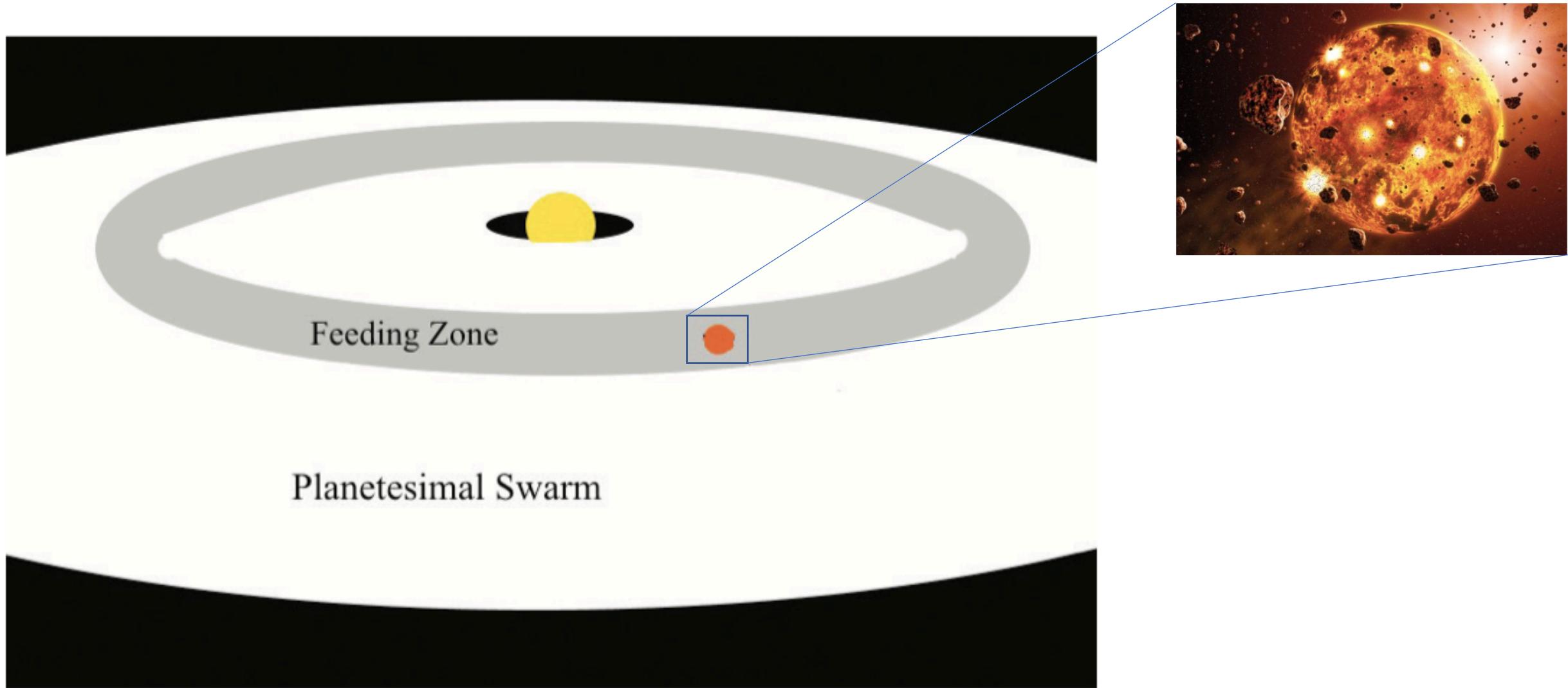
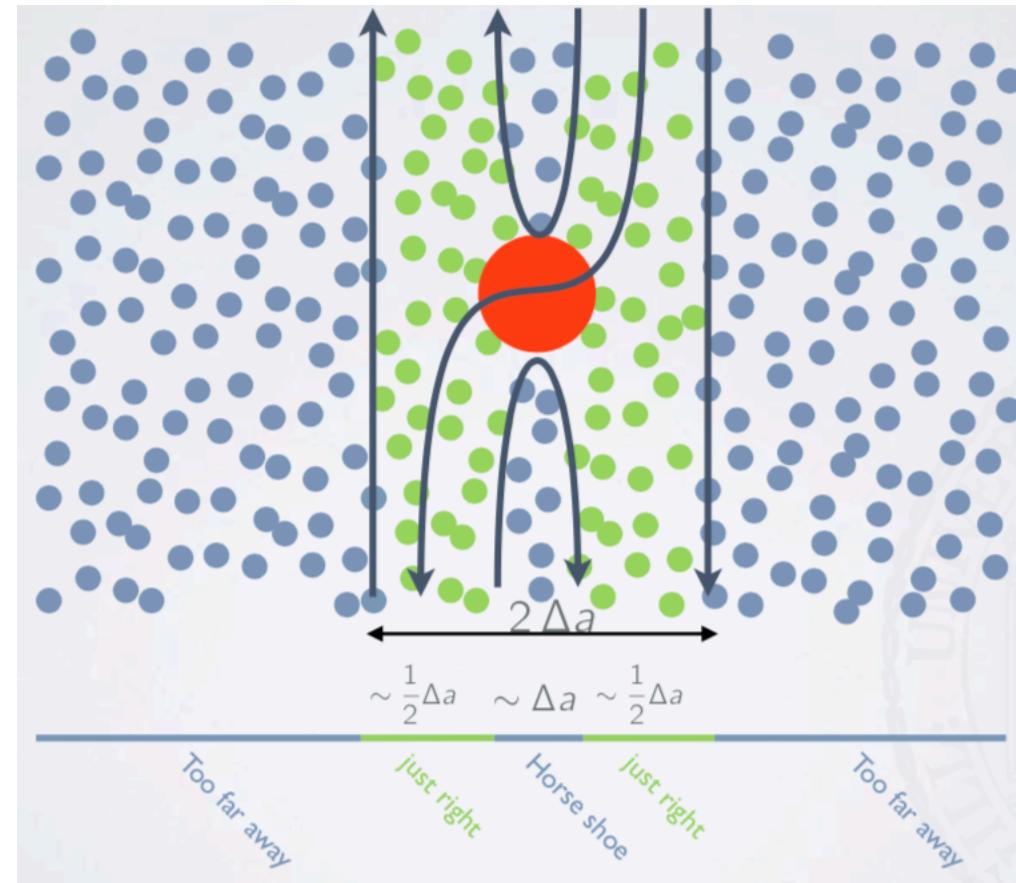


Class 21 – Apr 16<sup>th</sup>, 2020

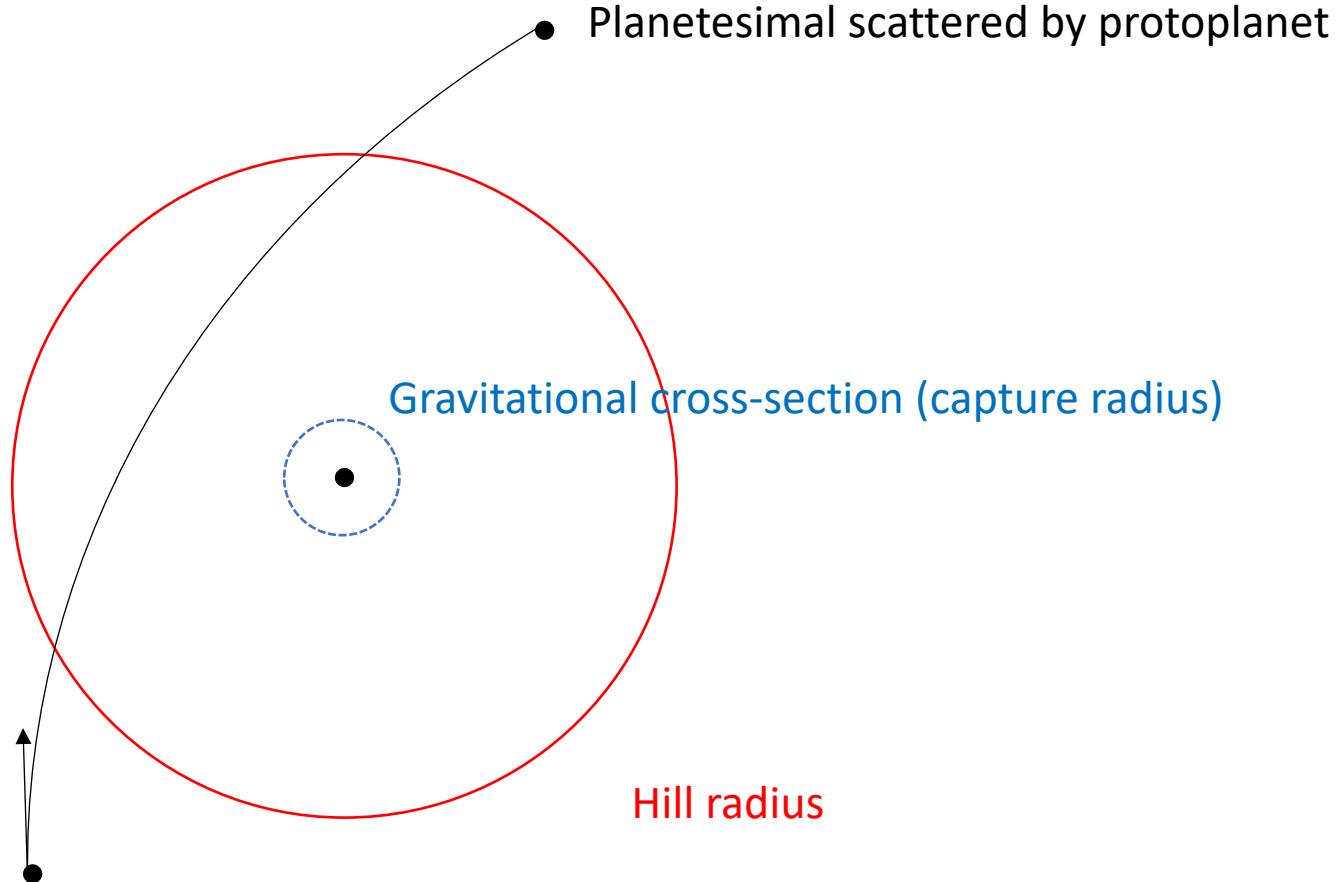
## Planetesimal Accretion

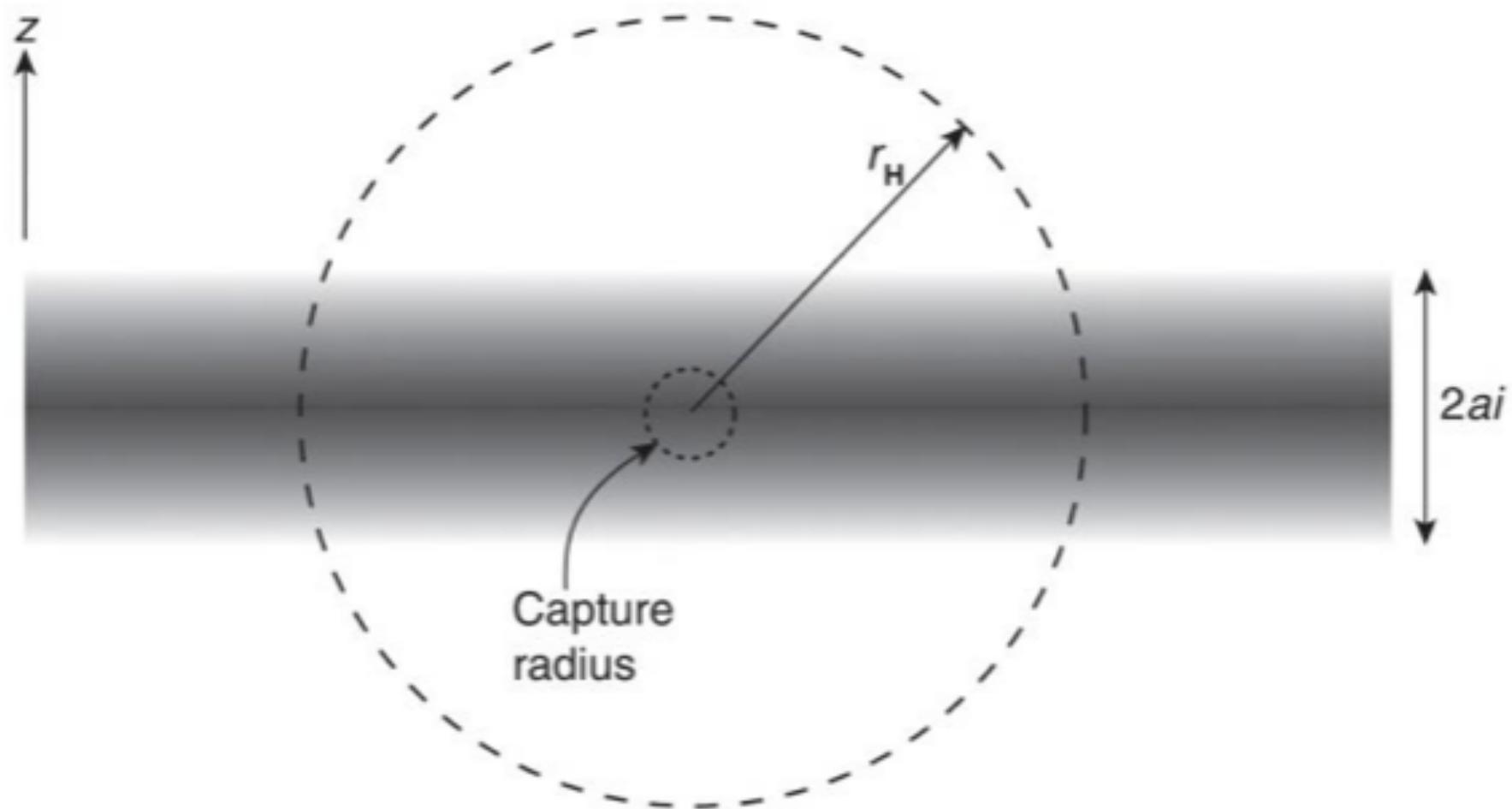


# Shear dominated



# Planetesimal Accretion is inefficient

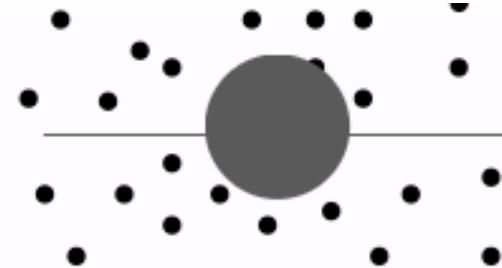
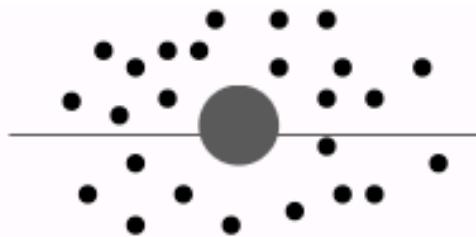




# From runaway growth to oligarchic growth

$$\frac{dm}{dt} = \frac{\sqrt{3}}{2} \Sigma \Omega \pi R^2 f$$

$$f = 1 + \frac{v_{esc}^2}{v_{rms}^2}$$



The growing embryo “heats” the planetesimal disk.

Low  $v_{rms}$  ( $f \gg 1$ )

$$\frac{1}{m} \frac{dm}{dt} \propto m^{1/3}$$

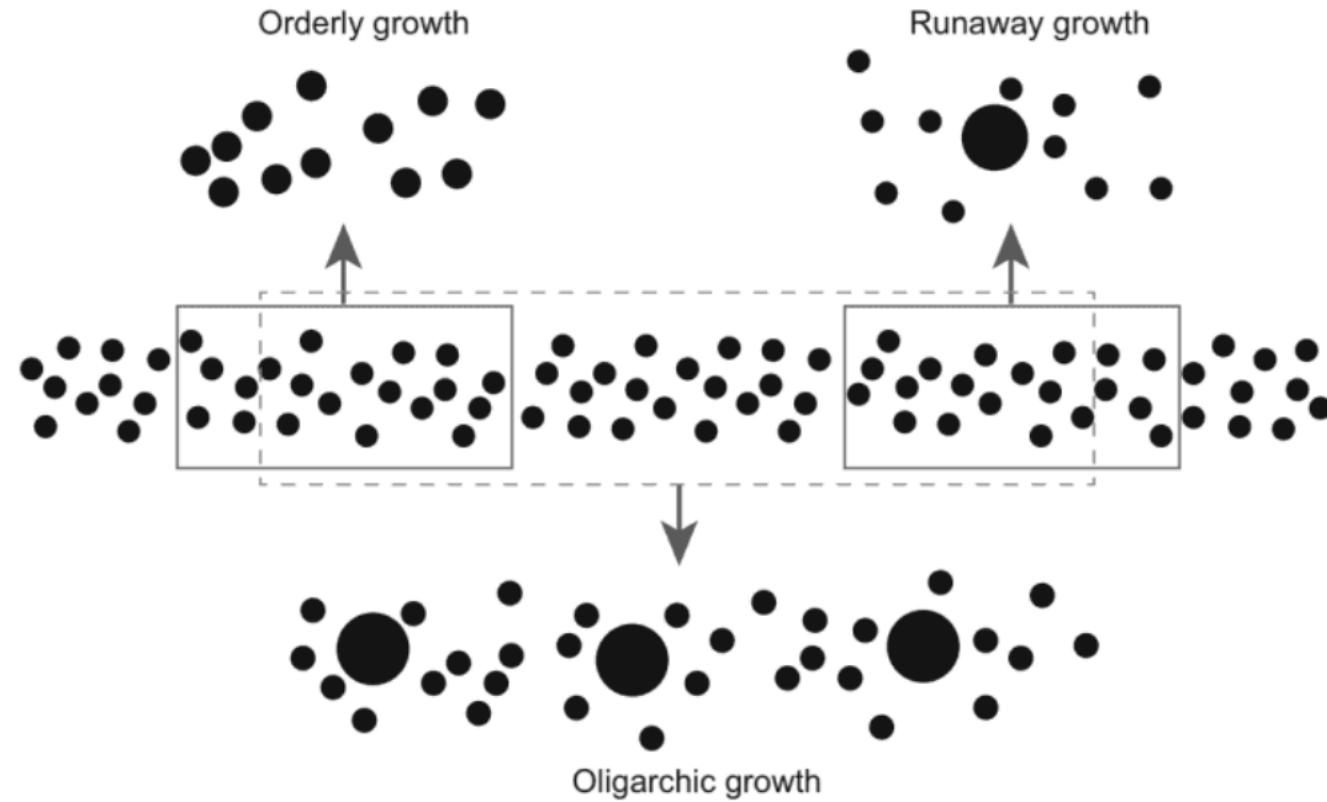
Largest body grows fastest  
**Runaway growth**

High  $v_{rms}$  ( $f \sim 1$ )

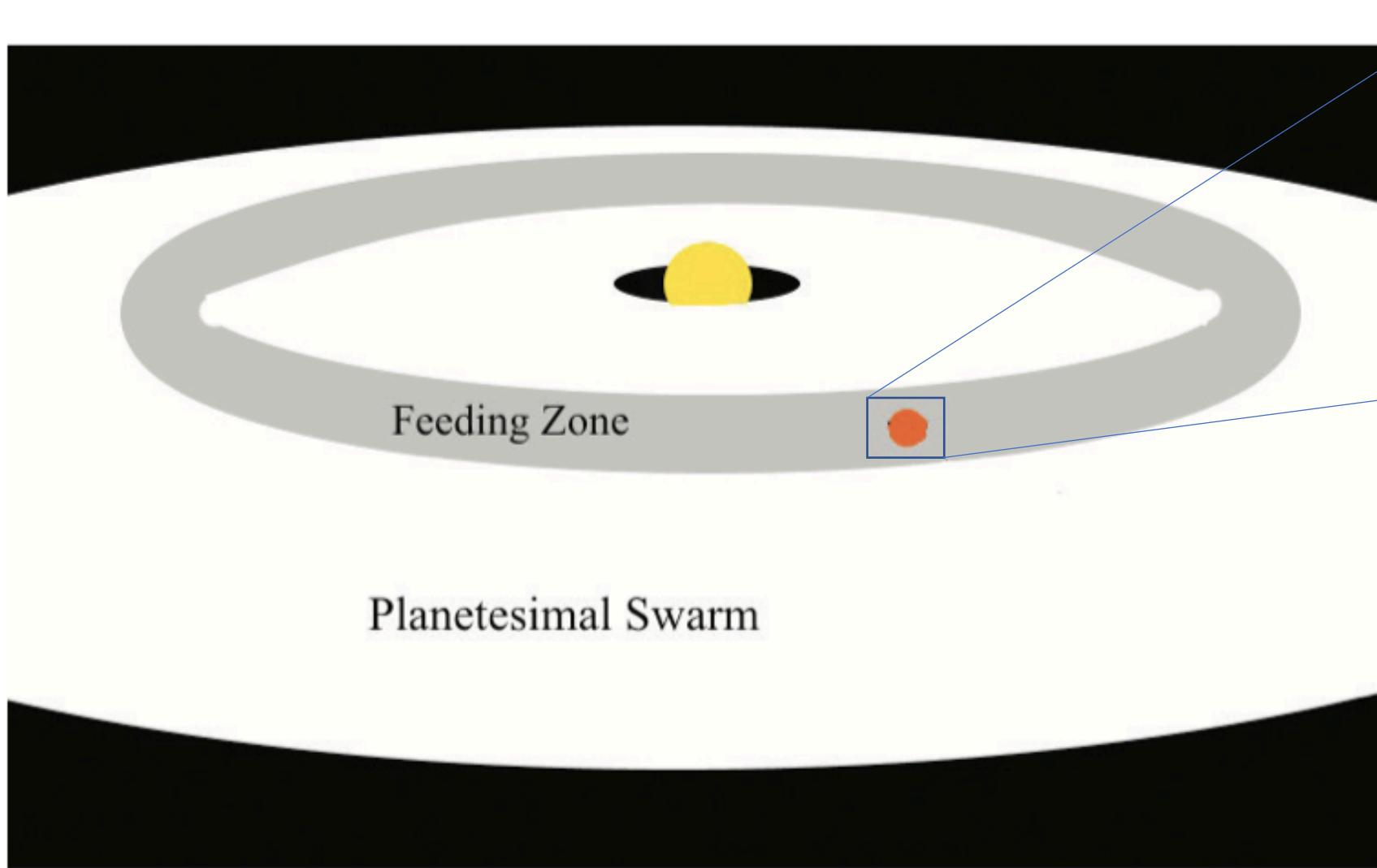
$$\frac{1}{m} \frac{dm}{dt} \propto m^{-1/3}$$

Largest body grows slowest  
**Oligarchic growth**

# Growth regimes



# Isolation Mass

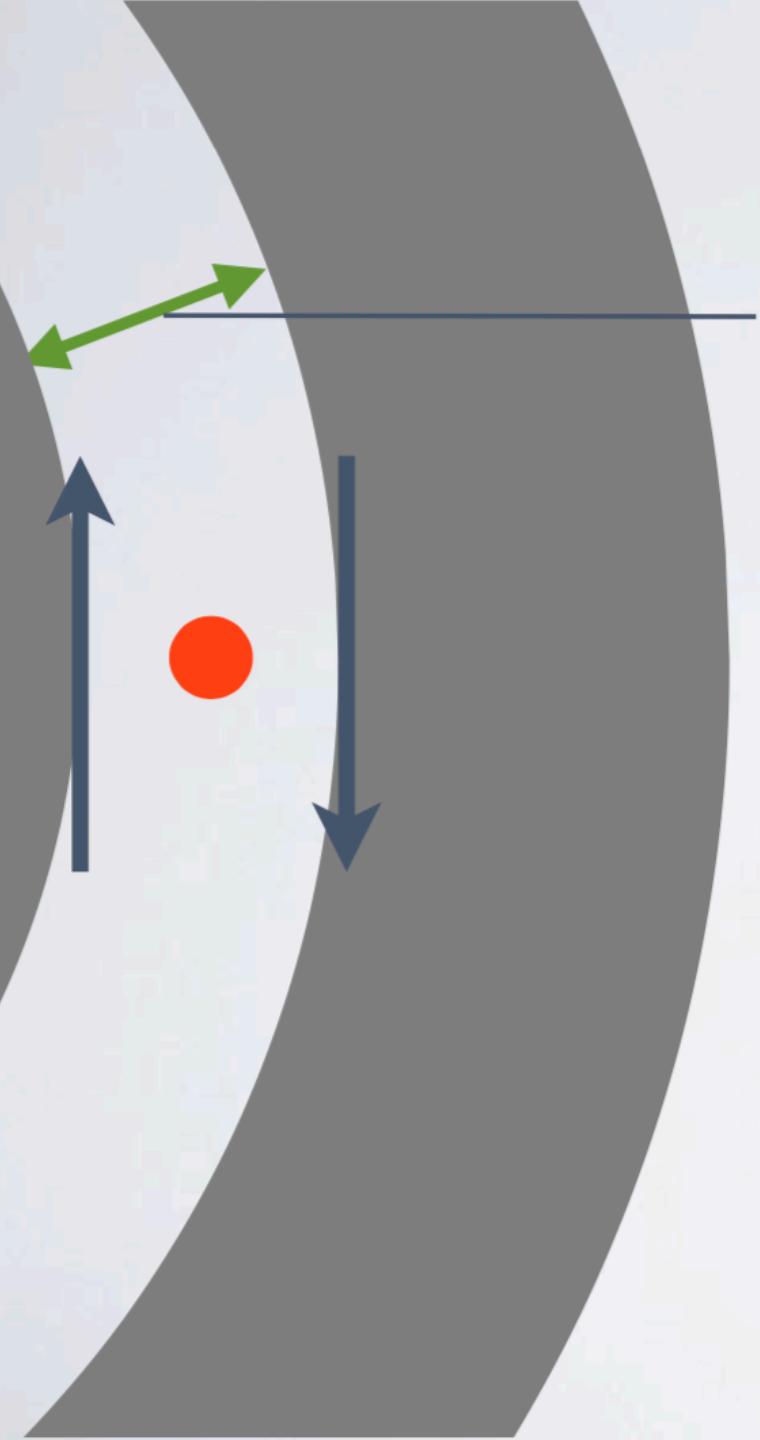


Planetsimal Swarm

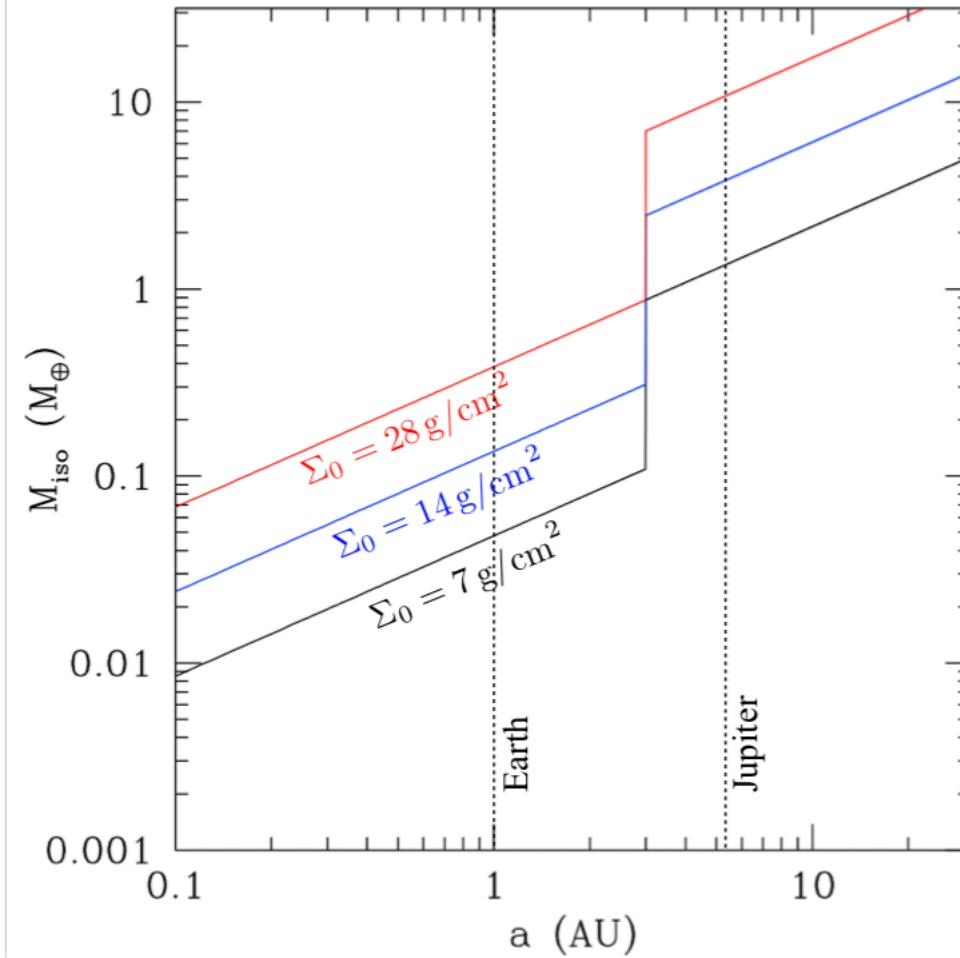
# Isolation Mass

Of the order of the Hill radius

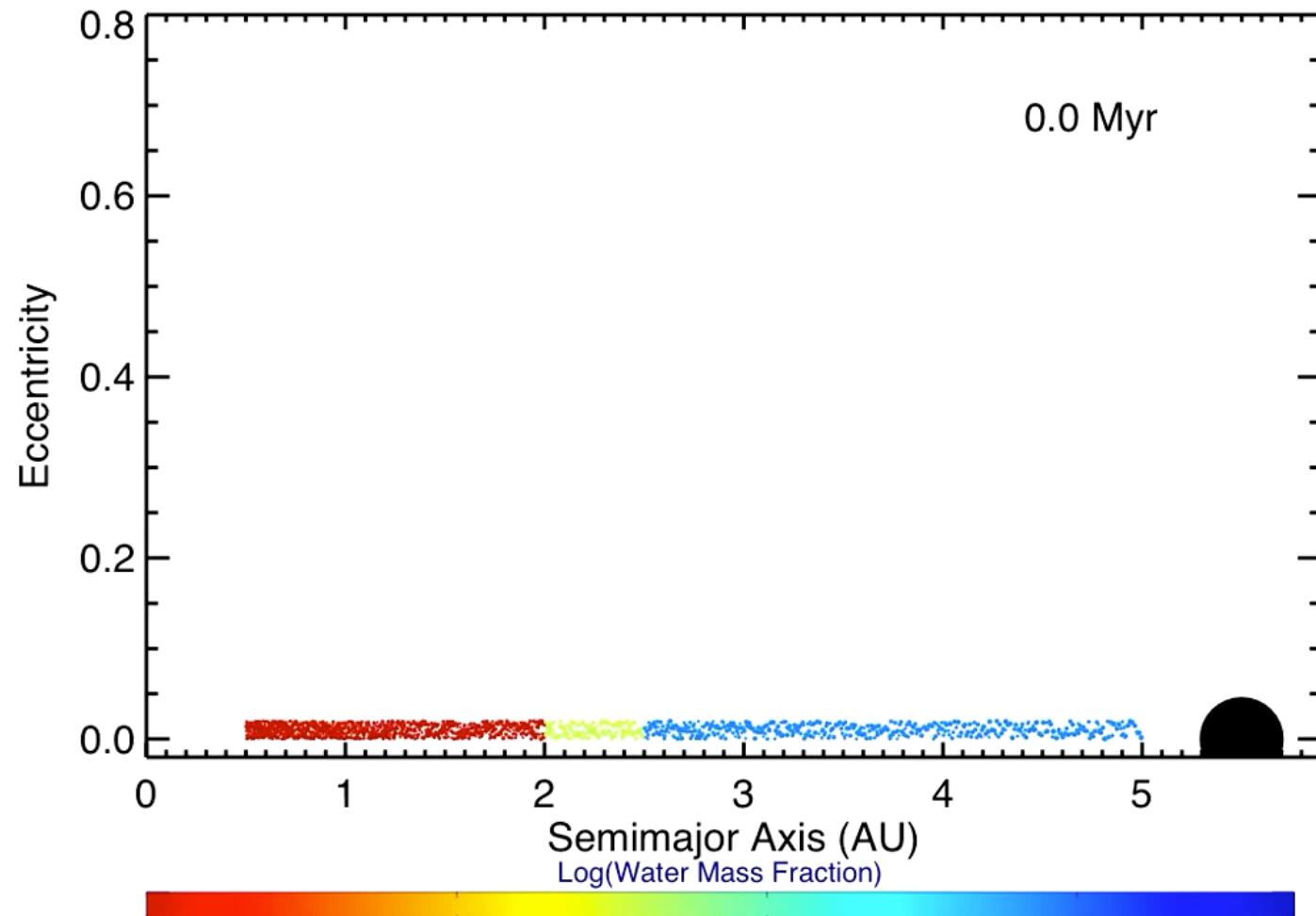
Protoplanet accretes all planetesimals in its feeding zone



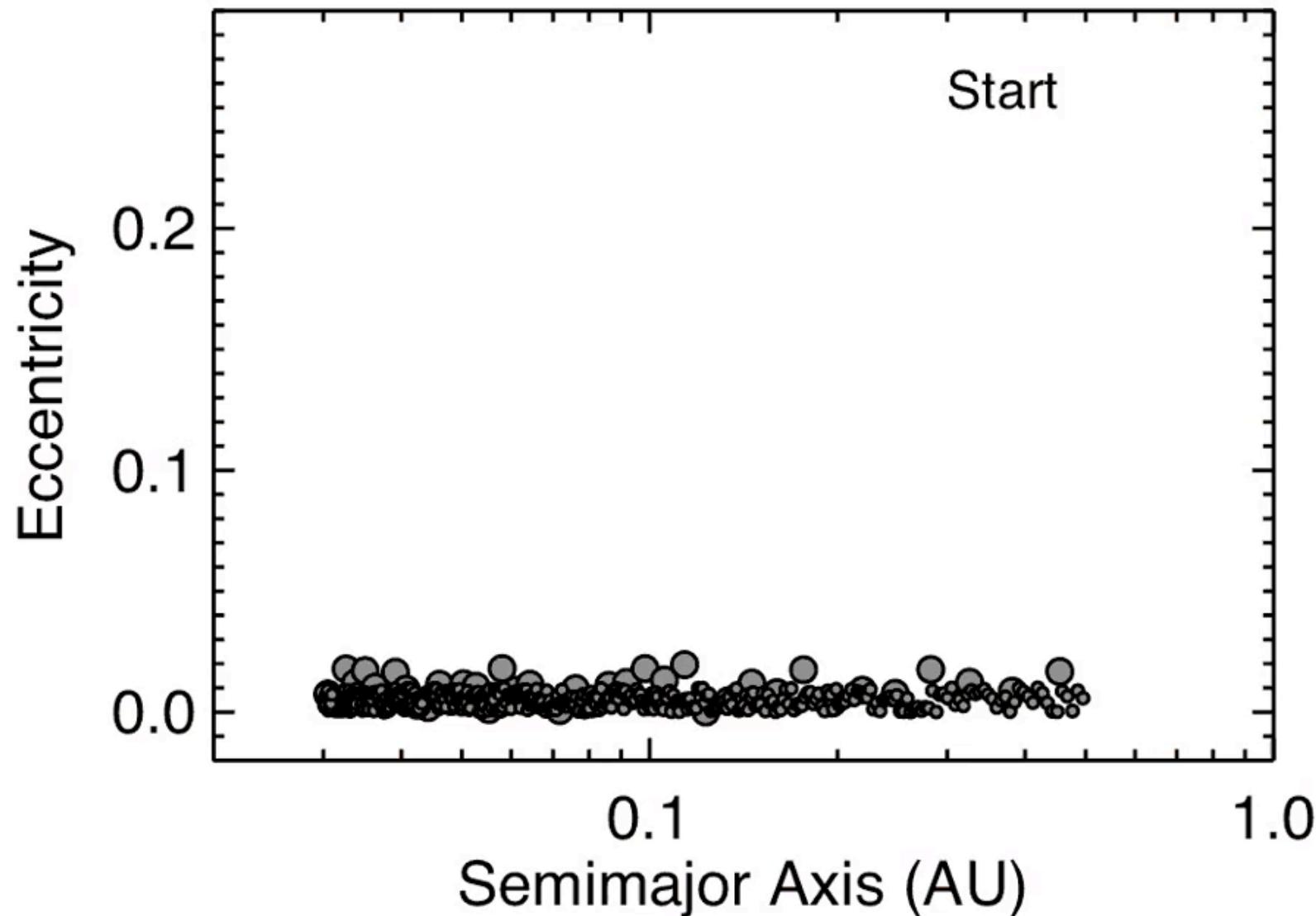
# Isolation Mass



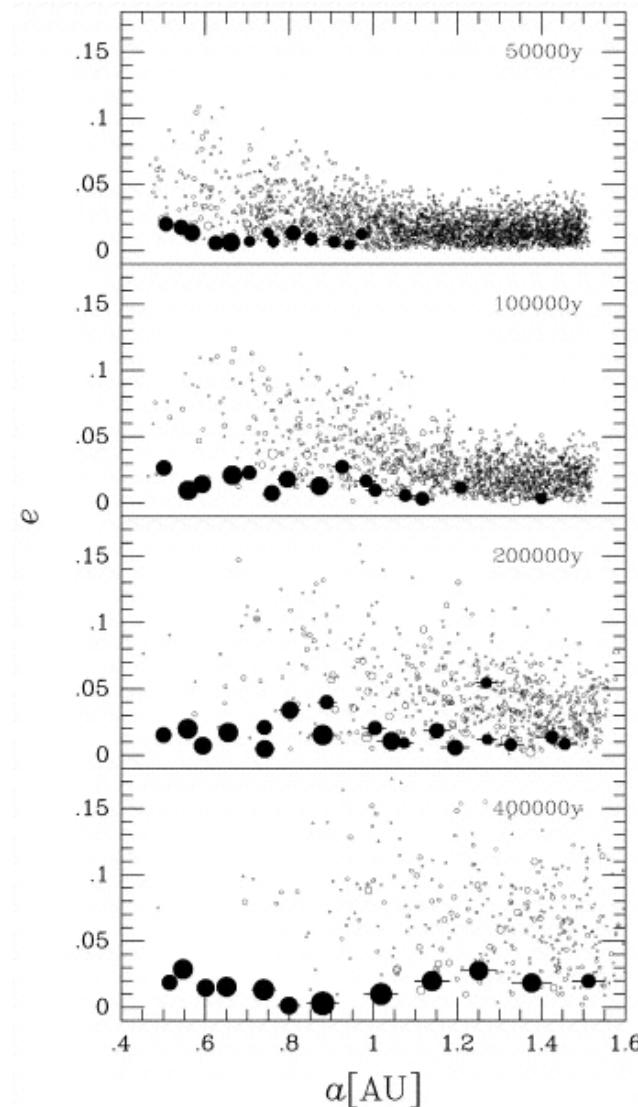
# Core Accretion and Oligarchic Growth



# Core Accretion and Oligarchic Growth



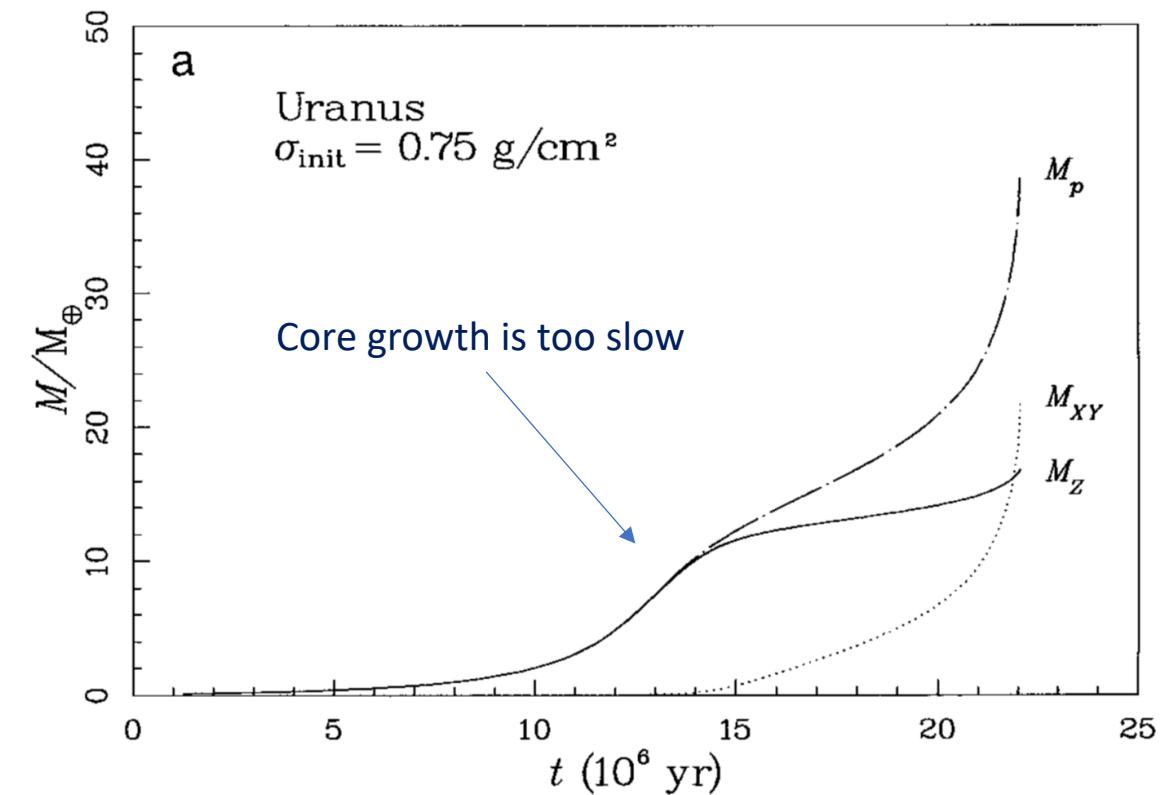
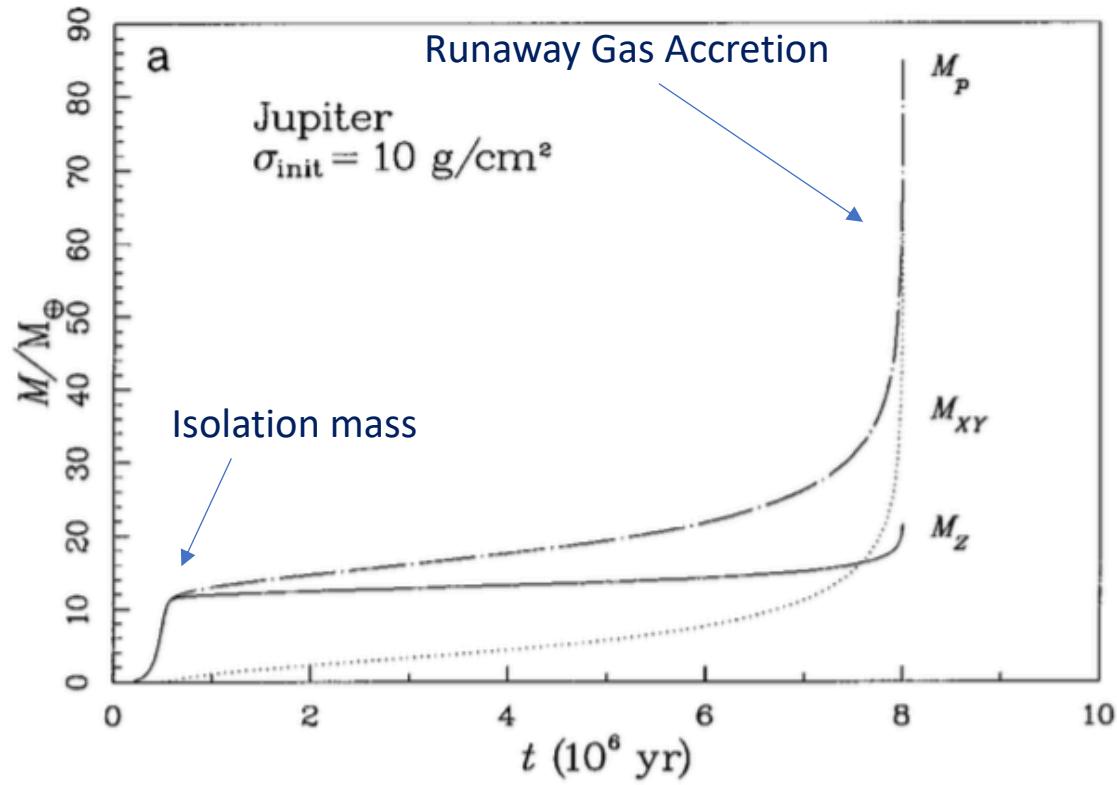
# Core Accretion and Oligarchic Growth



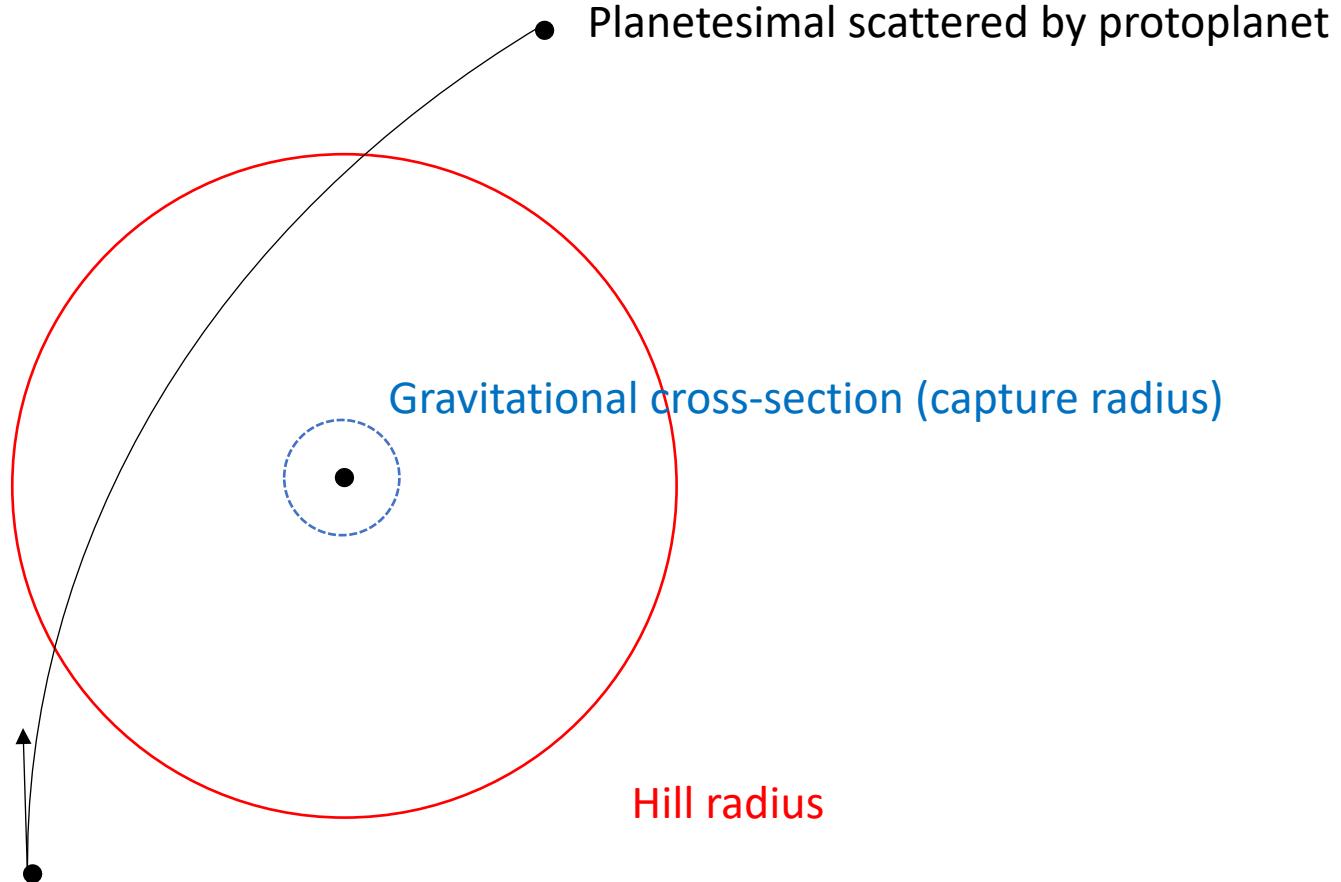
# Problem

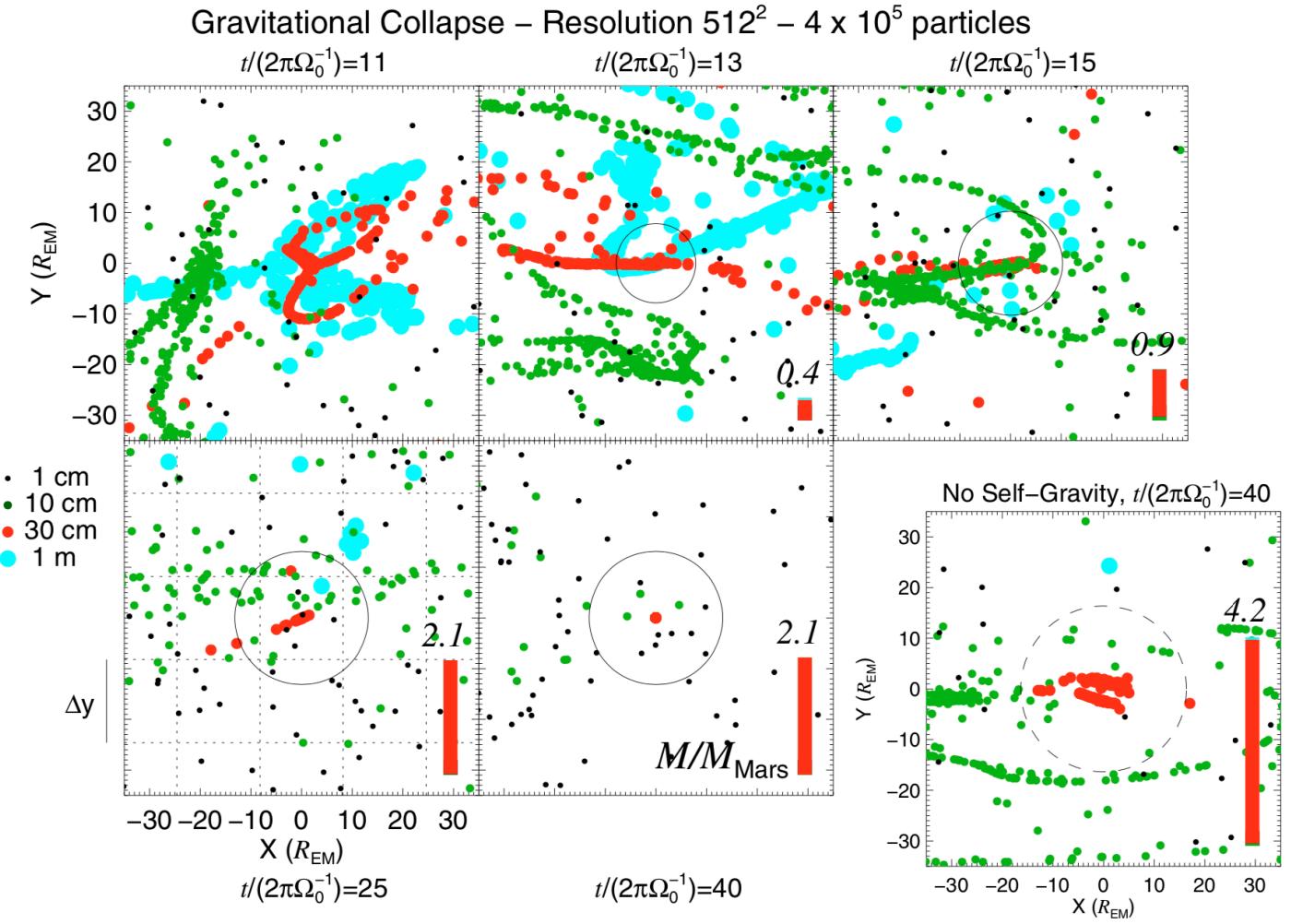
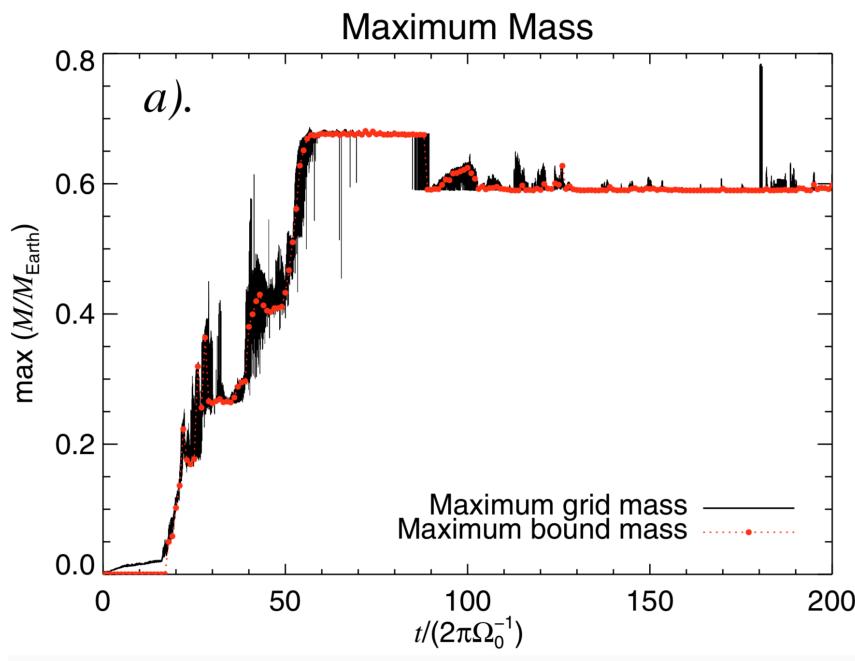
**Planetesimal accretion is TOO SLOW in the outer solar system**

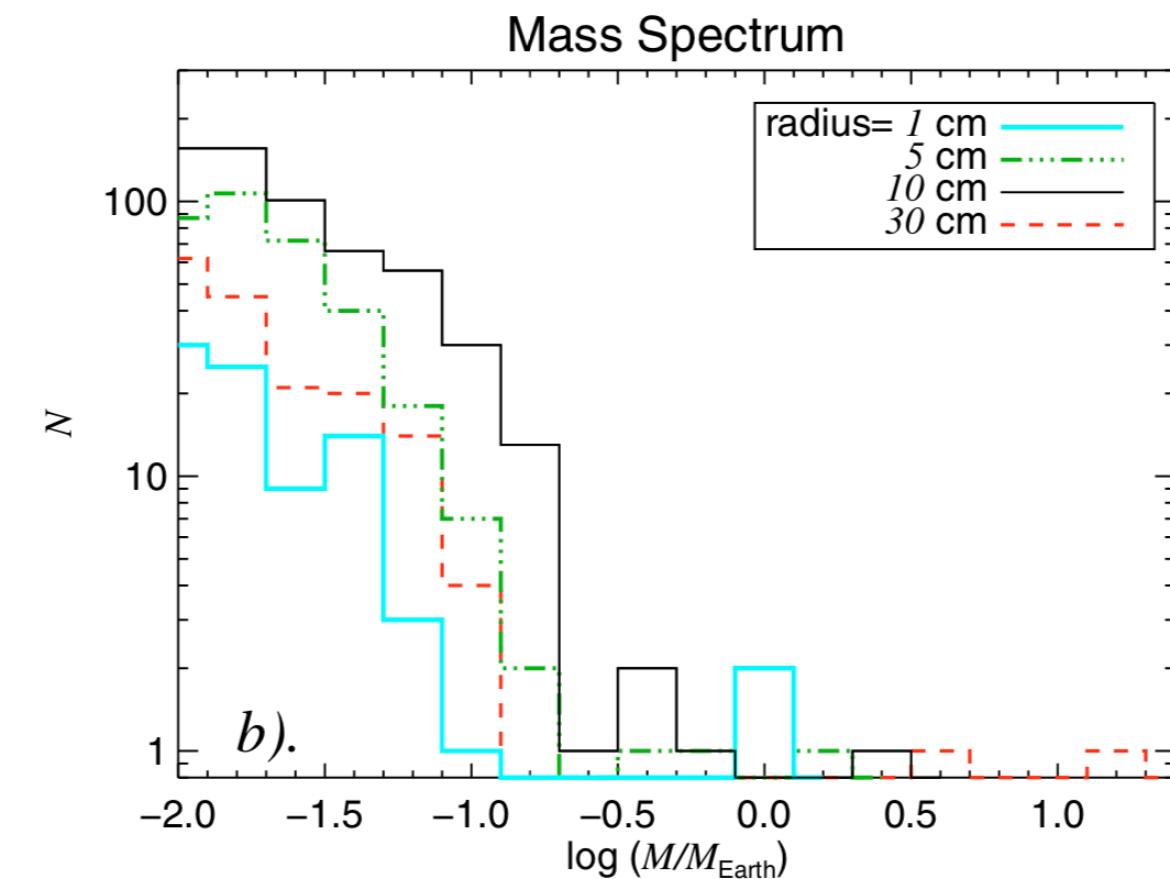
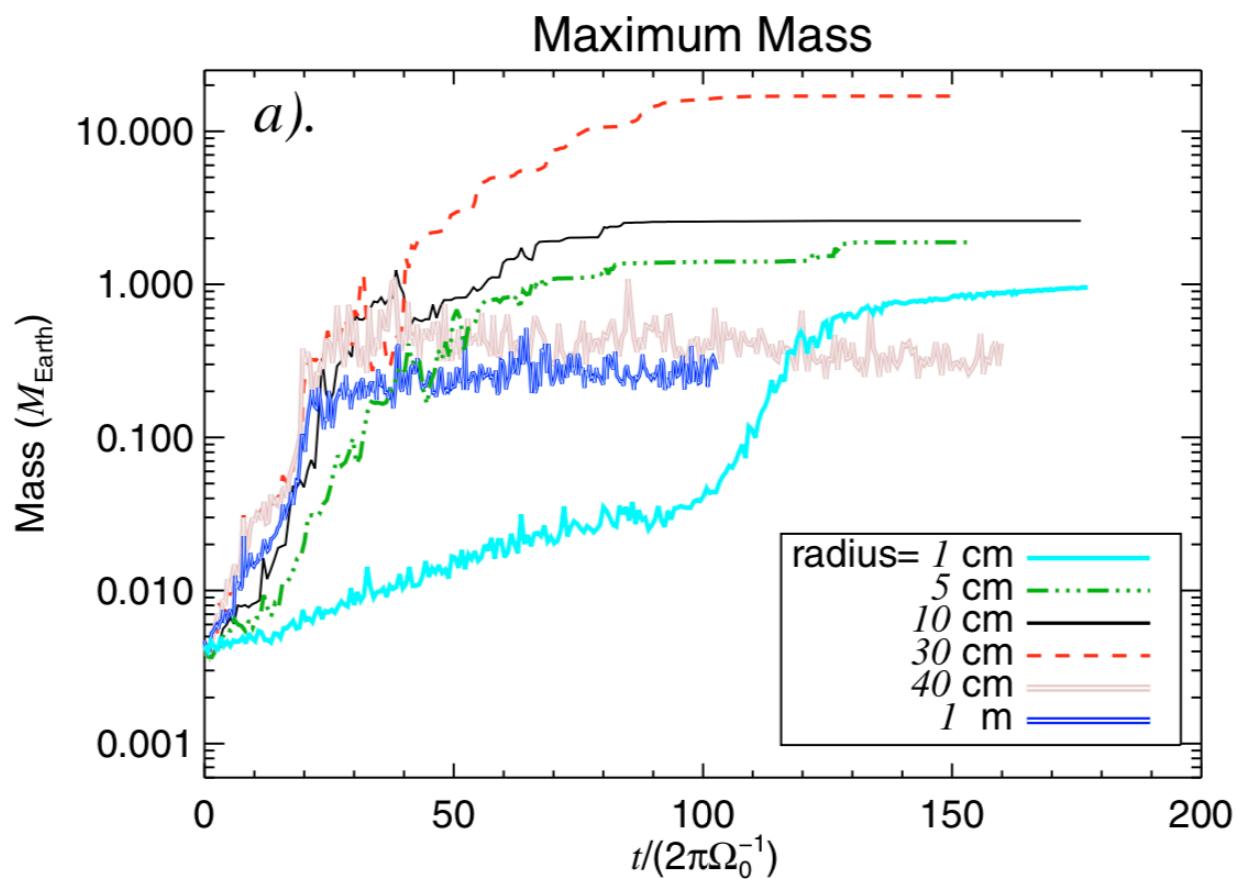
**Low growth rates for Uranus and Neptune**



# Planetesimal Accretion is inefficient







# Pebble Accretion

VIEW

Abstract

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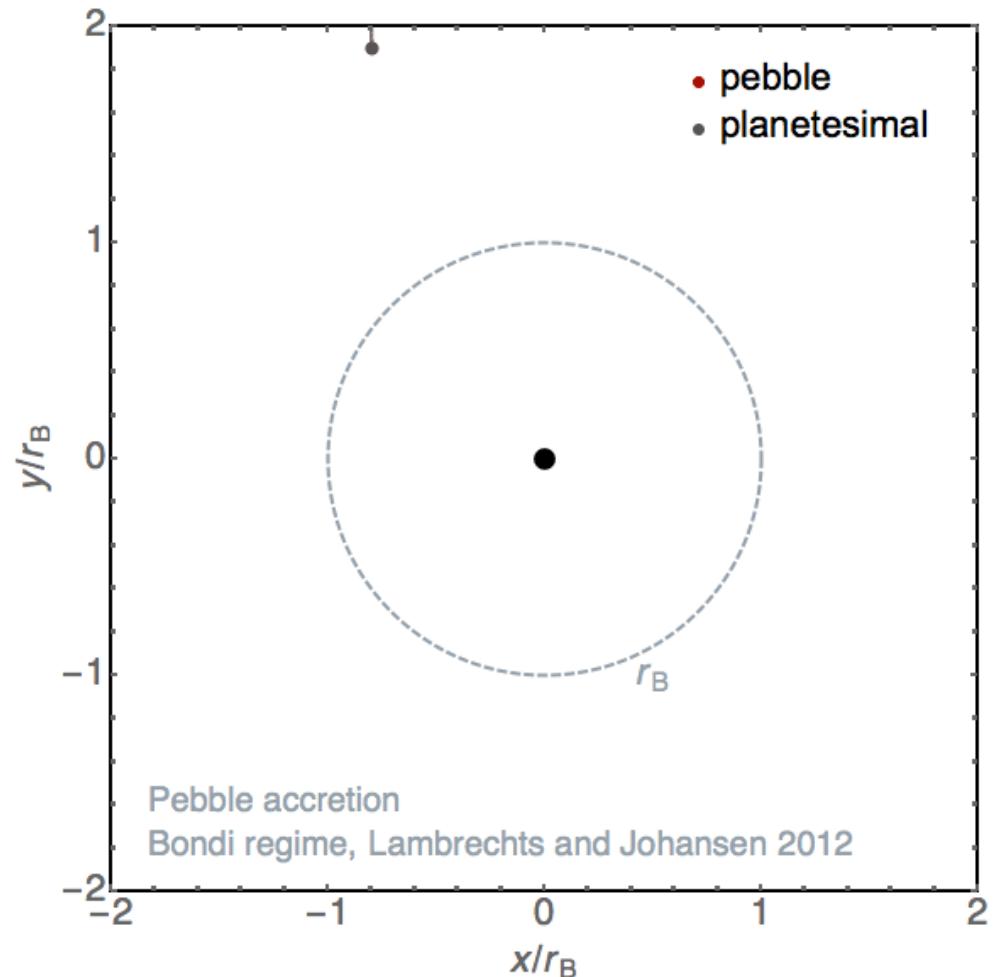
Export Citation

## Rapid growth of gas-giant cores by pebble accretion

Show affiliations

Lambrechts, M.; Johansen, A.

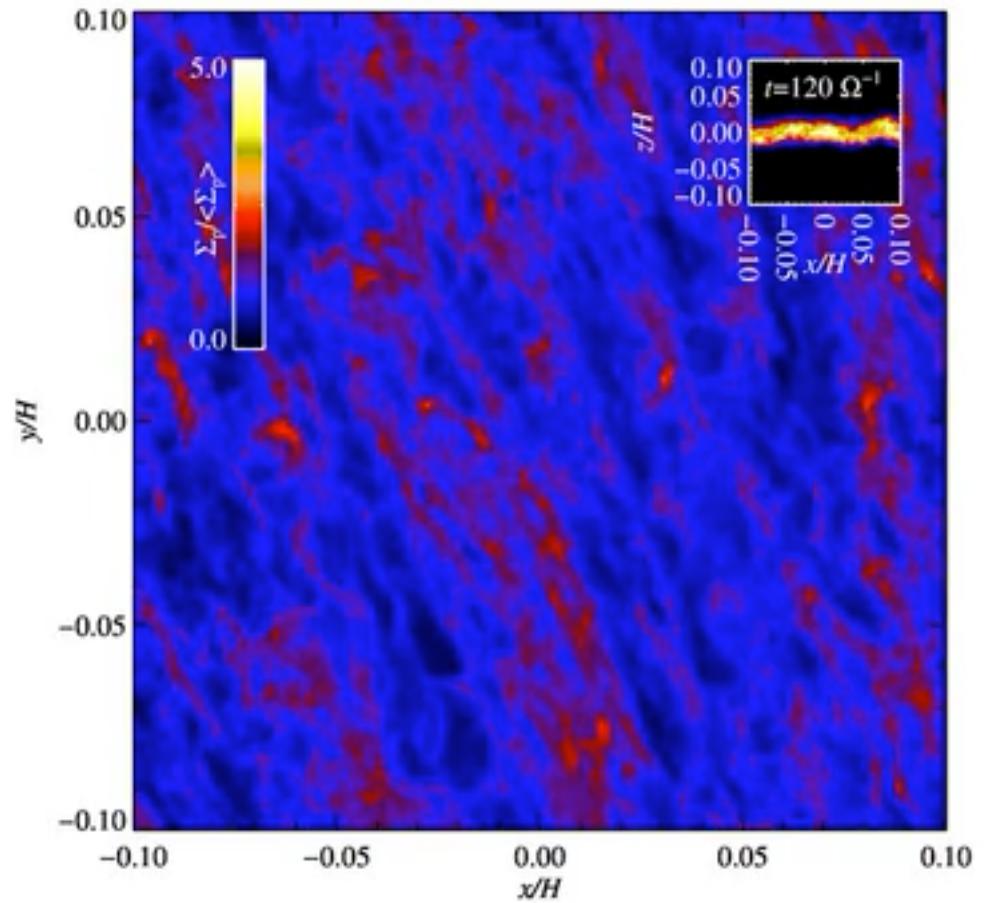
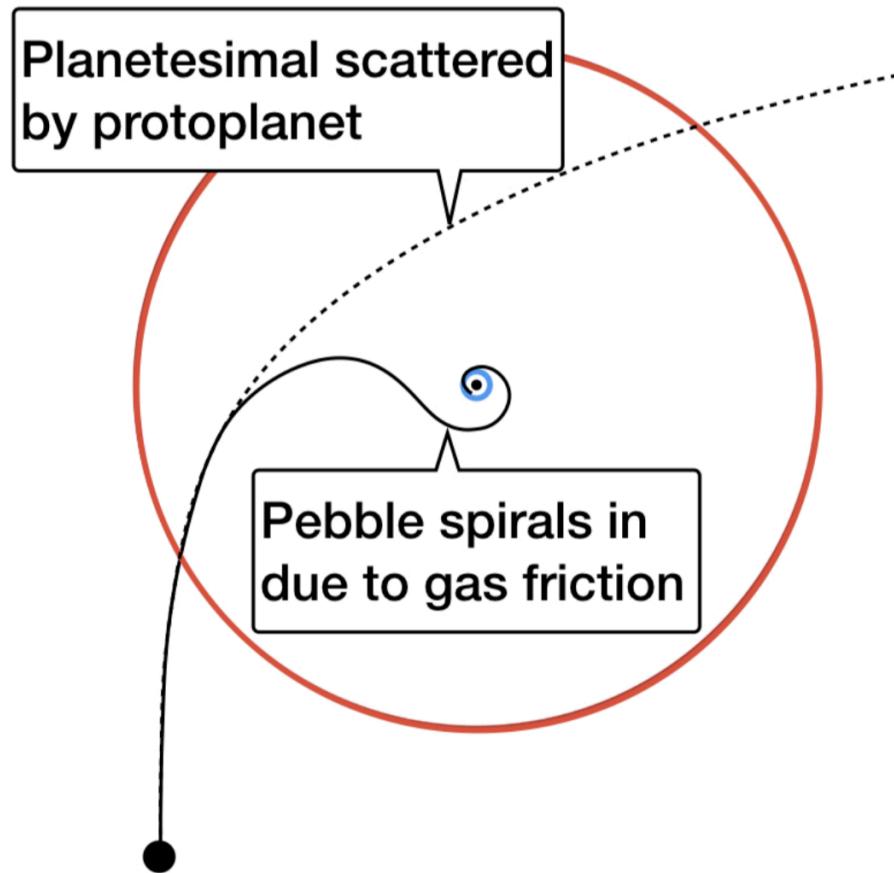
The observed lifetimes of gaseous protoplanetary discs place strong constraints on gas and ice giant formation in the core accretion scenario. The approximately 10-Earth-mass solid core responsible for the attraction of the gaseous envelope has to form before gas dissipation in the protoplanetary disc is completed within 1-10 million years. Building up the core by collisions between km-sized planetesimals fails to meet this timescale constraint, especially at wide stellar separations. Nonetheless, gas-giant planets are detected by direct imaging at wide orbital distances. In this paper, we numerically study the growth of cores by the accretion of cm-sized pebbles loosely coupled to the gas. We measure the accretion rate onto seed masses ranging from a large planetesimal to a fully grown 10-Earth-mass core and test different particle sizes. The numerical results are in good agreement with our analytic expressions, indicating the existence of two accretion regimes, one set by the azimuthal and radial particle drift for the lower seed masses and the other, for higher masses, by the velocity at the edge of the Hill sphere. In the former, the optimally accreted particle size increases



Klahr & Henning '97, Klahr '06, Inaba & Barge '08, Lyra+ '08, '09ab  
Ormel & Klahr '10, **Lambrechts & Johansen '12**,

See Johansen & Lambrechts '17 for a review

## Pebble Accretion



Klahr & Henning '97, Klahr '06, Inaba & Barge '08, Lyra+ '08, '09ab  
Ormel & Klahr '10, **Lambrechts & Johansen '12**,

See Johansen & Lambrechts '17 for a review

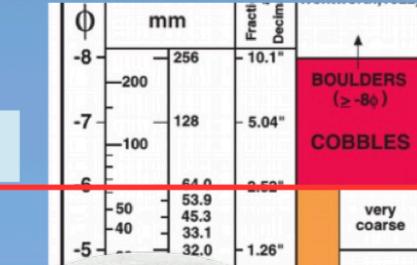
# Pebble definition

**Geologist:** particles  $2 \text{ mm} < d < 6.4 \text{ cm}$

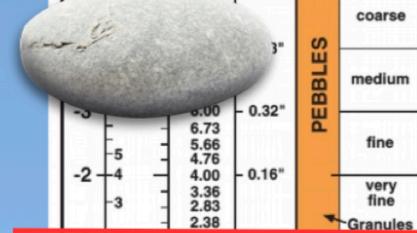
**Astrophysical:** particles that drift

6.4 cm

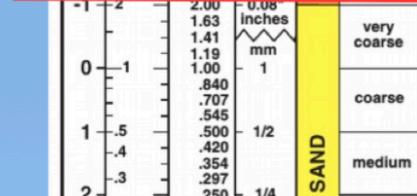
1 dm



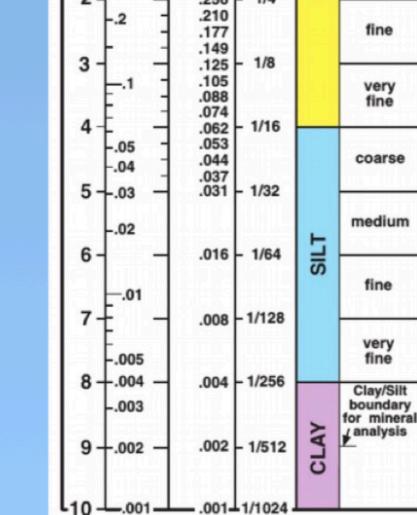
1 cm



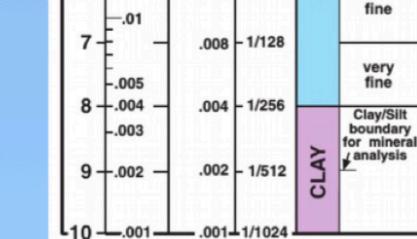
1 mm



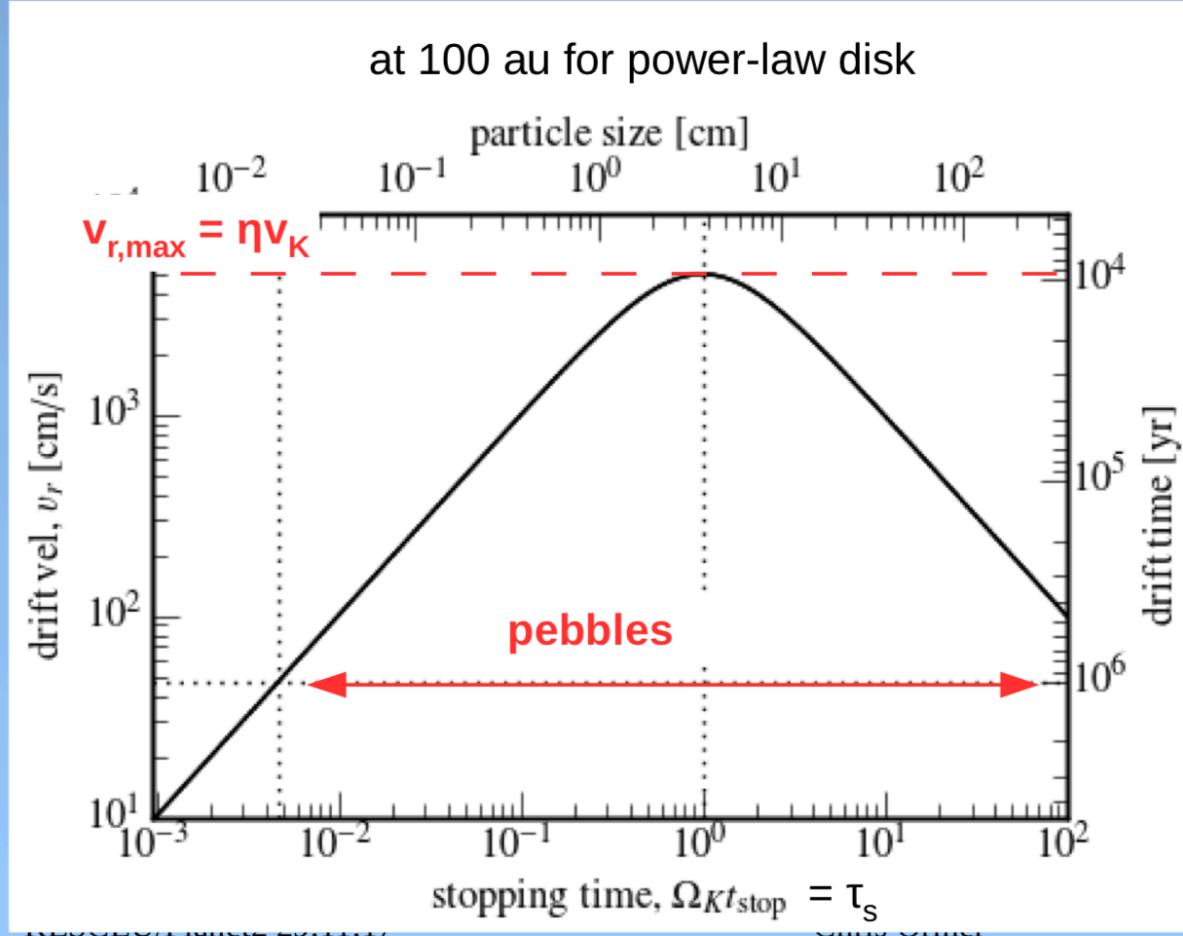
100 μm



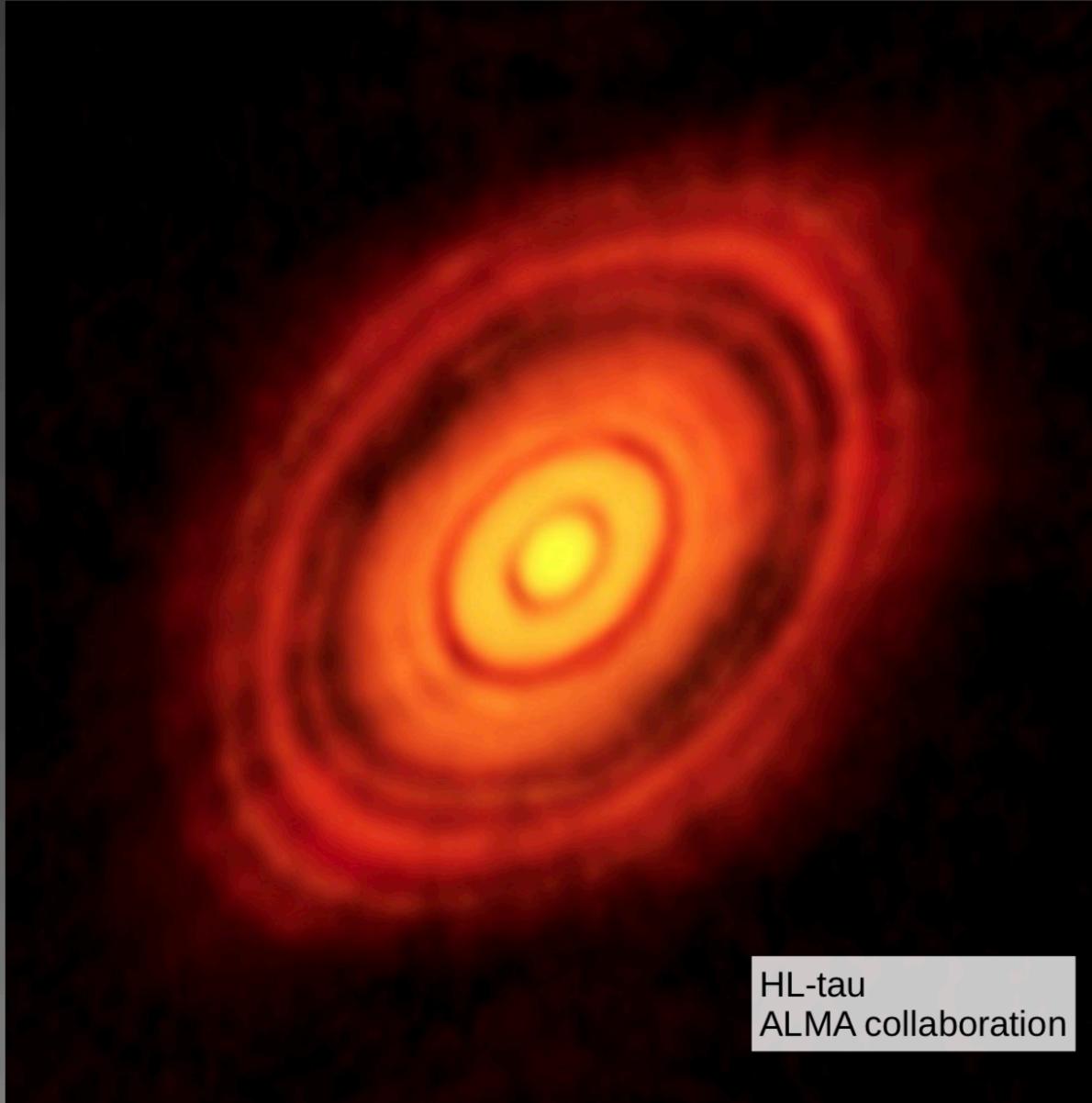
10 μm



1 μm

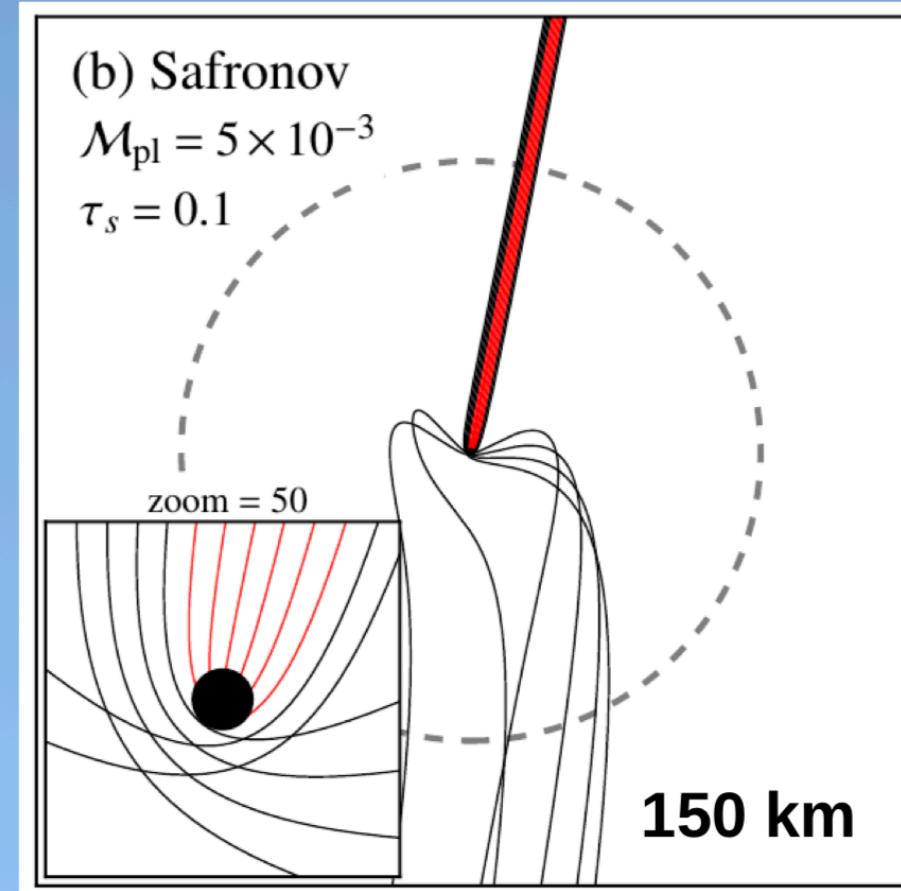
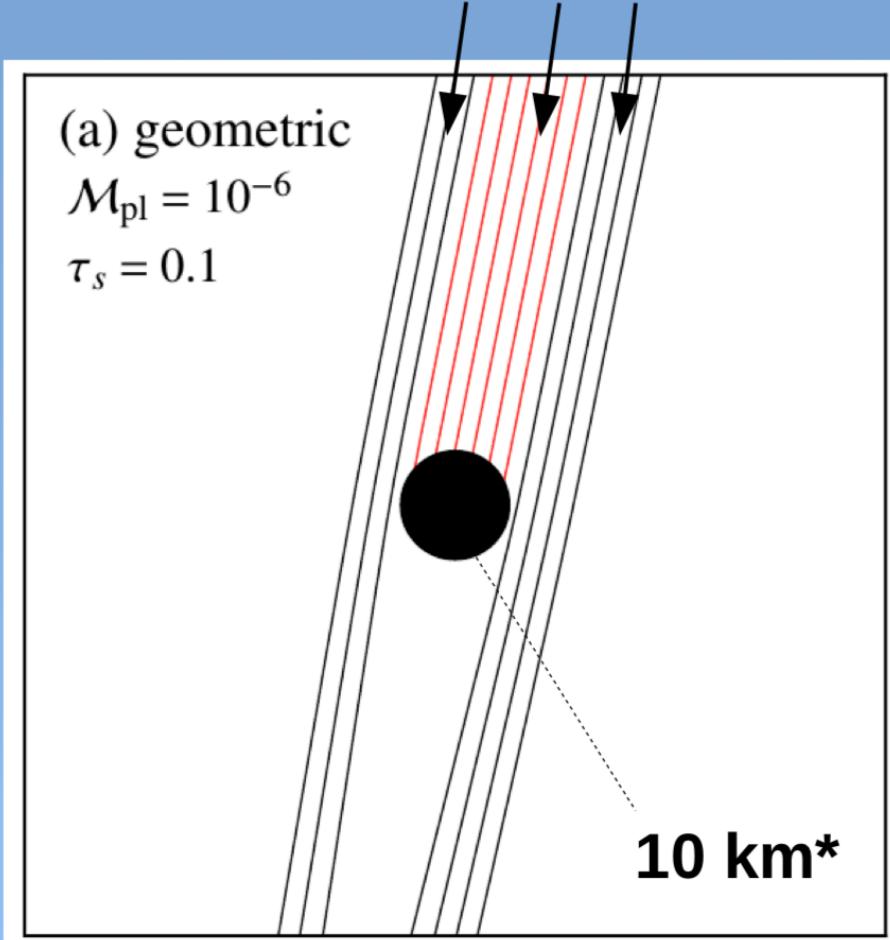


# A pebble disk



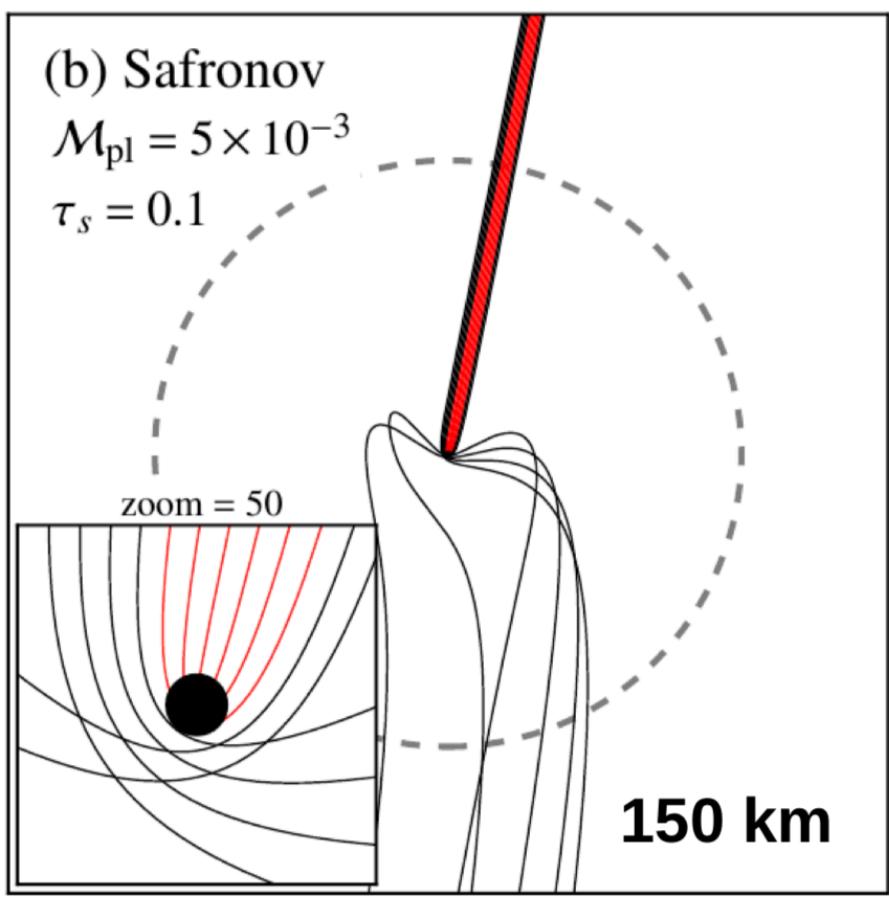
HL-tau  
ALMA collaboration

# No pebble accretion

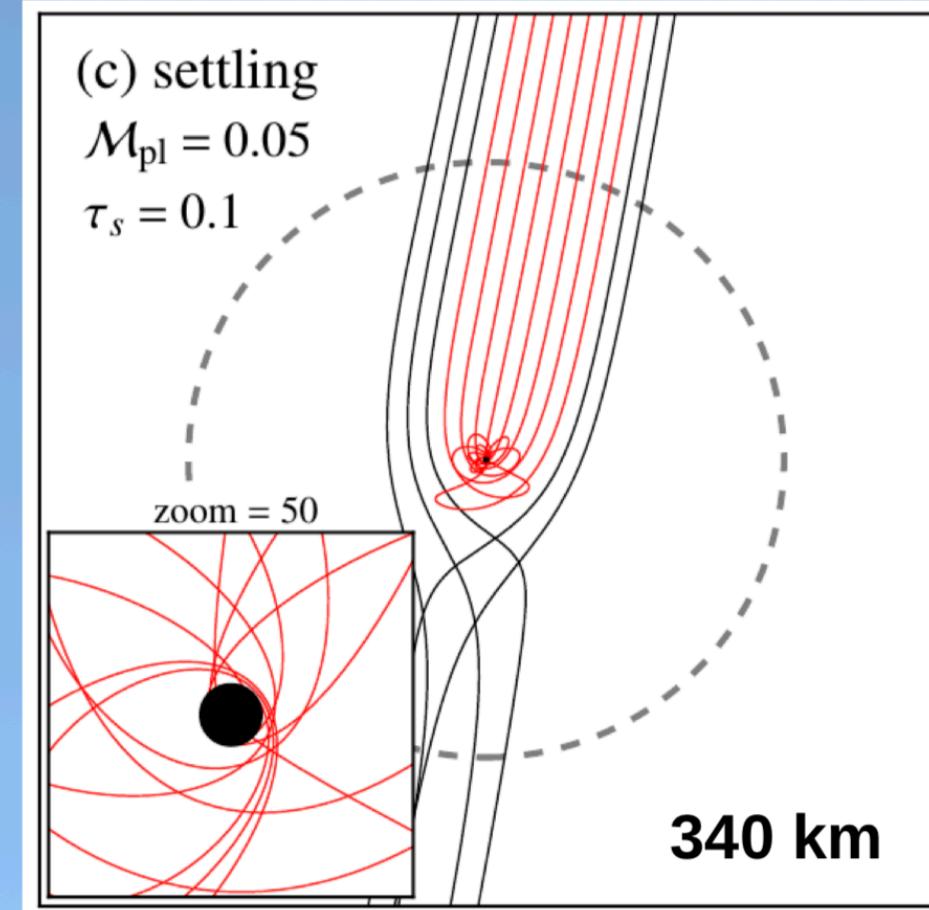


\* 1 au, solar-mass star, disk headwind 50 m sec<sup>-1</sup>

# Onset pebble accretion

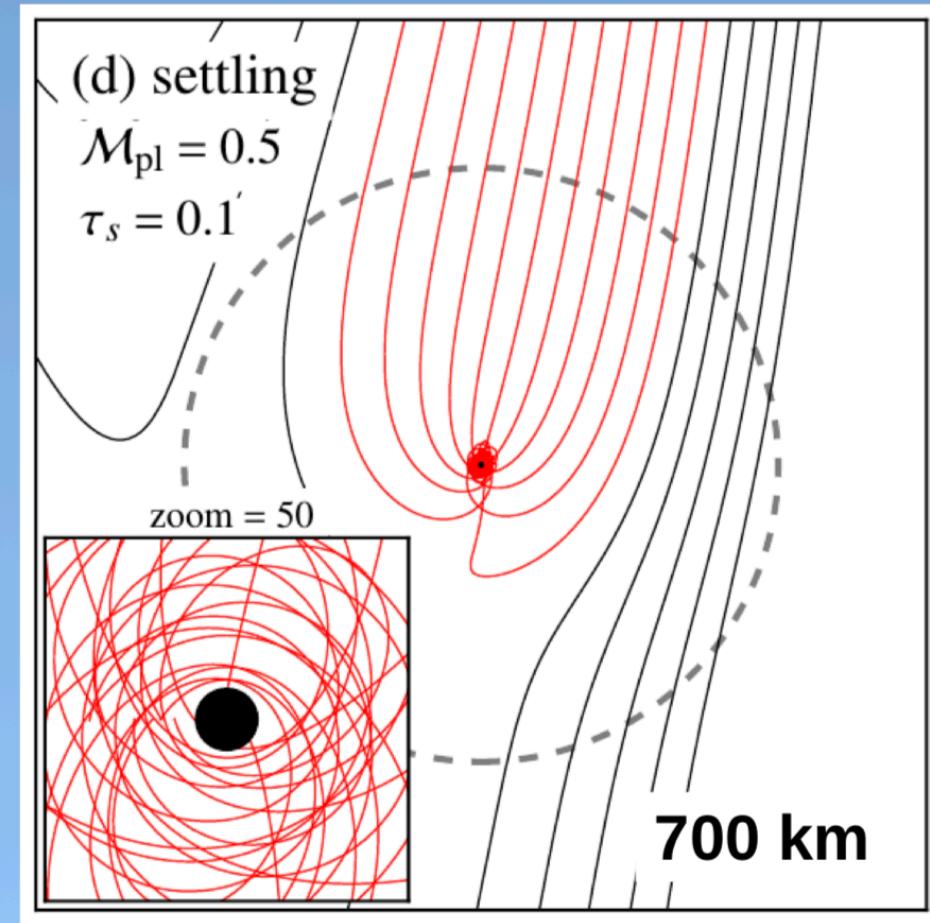
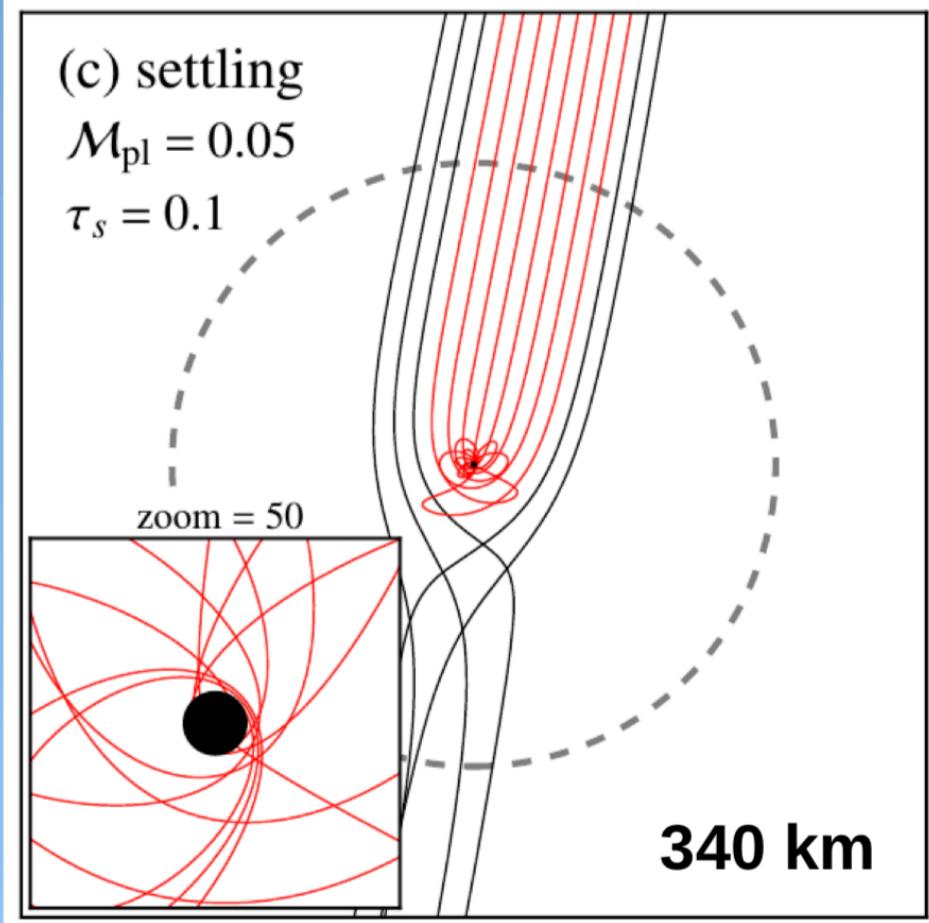


No Pebble accretion



Pebble accretion

# Onset pebble accretion



*Annual Review of Earth and Planetary Sciences*  
**Forming Planets via  
Pebble Accretion**

Anders Johansen<sup>1</sup> and Michiel Lambrechts<sup>2</sup>

<sup>1</sup>Lund Observatory, Lund University, 221 00 Lund, Sweden; email: anders@astro.lu.se

<sup>2</sup>Laboratoire Lagrange, Observatoire de la Côte d'Azur, Université Côte d'Azur,  
06304 Nice Cedex 4, France; email: michiel.lambrechts@oca.eu

## The emerging paradigm of pebble accretion

Chris W. Ormel

**Abstract** Pebble accretion is the mechanism in which small particles ('pebbles') accrete onto big bodies (planetesimals or planetary embryos) in gas-rich environments. In pebble accretion, accretion occurs by settling and depends only on the mass of the gravitating body, not its radius. I give the conditions under which pebble accretion operates and show that the collisional cross section can become much larger than in the gas-free, ballistic, limit. In particular, pebble accretion requires the pre-existence of a massive planetesimal seed. When pebbles experience strong orbital decay by drift motions or are stirred by turbulence, the accretion efficiency is low and a great number of pebbles are needed to form Earth-mass cores. Pebble accretion is in many ways a more natural and versatile process than the classical, planetesimal-driven paradigm, opening up avenues to understand planet formation in solar and exoplanetary systems.

### 1 Introduction