

STARS - S06

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AMNH After-School Program

AMERICAN
MUSEUM OF
NATURAL
HISTORY



From last class

The ISM is not empty. In dense molecular clouds, stars begin to form.

Star formation is governed by gravitational collapse. Thermal pressure opposes it.

Clouds are turbulent. Only the densest clumps form stars.

Angular momentum leads to a circumstellar disk.

Planets



formation.

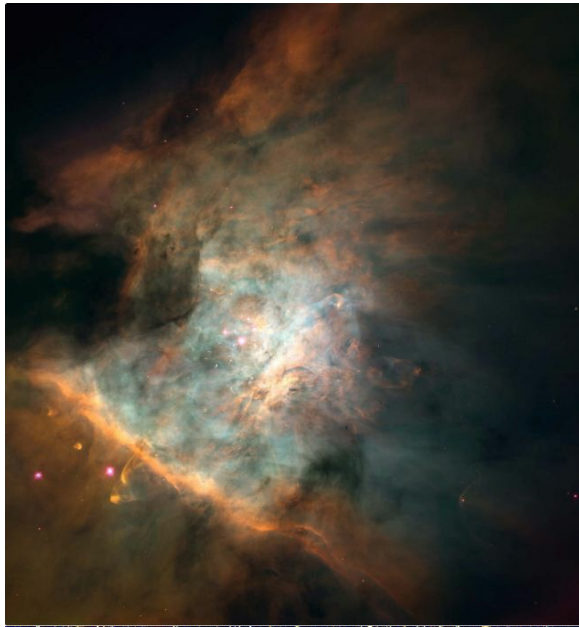
S

From last class

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Clouds are turbulent.



Molecular Cloud Fact Sheet

Temperature	10-50	K
Density	$10^2 - 10^6$	atoms/cm ³
(ISM Density	1	atom/cm ³)
(Air density	10^{19}	atoms/cm³)

Irregular and turbulent

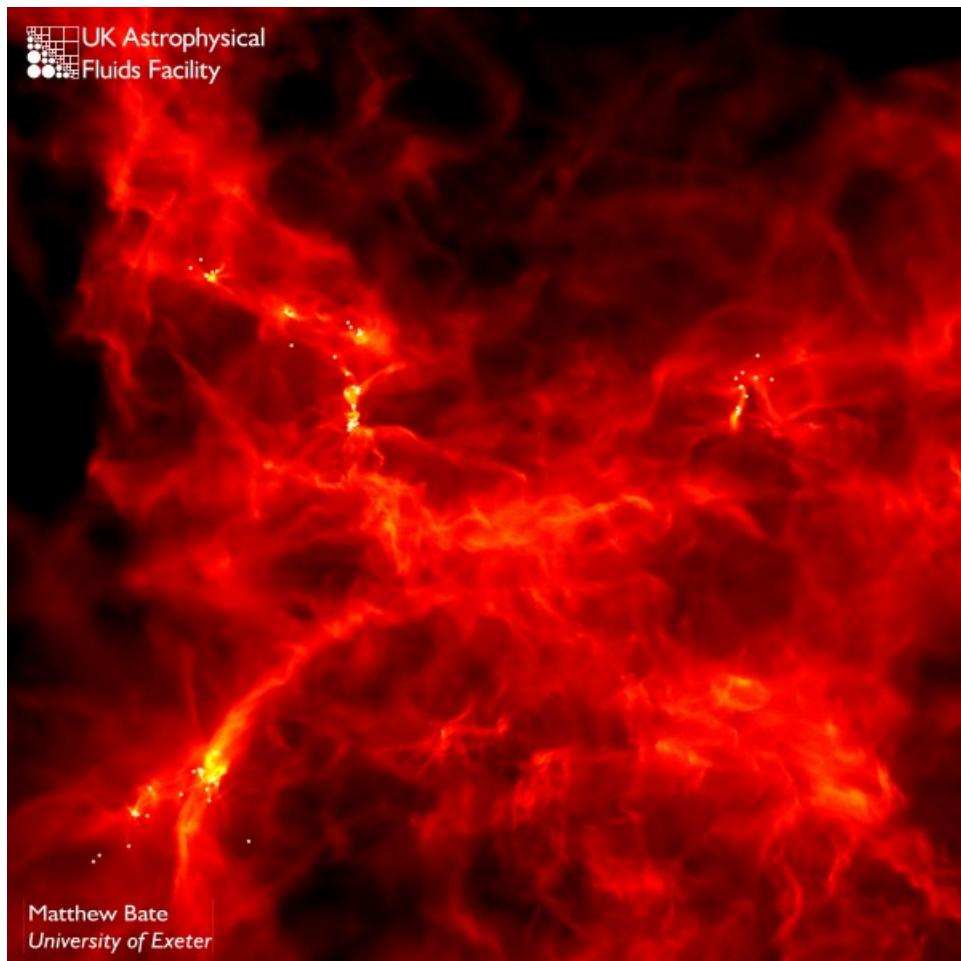
Sizes	10-100	parsecs
Mass	$10^2 - 10^6$	solar masses

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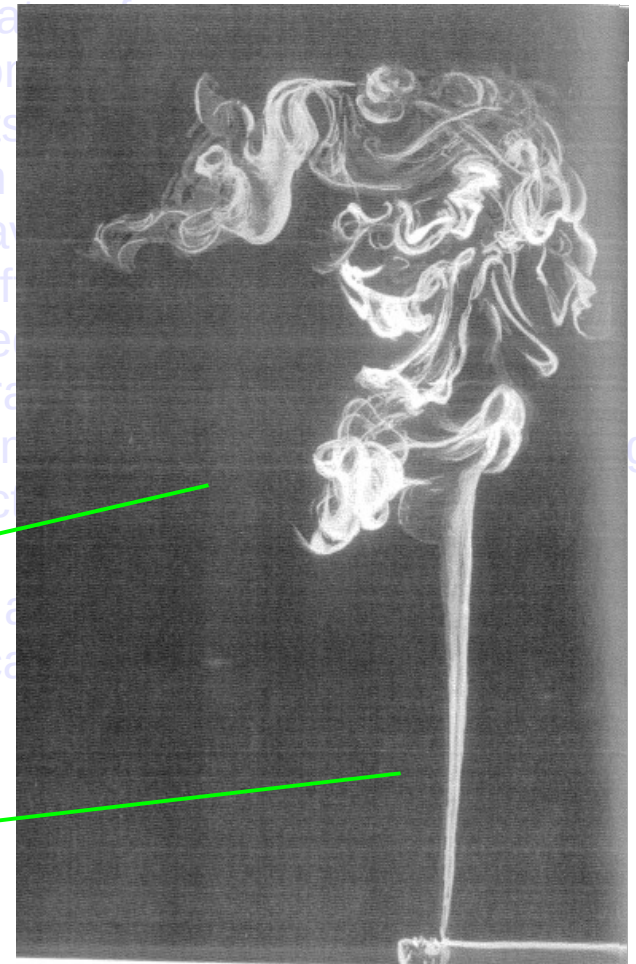
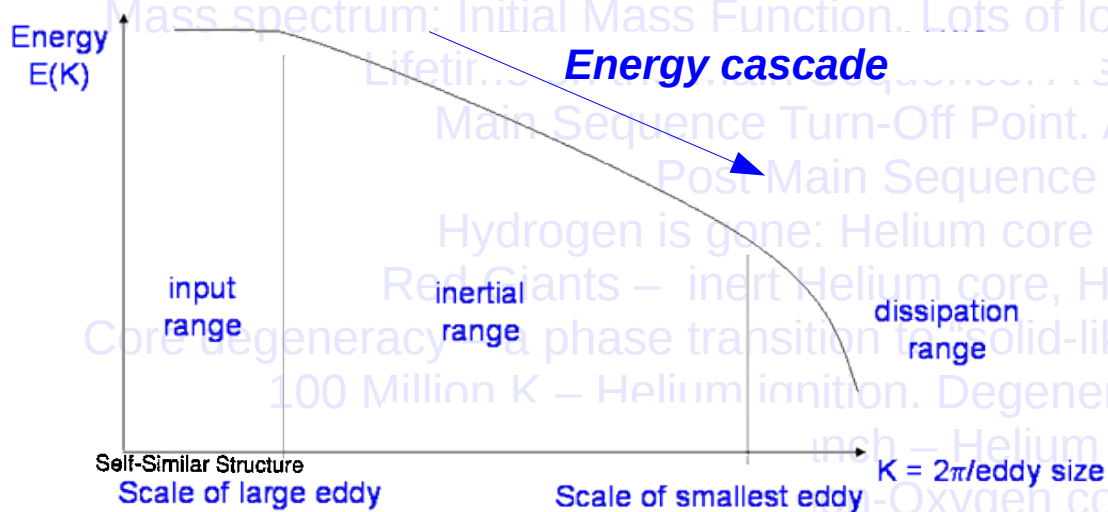
Computer simulation



Observation

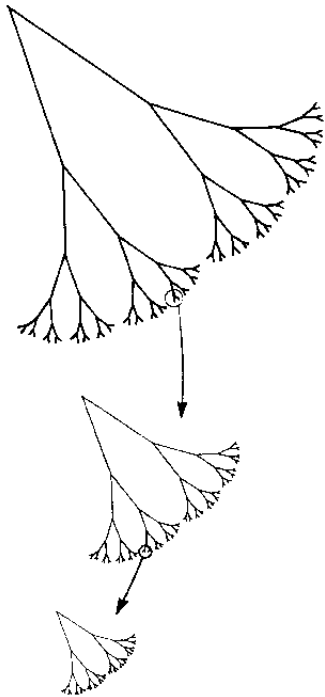
From last class

Turbulence is a self-similar flow. Size spectrum is well defined.



Turbulent flow

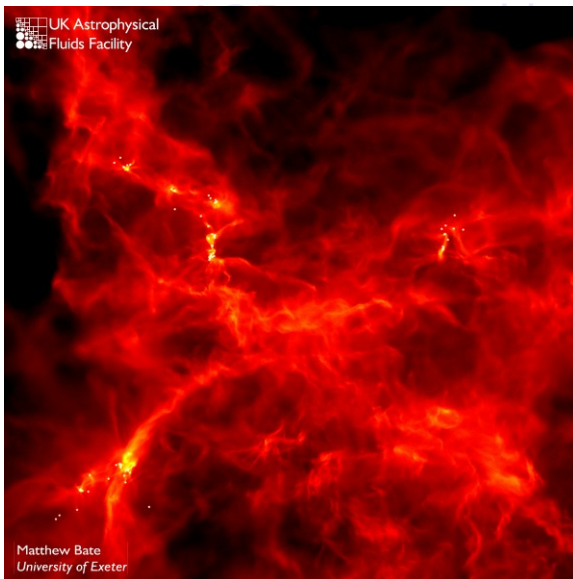
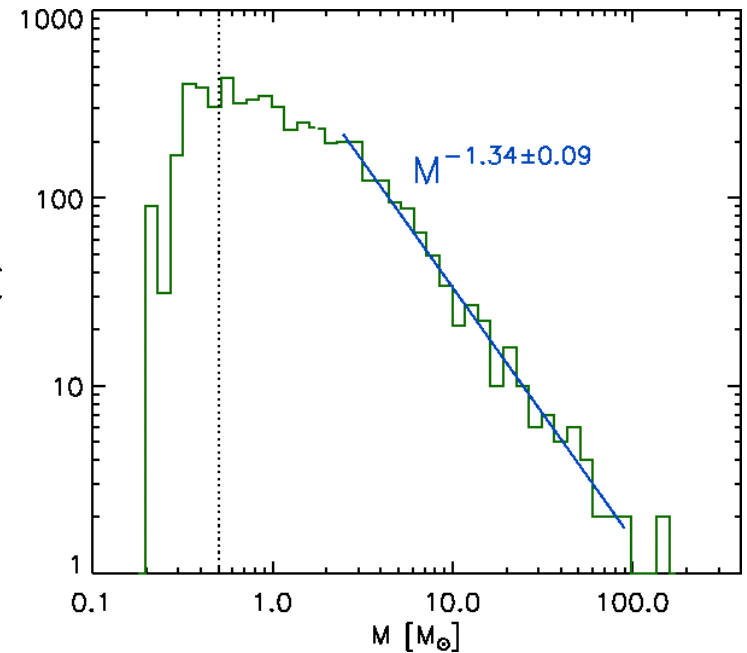
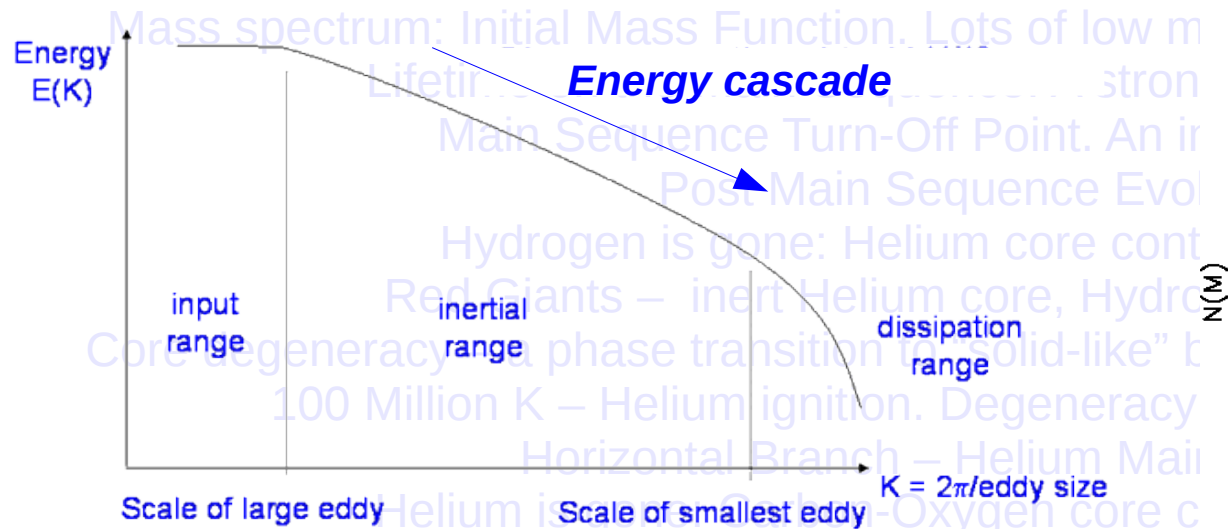
Laminar flow



From last class

Turbulence is a self-similar flow. Size spectrum is well defined.

Turbulent fragmentation of a molecular cloud leads to a well defined mass spectrum.



From last class

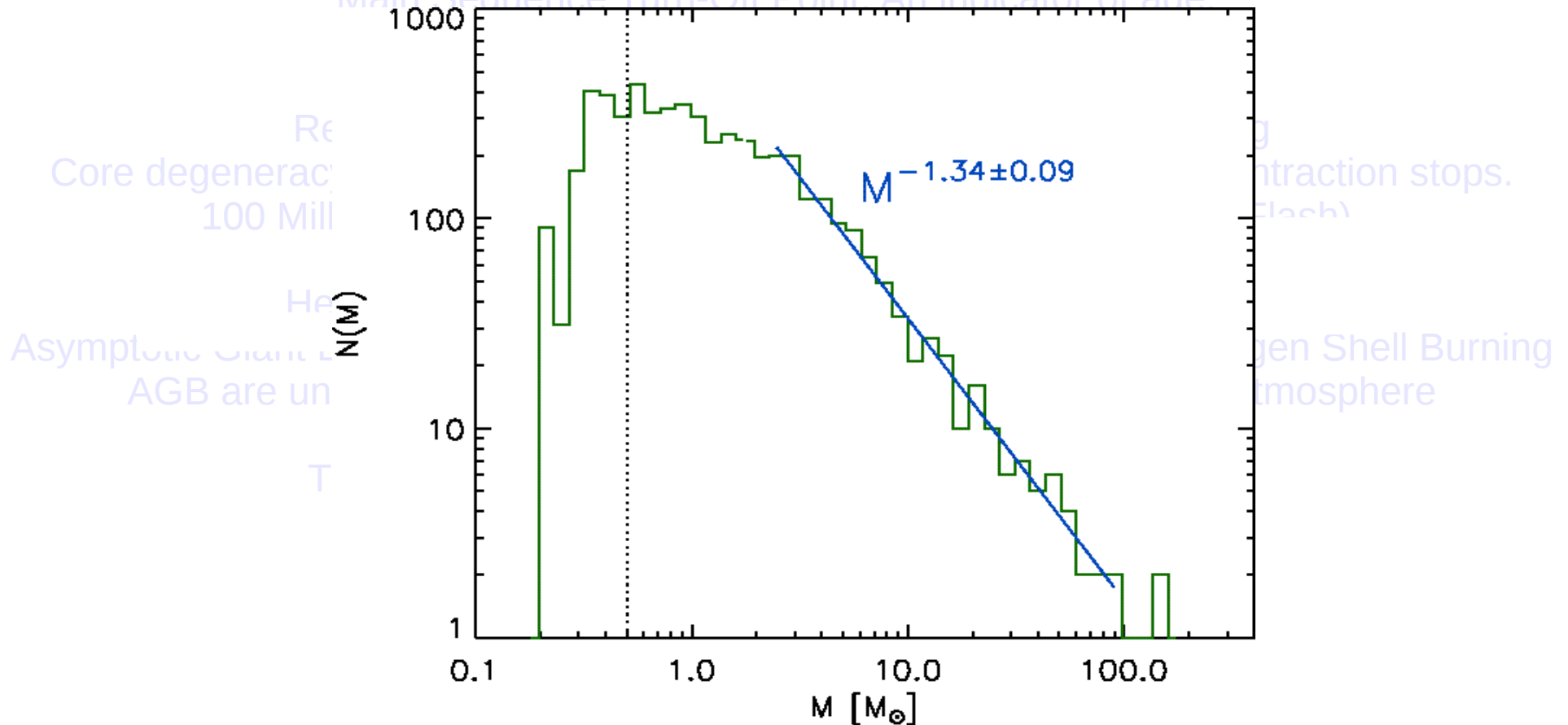
Turbulence is a self-similar flow. Size spectrum is well defined.

Turbulent fragmentation of a molecular cloud leads to a well defined mass spectrum.

Mass spectrum: **Initial Mass Function**. Lots of low mass stars, few high mass stars.

Lifetime on the Main Sequence: A strong function of mass.

Main Sequence Turn-Off Point. An indicator of age



Lots of **low mass stars**
Very few **high mass stars**

Most common mass: 0.5 Msun

From last class

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Angular momentum leads to a circumstellar disk.

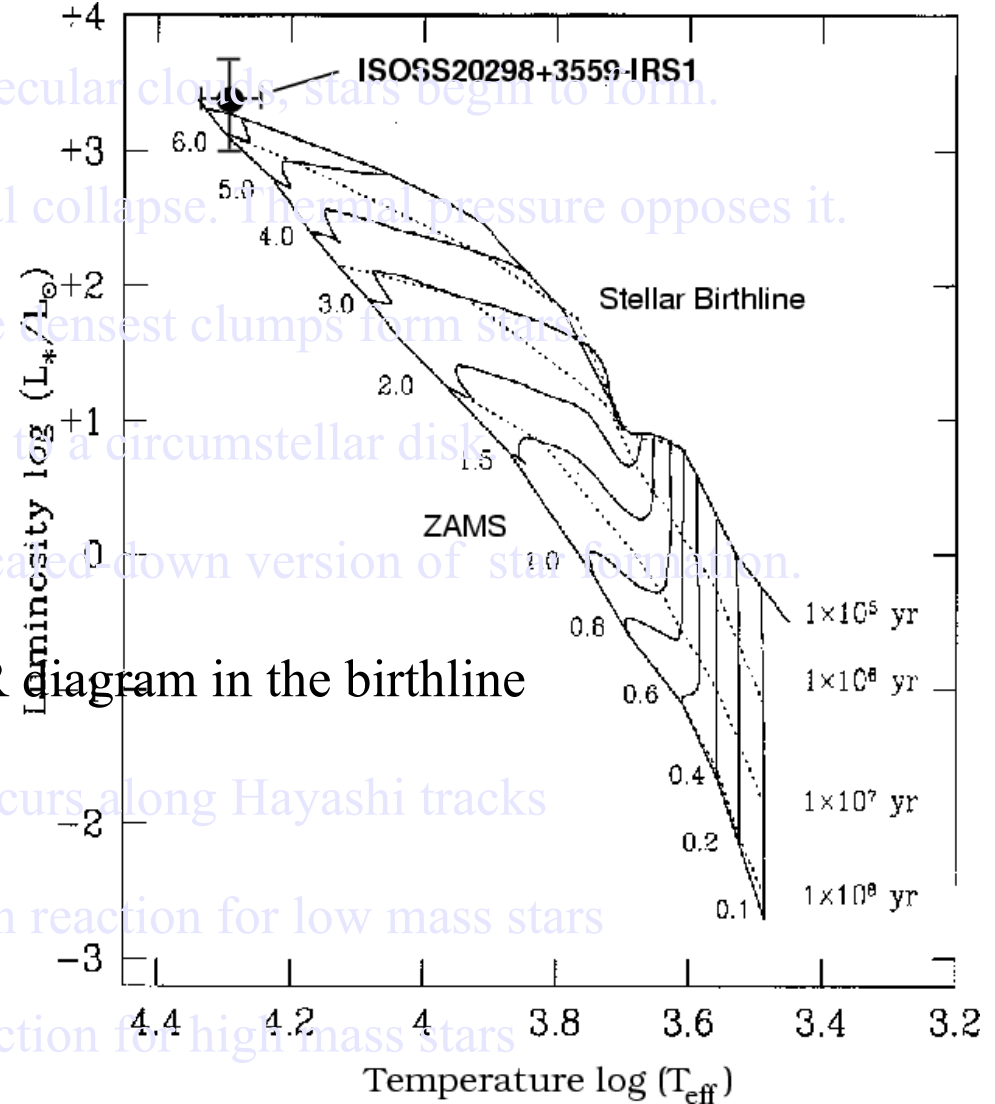
Planets form in the turbulent disk in a scaled-down version of star formation.

Protostars appear in the HR diagram in the birthline

Gravitational contraction occurs along Hayashi tracks

Proton-proton chain is the main reaction for low mass stars

CNO cycle is the main reaction for high mass stars



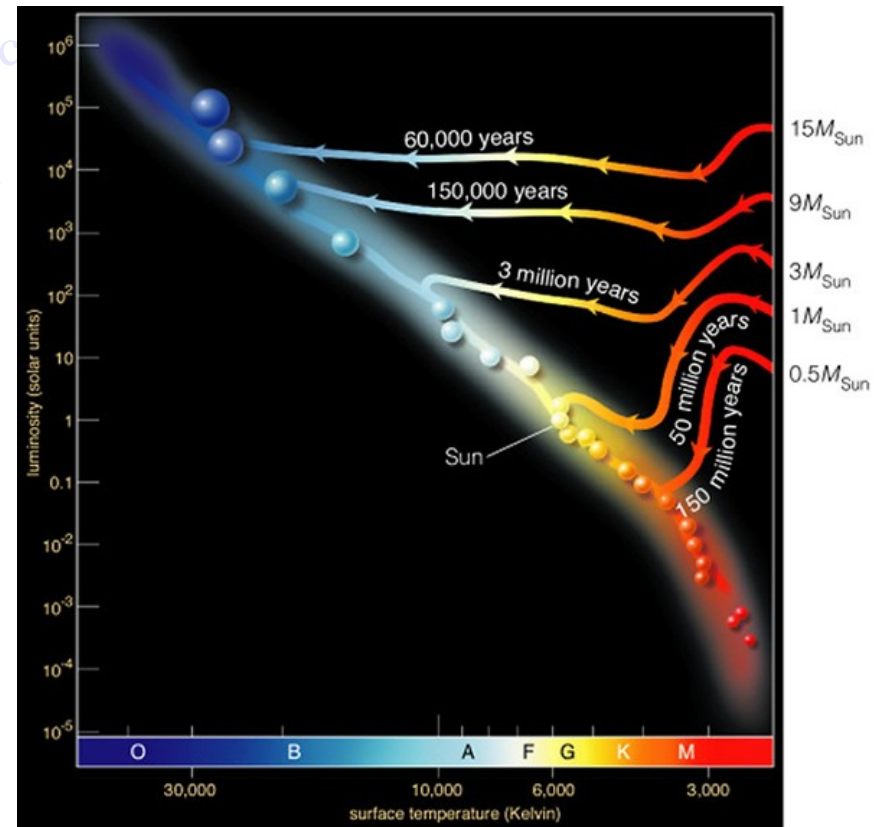
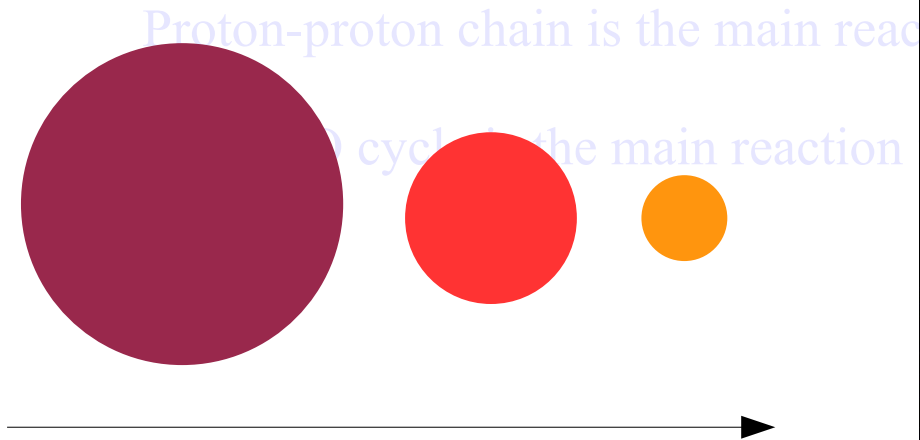
From last class

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Pre Main Sequence Evolution: gravitational contraction along Hayashi tracks



From last class

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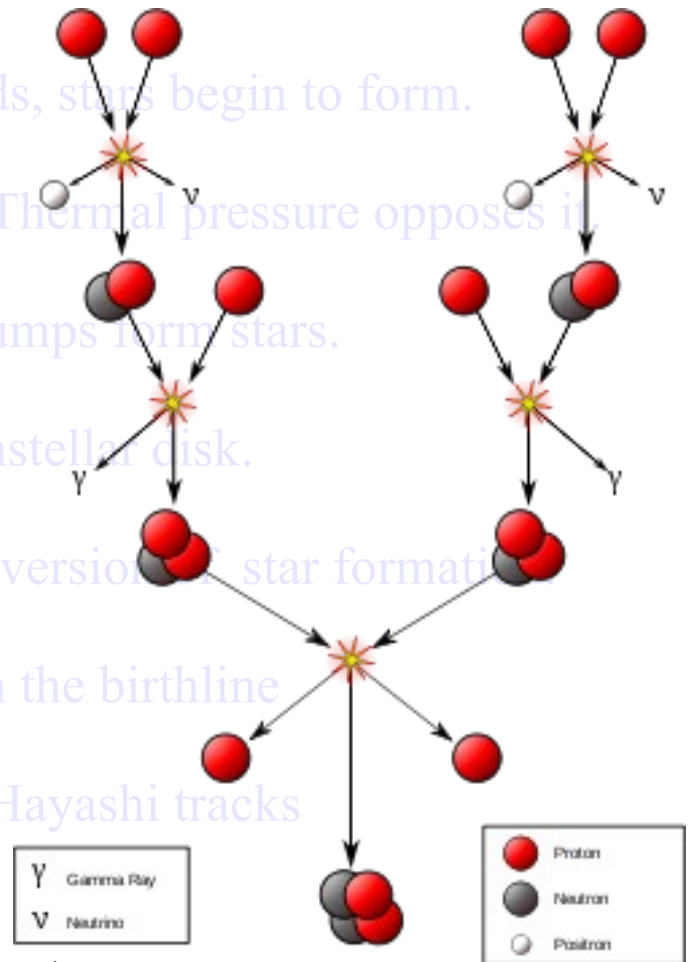
Planets form in the turbulent disk in a scaled-down version of star formation.

Protostars appear in the HR diagram in the birthline

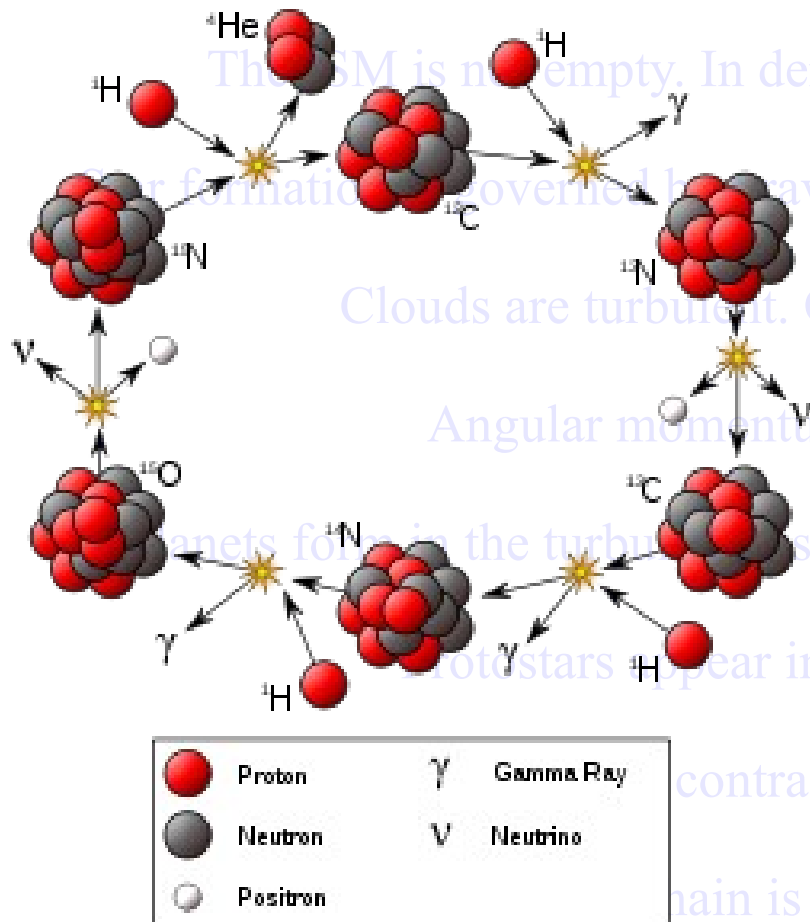
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From last class



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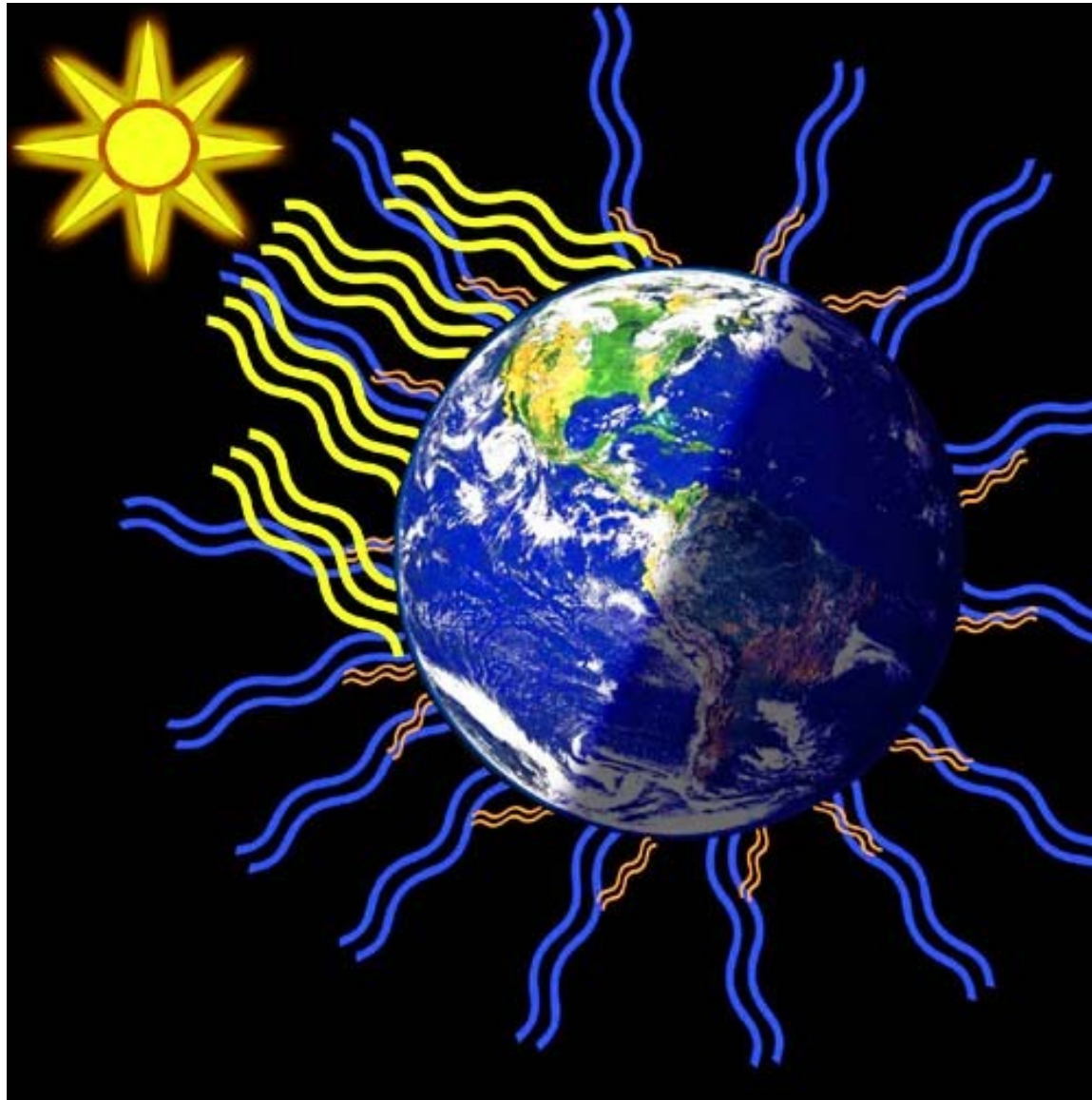
Outline

- Evolution of low mass stars
 - Lifetime on the Main Sequence
 - Turn-off point
 - Stellar Structure and Evolution
 - Energy source and Stellar Structure in
 - Red Giant Branch
 - Horizontal Branch
 - Asymptotic Giant Branch
 - Planetary Nebulae
 - White Dwarfs

Why is Earth's temperature constant?

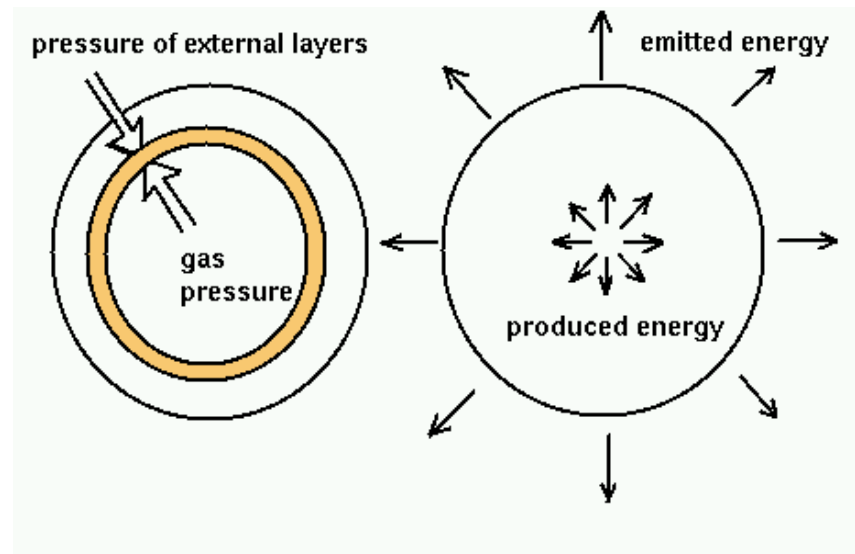


Why is Earth's temperature constant?



Radiative equilibrium

Radiative equilibrium



Hydrostatic equilibrium

In every layer, the
upwards push of gas pressure
matches the
inwards pull of gravity

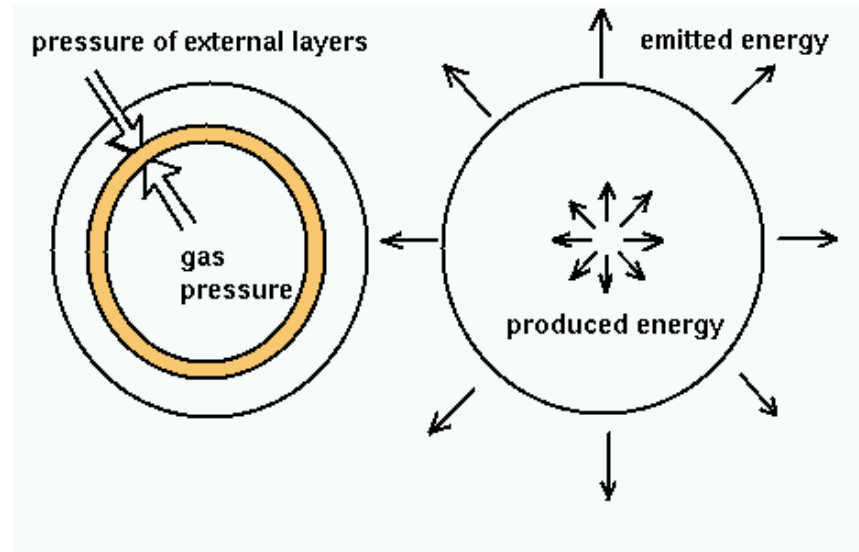
Radiative equilibrium

In every layer
outwards energy flow
matches the
energy injected from below.

(Otherwise, heating or cooling would occur)

Globally, the **Luminosity** (rate at which energy is radiated away) matches the rate of **energy production** at the core.

Radiative cooling

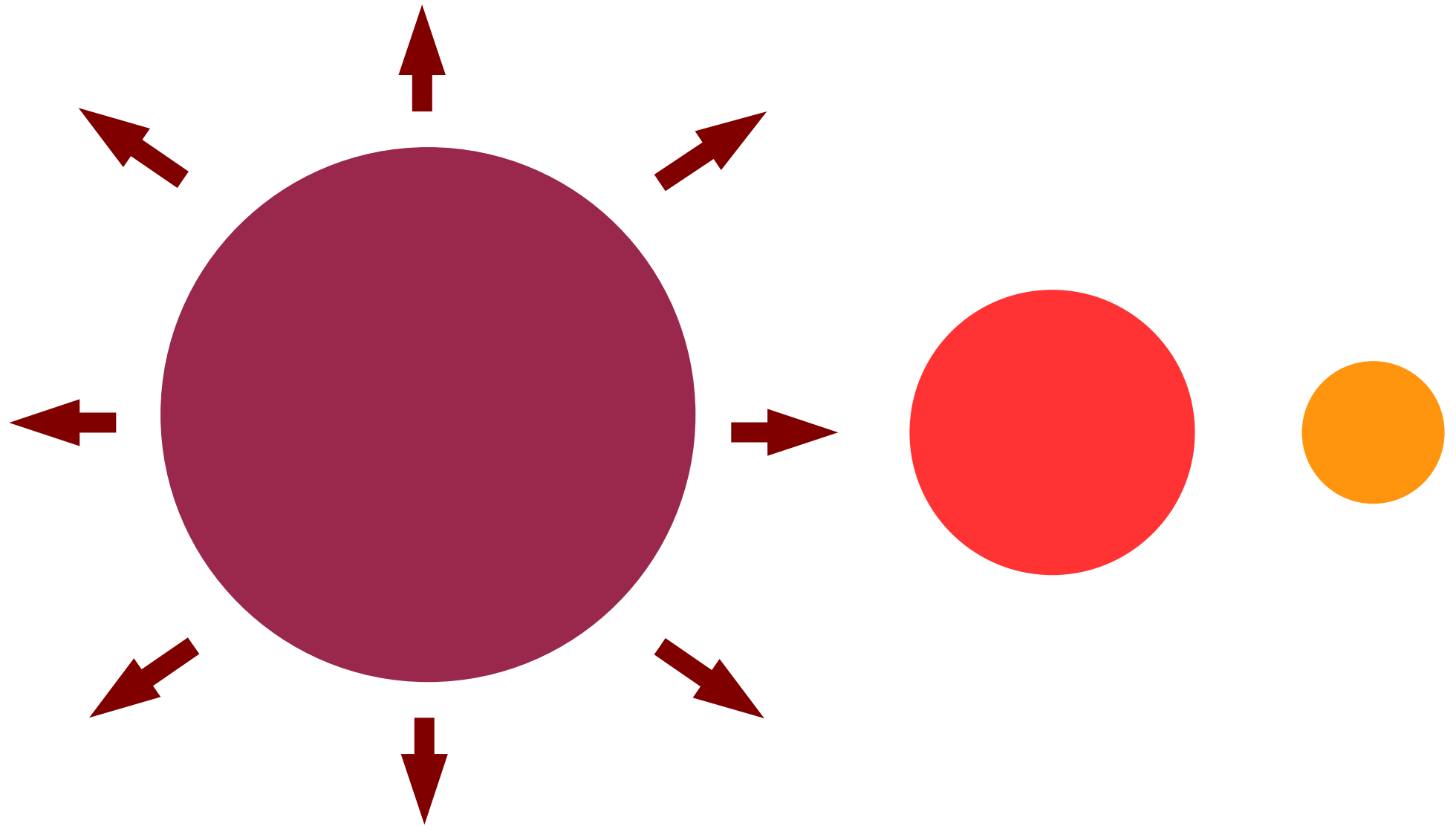


What we call “heat” is actually radiation

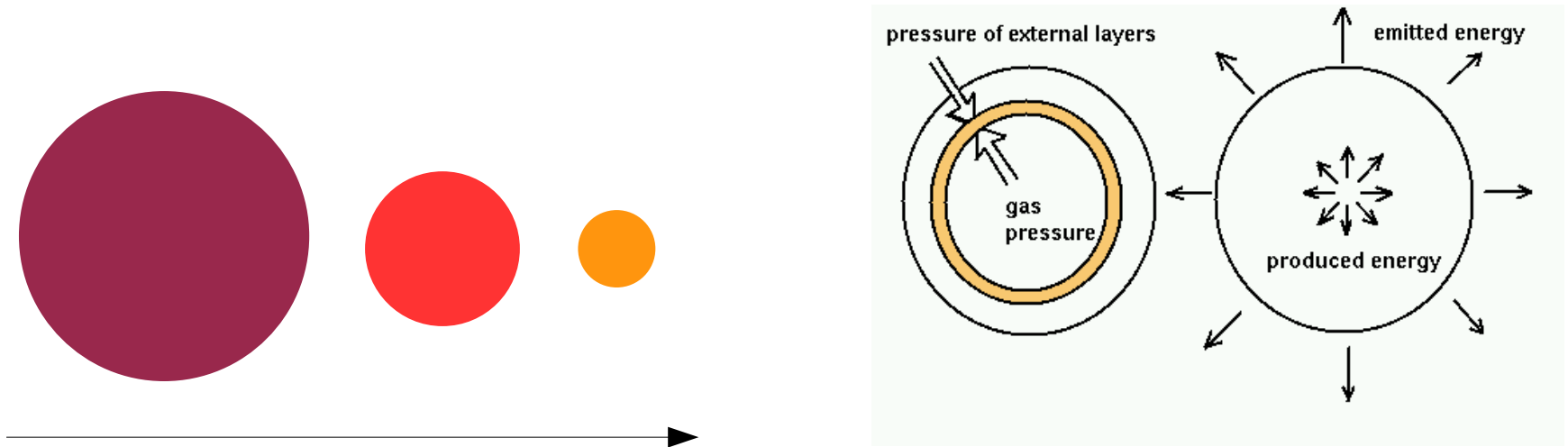
Radiative loss = Cooling

In a star in radiative equilibrium,
radiative losses (cooling)
are matched by
energy production (heating)
from nuclear reactions

So why does a proto-star heat when losing energy?



So why does a proto-star heat when losing energy?



Compression - Heating
Expansion - Cooling

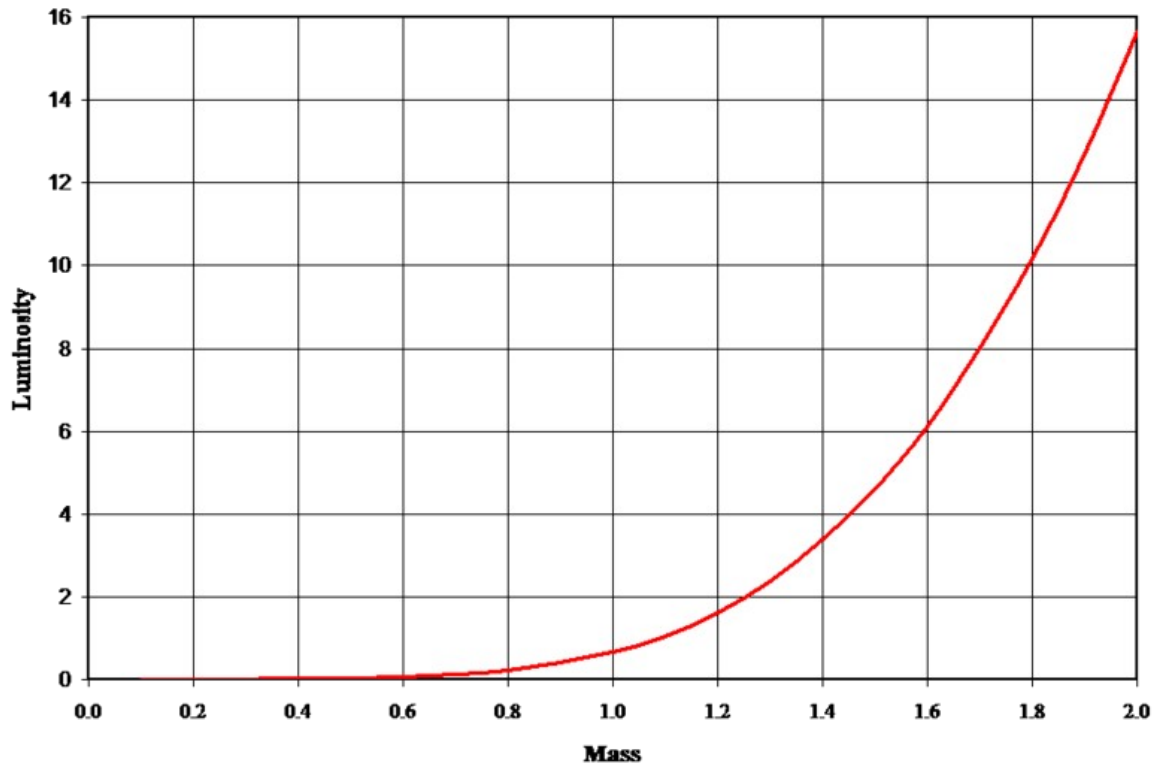
$$pV = nRT$$

1. Cooling leads to a lower pressure
2. Less support against gravity (compression)
3. **Compression** leads to **heating**

Lifetime in the Main Sequence

$$\text{Lifetime} = \frac{\text{Fuel}}{\text{Rate of Fuel Consumption}} = \frac{\text{Energy}}{\text{Luminosity}}$$

Mass – Luminosity relationship



- Luminosity

$$L \propto M^{3.5}$$

- Energy

$$E \propto M$$

- Lifetime

$$t \propto M^{-2.5}$$

Lifetime in the Main Sequence

$$t_{star} / t_{Sun} = \left(M_{star} / M_{Sun} \right)^{-2.5}$$

Lifetime in the Main Sequence

$$t_{star} / t_{Sun} = \left(M_{star} / M_{Sun} \right)^{-2.5}$$

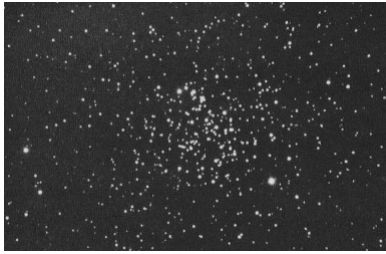
10 Msun – 1 million years

1 Msun - 10 billion years

0.1 Msun – 100 trillion years

High mass stars live fast and die young.

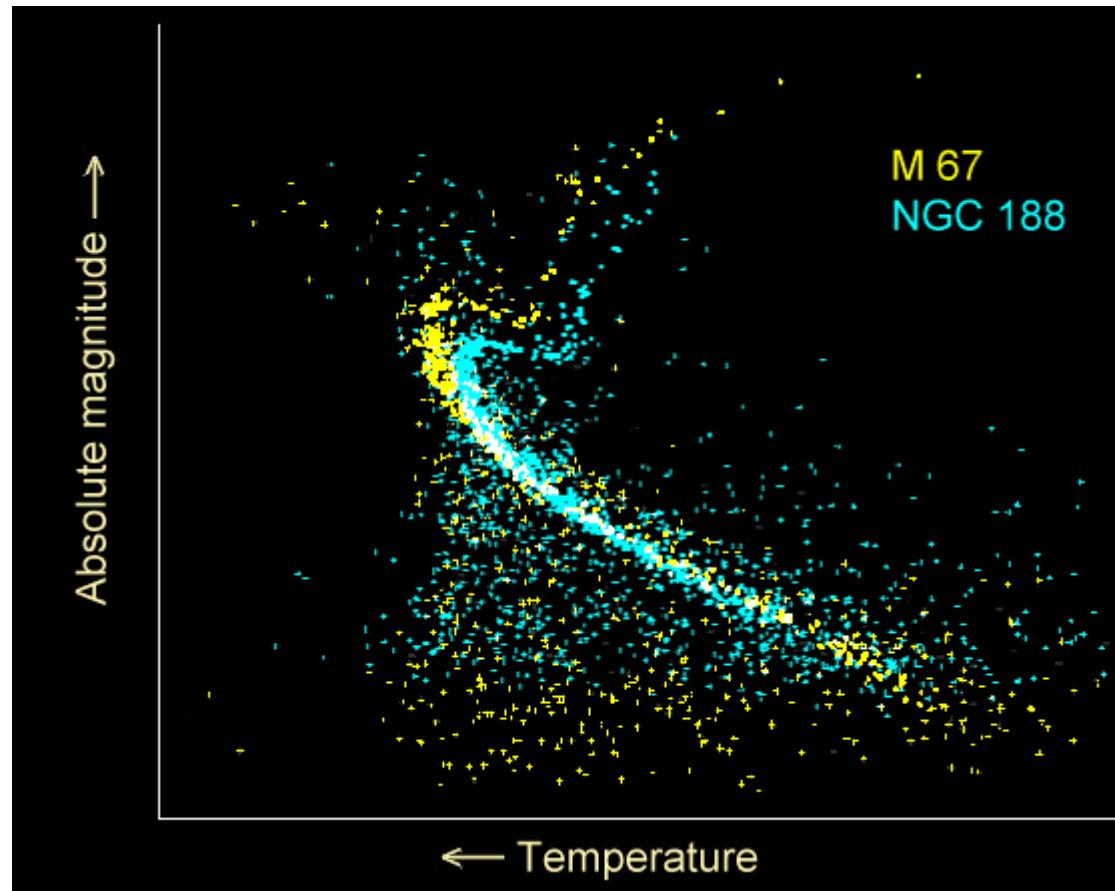
Low mass stars will still be around long after we're gone



M67

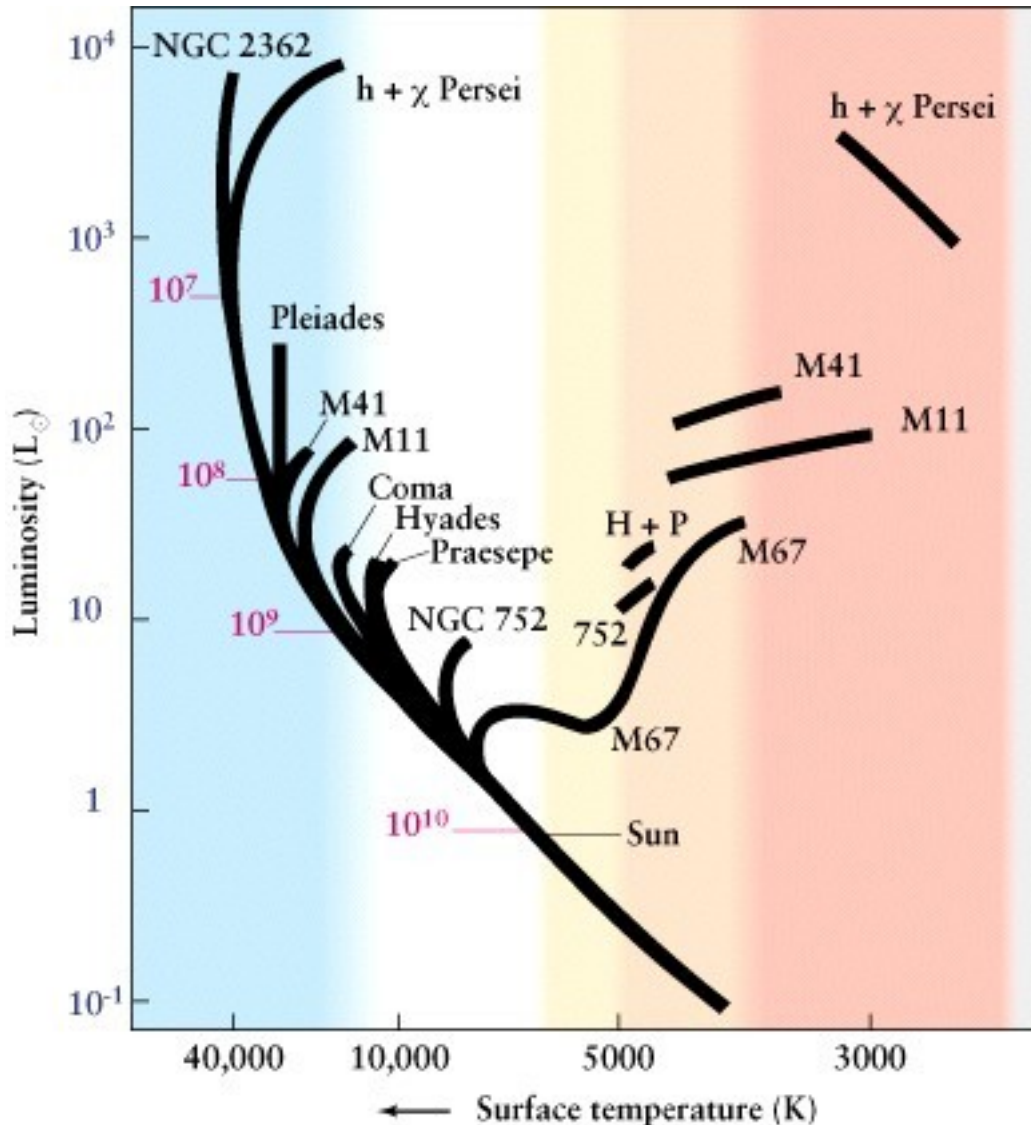


NGC188



Which one is the older?

The Main Sequence Turn-Off Point



As stars age, they leave the main sequence

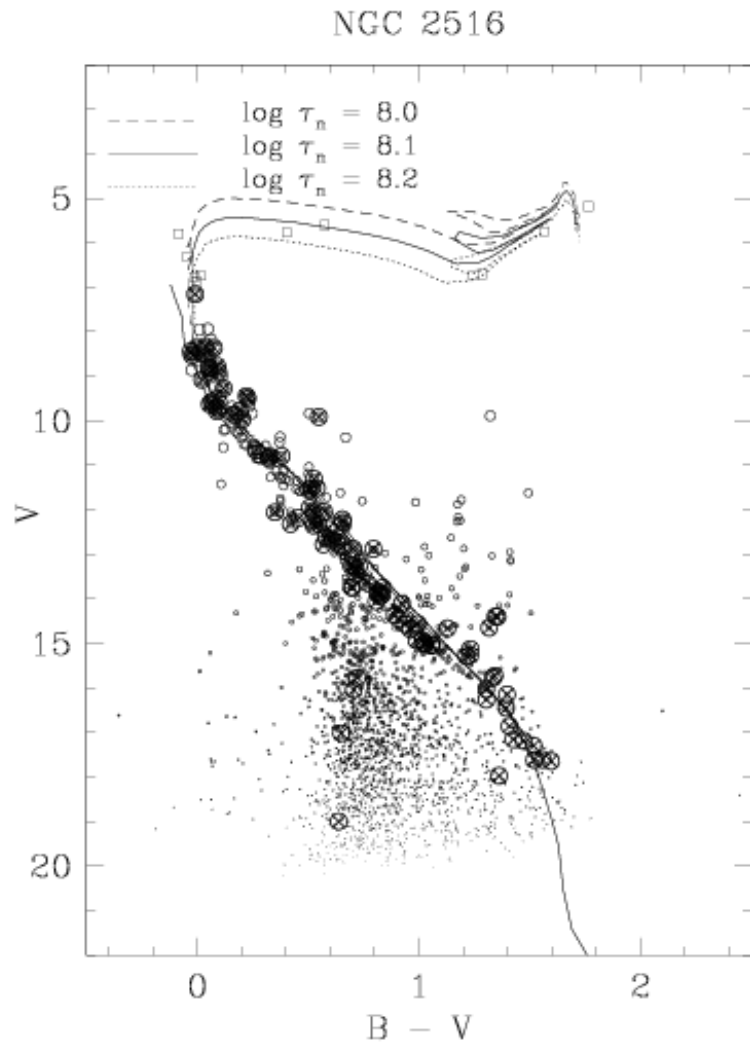
The point where stars are leaving the main sequence is called **turn-off point**

It is a function of age!

Application to clusters:

If you can tell the age of the star at the turn-off point, you can tell the age of the cluster.

The Main Sequence Turn-Off Point



Application to clusters:

If you can tell the age of the star at the turn-off point, you can tell the age of the cluster.

Isochrone Fitting

NGC 2516 – Age ~150 Myr



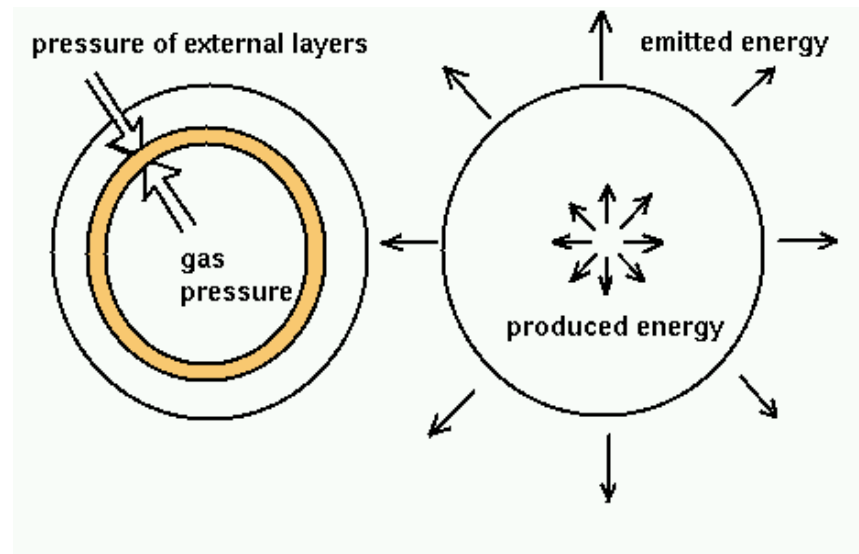


Hydrogen is gone! Now what?

*What will happen to
me?*



Radiative equilibrium



Hydrostatic equilibrium

In every layer, the
upwards gas pressure
matches the
inwards pull of gravity

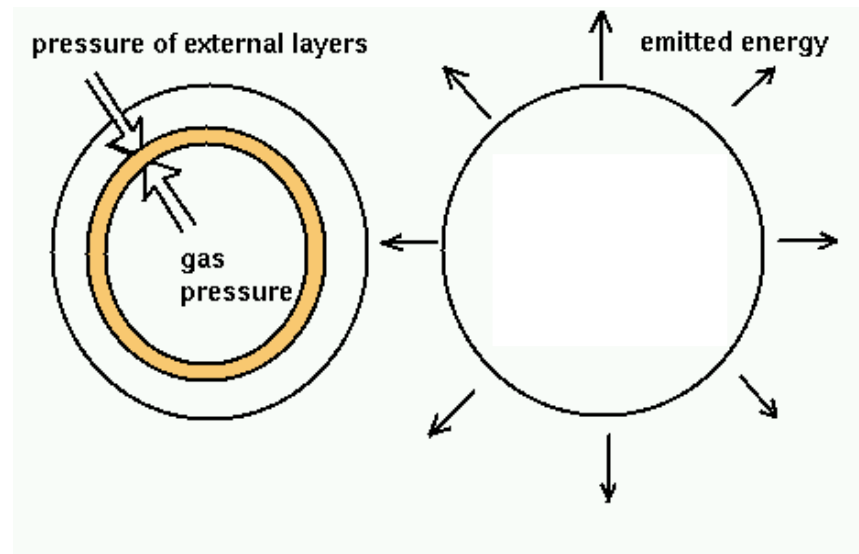
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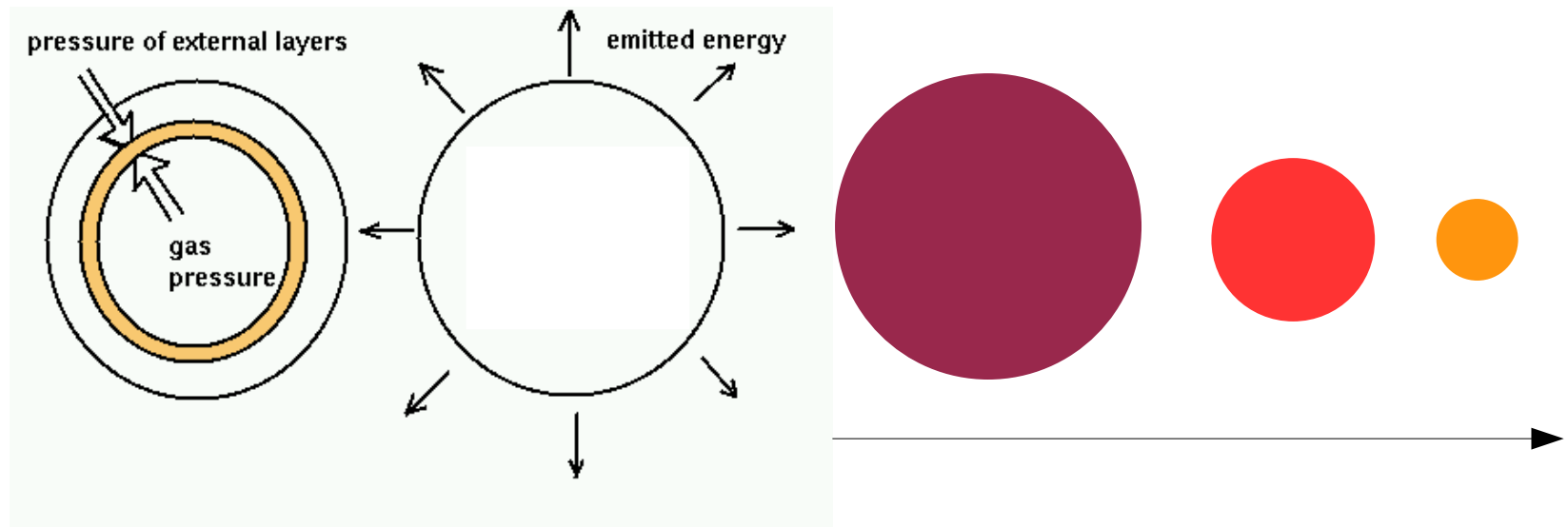
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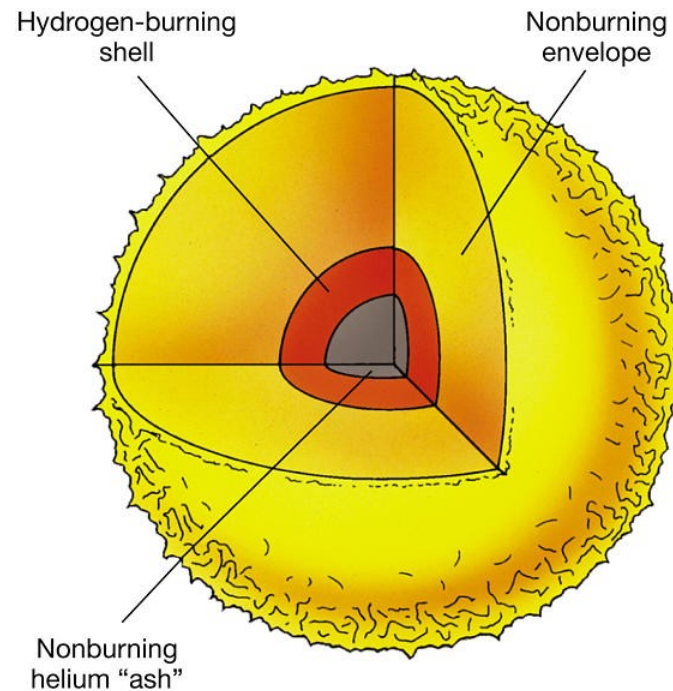
Hydrogen is gone! Now what?

Star stops producing energy.

The star **contracts** and **heats** up.

Eventually, the temperature becomes high enough to **burn hydrogen around the Helium core**

Hydrogen shell burning



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Hydrogen Shell Burning

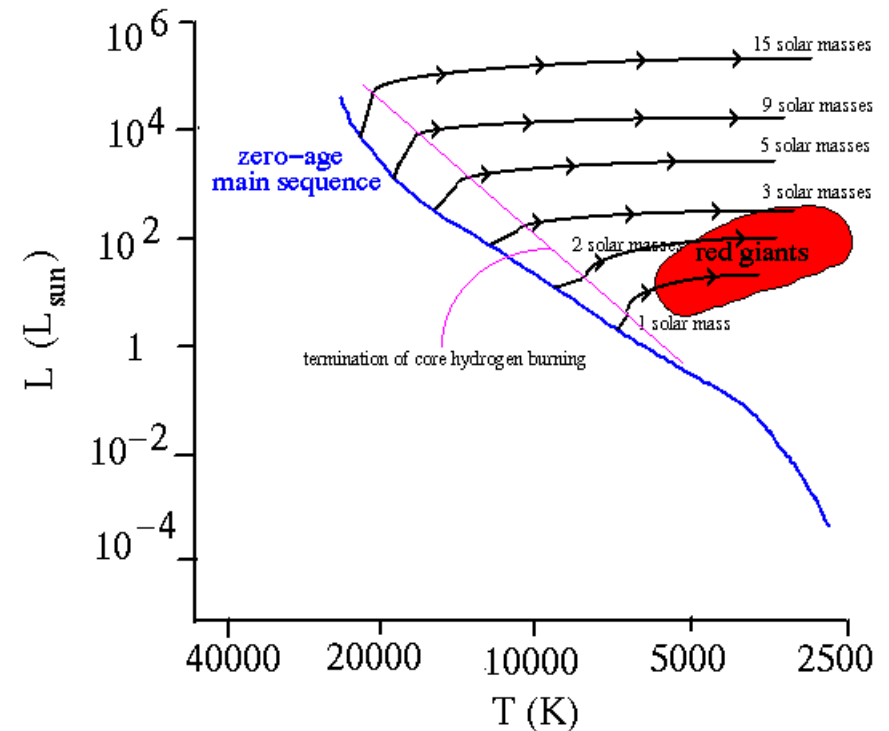
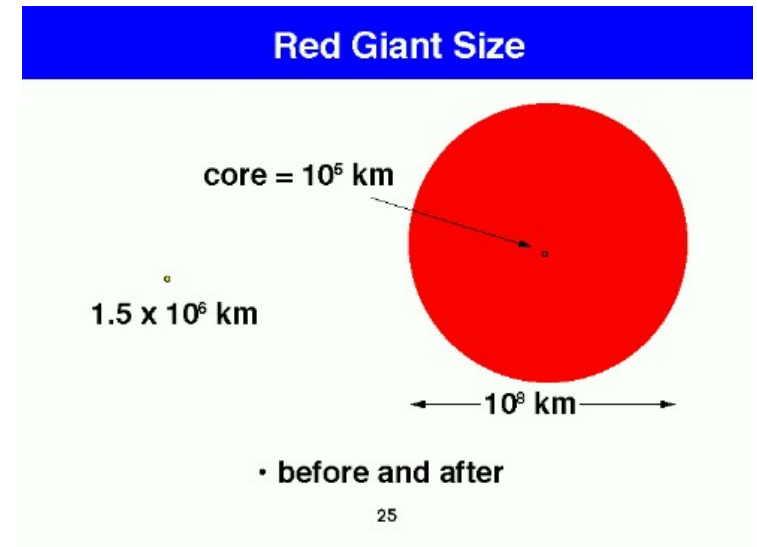
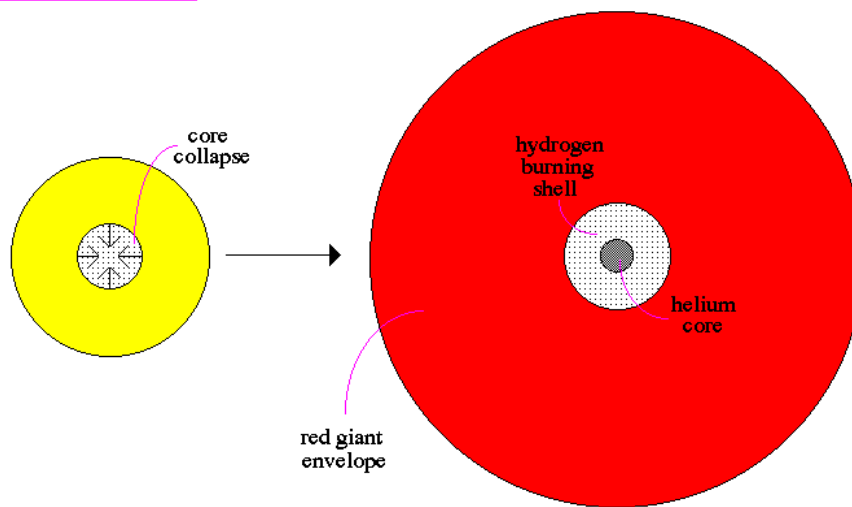
Hydrogen shell burning involves:

*More fuel than in MS-hydrogen burning
Higher temperatures (thus more efficient)*

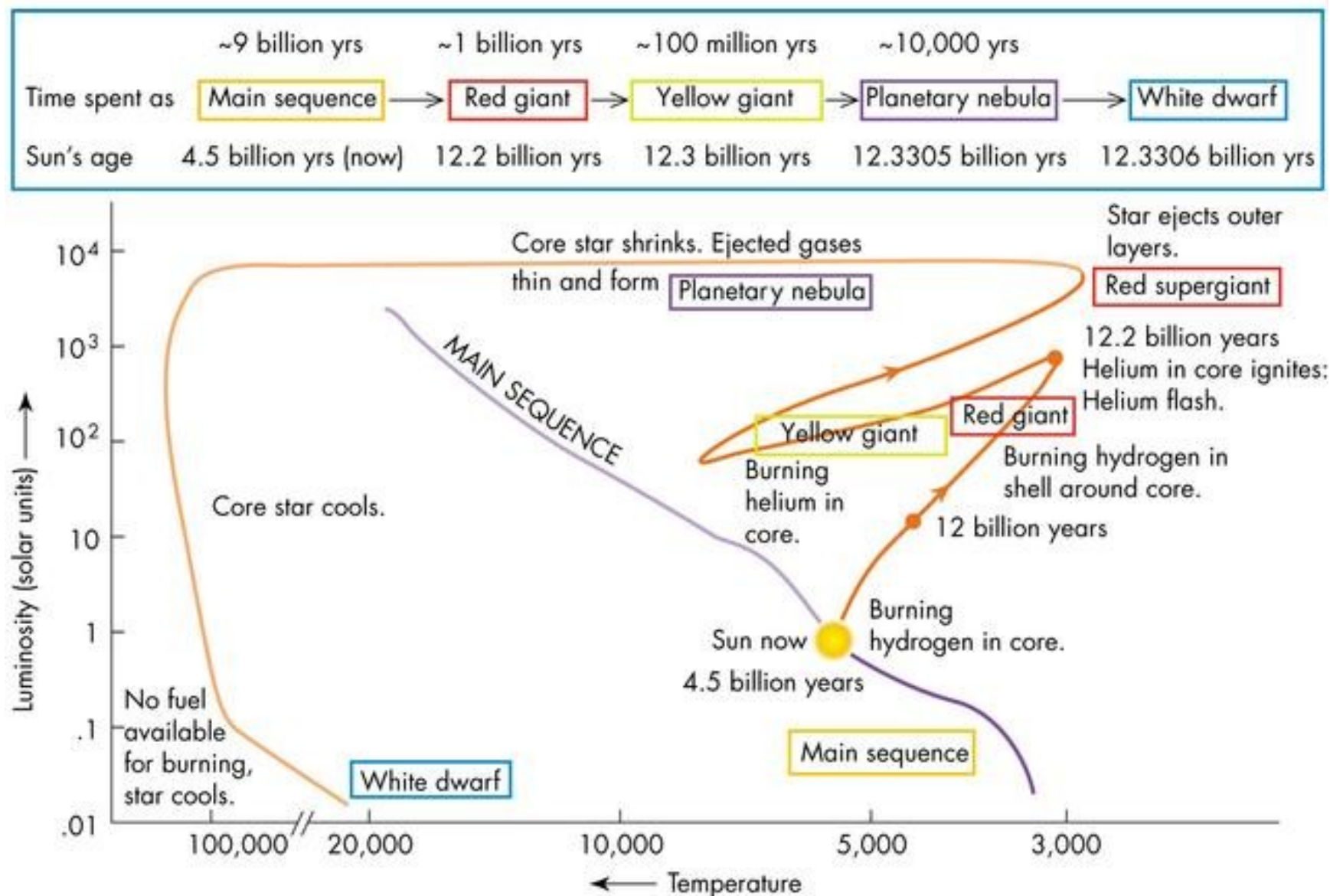
A lot more of energy is being produced.
The star gets very luminous and **swells**.

The expansion **cools** the outer layers.
The star becomes a red giant.

Hydrogen Shell Burning

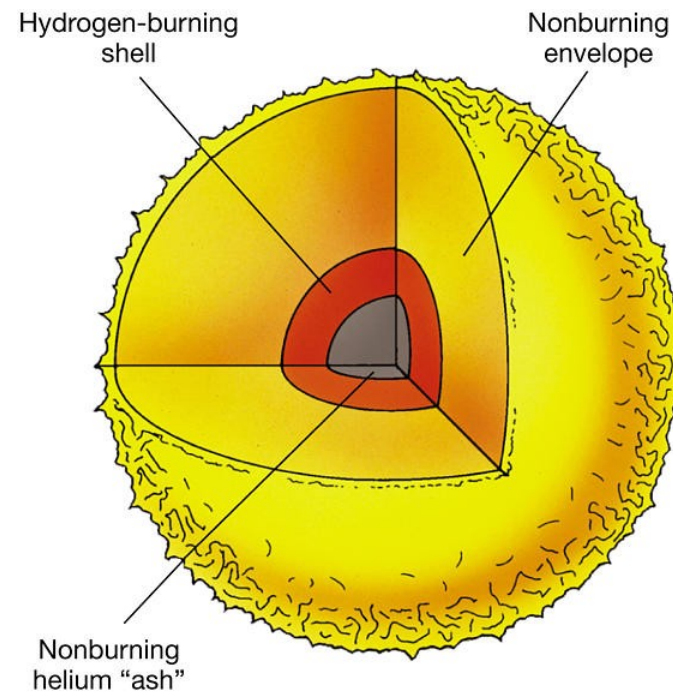


Evolutionary track



What happens to the inert Helium core?

Hydrogen shell burning



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What happens to the inert Helium core?

Core Degeneracy

It keeps contracting and heating

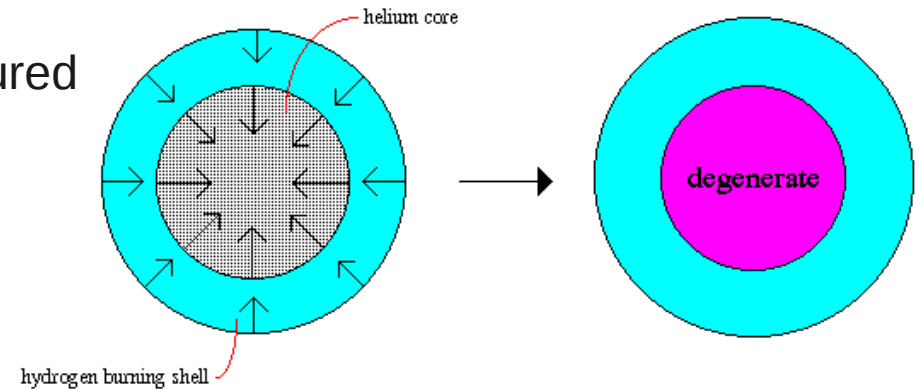
At some point the density is so high it goes **degenerate**

Degeneracy is just a “fancy” word

What it means is that a **phase transition** has occurred

It stops behaving like a gas

and starts behaving more **like a solid**



Ideal Gas

$$p \propto \rho T$$

Temperature rises, pressure rises

Temperature falls, pressure falls

Radiative loss → cooling →
less support against gravity → **contraction**

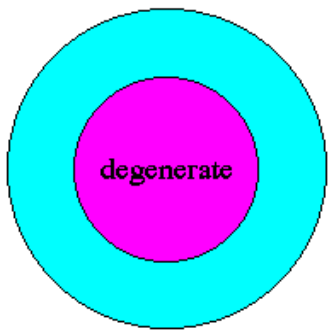
Degenerate Matter

$$p \propto \rho^{4/3}$$

If temperature rises or falls, pressure
couldn't care less

Radiative losses can continue indefinitely

The degenerate core is stable



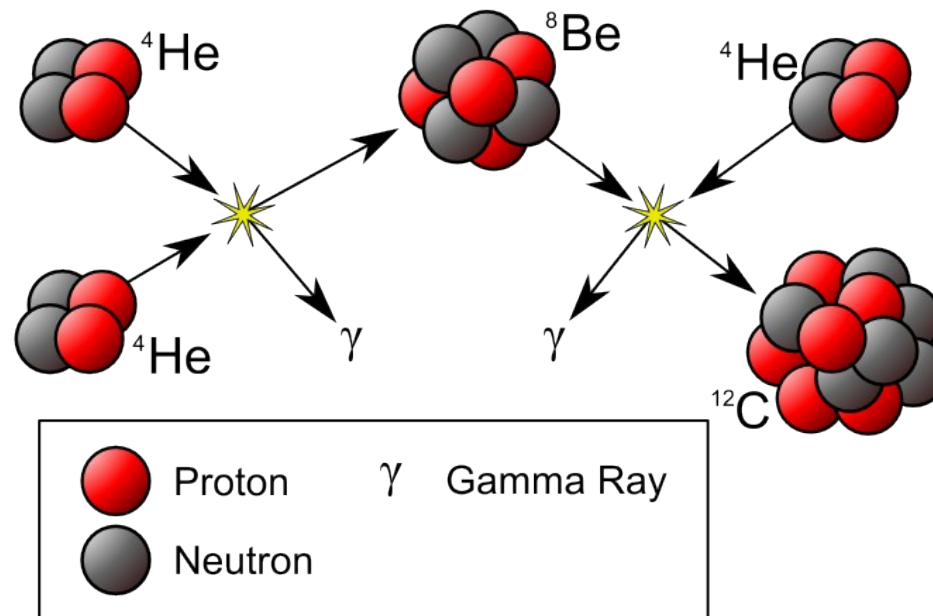
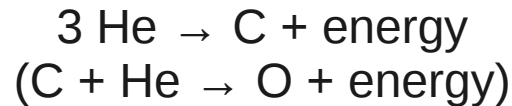
Helium Fusion

The inner degenerate Helium core is stable
But the outer Helium core keeps contracting and heating

When the temperature reaches 100 million K, **HELIUM FUSION** begins
Helium is burned into Carbon (and Oxygen)

Triple Alpha Reaction

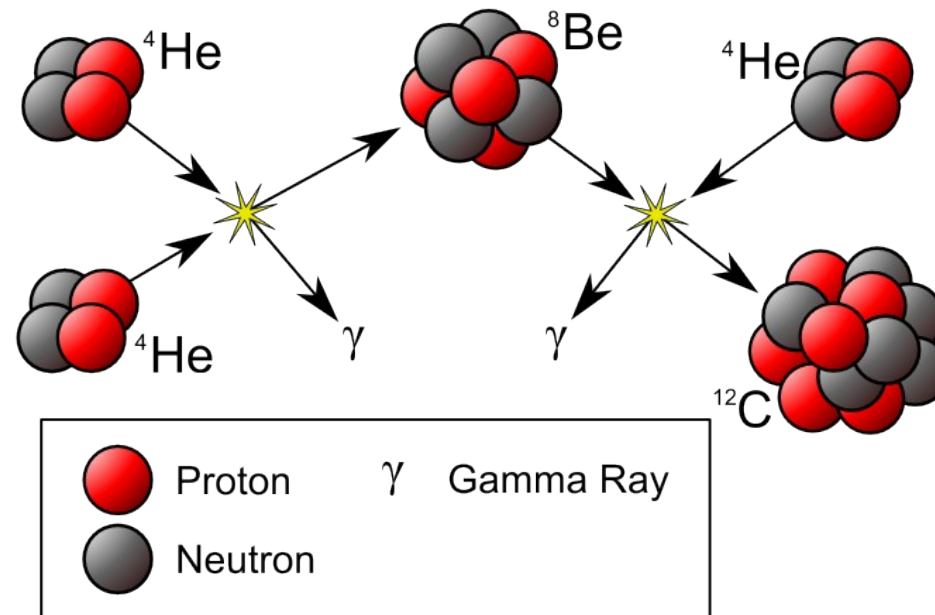
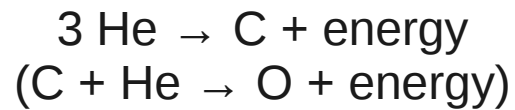
(Helium nucleus is called an “alpha” particle)



How much energy comes out of Helium fusion?

Triple Alpha Reaction

(Helium nucleus is called an “alpha” particle)



The Helium Flash

Fusion ignition in degenerate matter is a bomb ready to explode

Ideal Gas

$$p \propto \rho T$$

Nuclear reactions start

Heating → Expansion → Cooling

Cooling = Less nuclear reactions

Cooling → Contraction → Heating

Thermostat keeps nuclear reactions "tuned"

Controlled fusion

Degenerate Matter

$$p \propto \rho^{4/3}$$

Nuclear reactions start

Heating

Star does not expand

Nuclear burning increases

More Heating

No thermostat

Runaway temperature rise

Runaway fusion

The Helium Flash

Fusion ignition in degenerate matter is a bomb ready to explode

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Runaway fusion

The Helium Flash

Controlled fusion



Runaway fusion



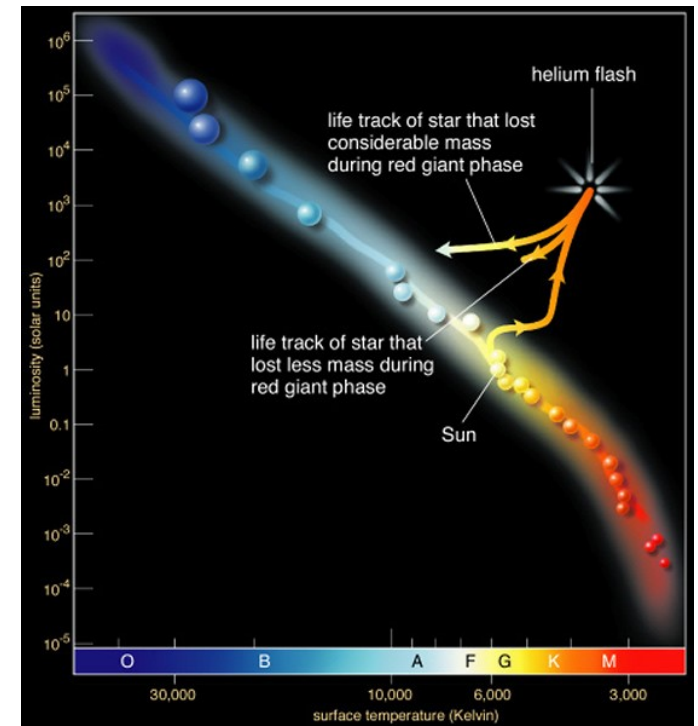
The Helium Flash

Fusion ignition in degenerate matter is a bomb ready to explode

No thermostat! Core just gets hotter and hotter

Runaway Helium burning: **100 billion times the Solar output** in just a few seconds

Helium Flash



The Helium Flash

Fusion ignition in degenerate matter is a bomb ready to explode

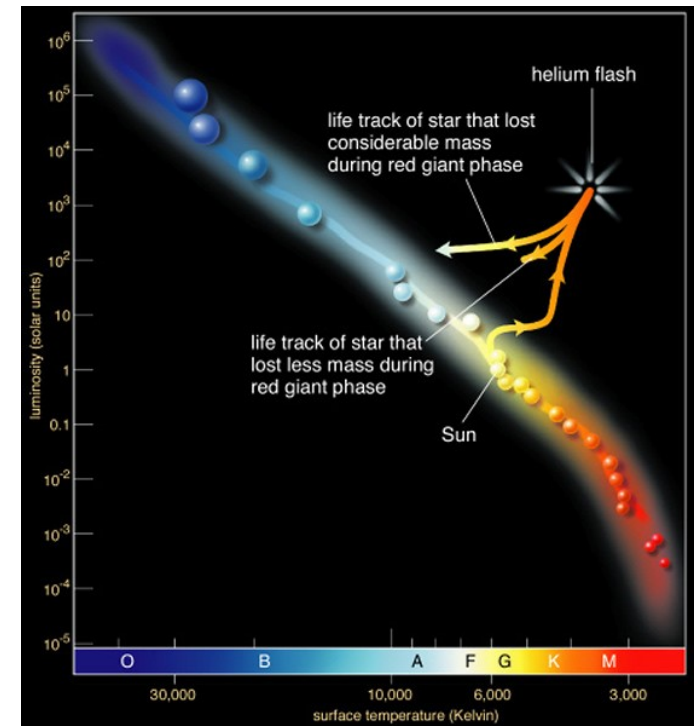
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Runaway Helium burning: **100 billion times the Solar output** in just a few seconds

Helium Flash

Yet, nothing is seen

Why?



The Helium Flash

Fusion ignition in degenerate matter is a bomb ready to explode

No thermostat! Core just gets hotter and hotter

Runaway Helium burning: **100 billion times the Solar output** in just a few seconds

Helium Flash

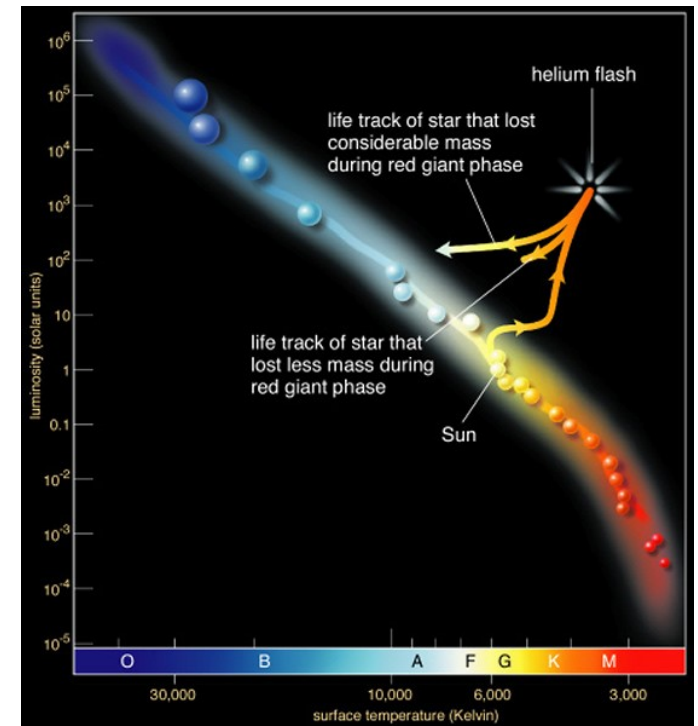
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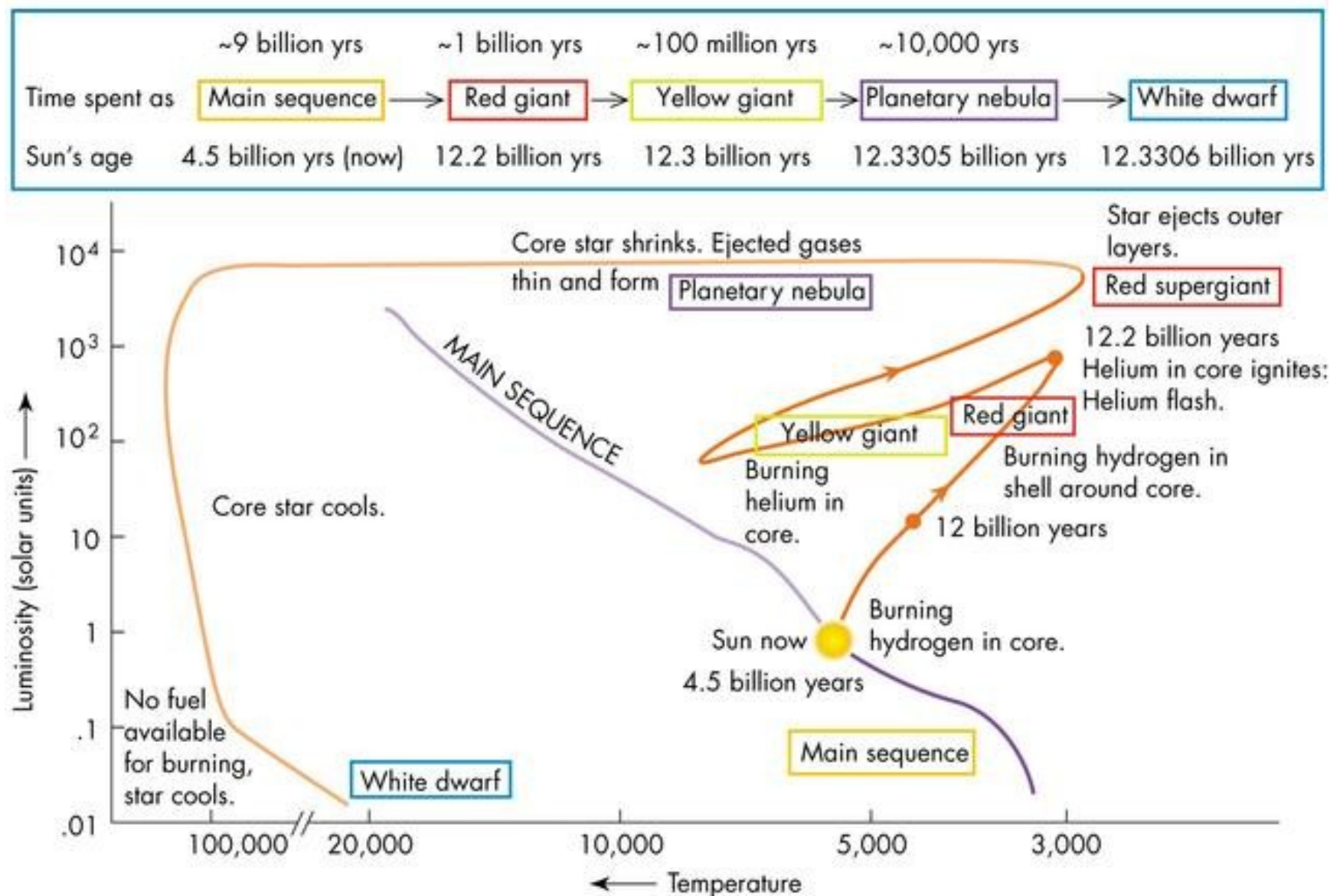
The energy is ALL used to lift the degeneracy

(i.e., to “melt” the degenerate core back into a normal gas)

Helium then burns **steadily** in a core of normal gas



Evolutionary track



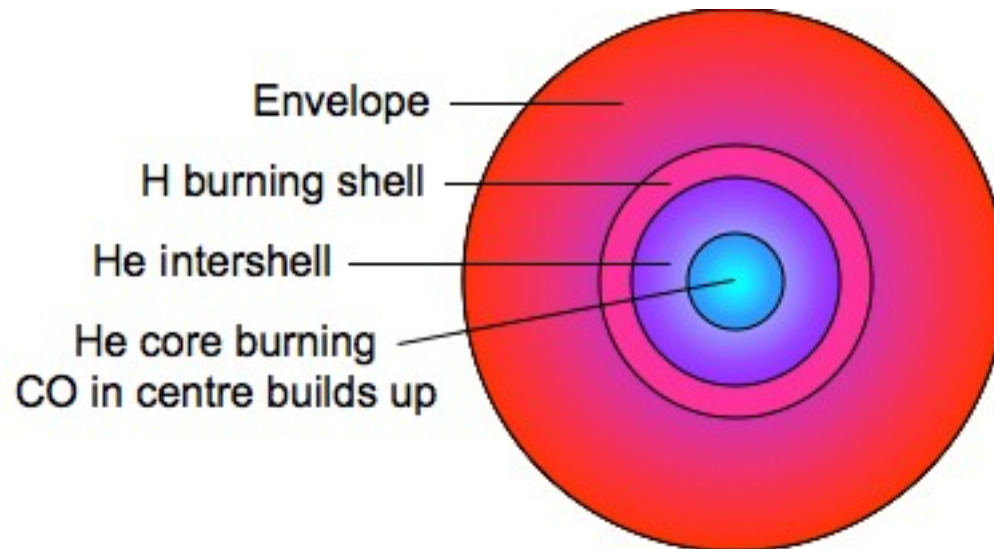
The Horizontal Branch

Helium burning in the core

Hydrogen shell burning

In the HR diagram, the star sets in the **Horizontal Branch**

The Horizontal Branch is the Helium Main Sequence





Helium is gone! Now what?

*What will happen to
me?*



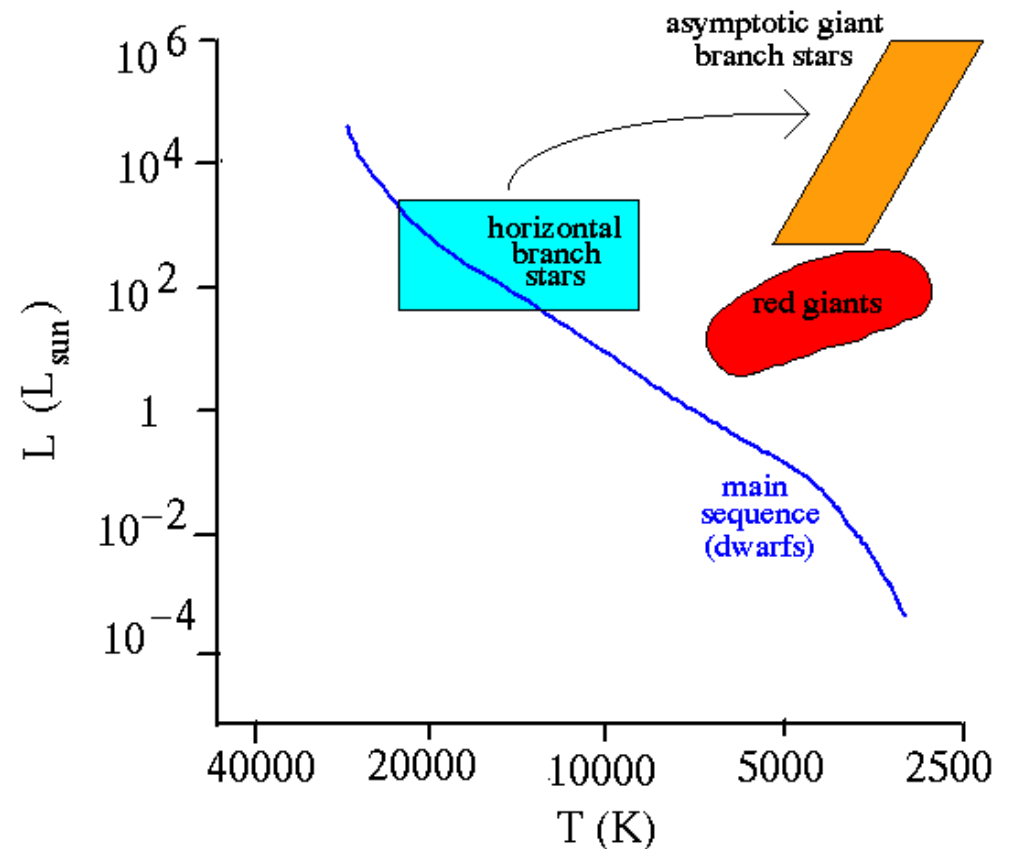
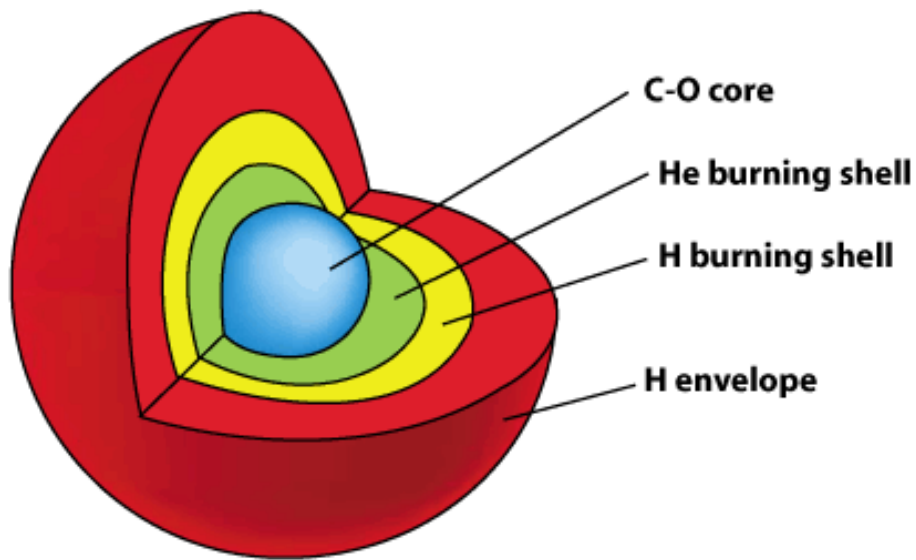
Helium is gone! Now what?

The Carbon-Oxygen core **contracts** and **heats** up.

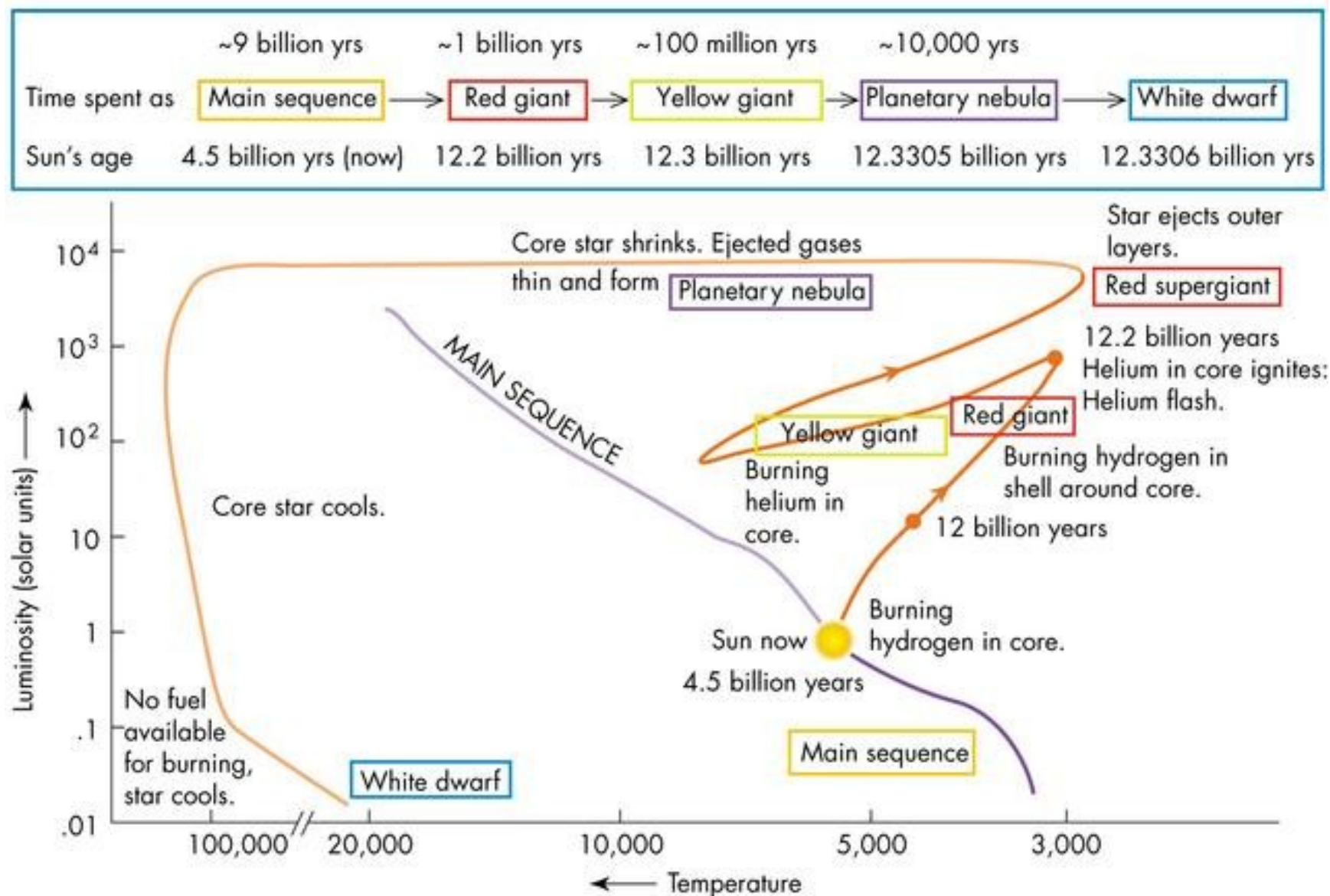
Helium shell burning

More energy is available, the star swells and becomes a red giant again

The star reaches the Asymptotic Giant Branch



Evolutionary track

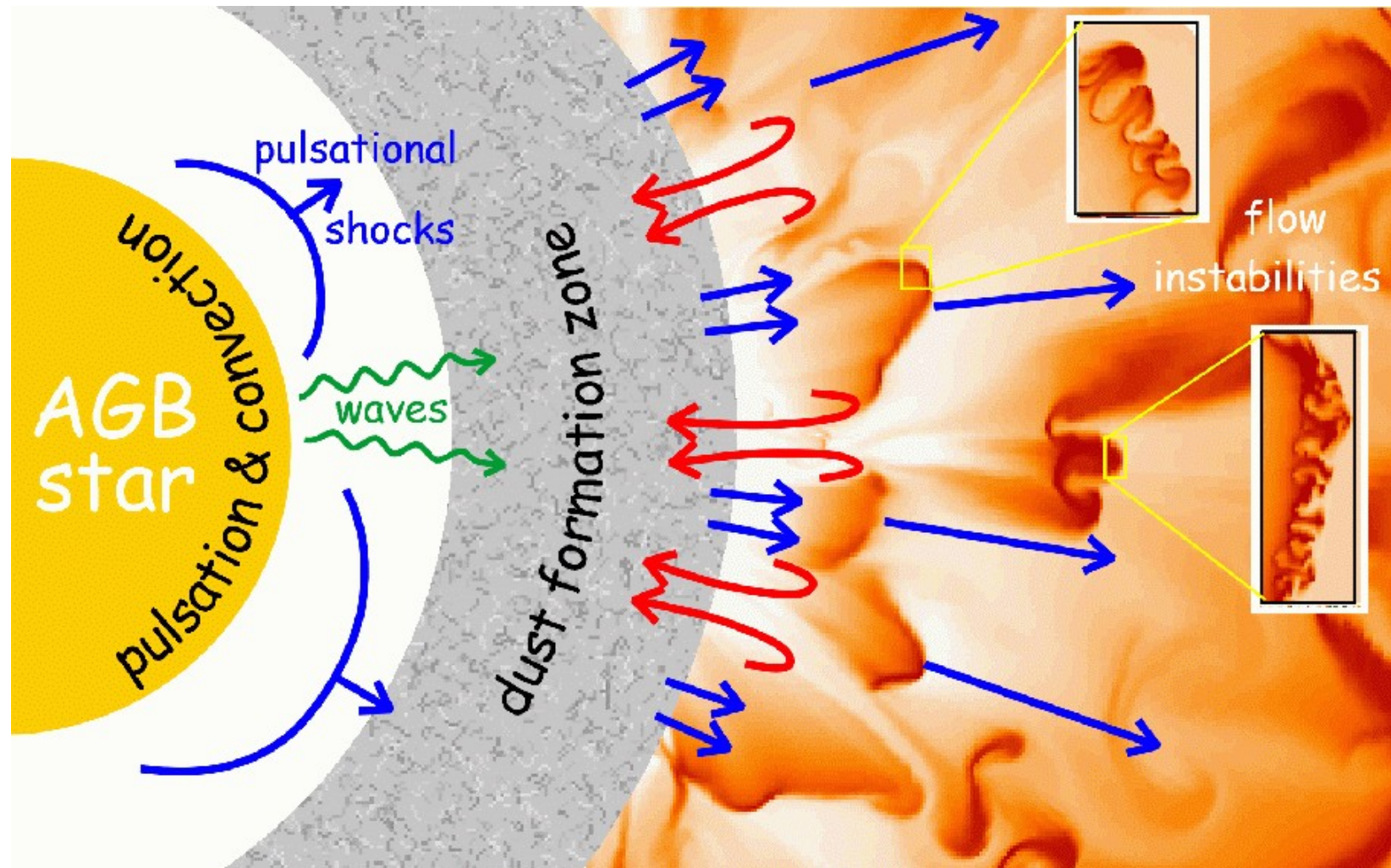


AGB stars are quite unstable

Helium burning is **very** sensitive to temperature ($\sim T^{40}$)

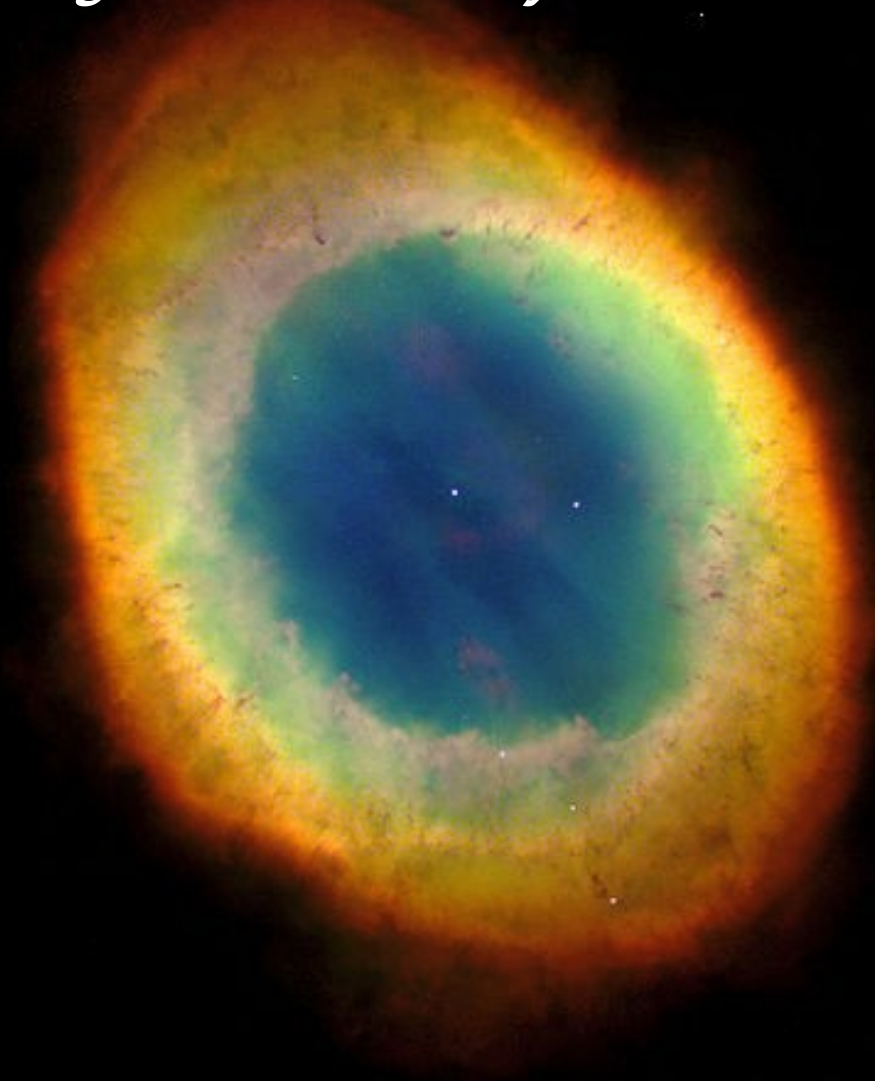
Small temperature fluctuations lead to **violent** variations in rate of nuclear reactions

Prone to instabilities

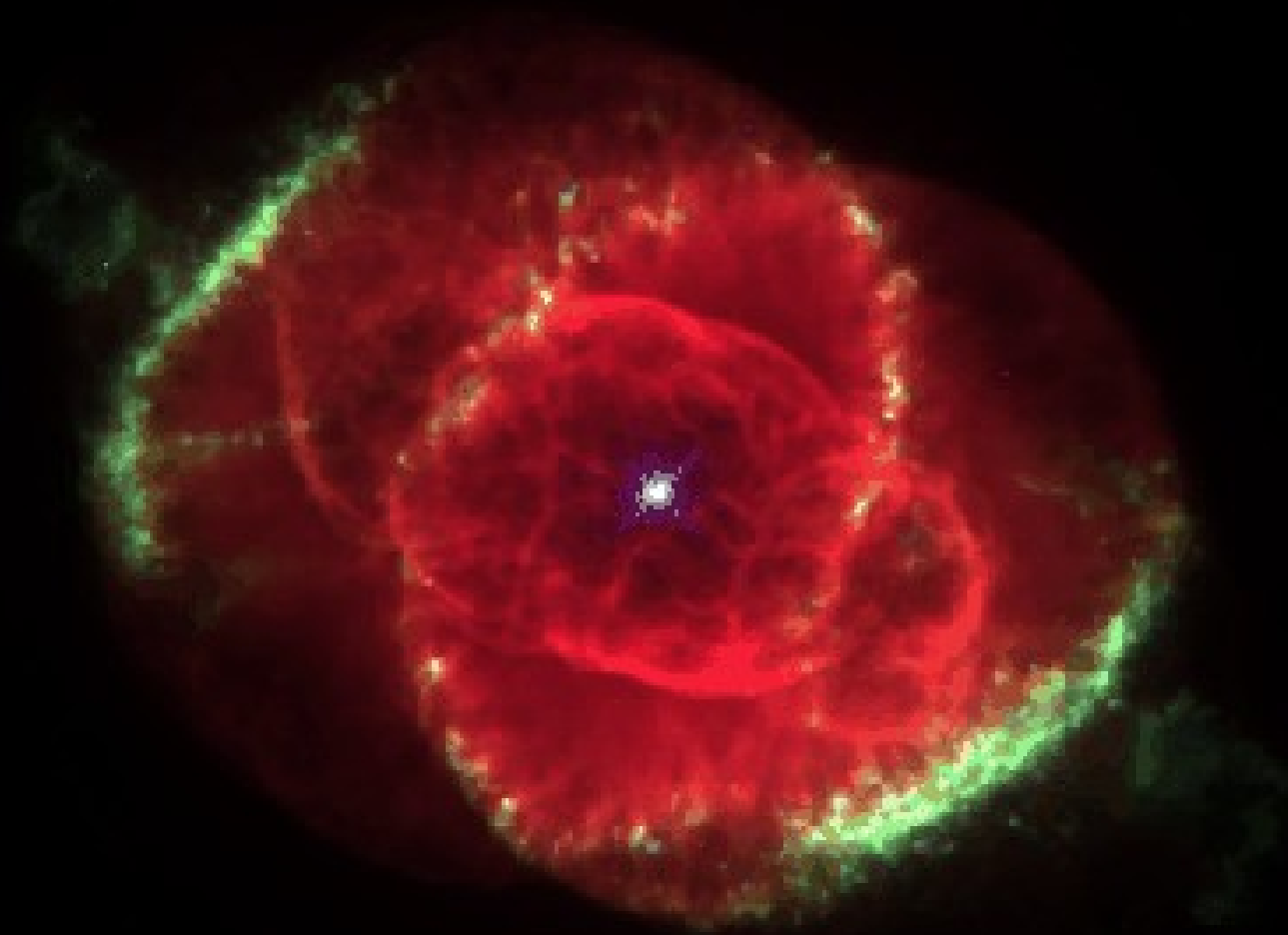


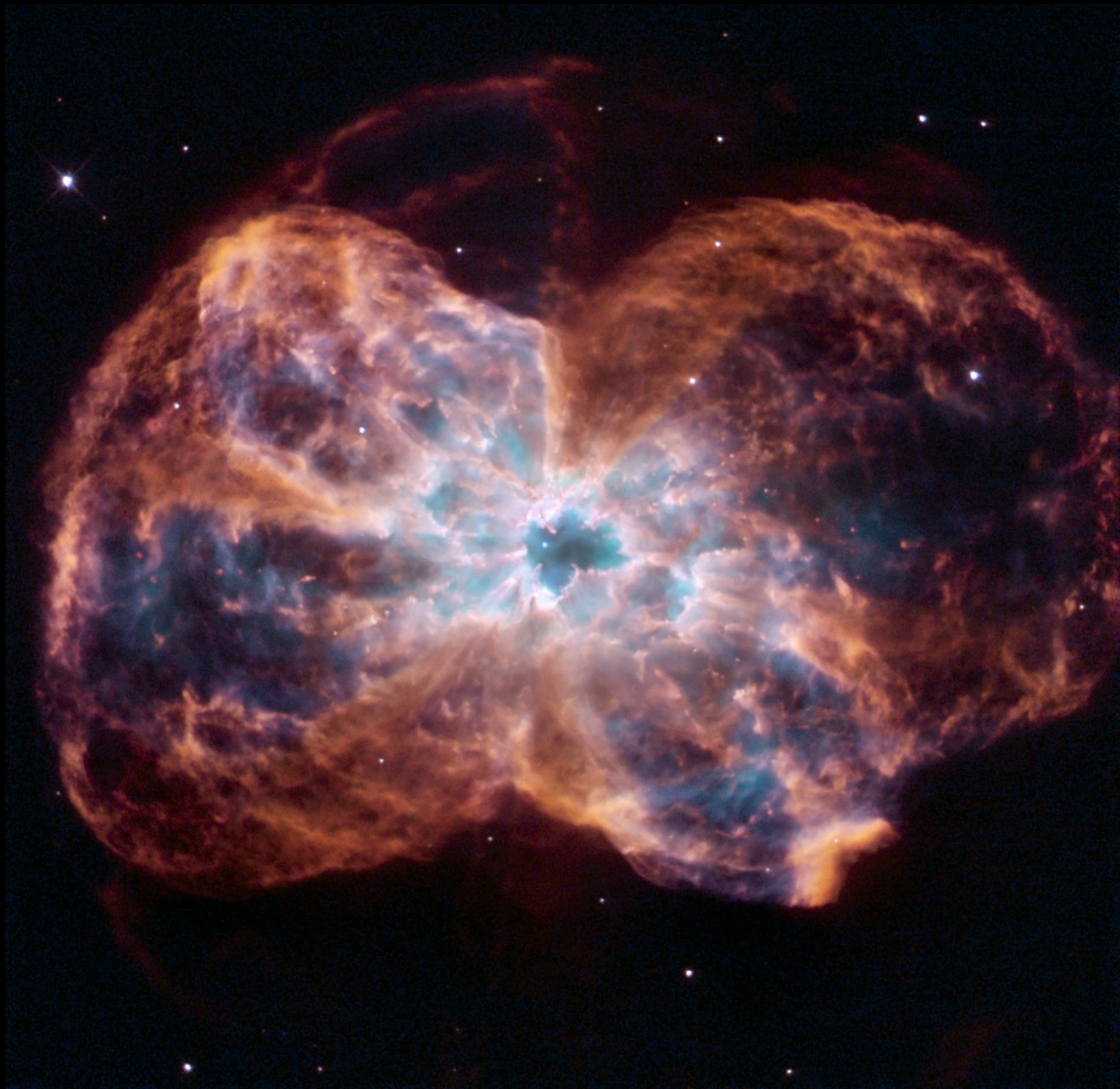
PLANETARY NEBULA

The gracious death of low mass stars





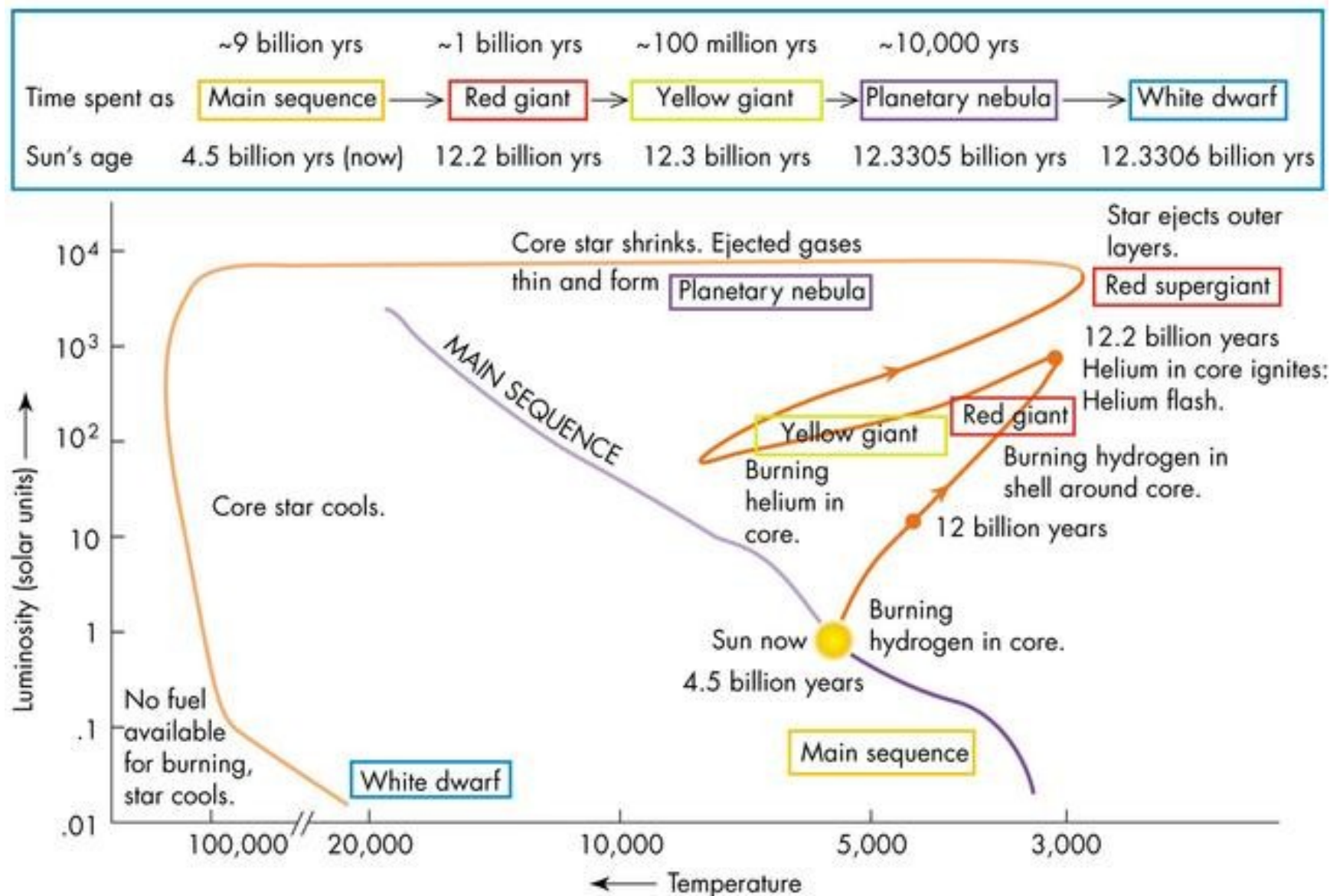






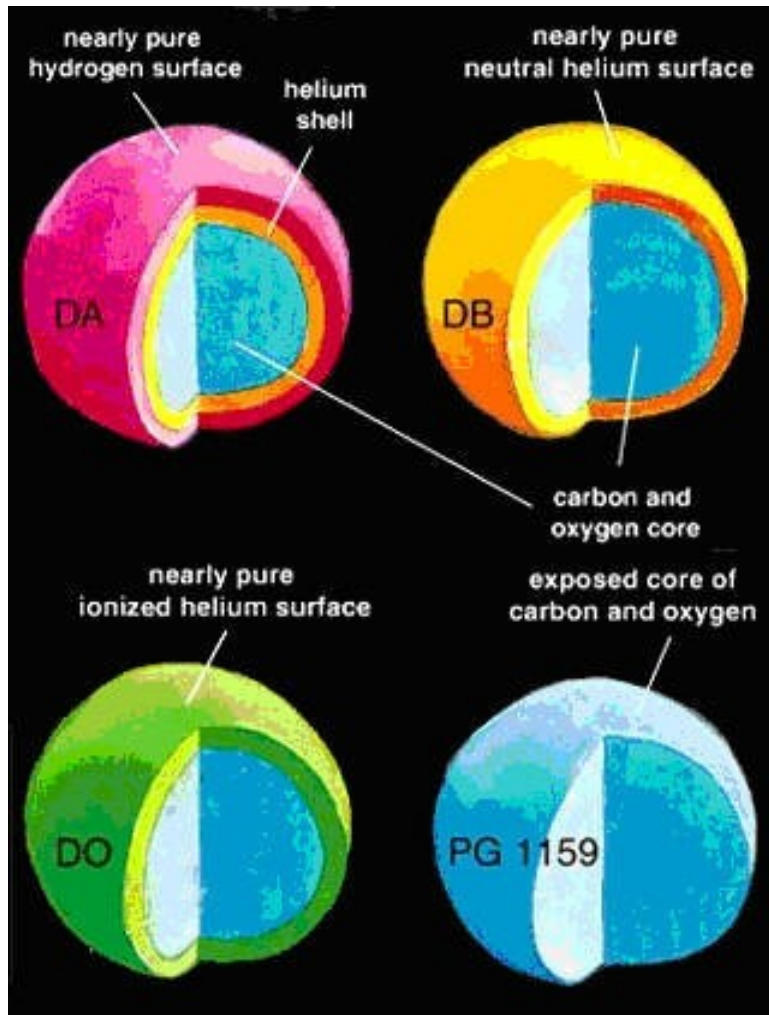


Evolutionary track

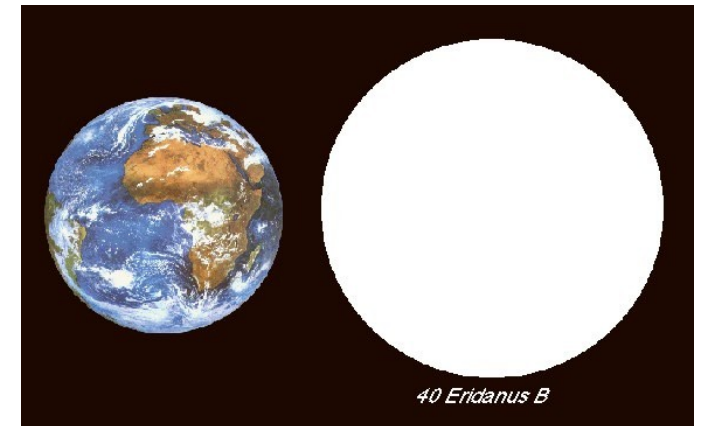


White dwarfs

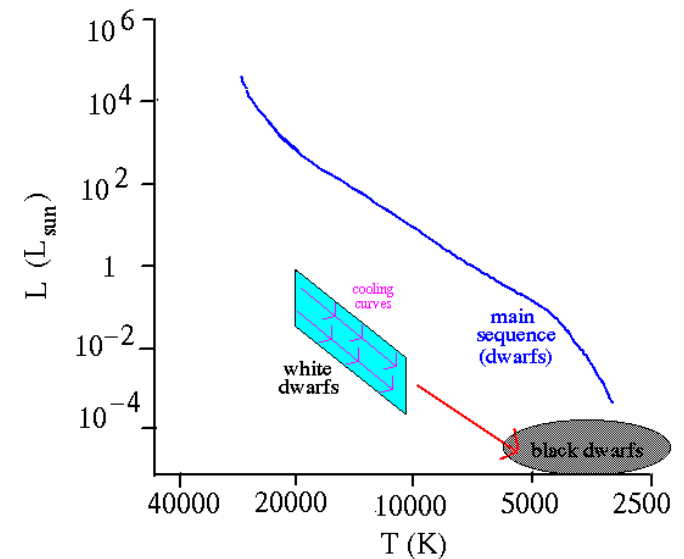
White dwarfs are the exposed degenerate core of the star



Types of white dwarfs



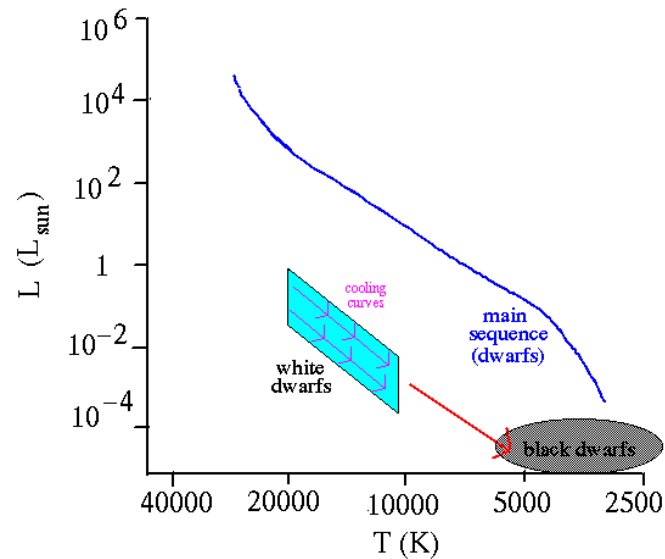
White dwarfs have planetary dimensions...



... and they do little but cooling.

White dwarfs

White dwarfs are the exposed degenerate core of the star

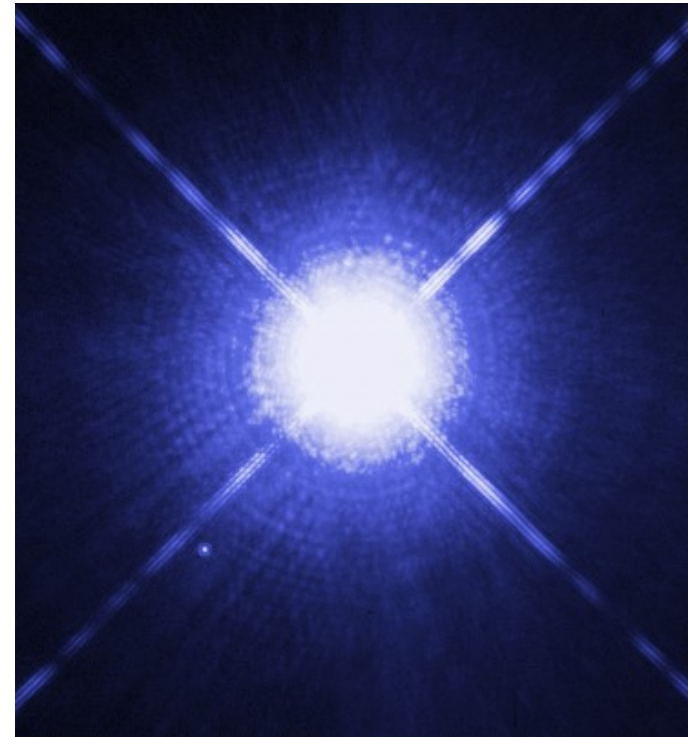


No energy production
Supported by degenerate pressure

Cooling takes a long time

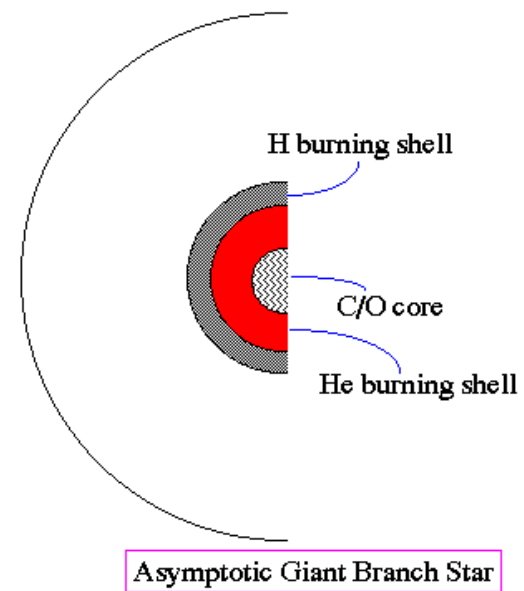
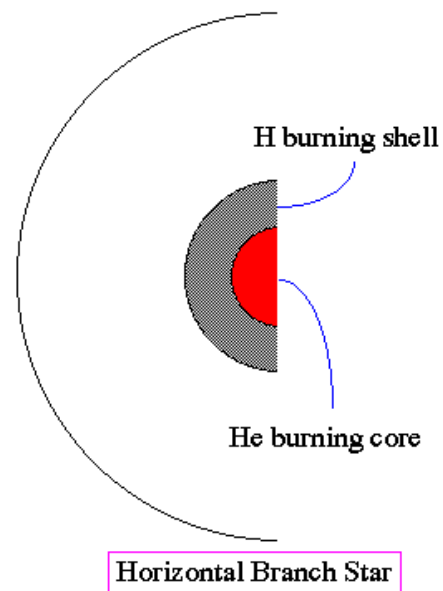
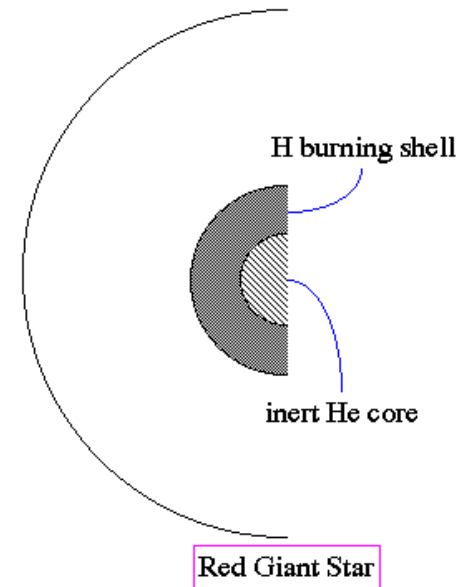
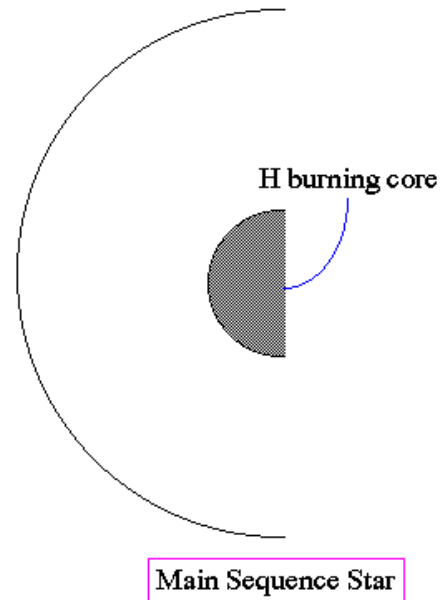
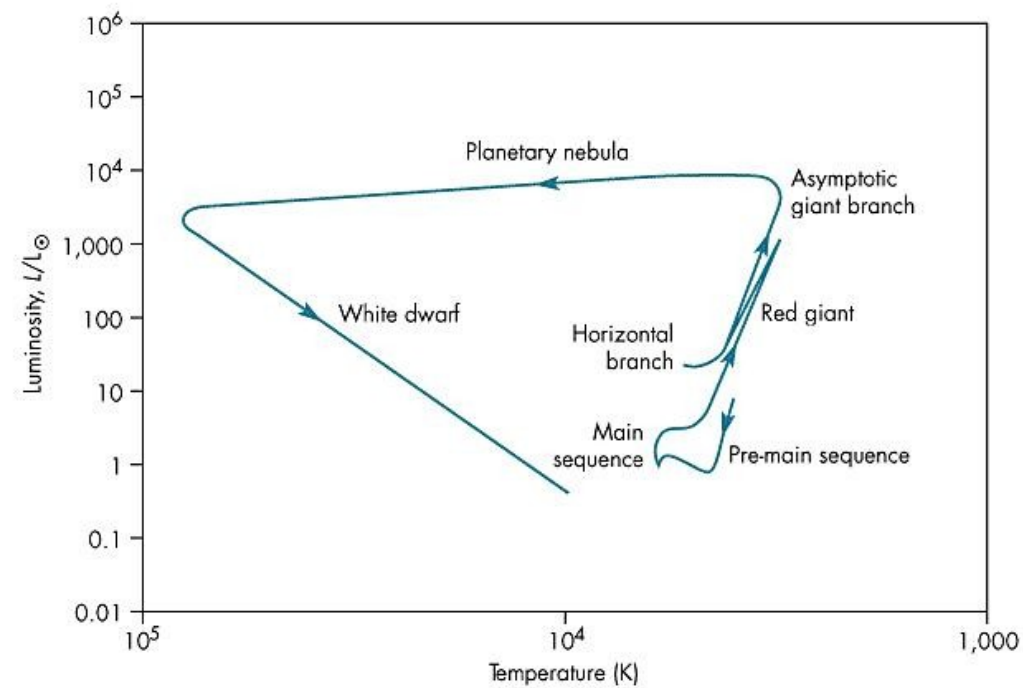
10^{15} yr to cool down to background temperature

The universe is not old enough to have black dwarfs
Coldest white dwarfs ~ 5000 K.

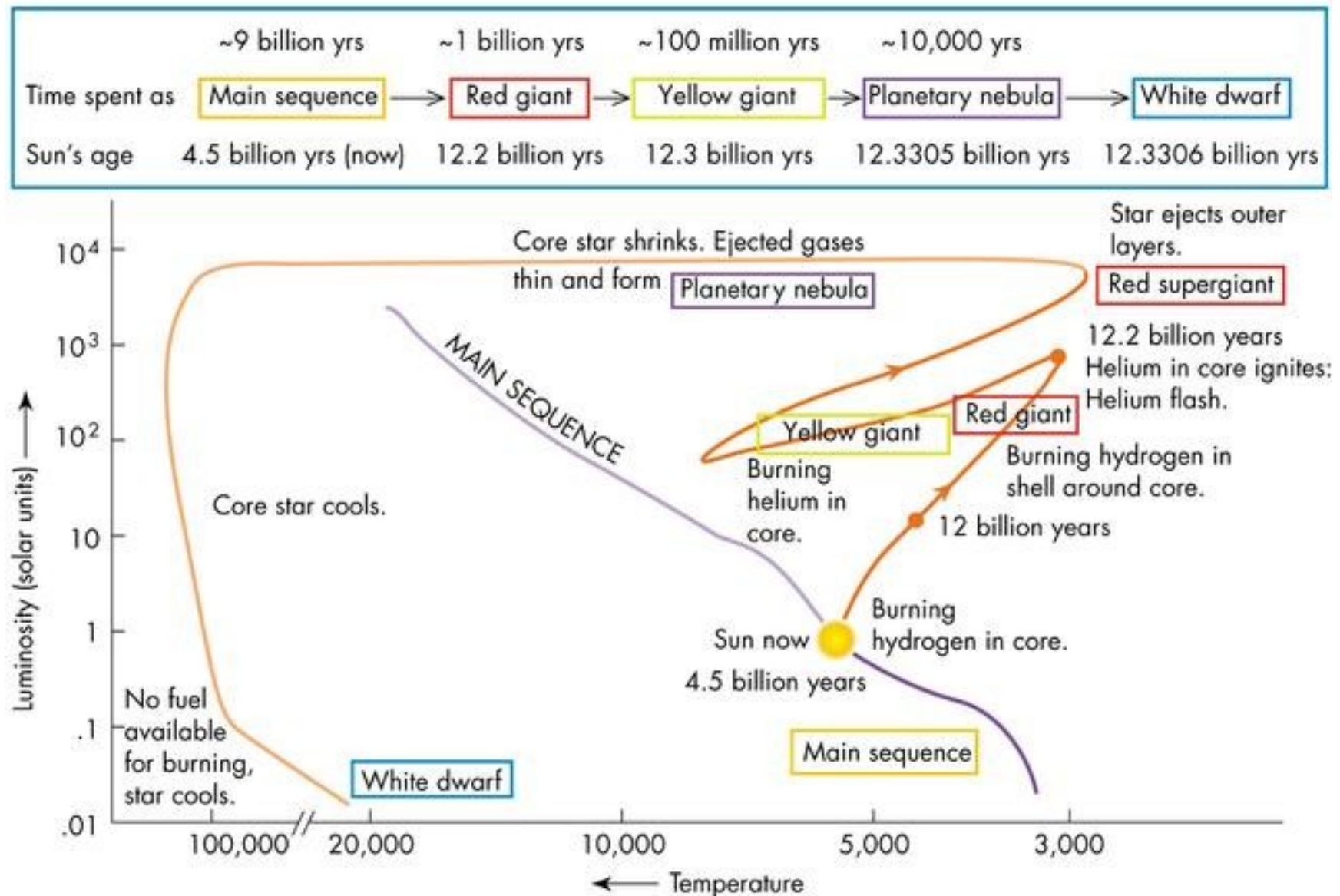


Sirius A (Main Sequence star)
and **Sirius B** (White Dwarf)

Evolution of a low mass star

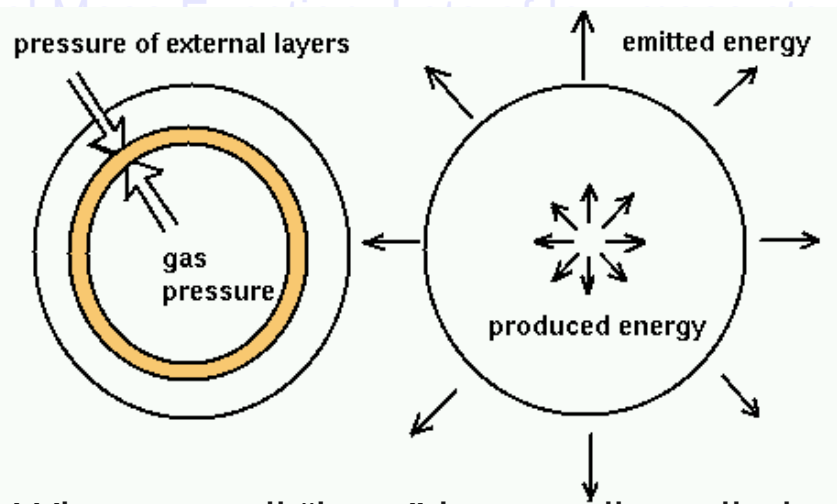


Post-Main Sequence Evolution - Timescales



Let's summarize

Radiative Equilibrium: Heating is matched by cooling



What we call “heat” is actually radiation

Radiative loss = Cooling

In a star in radiative equilibrium,

radiative losses (cooling)

are matched by

energy production (heating)

from nuclear reactions

Let's summarize

Turbulence is a self-similar flow. Size spectrum is well defined.

Turbulent fragmentation of a molecular cloud leads to a well defined mass spectrum.

Mass spectrum: Initial Mass Function. Lots of low mass stars, few high mass stars.

Lifetime on the Main Sequence: A strong function of mass.

Main Sequence Turn-Off Point. An indicator of age.

Post Main Sequence Evolution

Hydrogen is gone: Helium core contracts and heats

Red Giants - inert CO core, Hydrogen Shell Burning

Core degeneracy – a phase transition to “solid-like” behavior. Core contraction stops.

100 Million K – Helium ignition. Degeneracy is lifted (Helium Flash).

Horizontal Branch – Helium Main Sequence

Helium is gone: Carbon-Oxygen core contracts and heats

Asymptotic Giant Branch (AGB) star – inert CO core, Helium and Hydrogen Shell Burning

AGB are unstable. Violent pulsations eventually eject the whole atmosphere

Planetary Nebula

The exposed degenerate core is seen as a white dwarf

White dwarfs cool in long timescales

High mass stars life fast and die young.

Low mass stars will still be around long after we're gone

Let's summarize

Turbulence is a self-similar flow. Size spectrum is well defined.

Turbulent fragmentation of a molecular cloud leads to a well defined mass spectrum.

Mass spectrum: Initial Mass Function. Lots of low mass stars, few high mass stars.

Lifetime on the Main Sequence: A strong function of mass.

Main Sequence Turn-Off Point. An indicator of age.

Post Main Sequence Evolution

Helium core contracts and heats

Helium core, Hydrogen Shell Burning

Core contracts to "solid-like" behavior. Core contraction stops.

Helium core contracts and heats. Degeneracy is lifted (Helium Flash).

Helium Main Sequence

Oxygen core contracts and heats

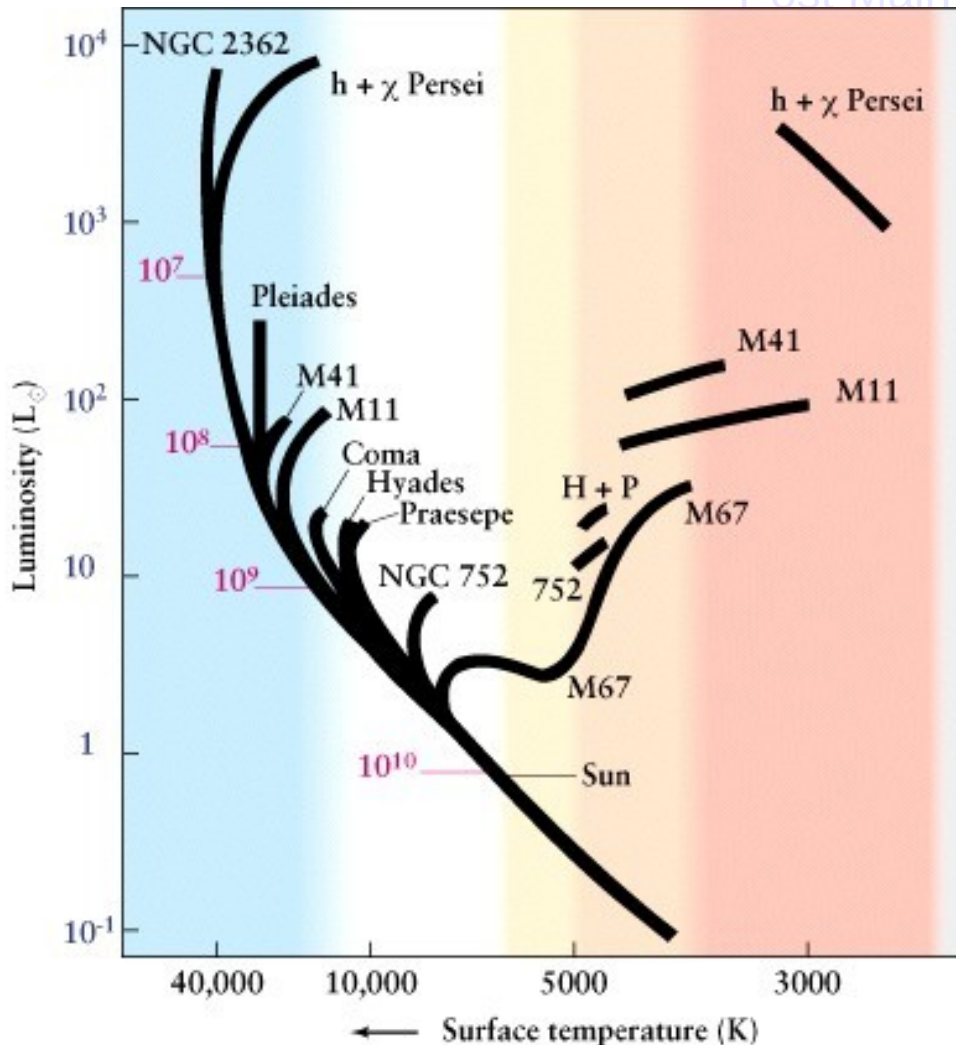
Inert CO core, Helium and Hydrogen Shell Burning

Stars eventually eject the whole atmosphere

Planetary Nebula

White core is seen as a white dwarf

cools in long timescales



Let's summarize

Post Main Sequence Evolution

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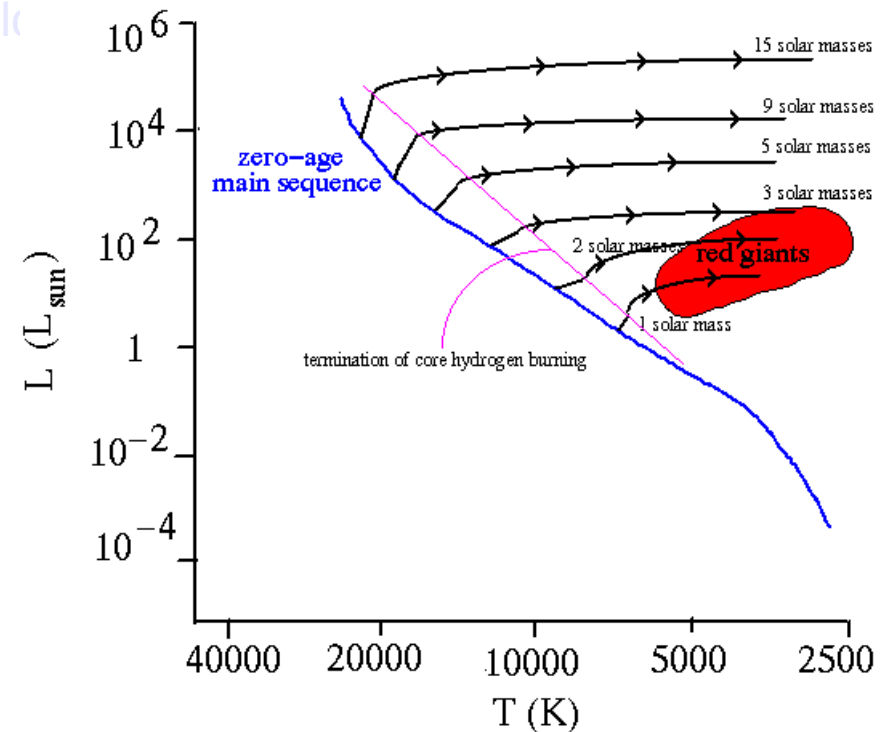
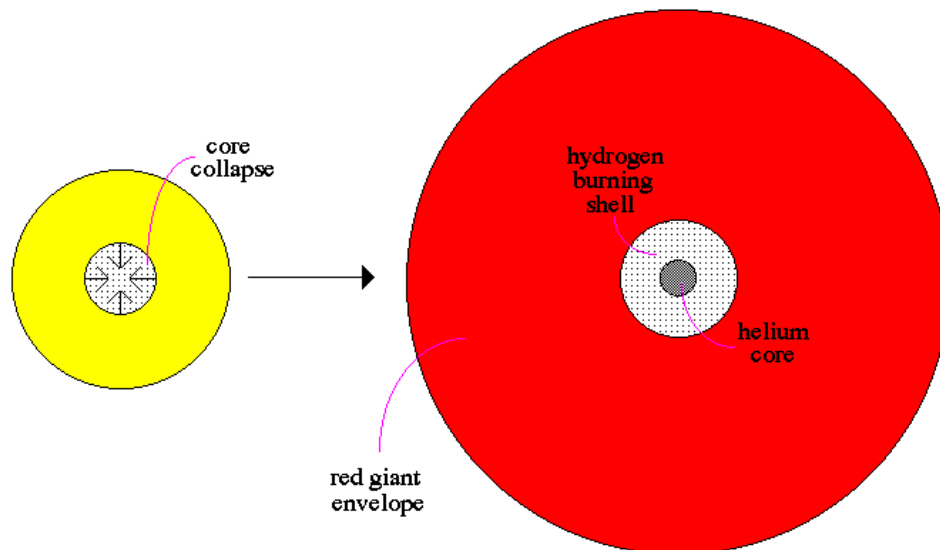
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Hydrogen Shell Burning



Let's summarize

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White dwarfs cool in long timescales

Ideal Gas

$$p \propto \rho T$$

Temperature rises, pressure rises

Temperature falls, pressure falls

Radiation → less support against gravity

→ **contraction**

Degenerate Matter

$$p \propto \rho^{4/3}$$

If temperature rises or falls, pressure
couldn't care less

Radiative losses can continue indefinitely

The degenerate core is stable

Let's summarize

Post Main Sequence Evolution

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Planetary Nebula

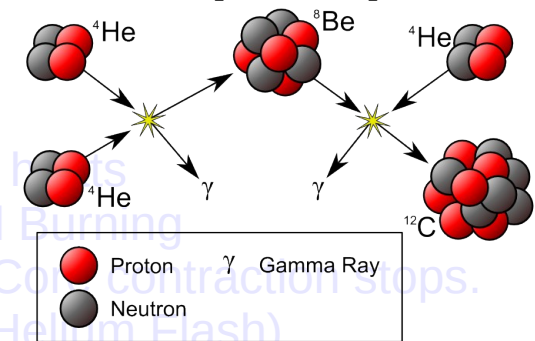
The exposed degenerate core
cools in 10⁴ years



Let's summarize

Post Main Sequence Evolution

Triple Alpha



Hydrogen is gone: Helium core contracts and heats

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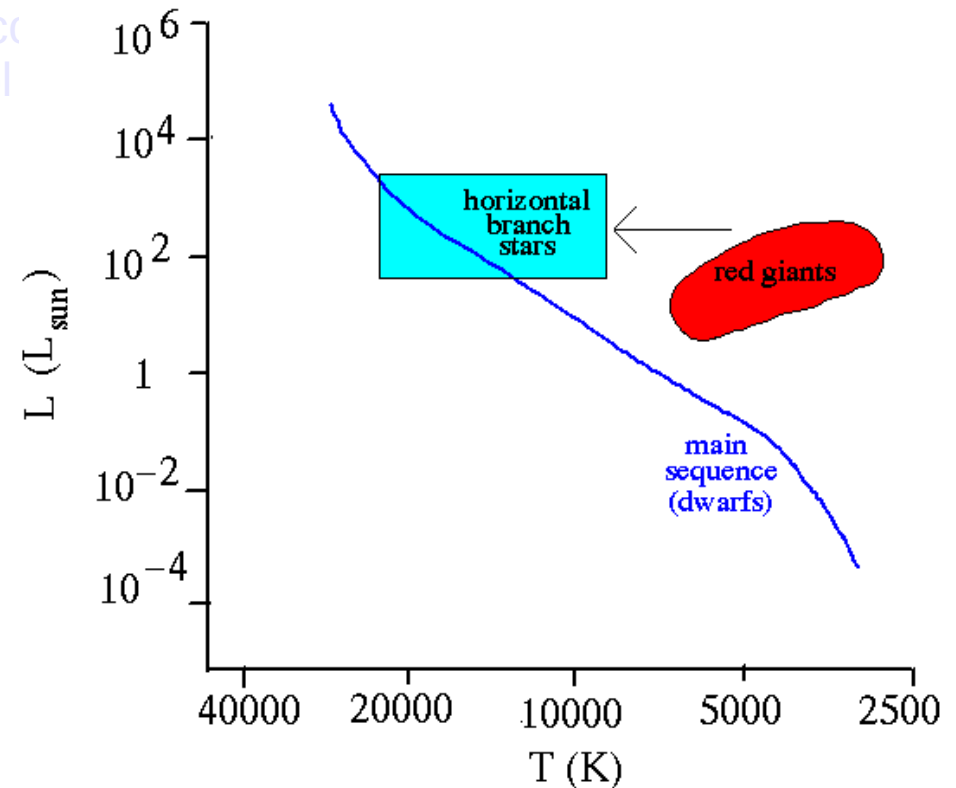
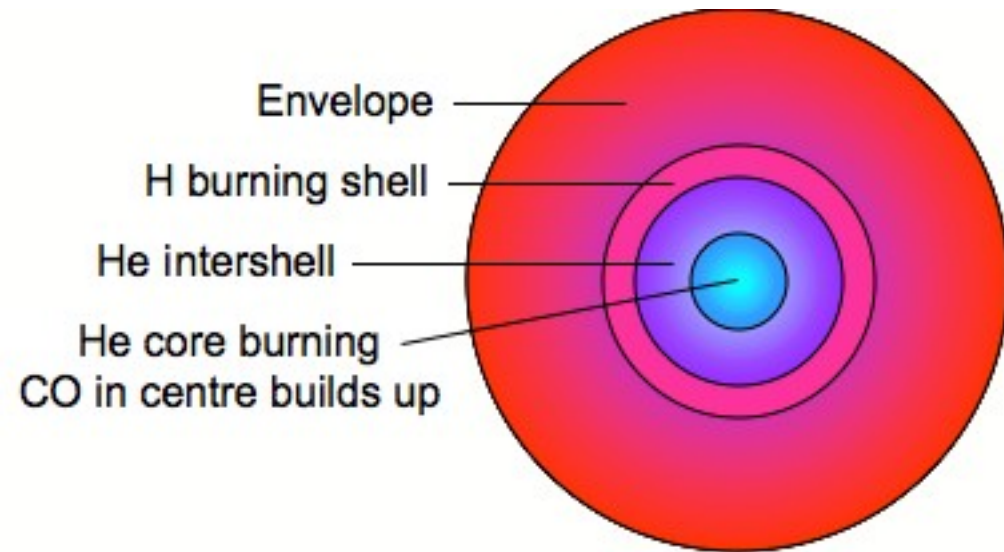
Asymptotic Giant Branch (AGB) star – inert CO core, Helium and Hydrogen Shell Burning

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Planetary Nebula

The exposed degenerate core

White dwarfs cool



Let's summarize

Post Main Sequence Evolution

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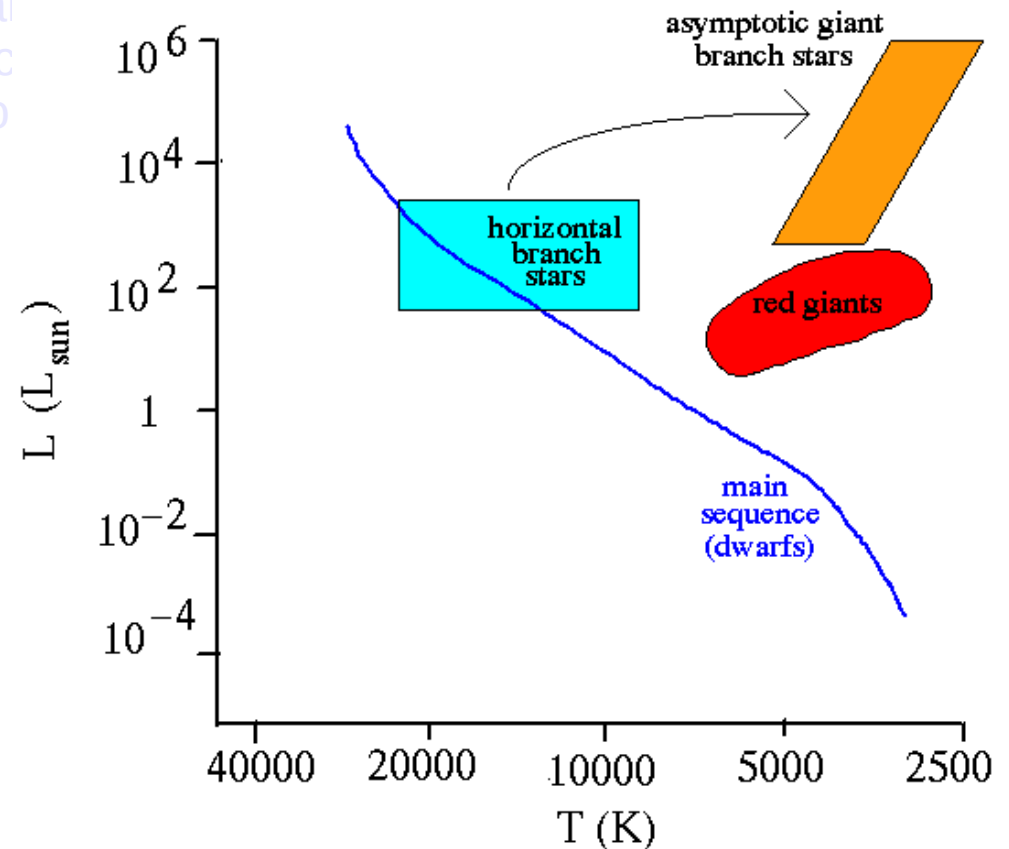
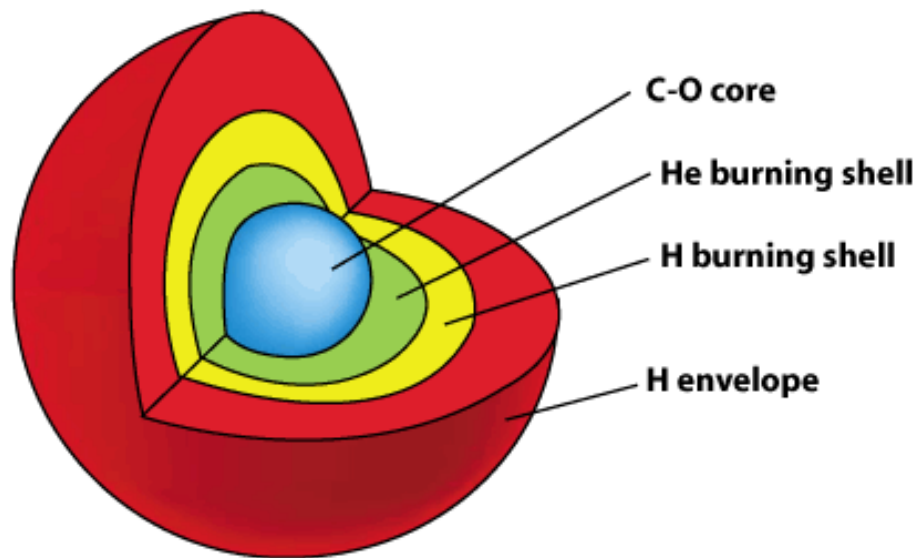
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Planetary

The exposed degenerate c
100



Let's summarize

Post Main Sequence Evolution



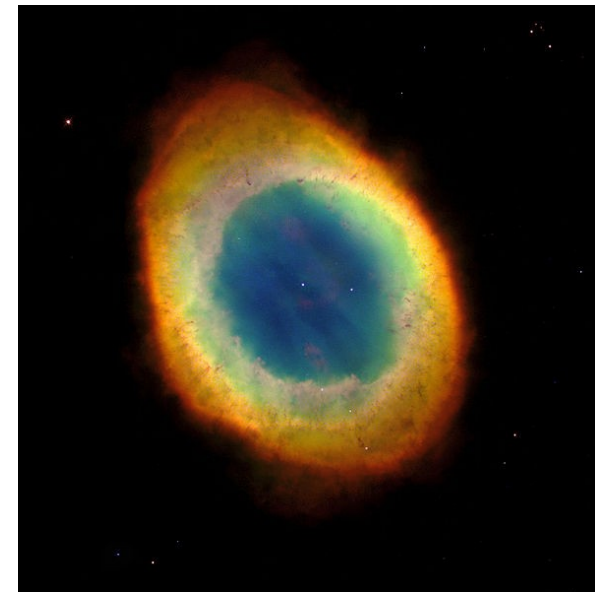
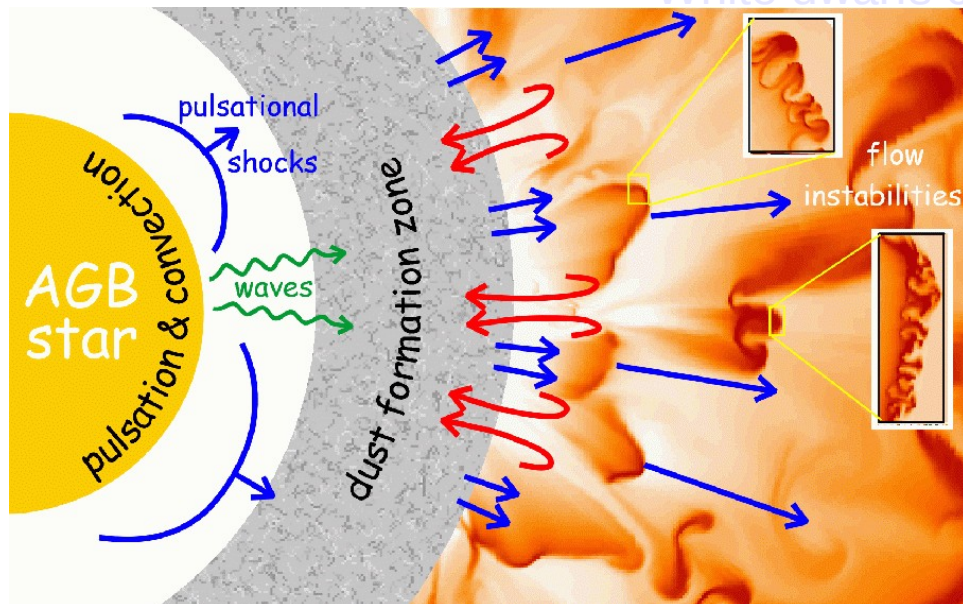
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Planetary Nebula

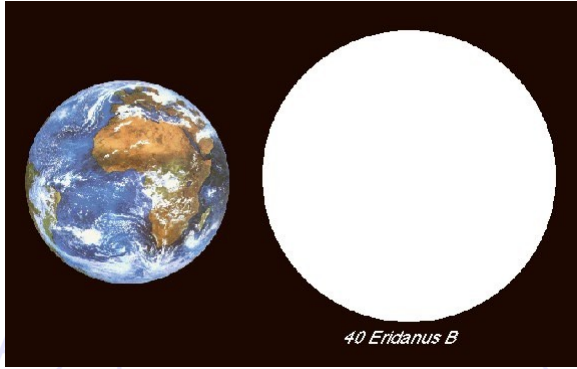
The exposed degenerate core is seen as a white dwarf

White dwarfs cool in long timescales



Let's summarize

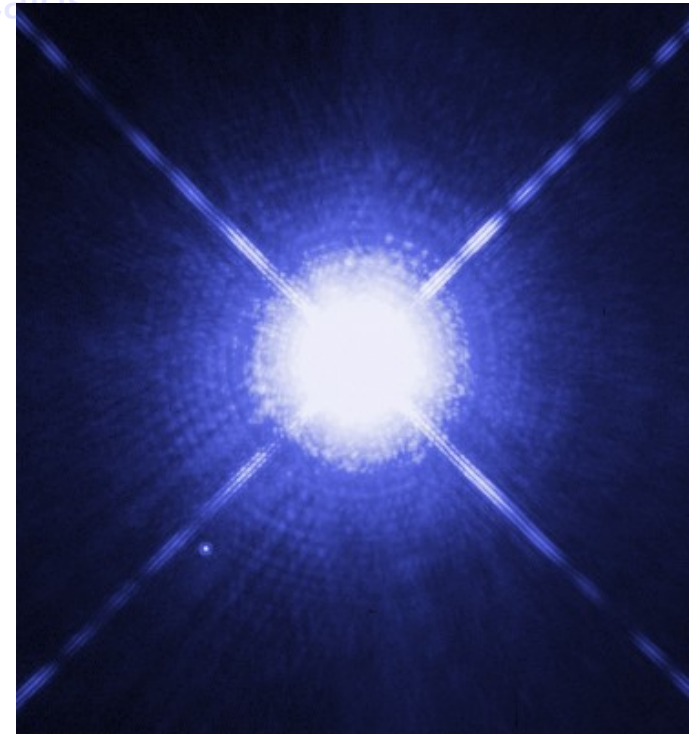
Post Main Sequence Evolution



40 Eridanus B

The exposed degenerate CO core is seen as a white dwarf

White dwarfs cool in long timescales



Let's summarize

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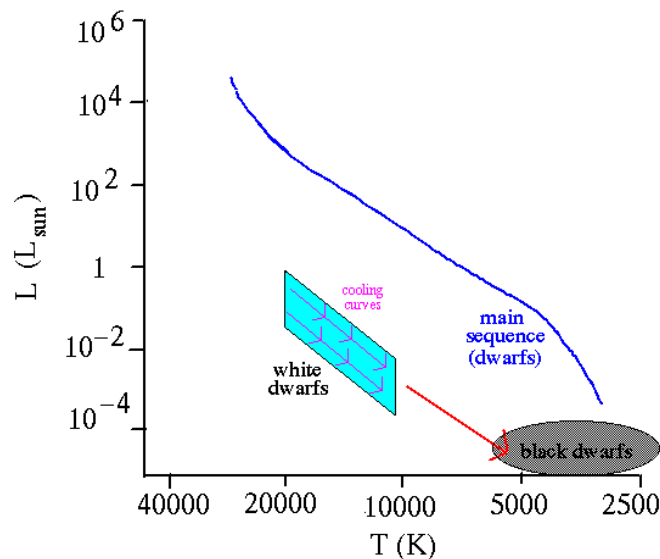
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AGB are unstable. Violent pulsations eventually eject the whole atmosphere

Planetary Nebula

The exposed degenerate core is seen as a white dwarf

White dwarfs cool in long timescales



No energy production
Supported by degenerate pressure

Cooling takes a long time

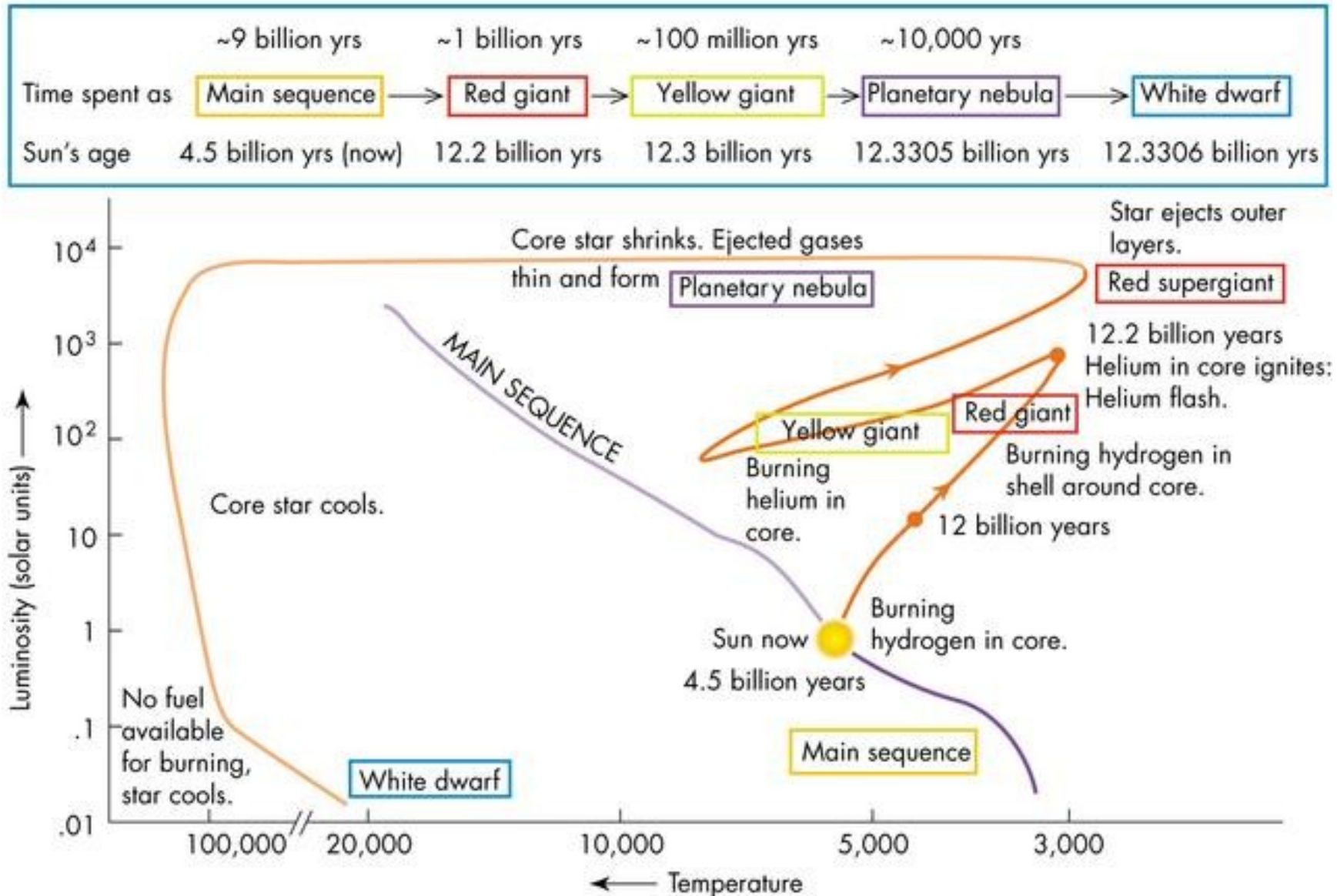
10^5 yr to cool down to background temperature

The universe is not old enough to have black dwarfs

Coldest white dwarfs ~5000 K.

Let's summarize

Evolutionary track of a low mass star

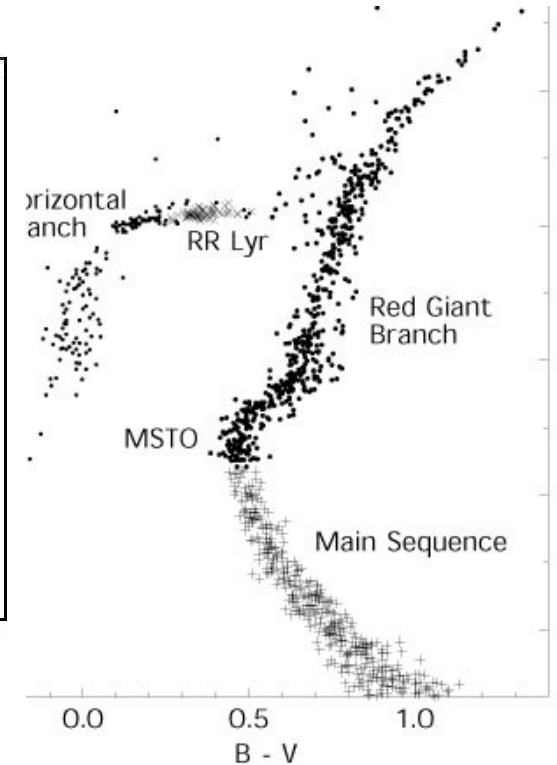
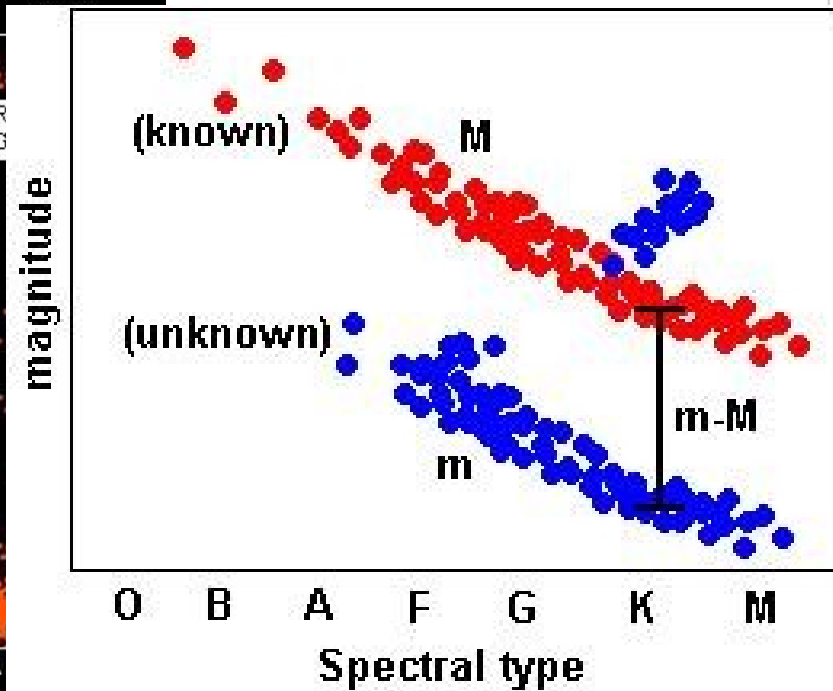
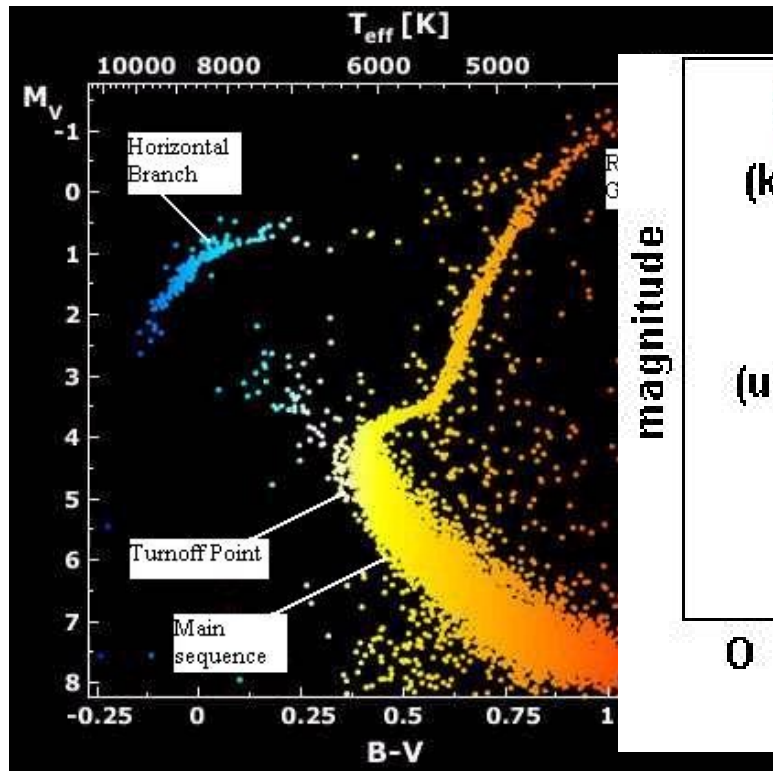


Stellar Distances

Main Sequence (HR Diagram) fitting

We know the absolute luminosity of the main sequence

Slide the observed sequence and you get the distance modulus!



Calibrated (or from model)

Observed

