit of Fomalhaut b and exclude the possibility that any flux from a giant planet surface contributes to the observed flux at visible wavelengths. This renders any direct connection between the observed light source and the dynamically inferred giant planet highly unlikely. We discuss several possible interpretations of the total body of observations of the Fomalhaut system and find that the interpretation that best matches the available data for the observed source is scattered light from a transient or semi-transient dust cloud.

*Key words:* circumstellar matter – planetary systems – stars: early-type

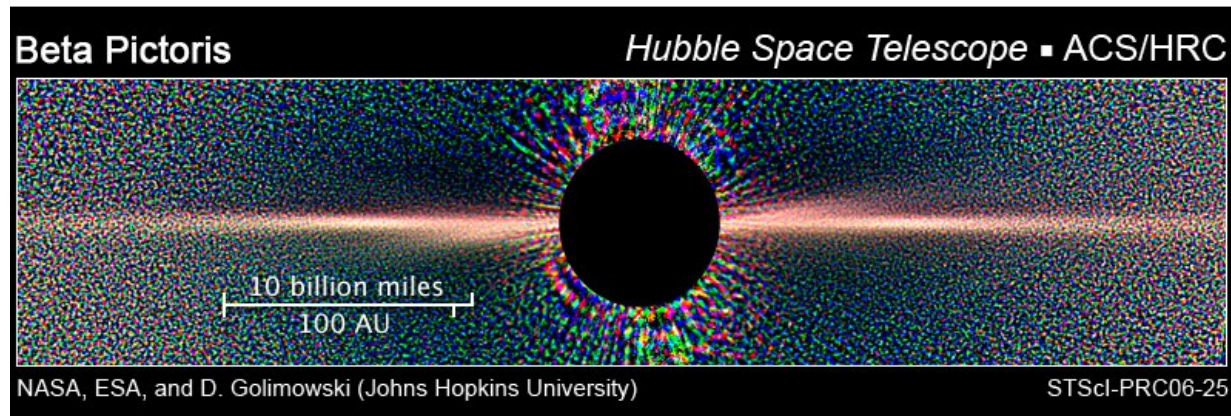
*Online-only material:* color figures

Planet not detected in infrared

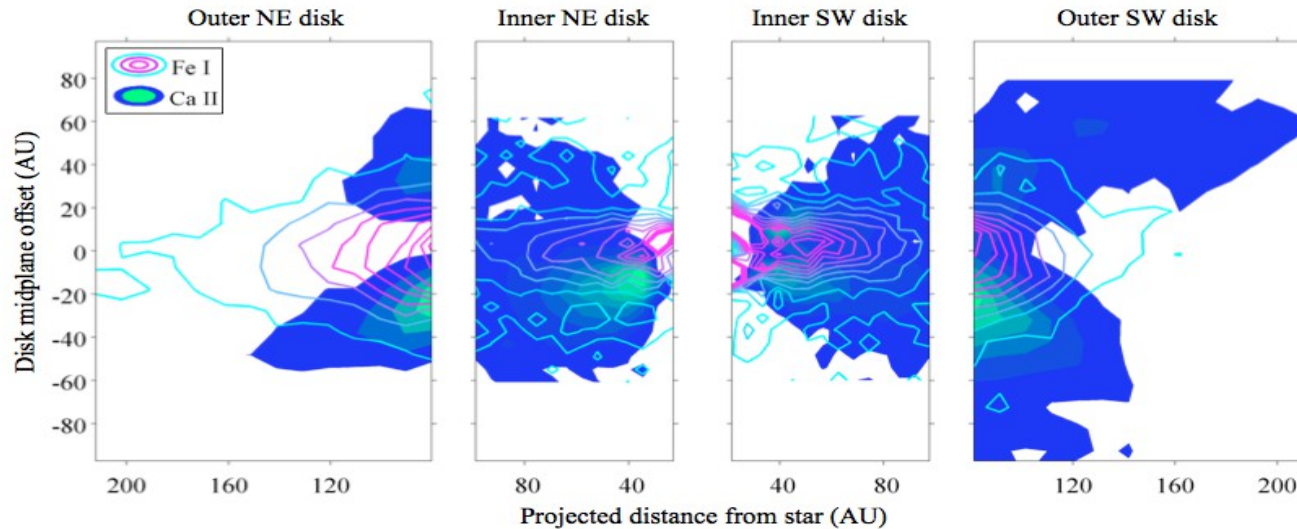
Are there  
alternative explanations?

# Debris disks are not completely gas-free

Dust



Gas



VLT imaging by  
Nilsson et al. (2012)



# Gas in debris disks

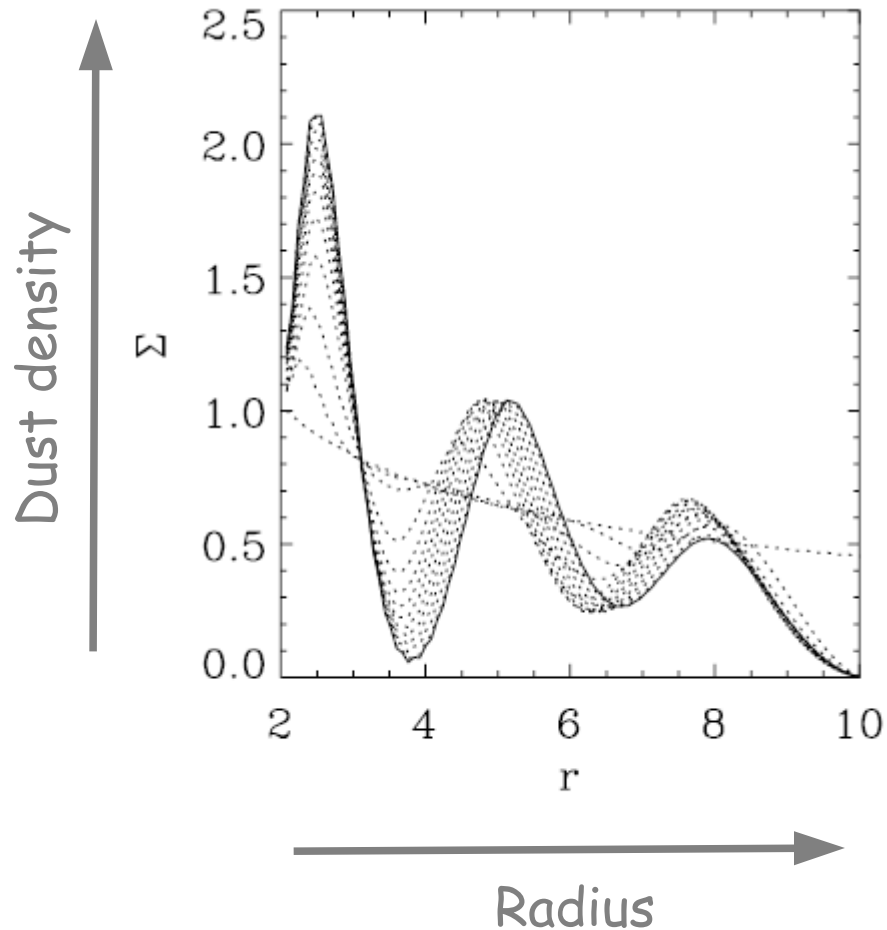
## Detections

$\beta$ Pictoris	many species	Lagrange et al. (1998), ...
51 Ophiuchi	many species	Roberge et al. (2002)
$\sigma$ Herculis	C II, N II	Chen & Jura (2003)
HD 32297	Na I, CII	Redfield (2007), Donaldson et al. (2012)
HD 135344	H <sub>2</sub> , CO	Thi et al. (2001), Pontoppidan et al. (2008)
49 Ceti	H <sub>2</sub> , CO	Dent et al. (2005), Roberge et al. (2012)
AU Mic	H <sub>2</sub>	France et al. (2007)
HD172555	SiO	Lisse et al. (2009)

## Source of gas: Outgassing processes

Infalling comets	Beust & Valiron (2007)
Grain sublimation	e.g. Rafikov (2012)
Grain-Grain collisions	Czechowski & Mann (2007)
Photo-stimulated desorption	Chen et al. (2007)
Planet-Planet collisions	Van den Ancker (2001), Lisse (2008)
Primordial?	

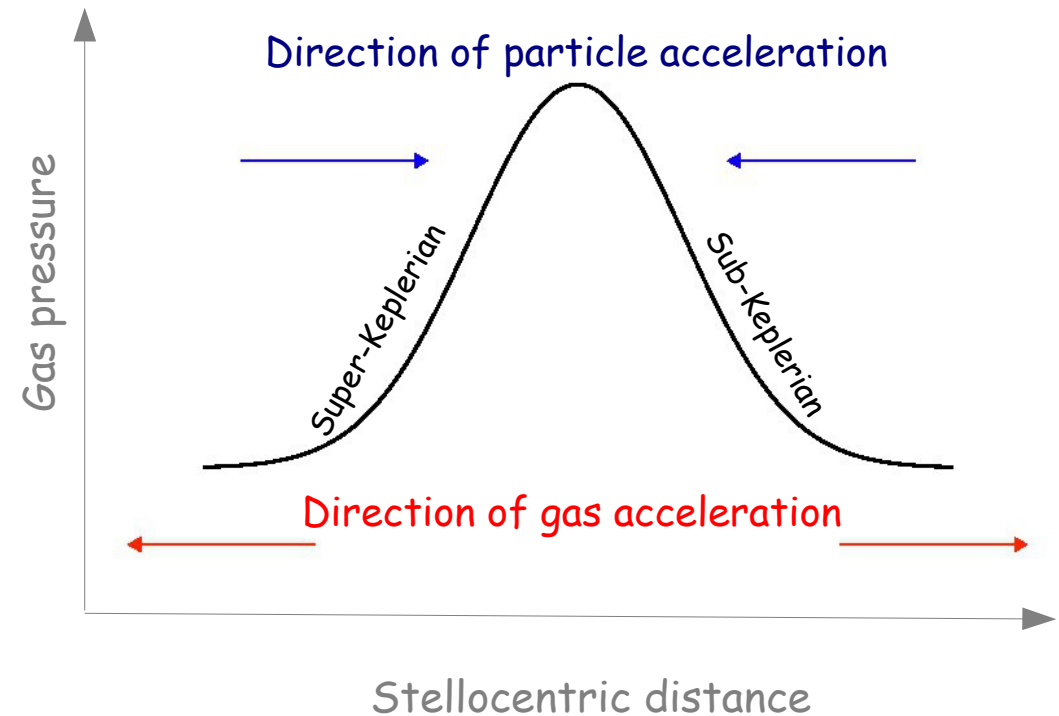
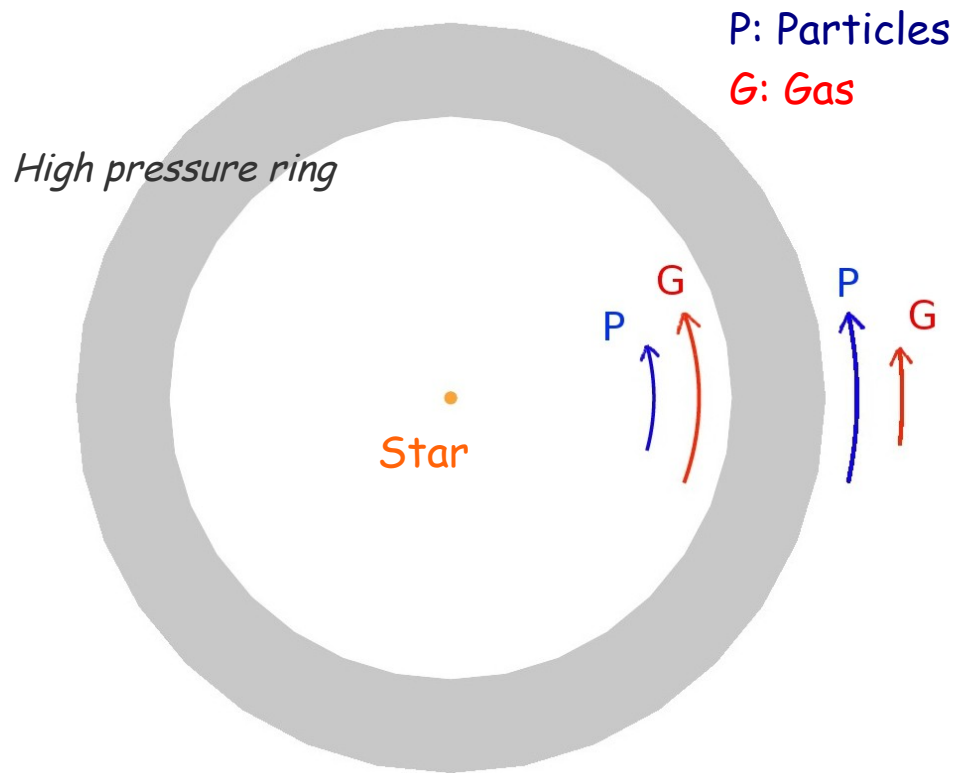
## Dust and gas together leads to instability...



Klahr & Lin (2005)

Suggested that an instability might cause dust in debris disks to clump together.

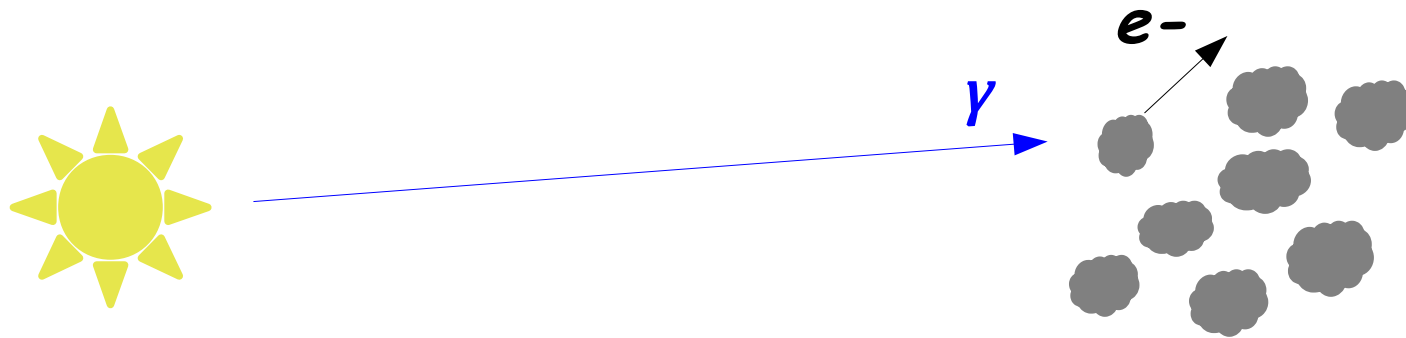
# Particles move toward pressure maxima



Adapted from Whipple (1972)

# Photoelectric heating

In optically thin debris disks,  
the **dust** is the **main heating agent** for the gas.



Dust intercepts starlight directly,  
emits electron, that heats the gas.

**Gas is photoelectrically heated by the dust itself**

# Runaway process: instability

Dust heats gas

Heated gas = high pressure region

High pressure concentrates dust

## Runaway process: instability



Dust heats gas

Heated gas = high pressure region

High pressure concentrates dust



## Model equations

Klahr & Lin (2005) used a simplified, 1-D model.

$$\frac{\partial}{\partial t} \Sigma_d + \frac{1}{r} \frac{\partial}{\partial r} r \Sigma_d v_r = 0.$$

Continuity equation

$$V_\phi = \Omega r + \frac{1}{2\Omega \Sigma_g} \frac{\partial}{\partial r} P$$

Terminal velocity

$$T_g = T_0 \left( \frac{\Sigma_d}{\Sigma_0} \right)^\beta,$$

Equation of state



# Model equations

Our simulation adds much more physics, and works in 2D.

Klahr & Lin (2005)

1D

$$\frac{\partial}{\partial t} \Sigma_d + \frac{1}{r} \frac{\partial}{\partial r} r \Sigma_d v_r = 0.$$

$$V_\phi = \Omega r + \frac{1}{2\Omega \Sigma_g} \frac{\partial}{\partial r} P$$

$$T_g = T_0 \left( \frac{\Sigma_d}{\Sigma_0} \right)^\beta,$$

*Inertia for both gas and dust*

*Energy equation*

*Drag force and  
drag force backreaction*

Lyra & Kuchner (2012)

2D

$$\frac{\partial \Sigma_g}{\partial t} = -(\mathbf{u} \cdot \nabla) \Sigma_g - \Sigma_g \nabla \cdot \mathbf{u}$$

$$\frac{\partial \mathbf{u}}{\partial t} = -(\mathbf{u} \cdot \nabla) \mathbf{u} - \frac{1}{\Sigma_g} \nabla P - \nabla \Phi - \frac{\Sigma_d}{\Sigma_g} \mathbf{f}_d$$

$$\frac{\partial S}{\partial t} = -(\mathbf{u} \cdot \nabla) S - \frac{c_v}{T} \frac{(T - T_p)}{\tau_T}.$$

$$\frac{d\mathbf{x}}{dt} = \mathbf{v}$$

$$\frac{d\mathbf{v}}{dt} = -\nabla \Phi + \mathbf{f}_d$$

$$\mathbf{f}_d = -\frac{(\mathbf{v} - \mathbf{u})}{\tau_f}$$

$$T_p = T_0 \frac{\Sigma_d}{\Sigma_0}.$$

# Linear Analysis

$$D_w \Sigma_d = -\Sigma_d \nabla \cdot \mathbf{w}$$

**Dust**

$$D_w w_x = 2\Omega w_y - \frac{1}{\tau_f}(w_x - u_x)$$

$$D_w w_y = -\frac{1}{2}\Omega w_x - \frac{1}{\tau_f}(w_y - u_y)$$

$$D_u \Sigma_g = -\Sigma_g \nabla \cdot \mathbf{u}$$

**Gas**

$$D_u u_x = 2\Omega u_y - \frac{1}{\Sigma_g} \frac{\partial P}{\partial x} - \frac{\epsilon}{\tau_f}(u_x - w_x)$$

$$D_u u_y = -\frac{1}{2}\Omega u_x - \frac{1}{\Sigma_g} \frac{\partial P}{\partial y} - \frac{\epsilon}{\tau_f}(u_y - w_y)$$

$$\psi = \psi_0 + \psi'$$

$$\psi' = \hat{\psi} \exp(ikx + st)$$

**Dispersion relation**

$$A\omega^5 + B\omega^4 + C\omega^3 + D\omega^2 + E\omega + F = 0$$

$$A = 1$$

$$B = 2\epsilon + 2$$

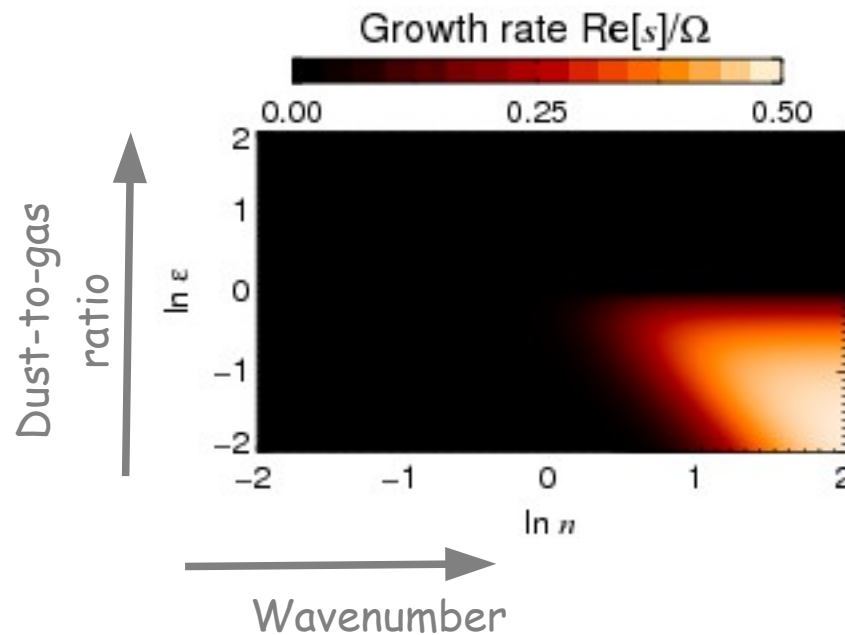
$$C = \epsilon^2 + \epsilon(n^2 + 2) + 3$$

$$D = \epsilon^2 n^2 + \epsilon(3n^2 + 2) + 2$$

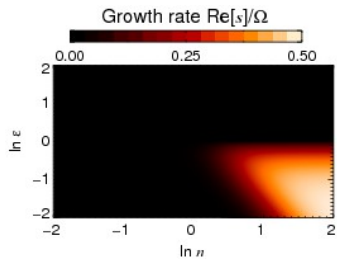
$$E = \epsilon^2(2n^2 + 1) + \epsilon(3n^2 + 2) + 2$$

$$F = \epsilon^2 n^2 - \epsilon n^2$$

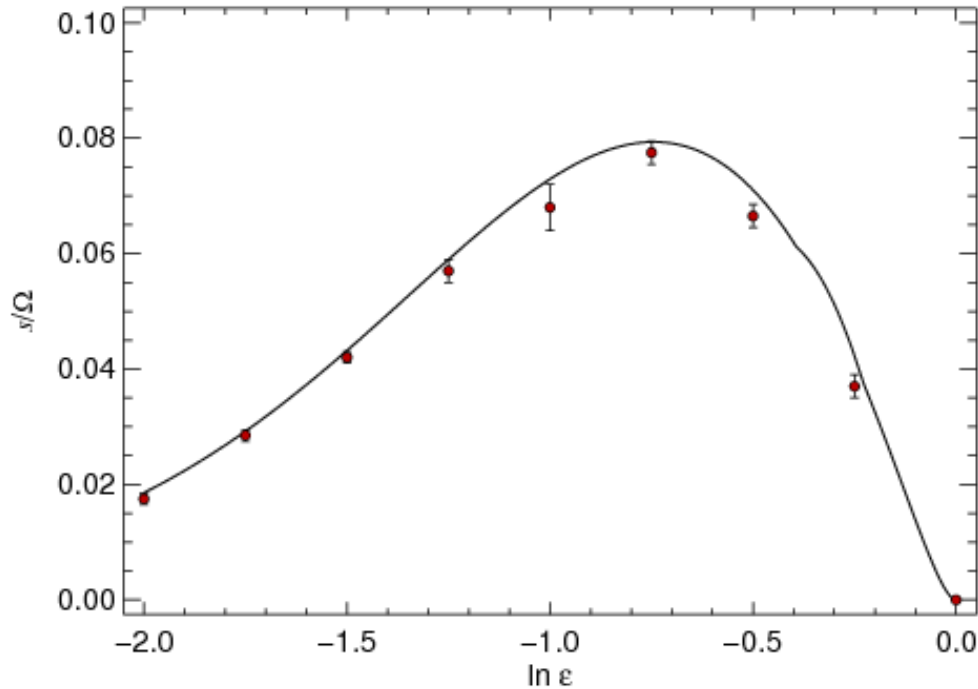
$$\epsilon = \Sigma_d / \Sigma_g \quad n = kH \quad \omega = s/\Omega$$



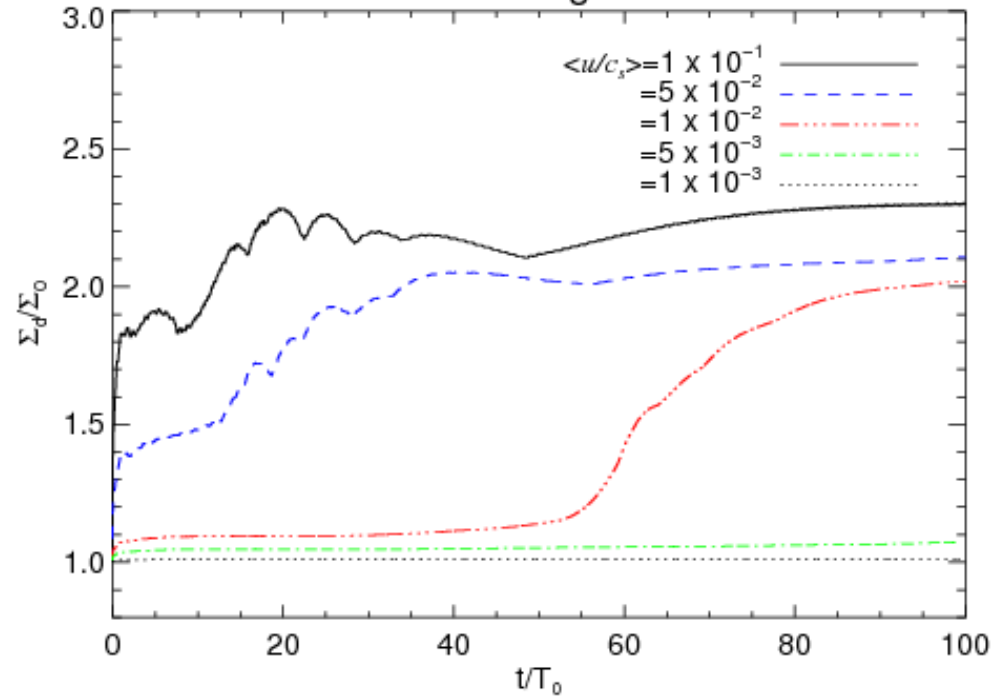
# Linear and nonlinear growth



Growth rates  $\alpha=10^{-2}$



Nonlinear growth



Linear growth only exists for  $\epsilon < 1$

But there is  
**nonlinear growth**  
beyond !

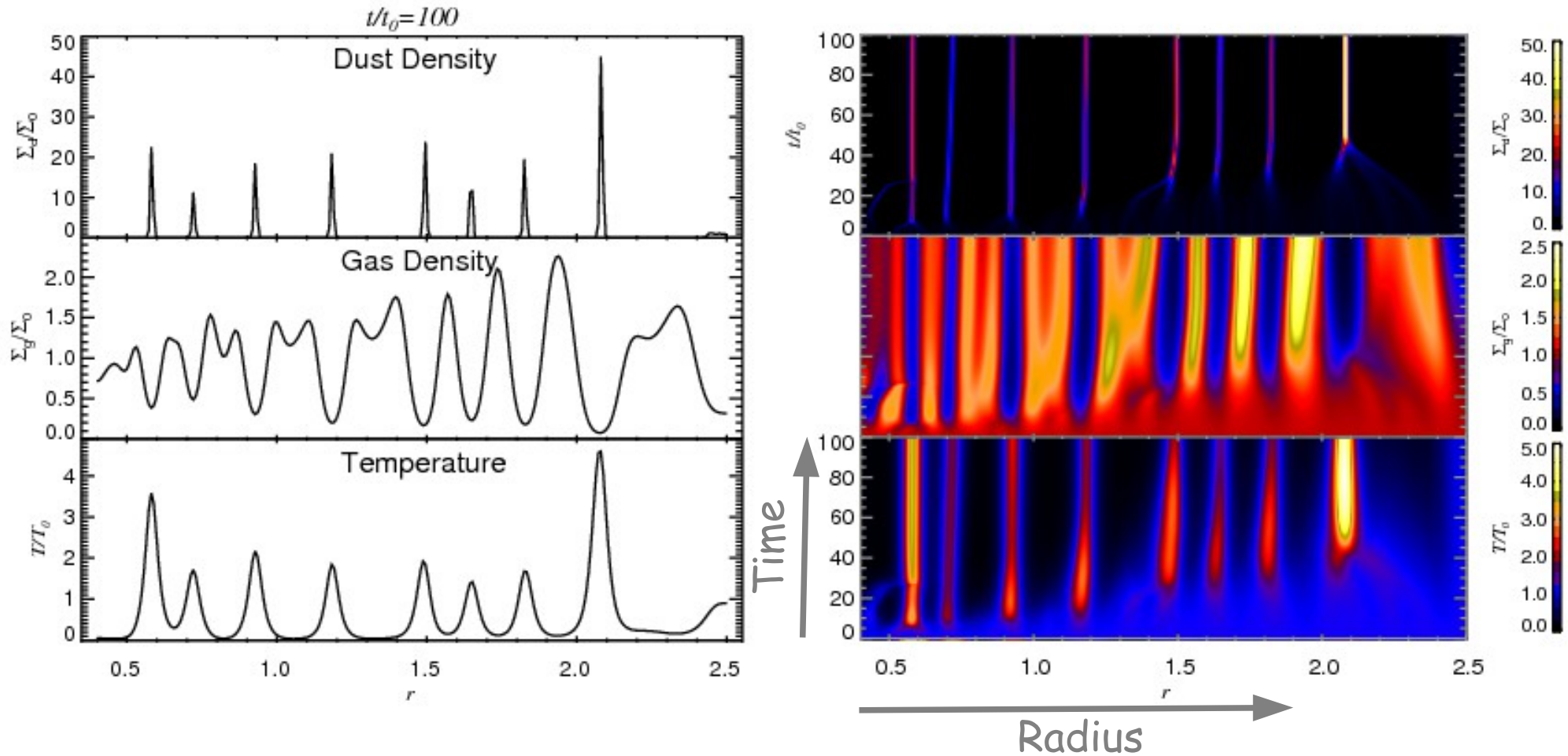
# Instability



Dust heats gas

Heated gas = high pressure region

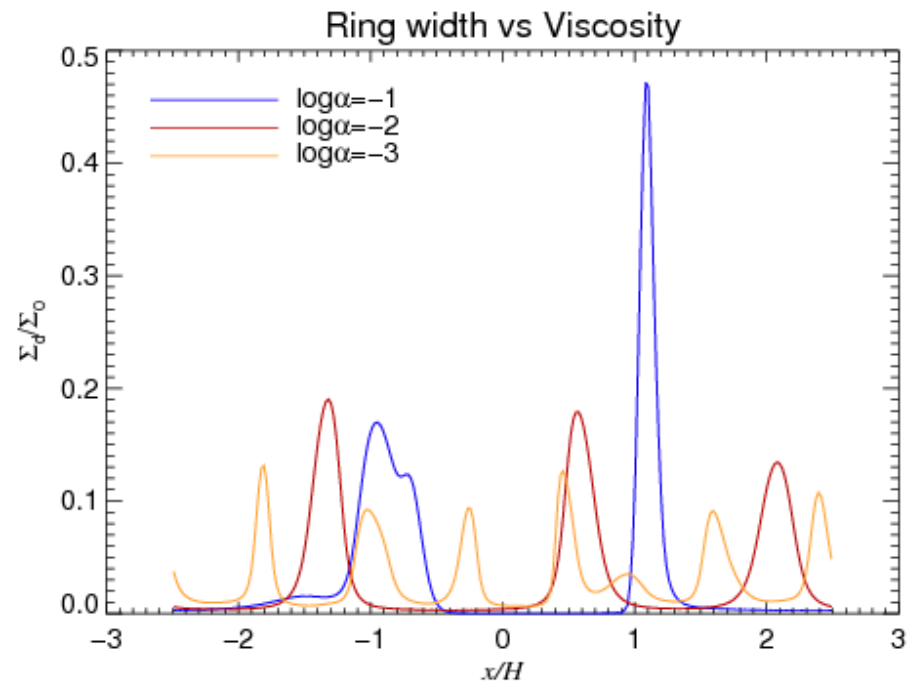
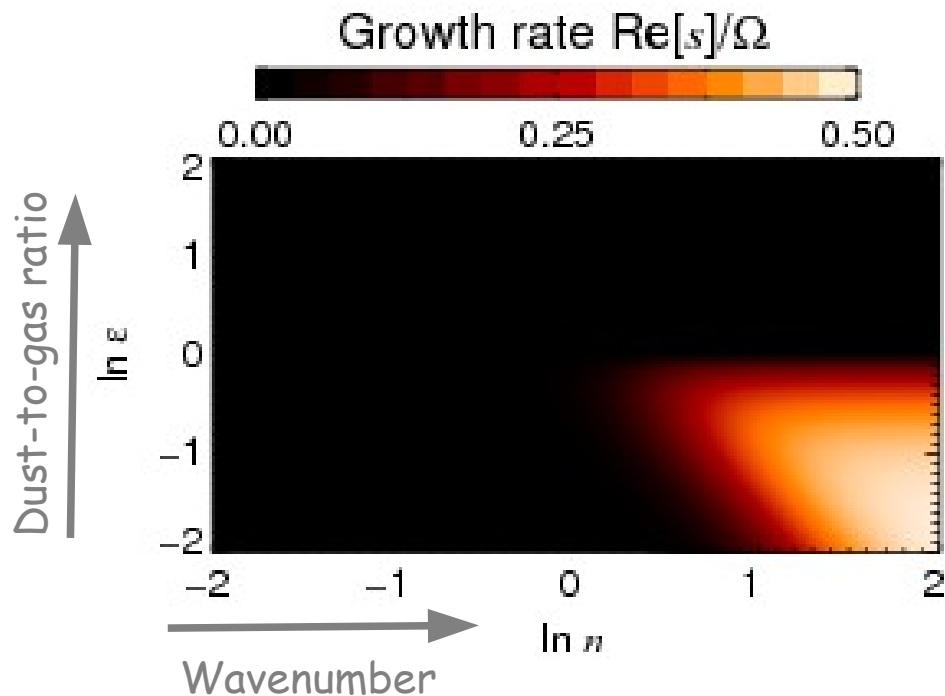
High pressure concentrates dust



Narrow hot dust rings  
Cold gas collects between rings

# Ring width

Ring spacing and width is determined by the wavelength of maximum growth.

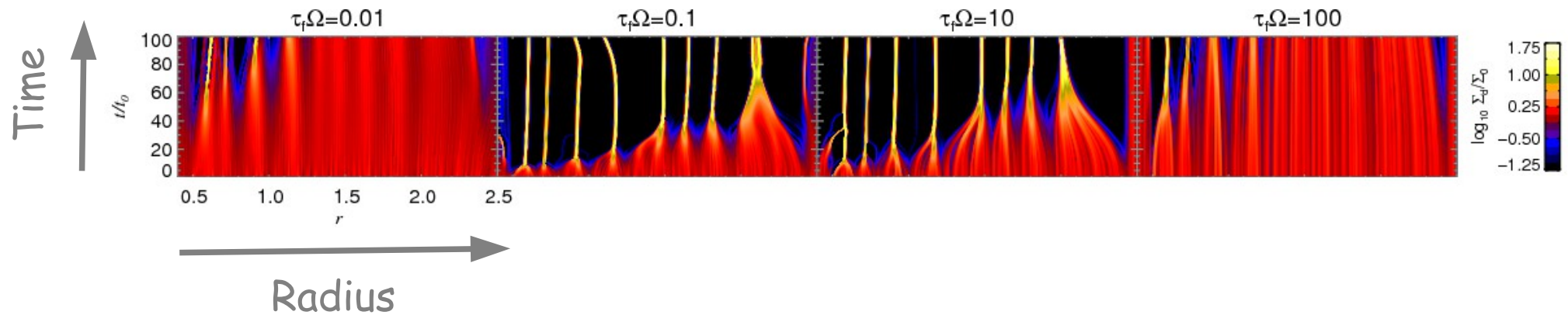


Which in turn is determined by viscosity

**Ring width  $\sim 10$  Kolmogorov lengths**

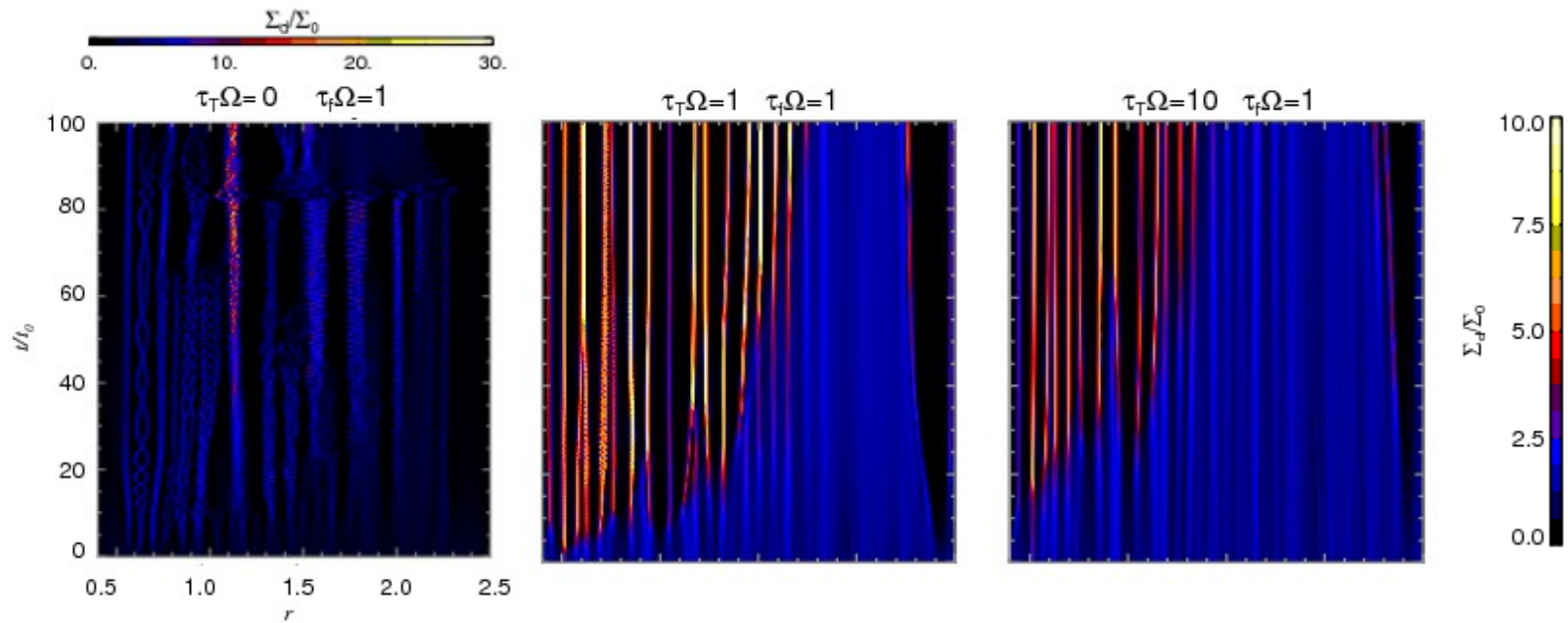
# Robustness

Growth over 4 orders of  
magnitude in dust-gas  
coupling time (friction time)



# Oscillations

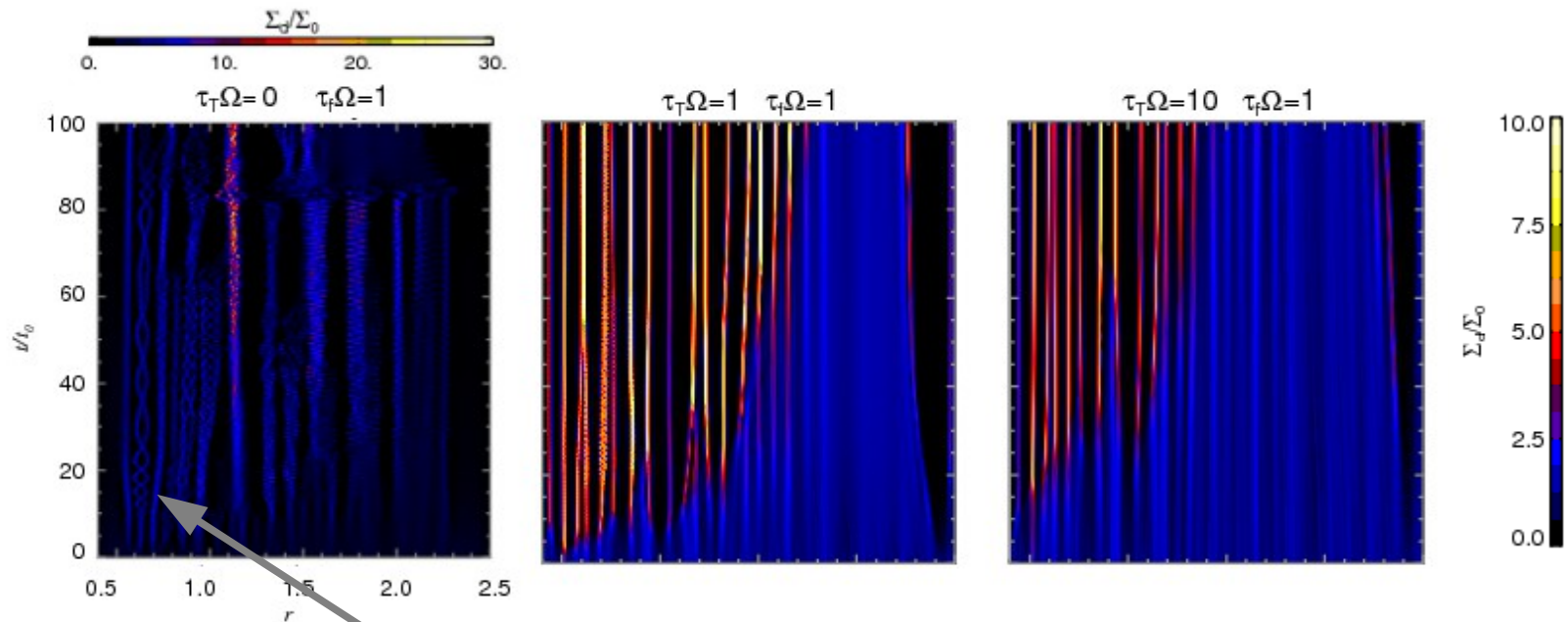
Thermal coupling time





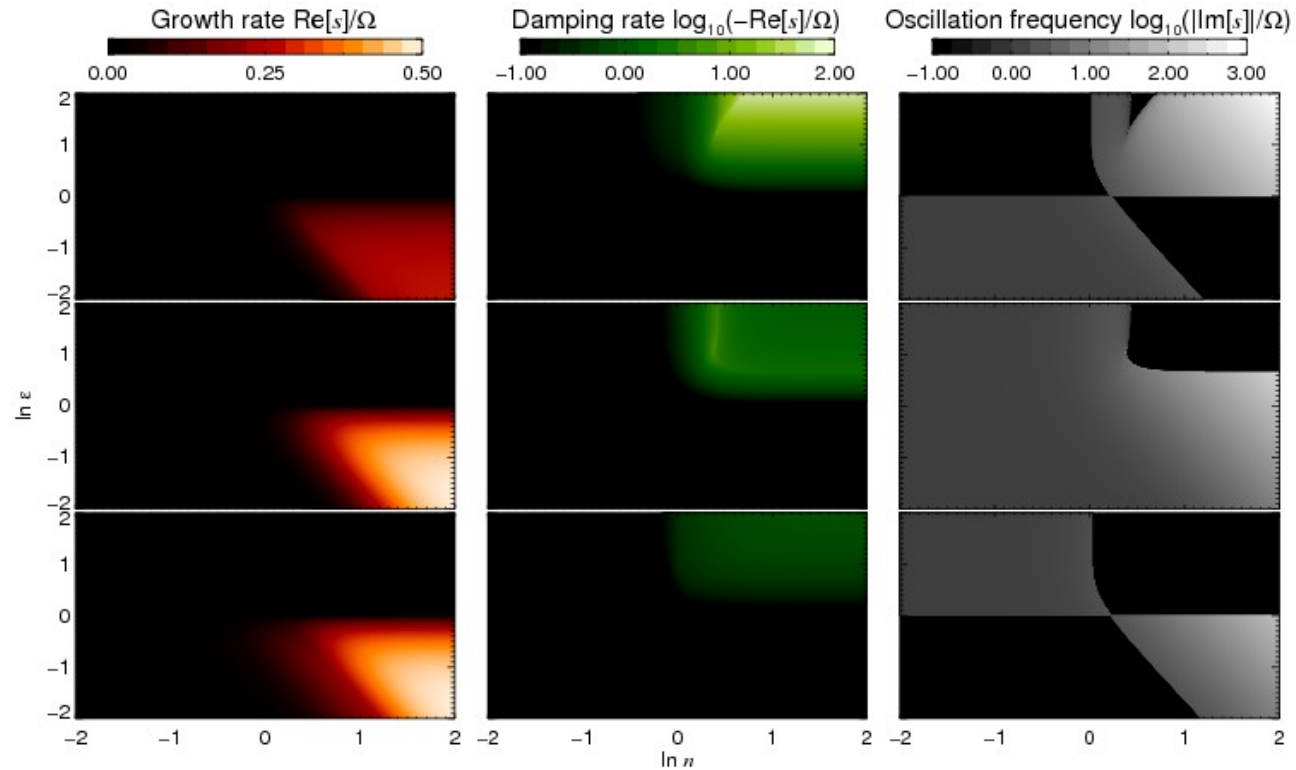
# Oscillations

Thermal coupling time



Oscillations appear  
with decreasing thermal time.

# Solutions



## Dispersion relation

$$A\omega^5 + B\omega^4 + C\omega^3 + D\omega^2 + E\omega + F = 0$$

$$A=1$$

$$B=2\epsilon + 2$$

$$C=\epsilon^2 + \epsilon(n^2+2) + 3$$

$$D=\epsilon^2 n^2 + \epsilon(3n^2+2) + 2$$

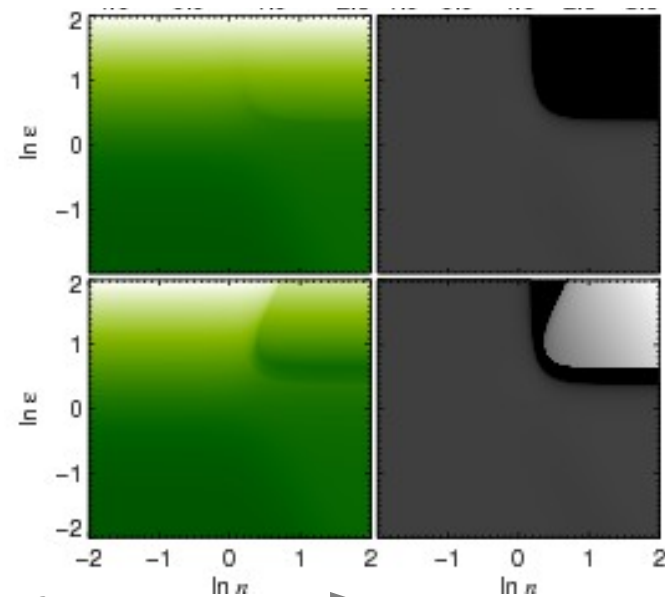
$$E=\epsilon^2(2n^2+1) + \epsilon(3n^2+2) + 2$$

$$F=\epsilon^2 n^2 - \epsilon n^2$$

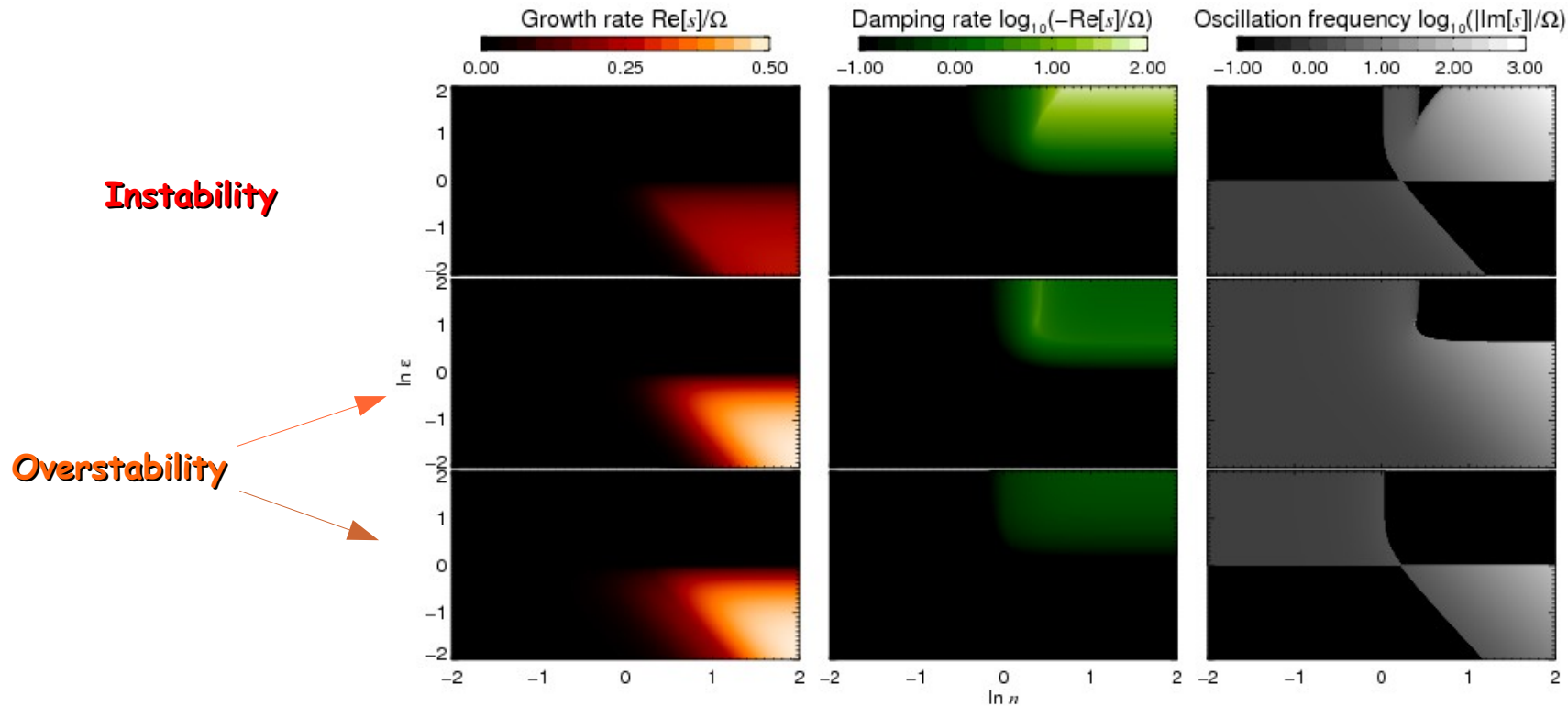
$$\epsilon = \Sigma_d / \Sigma_g \quad n = kH \quad \omega = s/\Omega$$

Dust-to-gas  
ratio

Wavenumber



# Solutions



## Dispersion relation

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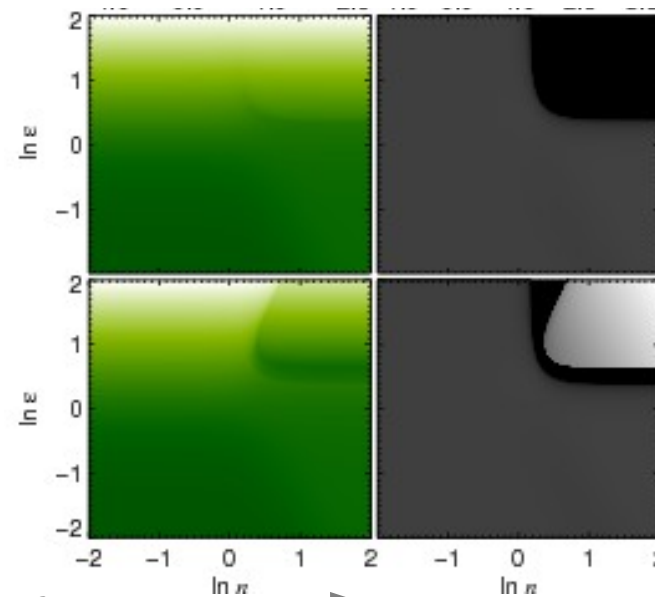
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Dust-to-gas  
ratio

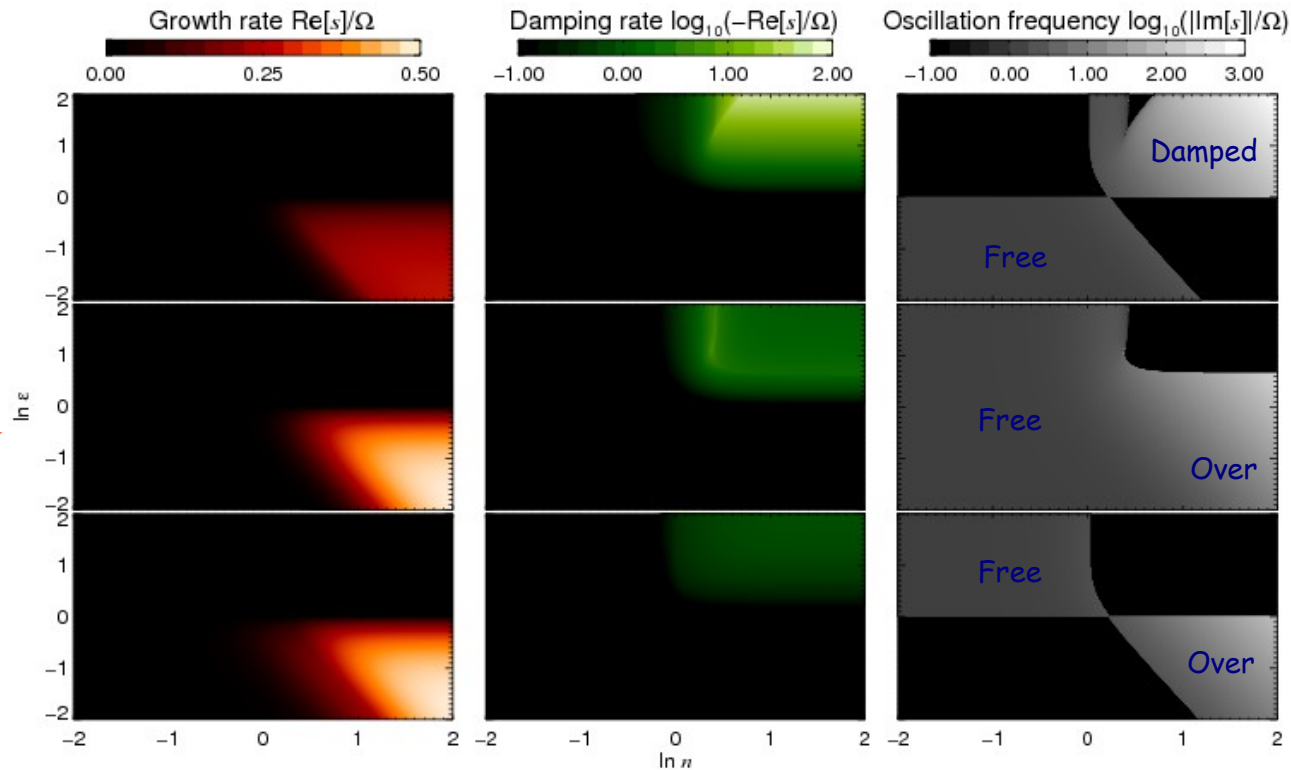
Wavenumber



# Solutions

Instability

Overstability



Damped and free Oscillations

## Dispersion relation

$$A\omega^5 + B\omega^4 + C\omega^3 + D\omega^2 + E\omega + F = 0$$

$$A=1$$

$$B=2\epsilon + 2$$

$$C=\epsilon^2 + \epsilon(n^2+2) + 3$$

$$D=\epsilon^2 n^2 + \epsilon(3n^2+2) + 2$$

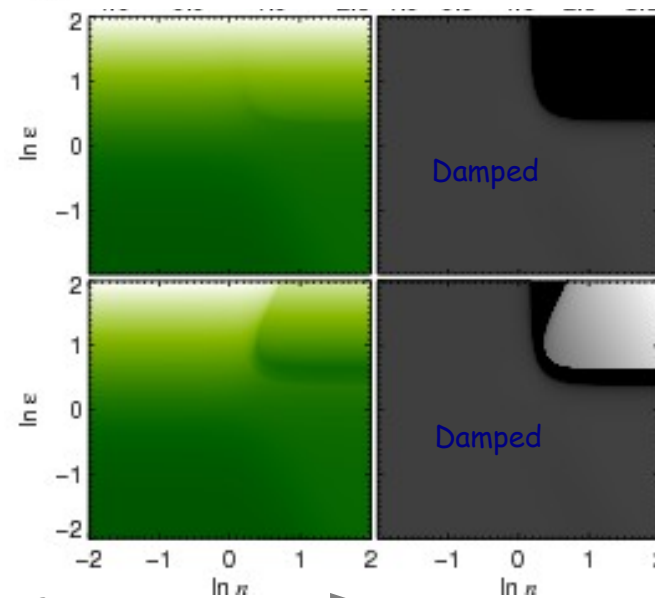
$$E=\epsilon^2(2n^2+1) + \epsilon(3n^2+2) + 2$$

$$F=\epsilon^2 n^2 - \epsilon n^2$$

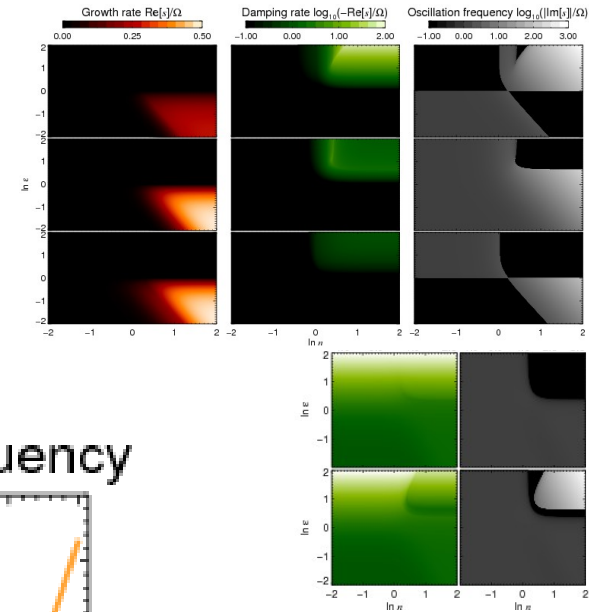
$$\epsilon = \Sigma_d / \Sigma_g \quad n = kH \quad \omega = s/\Omega$$

Dust-to-gas ratio

Wavenumber



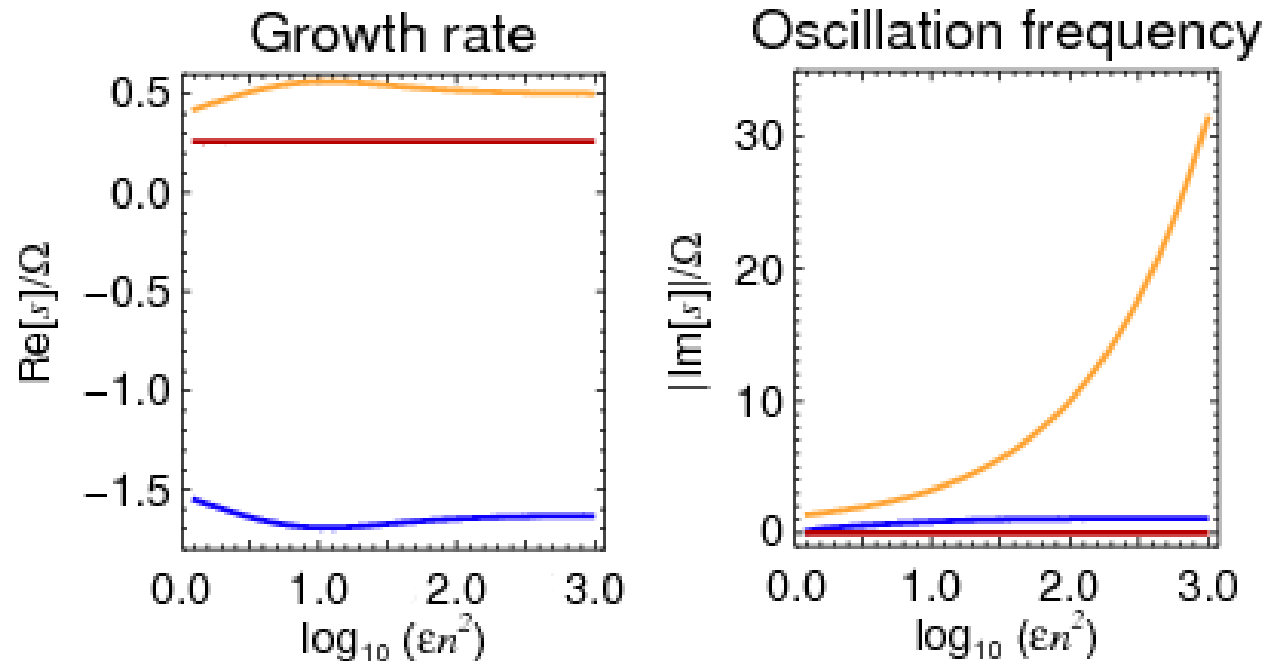
# Solutions



Overstability

Instability

Oscillations



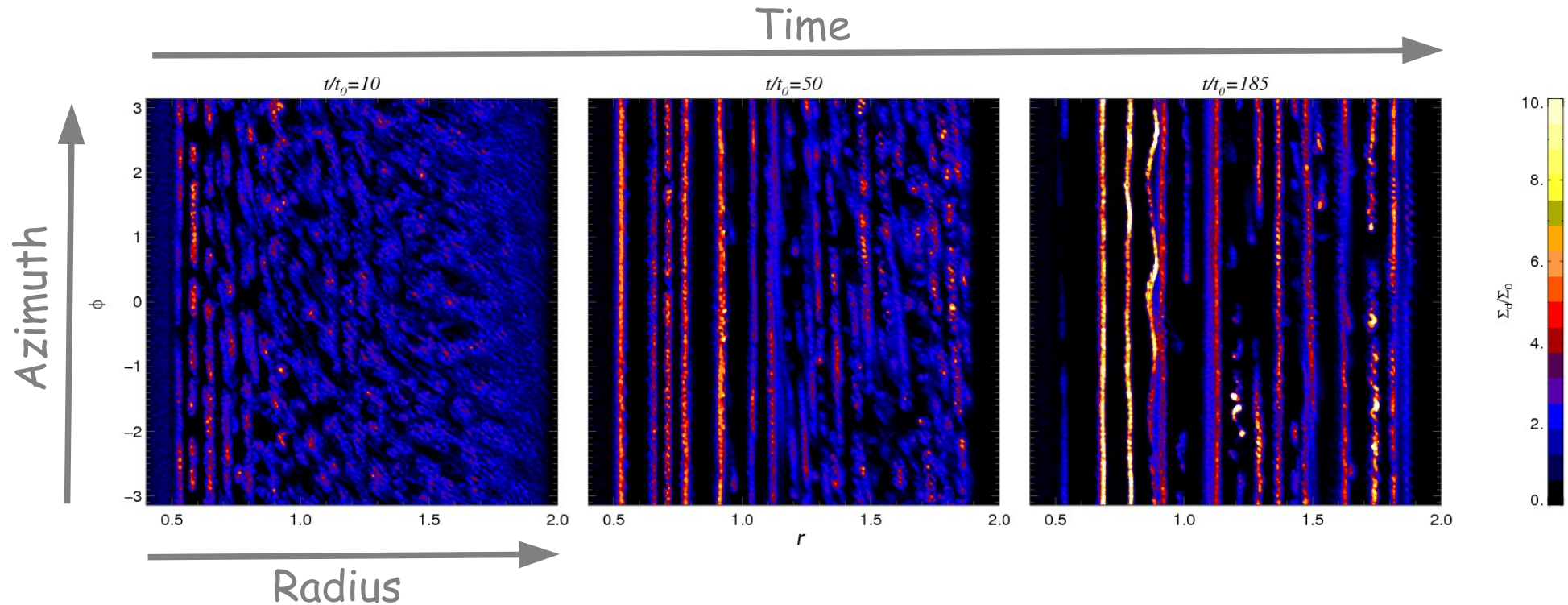
Max growth rate:  $\Omega/2$ .

**Million-fold amplification in five orbits!**

A very powerful instability.

# The model in 2D: Eccentric rings

Growth of axisymmetric modes  
+  
Damping of nonaxisymmetric modes.  
= *Rings !!!*

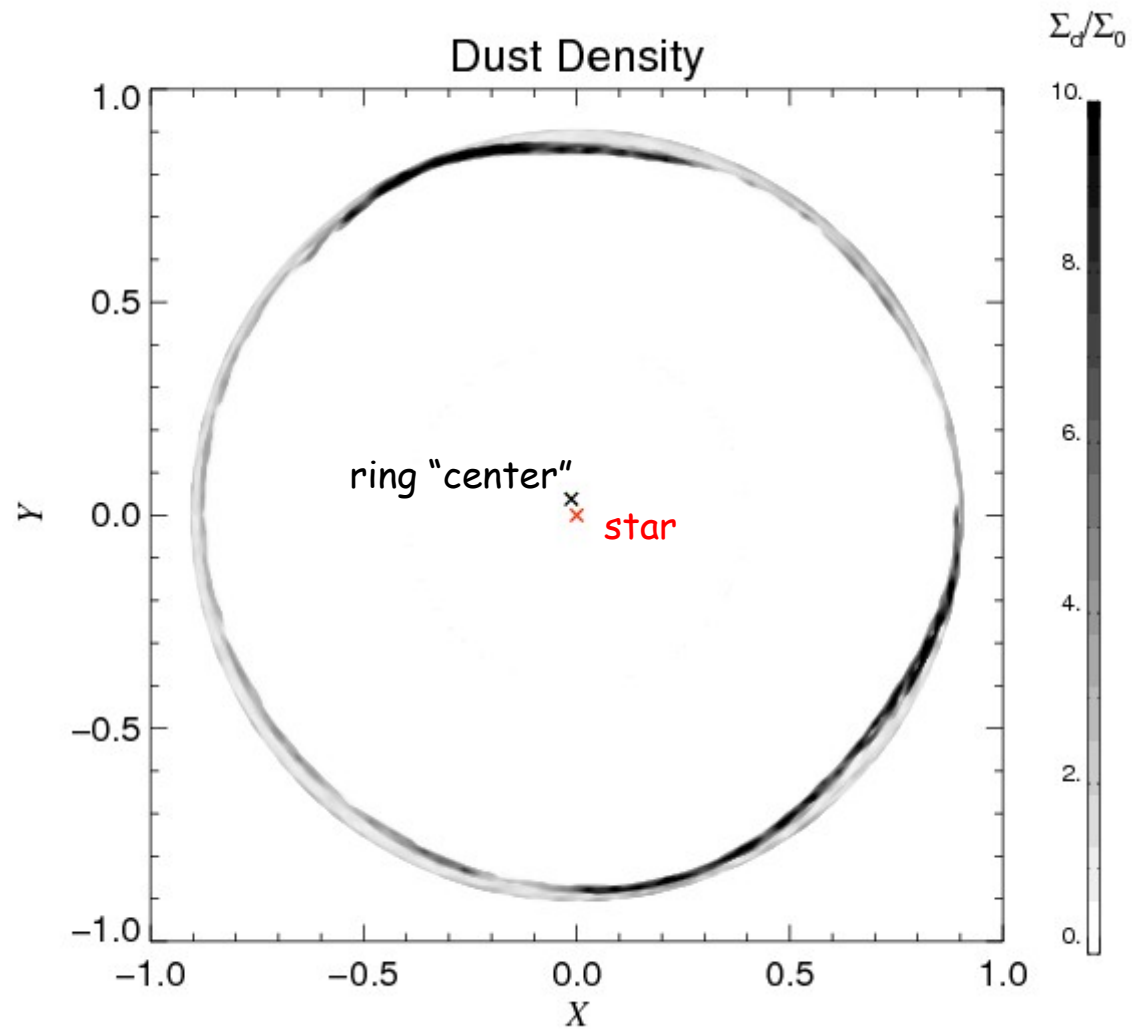


Epicyclic oscillations  
make the ring appear *eccentric !!!*





# Ring eccentricity



Eccentricity  $e=0.04$

# Summarizing

## Gravitational collapse of an interstellar cloud

Outward transport of angular momentum through turbulence generated by the MRI. Dust coagulates into pebbles and boulders, sedimenting towards the midplane.

Rocks in the turbulent medium are trapped in transient pressure maxima and undergo collapse into planetesimals and dwarf planets.

Vortices may be excited in the dead zone. Inside them, the first dozens of Mars-mass embryos are formed. IMF  $\sim -2$

Opacity transitions develop into regions of convergent migration. Low mass planets converge to these zones by inward/outward migration.

Convergent migration leads to resonances, these are disrupted by turbulent forcing. Collisions between embryos gives rise to oligarchs.

The disk thins due to photoevaporation. Planets released into stable orbits.

N-body interactions and stochastic forcing during disk evaporation produce the system's final architecture.

Debris disks with gas are subject to a thermo-centrifugal instability

The instability generates sharp eccentric rings. Caution before shouting "planet!". Not all that glitters is gold.

(a)

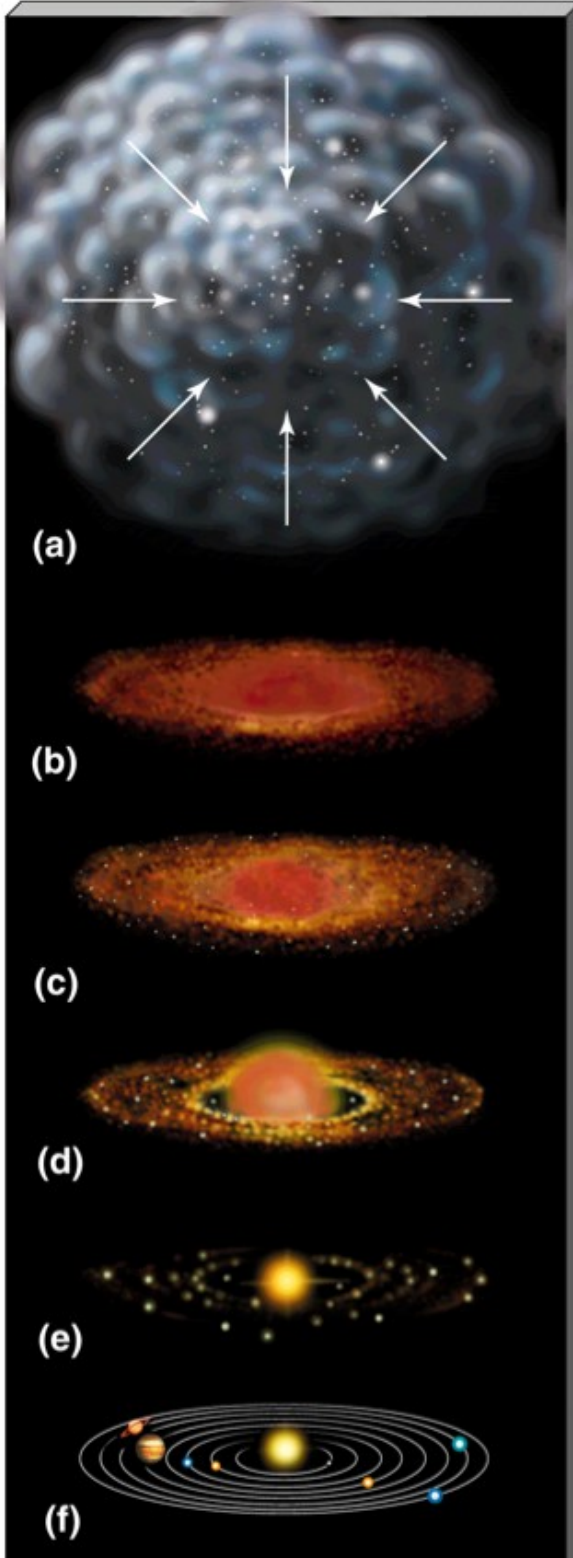
(b)

(c)

(d)

(e)

(f)

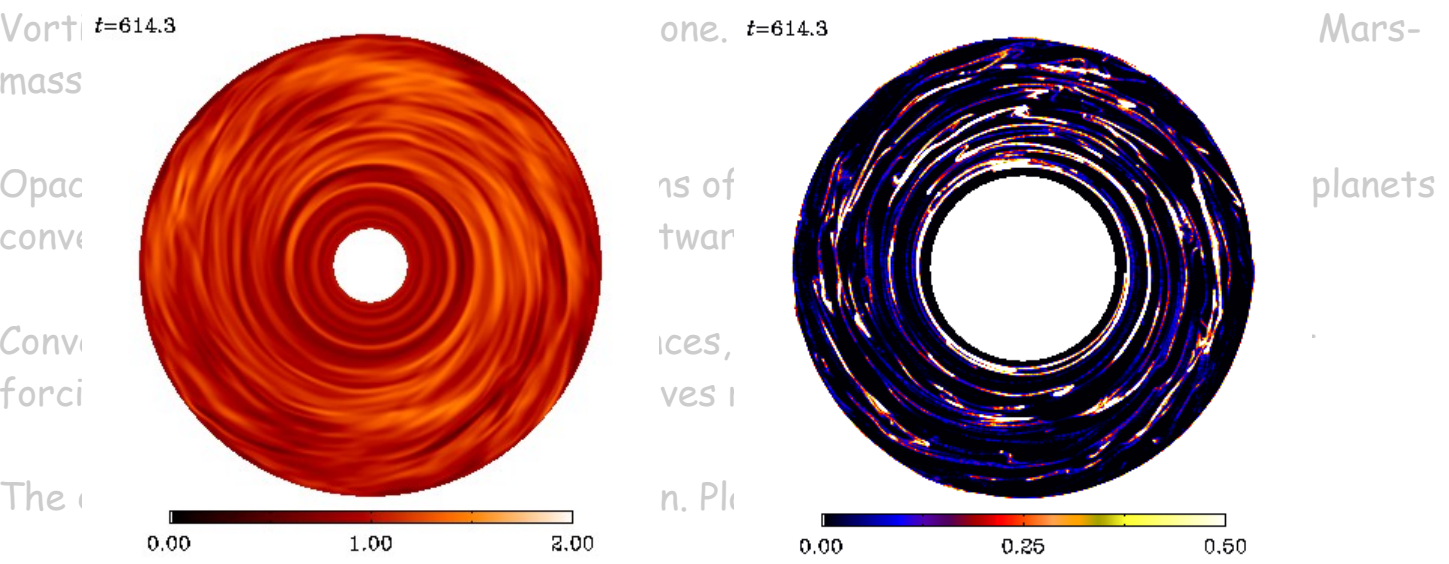


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Gravitational collapse of an interstellar cloud

Outward transport of angular momentum through turbulence generated by the MRI. Dust coagulates into pebbles and boulders, sedimenting towards the midplane.

Rocks in the turbulent medium are trapped in transient pressure maxima and undergo collapse into planetesimals and dwarf planets. **Gas** **Solids**



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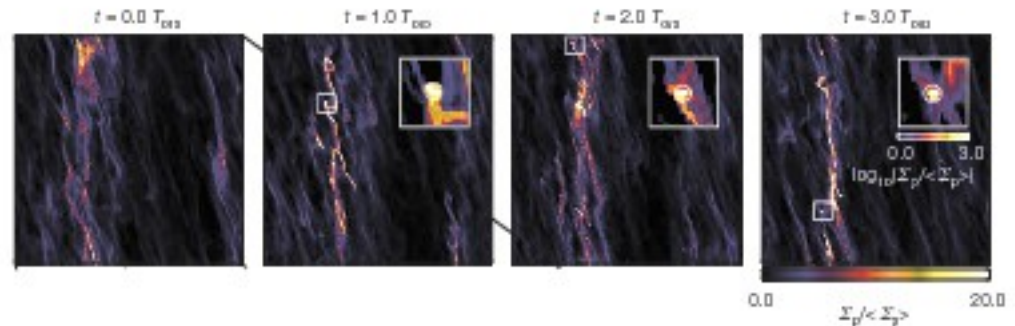
(b)

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(d)

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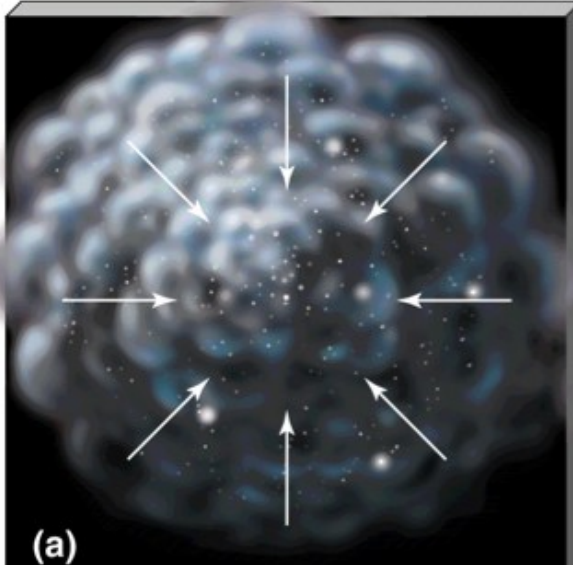
(f)



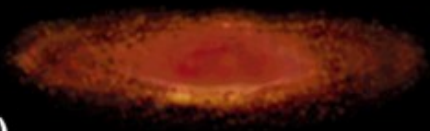
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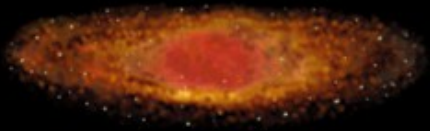
# Summarizing



(a)



(b)



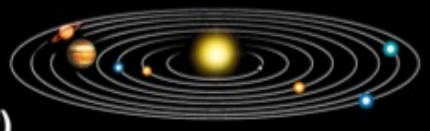
(c)



(d)



(e)

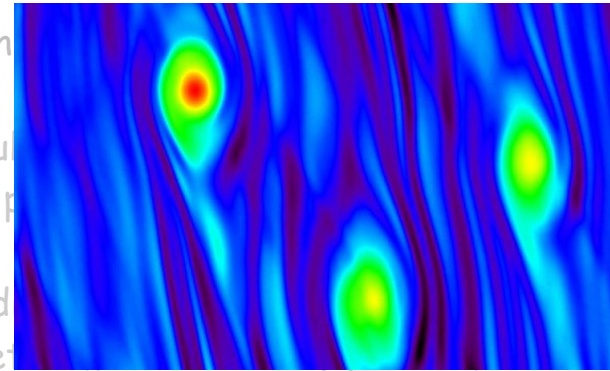


(f)

Gravitational collapse of an

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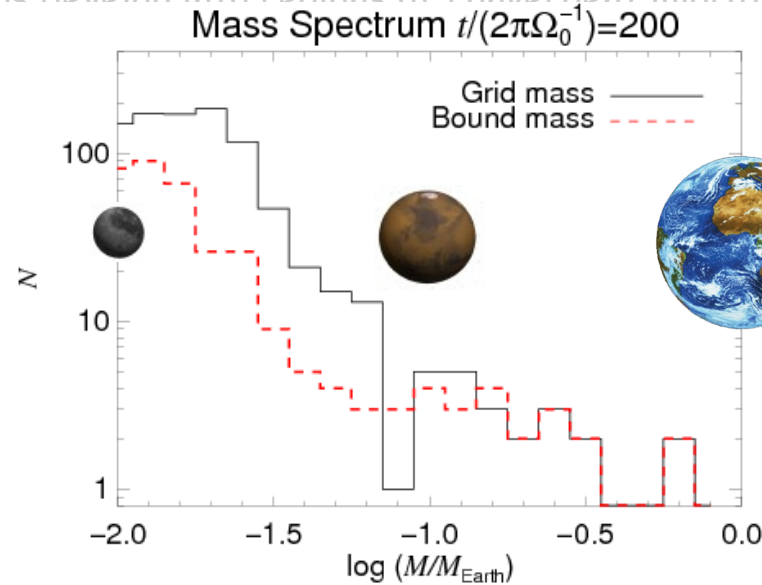
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The disk thins

N-body interaction system's final

Debris disks with



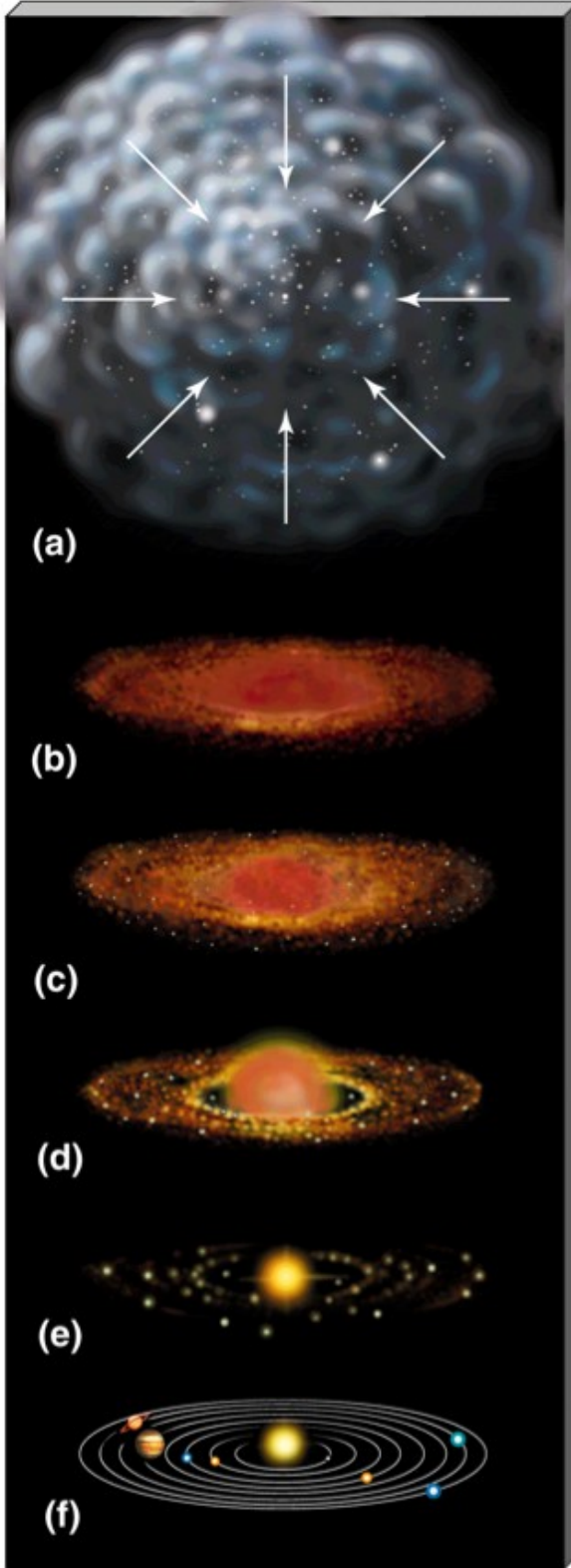
by turbulent

stable orbits.

interaction produce the

ability

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## Summarizing

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Outward transport of an MRI. Dust coagulates into

Rocks in the turbulent medium undergo collapse into planets

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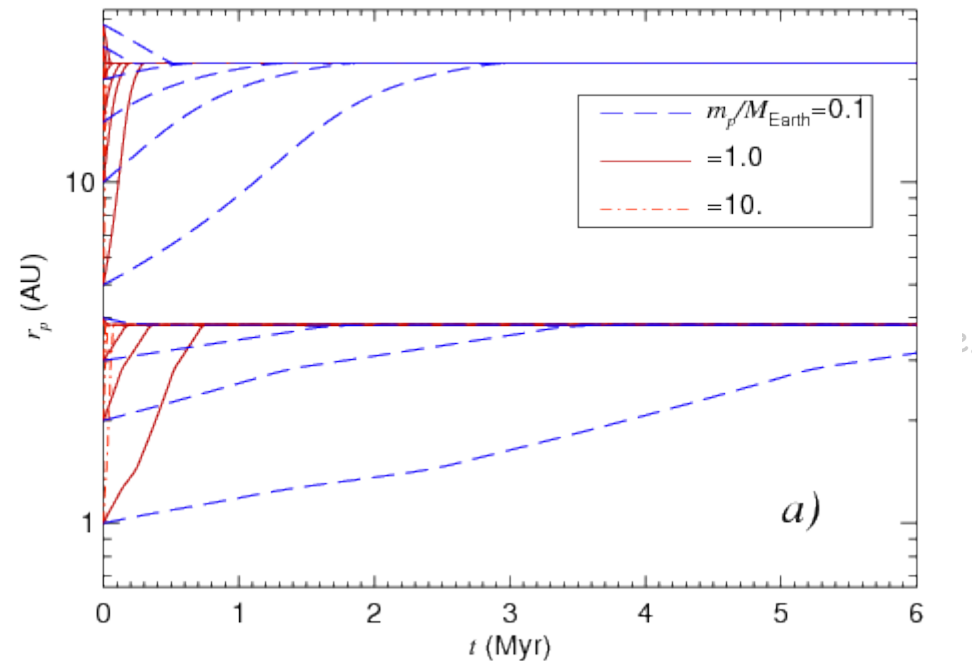
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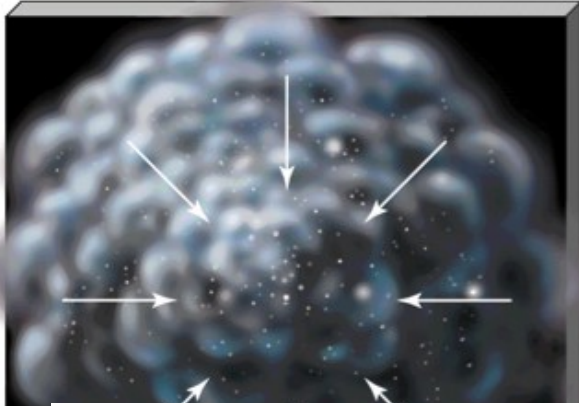
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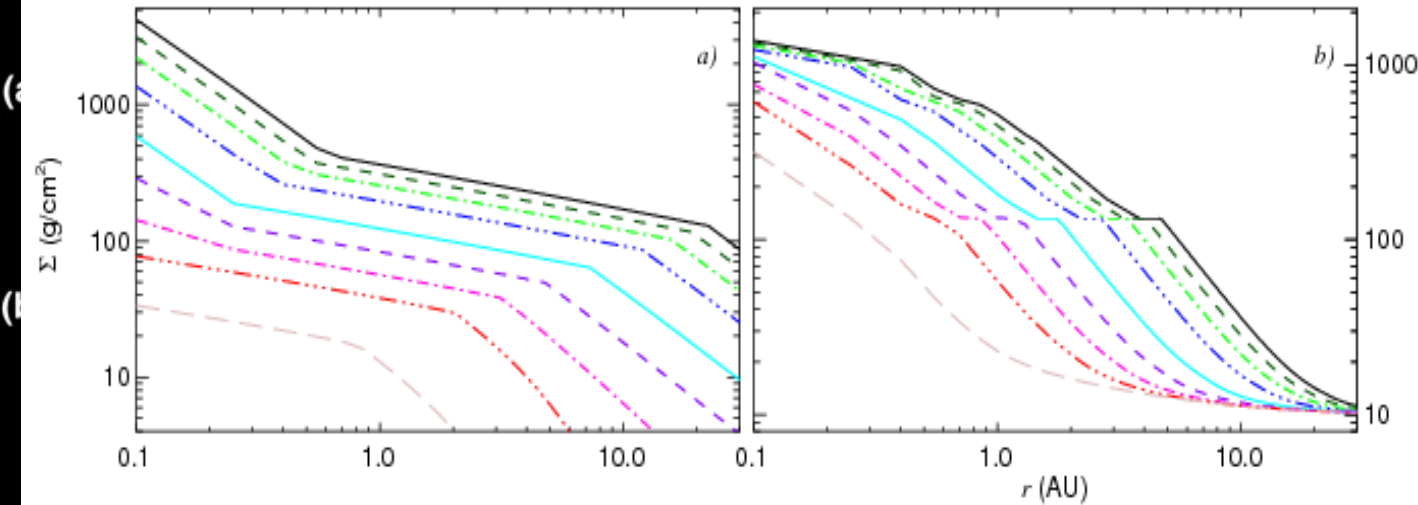
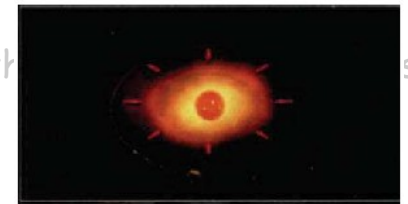
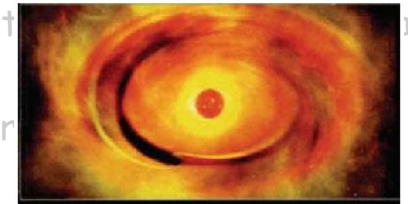
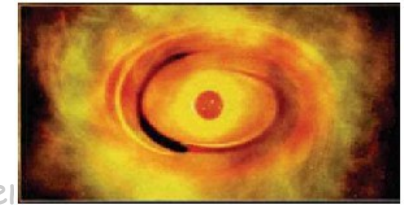




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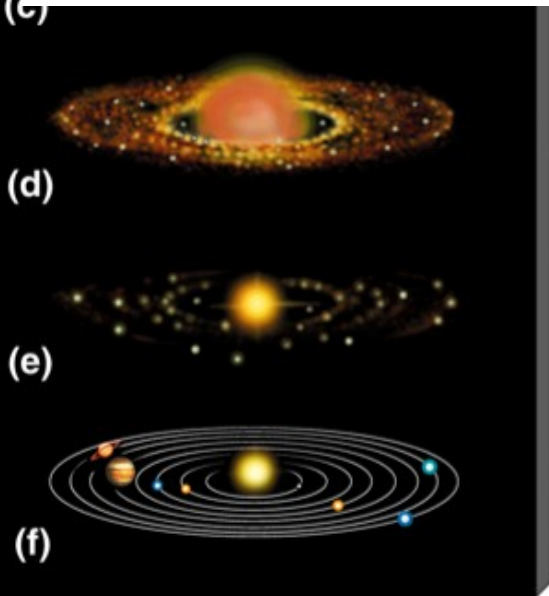
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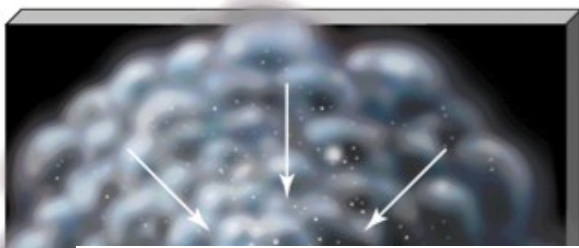
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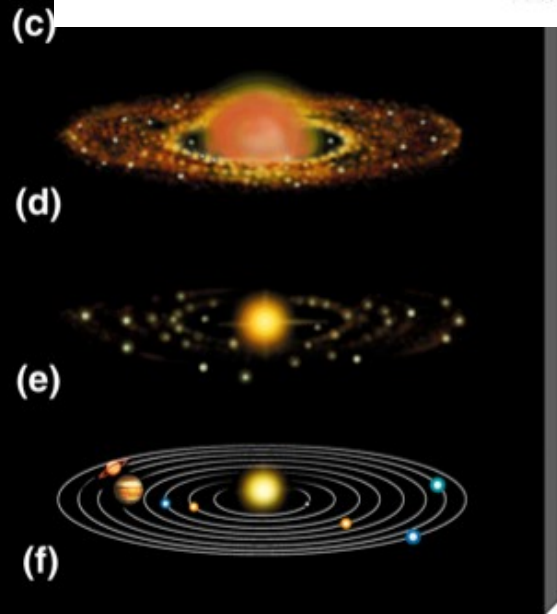
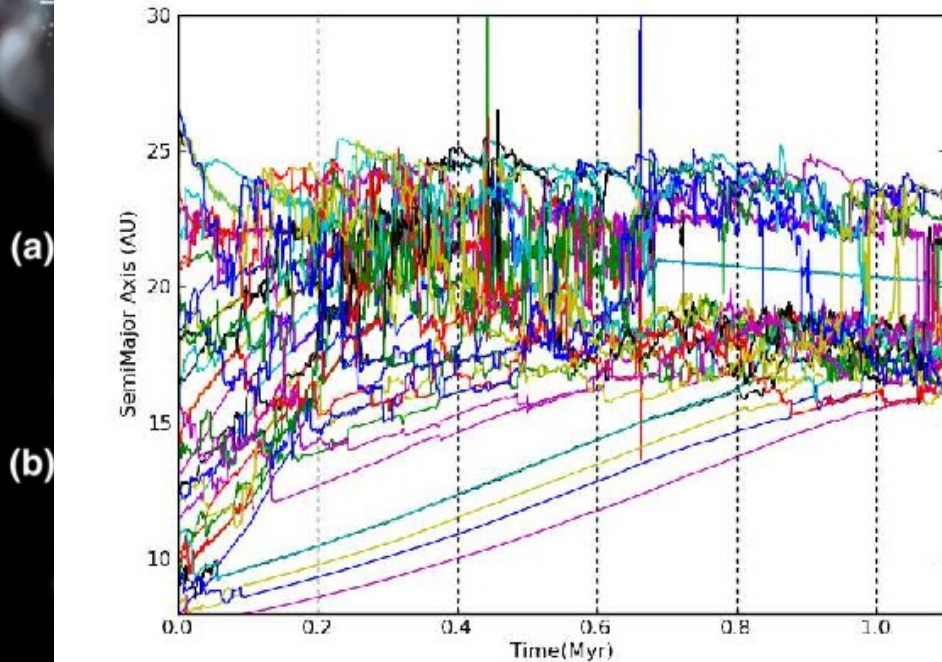






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Gravitational collapse of an interstellar cloud



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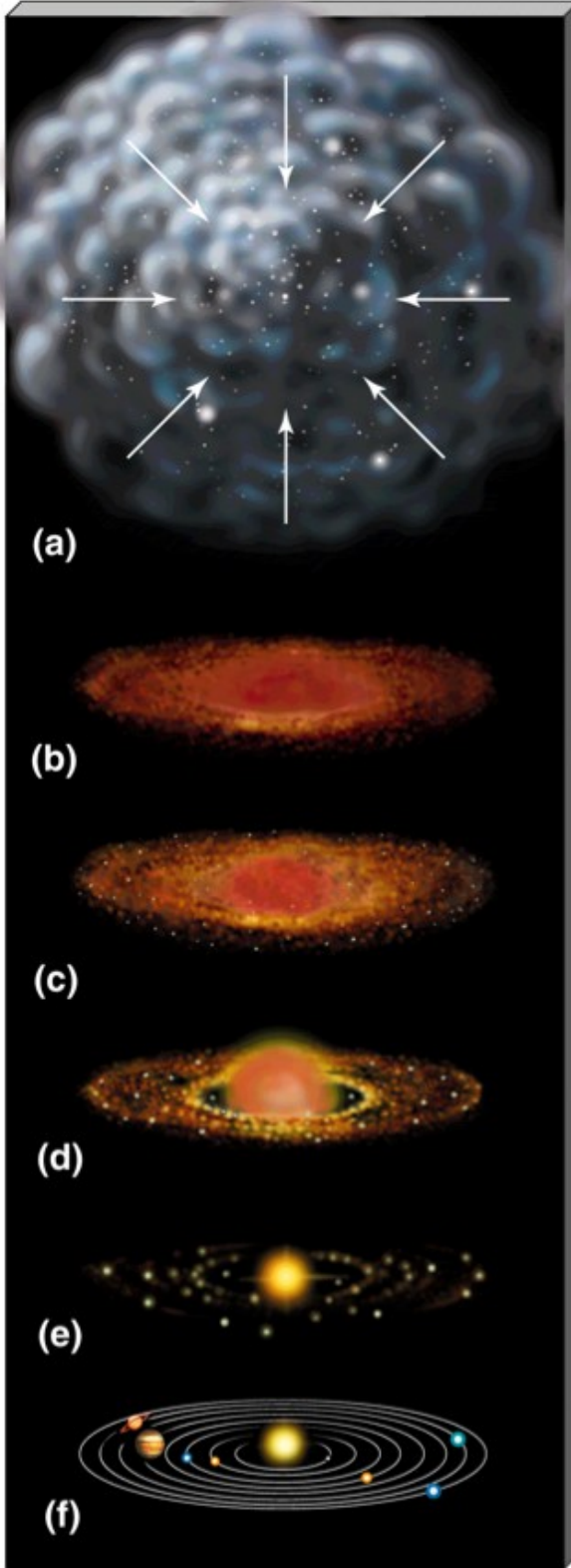
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Rocks in the turbulent  
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mass embryos are

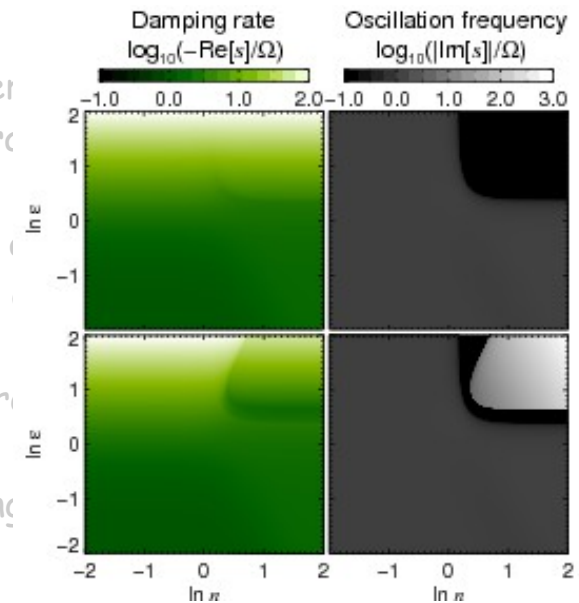
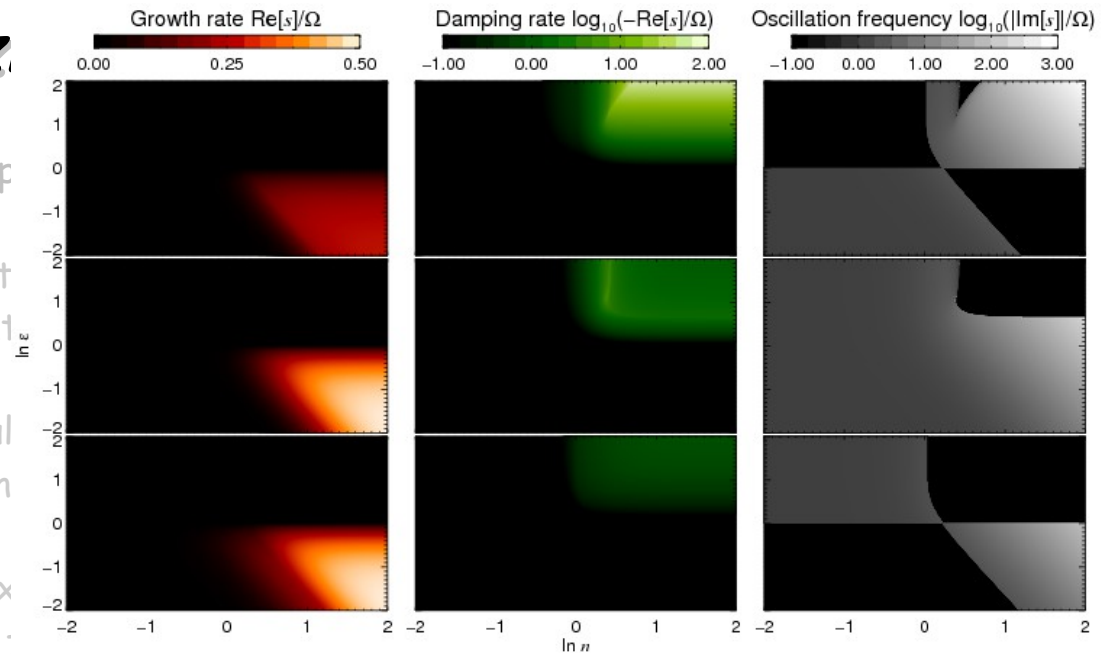
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**Dust heats gas**  
**Heated gas = high pressure region**  
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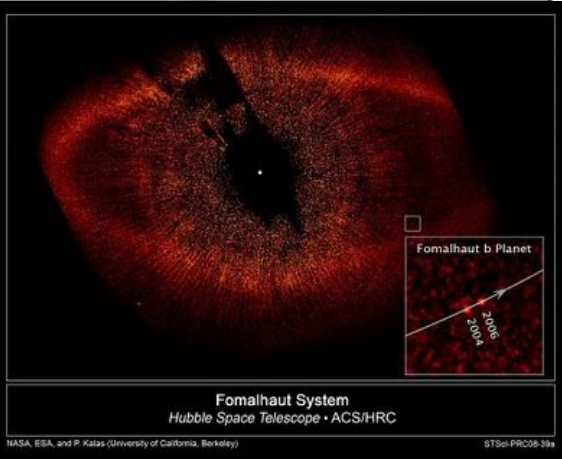
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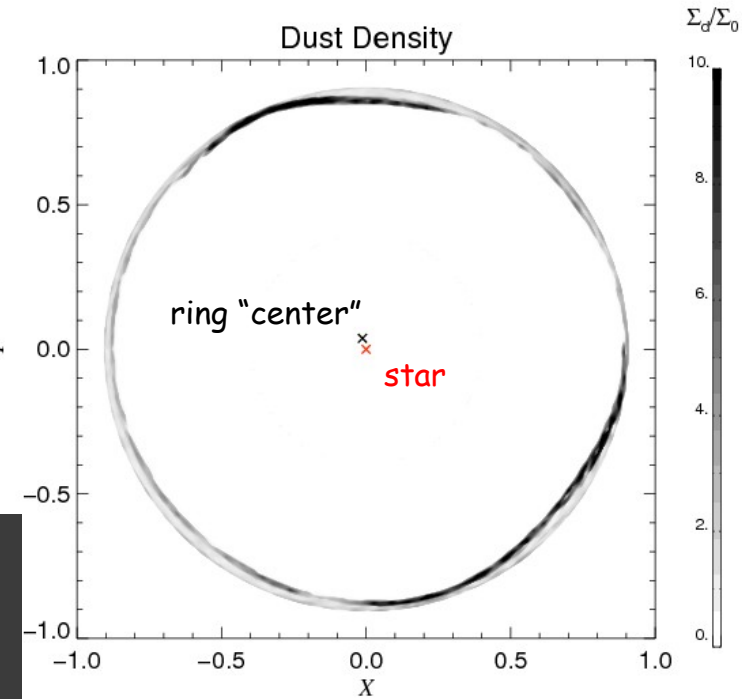


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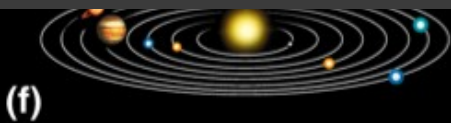
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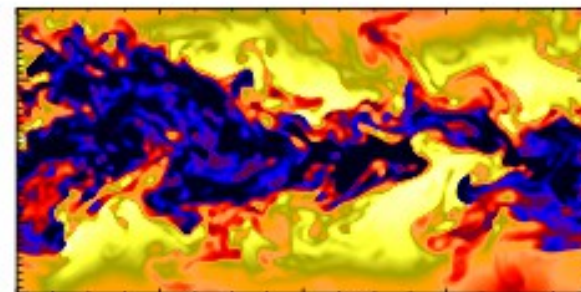
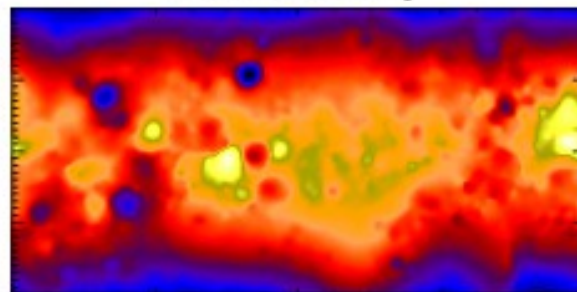
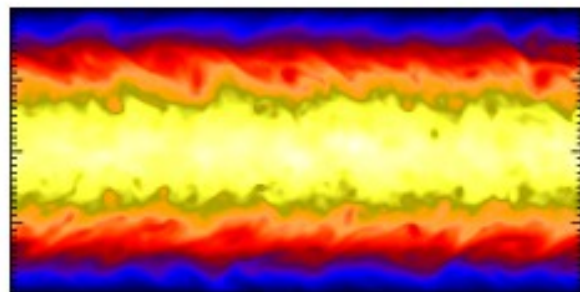


$t/T_0=10$

$t/T_0=100$

$t/T_0=250$

Gas Density



Dust Density

