

*Home work 1*

There are three cosmological models. In all the models, matter is non-relativistic. (1) Flat universe with  $\Omega_{\text{matter},0} = 0.3$ . (2) Open Universe with  $\Omega_{\text{vac},0} = 0$ ,  $\Omega_{\text{matter},0} = 0.3$ . (3) Open Universe with  $\Omega_{\text{matter},0} = 0.3$ ,  $\Omega_{\text{vac},0} = 0.3$ . The Hubble constant at present is the same for all the models.

(a) Which model is older?

(b) Make a plot of the look-back-time and the age of the Universe for the same three cases for  $z = 0 - 20$ . The Hubble constant at present is  $h = 0.7$ . For comparison also show the look-back-time and the age for a flat universe with no vacuum energy.

(c) Make a plot of  $\Omega_{\text{matter}}(1+z)$ ,  $\Omega_{\text{curv}}(1+z)$ , and  $\Omega_{\text{vac}}(1+z)$

(d) What is the temperature of CMB in the models at  $z = 1000$ ?

(e) What is the physical density of matter in the models at  $z = 100$ . Give the answer in units of hydrogen atoms per  $\text{cm}^3$ . The Hubble constant at present is  $h = 0.7$ .

(f) What is the Hubble constant at  $z = 2$ ? The Hubble constant at present is  $h = 0.7$ .